

Week 1 covers sections 1-5 of chapter 13 in the textbook. Topics include

- temperature and measurement scales
- measurements of amount and density
- the ideal gas law
- kinetic theory of gas

1. The Celsius temperature scale is based on the *triple point* of water, but it is more common to think of it as being  $0^{\circ}\text{C}$  when water freezes and  $100^{\circ}\text{C}$  when water boils at 1 atm of pressure. But the Fahrenheit scale is more well known to us so let's do some conversion of common Fahrenheit temperatures.  $105^{\circ}\text{F}$ ,  $98.6^{\circ}\text{F}$ ,  $72^{\circ}\text{F}$ ,  $32^{\circ}\text{F}$ ,  $0^{\circ}\text{F}$ . Keep going down in Fahrenheit, and see if you can find a Fahrenheit temperature that gives you the same number in Celsius. Make sure you can go backwards and convert some Celsius temperatures back to Fahrenheit.

$$T_F = \frac{9}{5} T_C + 32$$

$$\frac{9}{5} T_C = T_F - 32$$

$$T_C = \frac{5}{9} (T_F - 32)$$

$T_F$	$T_C$
$105^{\circ}\text{F}$	$40.6^{\circ}\text{C}$
$98.6$	$37$
$72$	$22$
$32$	$0$
$0$	$-18$

$$T = \frac{9}{5} T + 32$$

$$-\frac{9}{5} T \quad -\frac{9}{5} T$$

$$-\frac{4}{5} T = 32$$

$$T = -40$$

2. If I only tell you a *change* in Fahrenheit temperature of a substance but not the actual temperature, then you can figure out the corresponding change in Celsius, but still not the actual temp. A change in temperature measured in Fahrenheit is 1.8 times bigger than the change measured in Celsius. So if the temperature increased by  $30^{\circ}\text{F}$ , then by how much does the temperature change in Celsius? What does this mean about the "size" of a Celsius degree vs. the "size" of a Fahrenheit degree? Which one represents a larger change in temperature?

$$\Delta T_F = \frac{9}{5} \Delta T_C$$

$$T_{F,2} - T_{F,1}$$

3. The kelvin temperature scale is designed as an *absolute* temperature scale, meaning the lowest temperature any object could theoretically be is set to 0 K. The size of a Kelvin degree is the same as the size of a Celsius degree, so that a  $20^\circ\text{C}$  change in temperature is the same as a 20 K temperature change. Absolute zero in the Kelvin Scale is set to  $-273.15^\circ\text{C}$ . So, what is  $0^\circ\text{C}$  in Kelvin? What is  $20^\circ\text{C}$  in Kelvin. What is 70 K in Celsius? What is normal human body temperature in K?

$$T_K = T_C + 273.15$$

$$T_C = T_K - 273.15$$

$T_C$	$T_K$
$-273.15^\circ\text{C}$	0 K
$0^\circ\text{C}$	273.15 K
$20^\circ\text{C}$	293.15 K
$-203.15^\circ\text{C}$	70 K
$37^\circ\text{C}$	310 K

$$\Delta T_C = \Delta T_K$$

4. What is absolute zero in the Fahrenheit temperature scale? Find this by using  $T_C = -273.15$  first if you want, but then try using a substitution for  $T_C$  that will give you an expression for finding any Fahrenheit temperature given a Kelvin one.

5. What is the ~~molecular weight~~ <sup>atomic mass</sup> of Carbon-12? Find a periodic table to help. How many protons are in Carbon-12? How many neutrons? What about the number of protons in Carbon-14? What about the number of neutrons in Carbon-14?
- $\rightarrow 12 \frac{\text{g}}{\text{mol}}$   
 $\rightarrow 6p$   
 $\rightarrow 6n = 12 - 6p$   
 $\rightarrow 6p$   
 $\rightarrow 8n$   
 atomic mass - # of proton = # of neutrons

6. How many atoms are in a mole of Helium? How many atoms are in a mole of Carbon-12? What is the mass of a mole of Helium? What is the mass of a mole of Carbon-12?

$$m_{\text{He}} = 4 \text{ g}$$

$$6.022 \cdot 10^{23} \text{ atoms} = 1 \text{ mol of He}$$

$$m_{\text{C}} = 12 \text{ g}$$

7. What is the mass of a single  $\text{CO}_2$  molecule? What is the mass of a mole of  $\text{CO}_2$ ?

$$12 \text{ g} + 2(16 \text{ g}) = 44 \text{ g}$$

$$\frac{44 \text{ g/mol}}{6.022 \cdot 10^{23} \text{ molecules/mol}} = 7.3 \cdot 10^{-23} \frac{\text{grams}}{\text{molecule}} \cdot \frac{1 \text{ kg}}{1000 \text{ g}} = 7.3 \cdot 10^{-26} \text{ kg}$$

8. What is the mass of a mole of dry air which is 78%  $\text{N}_2$ , 21%  $\text{O}_2$ , and 1% Ar?

$$\rightarrow 28 \text{ g} \cdot 0.78 = \underline{\hspace{2cm}}$$

$$32 \text{ g} \cdot 0.21 = \underline{\hspace{2cm}}$$

$$40 \text{ g} \cdot 0.01 = \underline{\hspace{2cm}}$$

$$\underline{\underline{29 \text{ g/mol}}}$$

9. A balloon is filled with 0.4 mol of helium so that its volume is  $0.010 \text{ m}^3$ .

- Find the number of atoms.

- Find the number density.
- Find the mass density.
- Estimate the average distance between atoms. To do this, find the *volume per particle*, and then treat that volume like a cube and find the side length of the cube. Draw a picture of this model and use that to justify your approximation.

10. You have a pound of feathers and a pound of lead.

- Which one weighs more?
- Which one has more mass?
- Which one has the greater volume?
- Which one contains a larger number of moles?
- Which one contains a larger number of atoms?
- Which one contains a larger number of protons and neutrons?

11. You check your car tire pressure and see that the pressure is  $25 \text{ lb/in}^2$ . What is this in Pascal? (You'll need to look up a conversion factor). This is a gauge pressure, so what is the absolute pressure in the tire?
12. You check your car tire pressure when it is  $15^\circ\text{C}$  and it is  $25 \text{ lb/in}^2$ . By what factor do you increase the number of particles in the tire so that the pressure becomes that  $30 \text{ lb/in}^2$ ? (*Hint: The volume and temperature do not change.*)
13. The gas pressure inside of a 1 liter sealed container at room temperature is  $1 \text{ atm}$ . How many molecules are inside? How many moles of molecules?

14. If the pressure inside a tank is 1 atm when the temperature is 100 K, then what is the pressure when the temperature rises to 200 K?
15. If the pressure inside a tank is 1 atm when the temperature is 100 °C, then what is the pressure when the temperature rises to 200 °C? *CAREFUL!*
16. A gas is in a sealed container. By what factor does the pressure change if
- the volume is doubled?
  - the temperature is tripled?
  - the volume is double and the temperature is tripled?

- the volume is halved?

17. You are standing in a room at atmospheric pressure and room temperature. You estimate the room to be 10 m wide by 15 m long by 2 m high. How many moles of gas are in the room?

