

Week 4 covers sections of chapter 16 in the textbook. Topics include:

- charge
- electric field and electric force
- motion of particles within a constant electric field

1. Let's work on units.

- What are the units of electric field? Use the equation $\vec{F} = q \cdot \vec{E}$

$$\vec{F}_e = q \cdot \vec{E}$$

↓
 electric field strength ($\frac{N}{C}$)
 ↓
 charge → [Coulomb]

gravitational field
 strength
 (on earth)
 ↓
 $9.8 \frac{N}{kg}$
 $F_g = m \vec{g}$ → $g = \frac{Gm_0}{r^2}$
 $G = 6.67 \cdot 10^{-11} \frac{Nm^2}{kg^2}$

- What are the units of the Coulomb constant, k ? Use the equation $E = \frac{kq_0}{r^2}$ or $F = \frac{kq_0 q_1}{r^2}$.

$$\frac{N}{C} \rightarrow \left[E = \frac{kq_0}{r^2} \right] \rightarrow \text{Coulomb}$$

↓
 m^2

$$\left[\frac{N}{C} \right] = \left[\frac{\frac{Nm^2}{C^2}}{m^2} \right] [C]$$

$k = 9 \cdot 10^9 \frac{Nm^2}{C^2}$

$$E = \frac{q_0}{4\pi\epsilon_0 r^2}$$

- What are the units of the vacuum permittivity constant, ϵ_0 ?

Use the equation $k = \frac{1}{4\pi\epsilon_0}$.

$$4\pi k = \frac{1}{\epsilon_0}$$

$$\epsilon_0$$

$$\epsilon_0$$

$$\boxed{\epsilon_0 = 8.85 \cdot 10^{-12} \frac{C^2}{Nm^2}}$$

2. An elementary charge is the charge of either an electron or proton, and interestingly they are the same amount but different sign. How many elementary charges are in one Coulomb of charge? How many Coulombs of charge is one elementary

charge? How many electrons would there be in $1\mu\text{C}$ of charge?

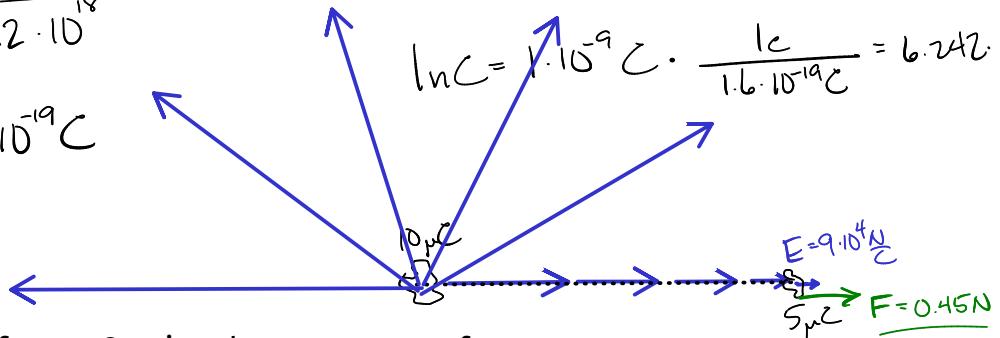
1 nC

$$\frac{6.242 \cdot 10^{18} \text{ e}}{6.242 \cdot 10^{18}} = \frac{1 \text{ C}}{6.242 \cdot 10^{18}}$$

$$1 \text{ e} = 1.6 \cdot 10^{-19} \text{ C}$$

$$1 \mu\text{C} = 1 \cdot 10^{-6} \text{ C} \cdot \frac{6.242 \cdot 10^{18} \text{ e}}{1 \text{ C}} = 6.242 \cdot 10^{12} \text{ e}$$

$$1 \text{ nC} = 1 \cdot 10^{-9} \text{ C} \cdot \frac{1 \text{ C}}{1.6 \cdot 10^{-19} \text{ C}} = 6.242 \cdot 10^9 \text{ e}$$



3. What is the electric field of a $10\mu\text{C}$ point charge 1 m away from the point charge?

active charge $E = \frac{kq}{r^2} = \frac{9 \cdot 10^9 \frac{\text{Nm}^2}{\text{C}^2} \cdot 10 \cdot 10^{-6} \text{ C}}{(1 \text{ m})^2} = 9 \cdot 10^4 \frac{\text{N}}{\text{C}}$

follow up: What is the force on another 5 microC charge at this place?

passive charge $F = qE = 5 \cdot 10^{-6} \text{ C} \cdot 9 \cdot 10^4 \frac{\text{N}}{\text{C}} = 0.45 \text{ N}$

4. Where is the electric field of a $10\mu\text{C}$ point charge 50 N/C ?

$$E = \frac{kq}{r^2}$$

?

5. How much charge is in a point charge if the electric field is 1 N/C 1 m away?

$$E = \frac{kq}{r^2}$$

6. If you double the distance away from a point charge, by what factor do you change the electric field strength? Triple? Half?

Quarter? $\rightarrow \frac{r_2}{r_1} = \frac{1}{4}$

$$\frac{r_2}{r_1} = 3 \quad \rightarrow \quad \frac{r_2}{r_1} = \frac{1}{2}$$

$$E = \frac{kq}{r^2}$$

$$E \propto r^{-2} \Rightarrow \frac{E_2}{E_1} = \left(\frac{r_2}{r_1}\right)^{-2}$$

$$\frac{E_2}{E_1} = (2)^{-2} = \frac{1}{4}$$

$$\frac{E_2}{E_1} = \left(\frac{1}{2}\right)^{-2} = 4$$

$$\frac{E_2}{E_1} = (3)^{-2} = \frac{1}{9}$$

7. If the electric field doubles, by what factor do the distances between these locations differ? What if the electric field is 10 times smaller?

$$\left[\frac{E_2}{E_1}\right]^{-\frac{1}{2}} = \left[\left(\frac{r_2}{r_1}\right)^{-2}\right]^{\frac{1}{2}}$$

$$\left(\frac{E_2}{E_1}\right)^{-\frac{1}{2}} = \frac{r_2}{r_1} = (2)^{-\frac{1}{2}} = \left(\frac{1}{2}\right)^{\frac{1}{2}} = \sqrt{\frac{1}{2}} = \frac{1}{\sqrt{2}} = \frac{\sqrt{2}}{2} = 0.71$$

8. A $3\ \mu\text{C}$ and a $5\ \mu\text{C}$ are 5 m away from each other. What is the magnitude of the electric field produced by the $3\ \mu\text{C}$ charge 5 m away from it? What is the force on the $5\ \mu\text{C}$ charge? If the $5\ \mu\text{C}$ charge was instead a $9\ \mu\text{C}$ charge, what is the force on it? In what direction does this force point?

9. Lets see if Newton's Third Law applies to the electric force. In the last problem you found the electric field of the $3\ \mu\text{C}$ charge

and then multiplied by the other charge. But this time find the electric field of the $5 \mu\text{C}$ charge 5 m away? Is it the same? What is the force on the $3 \mu\text{C}$ charge? Is it the same? What is its direction? Is this consistent with Newton's Third Law?

10. A $+20 \mu\text{C}$ charge is 2 m away from a $-5 \mu\text{C}$ charge. What is the electric field halfway between the two charges? What is it 1 m away from the $+20 \mu\text{C}$ charge on the side opposite the $-5 \mu\text{C}$ charge. What is the electric field 1 m away from the $-5 \mu\text{C}$ charge on the opposite side as the $+20 \mu\text{C}$ charge? Draw a picture of all of this to keep the locations straight.

11. For the charge distribution above, can you find where the electric field would equal zero? Think first about which of the three possibilities along the axis where these charges exist. Then set up an equation and solve for the distance away from the negative charge where the field is zero.
 12. I have collected 0.001C of charge on a sheet that has an area of 100 cm^2 . What is the electric field 1 mm away from this sheet? What is it 1 cm away? Is is the same value 1 m away? (*Thing about the inside out versions of this problem too.*)
 13. When I put charge on a large sheet, it is common to refer to the *charge density* of the sheet rather than the total charge and the total area. The charge density, σ is defined like this:

$$\sigma = \frac{Q}{A}.$$

Substitute this into the equation for the electric field of a large charged sheet.

14. You have two large circular sheets of diameter 15 cm. You orient the sheets so they are parallel to one another. Draw a picture of this. Now imagine moving electrons from one plate and placing them on the other plate. If you do this with a billion electrons then how much charge will be on each plate? This kind of device is called a *capacitor* and we will talk more about this next week. What will be the electric field between the plates? What will be the electric field outside of the positive plate? What will be the electric field outside of the negative plate?
15. A capacitor has a charge density of $1 \times 10^{-6} \text{ C/m}^2$. If the positively charged plate is on the left, and the negatively charged plate is on the right and they are separated by a distance of 1 cm. You place a proton in the center between the plates. What electric force does this charge experience? In what direction does it experience the force? What about if this were an electron?
16. Look up the mass of a proton and an electron (book, google, etc). If you were to let go of either the proton or electron in

the previous problem then what would the acceleration of that particle be? Write a general expression for the acceleration of a charged point particle if the electric force is the only force acting on it.

17. You have a capacitor where a total charge of $10 \mu\text{C}$ has moved between the plates, and the plates have an area of 0.01 m^2 . The plates are separated by a distance of 1 cm. If a proton is released from rest from the positive plate, then how fast is it going when it gets to the negative plate?

EXTRAS!

18. A positive and a negative charge will clearly attract on another until they collide, but if you put them perfectly lined up in an electric field, then they will maintain some distance from each other. Draw a uniform electric field that points to the right. Place a negative and positive charge within this field in an arrangement so that the charges will not move (and the force on them is zero). What distance apart are they. Assume it is a proton and an electron.

