

# Newton's Laws

1. Obj at rest remains at rest....

2.  $\vec{F} = \frac{d\vec{p}}{dt} = m\vec{a} \longrightarrow \vec{a} = \frac{d\vec{v}}{dt} \approx \frac{\Delta\vec{v}}{\Delta t}$

3. Action - Reaction

$$\vec{p} = m\vec{v}$$

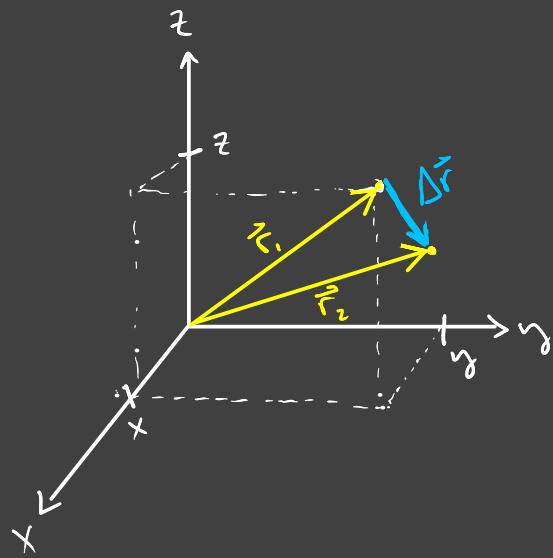
$$\vec{F}_{\text{NET}}$$

velocity  
↓

$$\frac{d\vec{x}}{dt} \approx \frac{\Delta\vec{x}}{\Delta t}$$

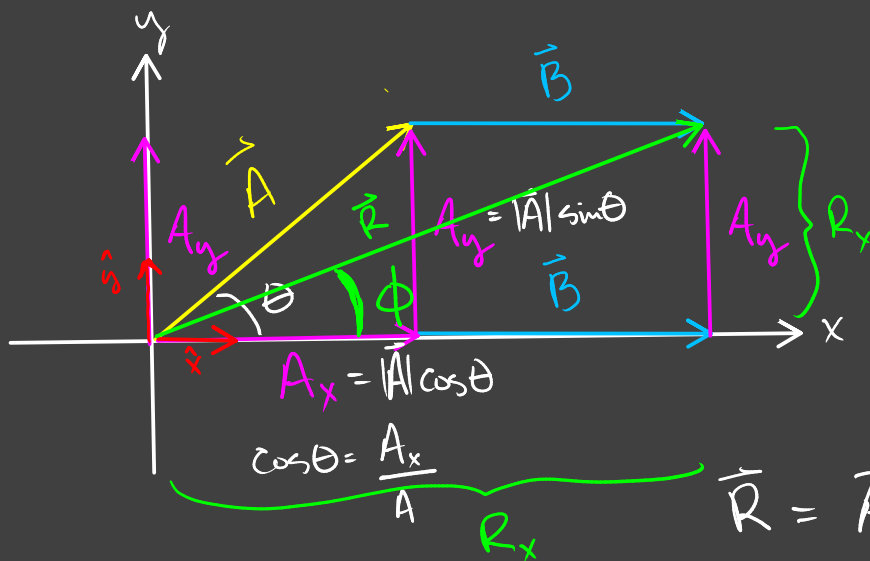
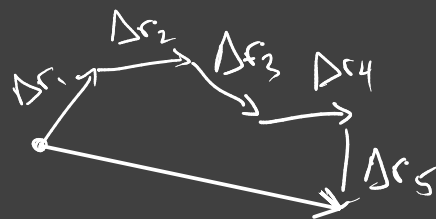
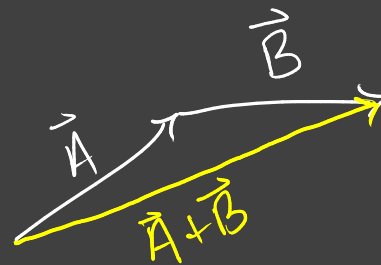
$x \Rightarrow$  position

$$\text{jerk} = \frac{da}{dt}$$



$$\vec{r}_1 + \Delta \vec{r} = \vec{r}_2$$

position  $\Delta$  displacement



$$\vec{A} = A_x \hat{x} + A_y \hat{y}$$

$$\vec{B} = B_x \hat{x} + B_y \hat{y}$$

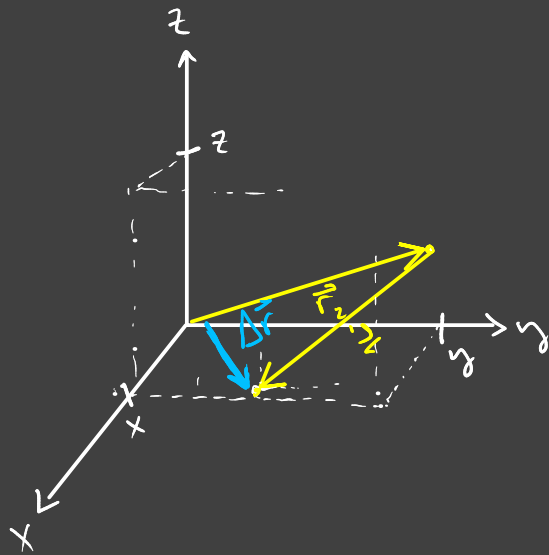
$$\vec{R} = \vec{A} + \vec{B} = \underbrace{(A_x + B_x)}_{R_x} \hat{x} + \underbrace{(A_y + B_y)}_{R_y} \hat{y}$$

$$|\vec{R}| = \sqrt{R_x^2 + R_y^2}$$

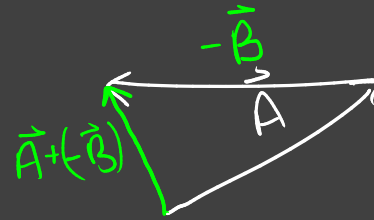
$$\tan \phi = \frac{R_y}{R_x} \sim \phi = \tan^{-1} \left( \frac{R_y}{R_x} \right)$$

	x	y
A:	$A_x$	$A_y$
B:	$B_x$	$B_y$
R:	$R_x$	$R_y$

$$\Delta \vec{r} = \vec{r}_2 - \vec{r}_1$$



$$\vec{A} - \vec{B}$$



$$\vec{A} - \vec{B} = (A_x - B_x)\hat{x} + (A_y - B_y)\hat{y}$$

• scalar multiplication

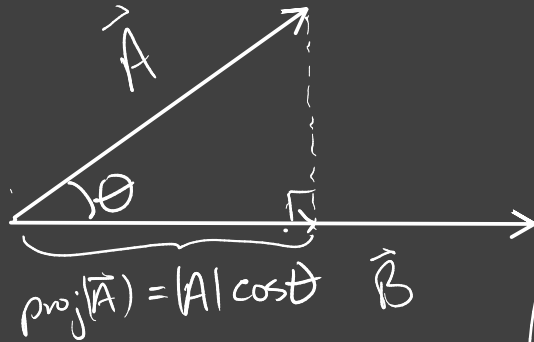
$$c\vec{A} = cA_x\hat{x} + cA_y\hat{y} + cA_z\hat{z}$$

HW: 9, 23, 24, 26, 27, 30, 46, 48

Friday

• dot product / scalar product

$$\vec{A} \cdot \vec{B} = \vec{B} \cdot \vec{A}$$



$$\vec{A} \cdot \vec{B} = |\vec{A}| \cos \theta \cdot |\vec{B}|$$

$$\vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos \theta$$

$$\vec{A} = A_x \hat{x} + A_y \hat{y} + A_z \hat{z}$$

$$\vec{A} \cdot \vec{B} = A_x B_x + A_y B_y + A_z B_z = \vec{B} \cdot \vec{A}$$

$$|\vec{r}| = \sqrt{\vec{r} \cdot \vec{r}} \quad \vec{r}^2 = \vec{r} \cdot \vec{r}$$

• cross product



$$|\vec{A} \times \vec{B}| = |\vec{A}| |\vec{B}| \sin \theta$$

$$\vec{A} \times \vec{B} = -\vec{B} \times \vec{A}$$

$$\vec{A} \times \vec{B} = \begin{vmatrix} \hat{x} & \hat{y} & \hat{z} \\ A_x & A_y & A_z \\ B_x & B_y & B_z \end{vmatrix}$$

$$= (A_y B_z - B_y A_z) \hat{x} - (A_x B_z - B_x A_z) \hat{y} + (A_x B_y - B_x A_y) \hat{z}$$

# Derivative of Vectors

$$\frac{dx}{dt} = \lim_{\Delta t \rightarrow 0} \frac{x(t+\Delta t) - x(t)}{\Delta t}$$

$$\frac{d\vec{r}}{dt} = \lim_{\Delta t \rightarrow 0} \frac{\vec{r}(t+\Delta t) - \vec{r}(t)}{\Delta t}$$

$$\frac{d(\vec{r} + \vec{s})}{dt} = \frac{d\vec{r}}{dt} + \frac{d\vec{s}}{dt}$$

$$\frac{d(f\vec{r})}{dt} = \vec{r} \frac{df}{dt} + f \frac{d\vec{r}}{dt}$$

$$\vec{r} = x\hat{x} + y\hat{y} + z\hat{z}$$

$$\frac{d\vec{r}}{dt} = \frac{dx}{dt}\hat{x} + \frac{dy}{dt}\hat{y} + \frac{dz}{dt}\hat{z} + x \cancel{\frac{d\hat{x}}{dt}} + y \cancel{\frac{d\hat{y}}{dt}} + z \cancel{\frac{d\hat{z}}{dt}}$$

$$\frac{d\vec{r}}{dt} = \frac{dx}{dt} \hat{x} + \frac{dy}{dt} \hat{y} + \frac{dz}{dt} \hat{z}$$

$$\vec{V} = V_x \hat{x} + V_y \hat{y} + V_z \hat{z}$$

$$V_x = \frac{dx}{dt} \quad V_y = \frac{dy}{dt} \quad V_z = \frac{dz}{dt}$$







