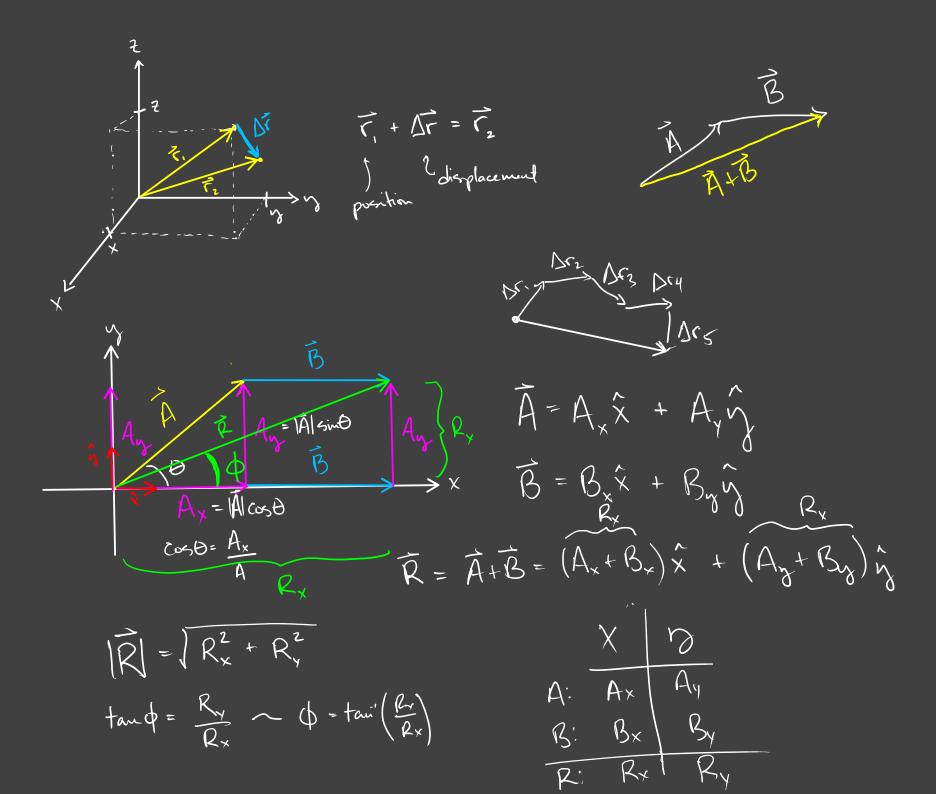
Neuton's Laws velocita 1. Object rest remains at rest....  $2. \implies d\vec{p} = m\vec{a}$ > \( \alpha = \frac{17}{4t} \approx \frac{\Delta \cdot 3. Action - Reaction X => position



$$\Delta \hat{C} = \hat{C}_2 - \hat{C}_1$$

$$\vec{\Lambda} - \vec{R} = (A_x - B_x)\hat{x} + (A_y - B_y)\hat{x}$$

HW: 9,23,24,26,27,30,46,48 Friday

and product / scalar product

$$\vec{A} \cdot \vec{B} = \vec{B} \cdot \vec{A}$$
 $\vec{A} \cdot \vec{B} = |\vec{A}| \cos \theta \cdot |\vec{B}|$ 
 $\vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos \theta$ 
 $\vec{A} \cdot \vec{B} = A_x \hat{x} + A_y \hat{y} + A_z \hat{z}$ 
 $\vec{A} \cdot \vec{B} = A_x \hat{x} + A_y \hat{y} + A_z \hat{z}$ 

· cross product

$$\vec{A} \times \vec{B} = -\vec{B} \times \vec{A}$$

$$\frac{dx}{dt} = \lim_{\Delta t \to 0} \frac{x(t+\Delta t) - x(t)}{\Delta t}$$

$$\frac{d\vec{r}}{dt} = \lim_{\Delta t \to 0} \frac{\vec{r}(t + \Delta t) - \vec{r}(t)}{\Delta t}$$

$$\frac{J(r+3)}{Jt} = \frac{Jr}{Jt} + \frac{Js}{Jt}$$

$$\frac{d(f\vec{r})}{dt} = \vec{r} \frac{df}{dt} + f \cdot \frac{d\vec{r}}{dt}$$

$$\vec{r} = \chi \dot{\chi} + \chi \dot{\chi} + 7 \ddot{\chi}$$

$$\frac{d\hat{r}}{dt} = \frac{dx}{dt}\hat{x} + \frac{dy}{dt}\hat{y} + \frac{dz}{dt}\hat{z} + x\frac{d\hat{x}}{dt} + y\frac{d\hat{y}}{dt} + z\frac{d\hat{z}}{dt}$$

$$\frac{dx}{dt} = \frac{dx}{dt} x + \frac{dy}{dt} y + \frac{1}{2} x^{2}$$

$$\overrightarrow{V} = V_{x} x + V_{y} y + V_{z} z$$

$$V_{x} = \frac{dx}{dt} \qquad V_{y} = \frac{dx}{dt} \qquad V_{z} = \frac{dz}{dt}$$

3. 
$$\vec{F}_{12} = -\vec{F}_{21}$$

1st - Newton's Law hold in inertial reference frames dè = m di t  $\frac{2^{nd}}{2^{nd}} = \frac{1}{\sqrt{2}} = \frac{1}{\sqrt{2}}$  $\frac{d\hat{r}}{dt} = \hat{r} = \bar{V}$  $\frac{d\vec{v}}{dt} = \vec{v} = \vec{a}$  $\frac{d\vec{p}}{dt} = \vec{p} = \vec{F} = m\vec{v} = m\vec{r}$ 

$$\vec{F} = M\vec{F}$$

$$\vec{F} = F_{X}\hat{X}$$

$$\vec{F} = F_{$$

$$\dot{X} = \frac{F_{x}}{m} + V_{xo}$$

$$X = \int \frac{dx}{dt} dt \qquad X = \int \dot{x} dt = \int \left( \frac{F_x}{m} t + V_{xo} \right) dt$$

$$\Rightarrow x = \frac{F_x}{m} t dt + V_{xo} dt$$

$$\chi = \frac{1}{2} \cdot \sum_{m} \cdot t^2 + v_{xo}t + D$$

$$\Rightarrow X(t) = \frac{1}{2} \sum_{i=1}^{k} t^2 + V_{xi} \cdot t + X_{si}$$

3rd F=-F21; force occur in pairs

$$\vec{F} = \vec{F}_{12} + \vec{F}_{12} = \hat{\rho}$$

$$\overrightarrow{F}_1 = \overrightarrow{F}_{12} + \overrightarrow{F}_{12} = \overrightarrow{\rho}_1$$
 $\overrightarrow{F}_2 = \overrightarrow{F}_{21} + \overrightarrow{F}_{22} = \overrightarrow{\rho}_2$ 

$$\overrightarrow{P} = \overrightarrow{p}_1 + \overrightarrow{p}_2$$

$$\overrightarrow{P} = \overrightarrow{p}_1 + \overrightarrow{p}_2$$

$$\overrightarrow{P} = \overrightarrow{F}_{12} + \overrightarrow{F}_{2x} + \overrightarrow{F}_{2x} + \overrightarrow{F}_{2x}$$

$$\overrightarrow{P} = \overrightarrow{F}_{2x} + \overrightarrow{F}_{2x} + \overrightarrow{F}_{2x}$$

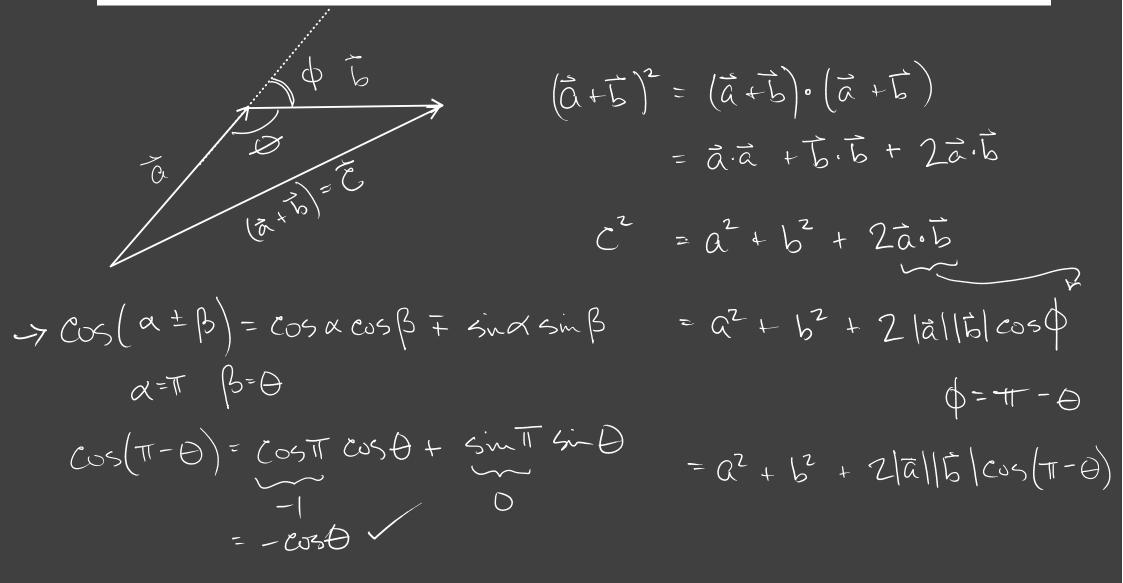
$$\overrightarrow{P} = \overrightarrow{F}_{2x} + \overrightarrow{F}_{2x} + \overrightarrow{F}_{2x}$$

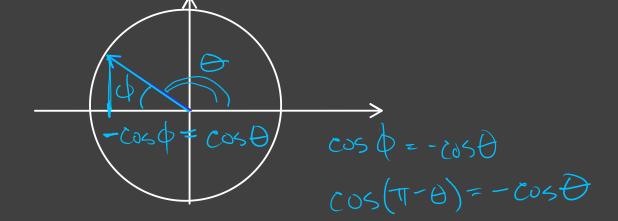
$$\overrightarrow{P} = \overrightarrow{F}_{2x} + \overrightarrow{F}_{2x} + \overrightarrow{F}_{2x} + \overrightarrow{F}_{2x}$$

$$\overrightarrow{P} = \overrightarrow{F}_{2x} + \overrightarrow{F}_{2x} + \overrightarrow{F}_{2x} + \overrightarrow{F}_{2x} + \overrightarrow{F}_{2x}$$

$$\overrightarrow{P} = \overrightarrow{F}_{2x} + \overrightarrow{F}_{2x$$

1.9 ★ In elementary trigonometry, you probably learned the law of cosines for a triangle of sides a, b, and c, that  $c^2 = a^2 + b^2 - 2ab\cos\theta$ , where  $\theta$  is the angle between the sides a and b. Show that the law of cosines is an immediate consequence of the identity  $(\mathbf{a} + \mathbf{b})^2 = a^2 + b^2 + 2\mathbf{a} \cdot \mathbf{b}$ .





1.23 **\*\*** The unknown vector **v** satisfies  $\mathbf{b} \cdot \mathbf{v} = \lambda$  and  $\mathbf{b} \times \mathbf{v} = \mathbf{c}$ , where  $\lambda$ , **b**, and **c** are fixed and known. Find **v** in terms of  $\lambda$ , **b**, and **c**.

$$\vec{A} \times (\vec{B} \times \vec{c}) = (\vec{A} \cdot \vec{c}) \vec{B} - (\vec{A} \cdot \vec{B}) \vec{c}$$

$$\hat{b} \times (\hat{b} \times \hat{v}) = (\hat{b} \cdot \hat{v}) \hat{b} - (\hat{b} \cdot \hat{b}) \hat{v} = \hat{b} \times \hat{c}$$

$$\vec{V} = \frac{\lambda \vec{b} - \vec{b} \times \vec{c}}{b^2}$$

24

- 1.24  $\star$  In case you haven't studied any differential equations before, I shall be introducing the necessary ideas as needed. Here is a simple excercise to get you started: Find the general solution of the first-order equation df/dt = f for an unknown function f(t). [There are several ways to do this. One is to rewrite the equation as df/f = dt and then integrate both sides.] How many arbitrary constants does the general solution contain? [Your answer should illustrate the important general theorem that the solution to any *n*th-order differential equation (in a very large class of "reasonable" equations) contains n arbitrary constants.]
- 1.25 ★ Answer the same questions as in Problem 1.24, but for the differential equation df/dt = -3f.

$$\frac{df}{dt} = f$$

$$\int \frac{df}{dt} = f$$

$$\int \frac{df}{dt} = f$$

$$\int \frac{df}{dt} = f$$

$$\int \frac{df}{dt} = f$$

$$= -3t + C$$

$$e$$

$$\int \frac{df}{dt} = f$$

$$= -3t + C$$

$$e$$

$$f(t=0) = A$$

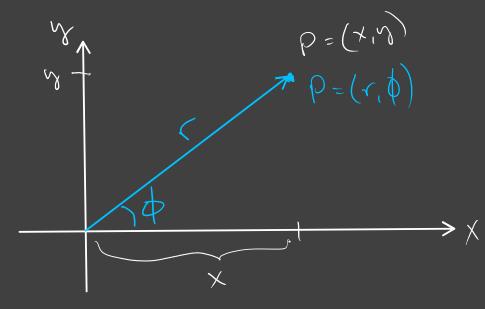
$$\frac{df}{dt} = At \implies f = \frac{At^2}{2}t^2 + C$$

$$\Rightarrow \frac{df}{df} = f$$

$$\Delta f = \frac{df}{dt} \cdot \Delta t$$

$$\frac{d}{dt} = e^{t}$$

Paar Coordinates

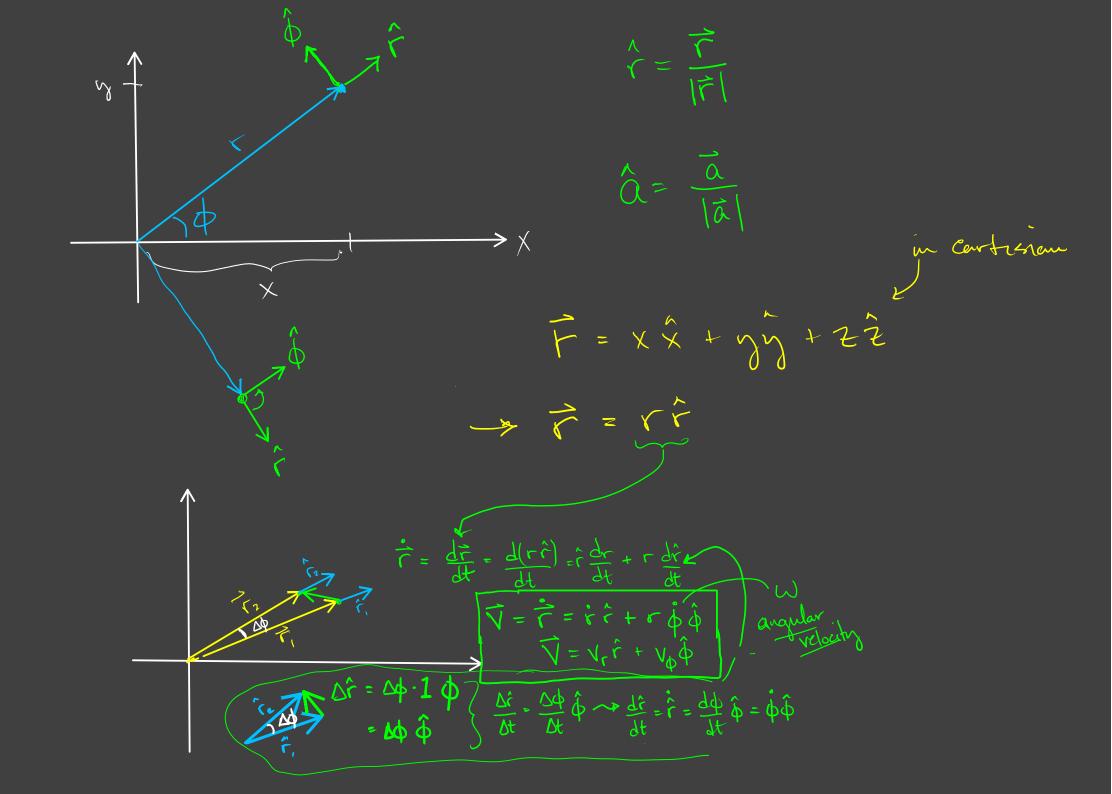


$$\varphi = \sqrt{x^2 + y^2}$$

$$\varphi = \tan(x)$$

$$\chi = r \cos \varphi$$

$$\chi = r \sin \varphi$$



$$A = \phi \cdot C$$
 $A = \alpha \cdot C$ 
 $A =$ 

Now for acceleration

$$= \frac{d}{dt}(\hat{r}\hat{r}) + \frac{d}{dt}(r\hat{\phi}\hat{\phi})$$

$$= \ddot{\hat{r}} + \ddot{\tilde{r}} + \ddot{$$

$$\overline{Q} = \overline{r} = (r - r \dot{\phi}^2) \hat{r} + (2r\dot{\phi} + r \dot{\phi}) \hat{\phi}$$

$$\frac{1}{2} = \frac{1}{4} = \frac{1$$

special each of coverlent (, 
$$\dot{r} = 0$$
,  $\dot{r} = 0$ )
$$\dot{r} = -r \dot{\phi}^2 \dot{r} + r \dot{\phi} \dot{\phi}$$

$$\dot{r} = m \dot{r} = -m r \omega^2 \dot{r} + m r d \dot{\phi}$$

$$centripetal torque$$
force

Newton's 
$$2^{n2}$$
 (polar)
$$\vec{F} = m(\ddot{r} - r\dot{\phi}^2)\hat{r} + m(2\dot{r}\dot{\phi} + r\dot{\phi})\hat{\phi}$$

$$\vec{F}_r = m(\ddot{r} - r\dot{\phi}^2)$$

$$\vec{F}_{\phi} = m(2\dot{r}\dot{\phi} + r\dot{\phi})$$

time for one complete trip > period

$$\vec{F} = m\vec{r} = -mr\dot{\phi}^2 \hat{r} + mr\dot{\phi}\dot{\phi}$$

$$rot force$$

$$\vec{F} = Z\vec{F}$$

$$F_{NET,R} = -F_T + majors \dot{\phi}$$

$$F_{NET,R} = -mr\dot{\phi}^2 \hat{r} + mr\dot{\phi}\dot{\phi}$$

$$(-F_T + majors \dot{\phi})\hat{r} + (-major \dot{\phi})\hat{\phi} = -mr\dot{\phi}^2 \hat{r} + mr\dot{\phi}\dot{\phi}$$

$$-F_{\tau} + macos \phi = -mr \dot{\phi}^{2}$$

$$-macos \phi = mr \dot{\phi}$$

$$\phi = -9 \sin \phi$$

$$\phi = +9 \int \sin \phi dt$$

$$\phi_z = \phi, + \phi \cdot \Delta t$$

$$\phi_z = \phi, + \phi \cdot \Delta t$$

$$\sin \phi \approx \phi$$

$$\sin \phi \approx \phi$$

$$\phi = -3 \sin \phi$$

$$\sin \phi = \phi - 0^3 + \phi$$

$$\sin \phi \approx \phi$$

$$\phi = -3 \sin \phi$$