Chapter 6 +7 -> Principle of Least Action and the Lagrangian Lagrangian Hamiltonian

("sgeneralized coordinates" Newton's Laws La Principle of Least Action $T = \frac{1}{2}mv^2 = \frac{1}{2}m\dot{x}^2$ Lacrangian L = T - U U = max $\frac{\text{Action}}{2} = \int_{-\infty}^{+\infty} \mathcal{L}(x(t), \dot{x}(t), t) dt$ $\int_{t_1}^{t_2} \left(\frac{1}{2} m \dot{x}^2 - m a x \right) dt$ what is x(t) and $\dot{x}(t)$ so this integral is smallest $= \int_{1}^{t_{1}} \chi(x,\dot{x},t) dt$

$$\frac{d}{dt}\left(\frac{\partial \mathcal{L}}{\partial \dot{x}}\right) - \frac{\partial \mathcal{L}}{\partial x} = 0$$

$$\frac{d}{dt}\left(\frac{\partial \mathcal{L}}{\partial \dot{x}}\right) = \frac{\partial \mathcal{L}}{\partial x}$$

Euler - Lagranger Equation

$$= \frac{1}{2} m \left(\dot{x}^2 + \dot{y}^2 + \dot{z}^2 \right) = \frac{1}{2} m V^2$$

$$\mathcal{L} = \frac{1}{2}m\dot{x}^2 - U(x)$$

$$\frac{d}{dt}\left(\frac{\partial \mathcal{L}}{\partial \dot{x}}\right) = \frac{\partial \mathcal{L}}{\partial x}$$

$$\frac{d}{dt} \left(\frac{\partial x}{\partial x} \left(\frac{1}{2} m \dot{x}^2 - U(x) \right) \right) = \frac{\partial x}{\partial x} \left(\frac{1}{2} m \dot{x}^2 - U(x) \right)$$

$$\frac{d}{dt} \left(m \dot{x} \right) = -\frac{dU}{dx}$$

$$m\ddot{x} = -\frac{dl}{dx}$$

$$m\ddot{y} = -\frac{dl}{dt}$$

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$$m\ddot{y} = -\frac{dl}{dt}$$

$$m\ddot{z} = -\frac{dl}{dt}$$

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$$m\ddot{x} \hat{x} + m\ddot{y}\hat{y} + m\ddot{z}\hat{z} = -\frac{3U}{3x}\hat{x} - \frac{3U}{3y}\hat{y} - \frac{3U}{3z}\hat{z}$$

$$S\ddot{F} = m\ddot{r} = -\vec{\nabla}U = S\ddot{F}$$

V=rw
$$V = rw$$

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$$V = \frac{1}{2}mv^2 - magh$$

$$V = \frac{1}{2}mv^2 + magh$$

$$V = \frac{1}{2}m$$

$$\frac{\partial \mathcal{L}}{\partial \dot{\phi}} = \frac{1}{2} m \ell^2 (2\dot{\phi}) = m \ell^2 \dot{\phi}$$

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$$\frac{\partial \mathcal{L}}{\partial \dot{\phi}} = \frac{1}{2} (m \ell^2 \dot{\phi}) = m \ell^2 \dot{\phi}$$

$$= -mg \ell \sin \phi$$

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$$\dot{\phi} = -\frac{9}{2}\sin\phi$$

$$ml^{2}\dot{\phi} = -malsin\phi$$

$$\dot{\phi} = -3 \sin\phi$$

$$\frac{d}{dt}\left(\frac{\partial \mathcal{L}}{\partial \dot{x}}\right) = \frac{\partial \mathcal{L}}{\partial x}$$
Remember small angle
approx Sint $\approx \phi$

$$\frac{1}{2}\left(\frac{3}{2}\right) = \frac{3}{2}$$

$$\frac{\partial \mathcal{L}}{\partial \dot{\phi}} = m(l+x)^2 \dot{\phi}$$

$$\frac{1}{dt}\left(\frac{\partial I}{\partial \dot{\phi}}\right) = m(l+x)^{2}\dot{\phi} + m2(l+x)\dot{x}\dot{\phi}$$

$$\frac{1}{4}\left(\frac{\partial k}{\partial k}\right) = M\ddot{x}$$

$$\frac{\partial L}{\partial x} = m(l+x)\dot{\phi}^2 + mg\cos\phi - kx$$

$$(1+x)\ddot{\phi} + 2\dot{x}\dot{\phi} + gcom\dot{\phi} = 0$$

$$m\ddot{x} = m(l+x)\dot{\phi}^2 + mg\cos\phi - kx$$

$$\ddot{X} = (1+x)\dot{\phi}^2 + g\cos\phi - \frac{L}{m}X$$