Electrostatics
· what Forces

· what forces are on therais?

· what gives rien to those forus?

· how much energy can be stoved (released)?

Cheran -> concarration of charge -> in an isolated system
the total electric charge herer
changes

Je quantization of charge

charge of an electron/proton is the smallest isolated

charge —> e (elementary charge)

q is variable for charge

SI unit for charge is Coulomb
$$|e = 1.602... \times 10^{-19} \text{ C}$$

$$|C = \frac{1}{1.602 \cdot 10^{-19}} = 6.242 \cdot 10^{5} \text{ e}$$

So now to electrostatics:

The fore between $q_1 + q_2$ is directly proportional to

the product of charge and

inversely proportional to

the equan of the distance

between them. $= k q_1 q_2 \hat{r}^2$ product

between them.

F₂₁ = k 9, 92 r₂₁ 3 product

 $\frac{1}{\sqrt{2}} = \frac{1}{2} = \frac$

What about more than two charge?

[®] Gz

How do we do work? W = Force o displacement W = JF dt product mean relative directions of form and displacement matter Work I / Where force is zero I have to pur against the I have to puch against the Coulomb force (equal topposite)

$$W = -kq_1q_2 \int_{\infty}^{r_2} \hat{r} \cdot \hat{r} dr$$

$$V = -kq_1q_2 \int_{\infty}^{r_2} r^2 dr$$

$$W = -kq_1q_2 \left(-1\right) r^{-1} \Big|_{\infty}^{r_2}$$

$$W = \frac{kq_1q_2}{r} \Big|_{\infty}^{r_2}$$

$$= \frac{kq_1q_2}{r} \Big|_{\infty}^{r_2}$$

$$= \frac{kq_1q_2}{r} \int_{\infty}^{r_2} r^2 dr$$

Now, is this electric form conservative? La what does this mean -> path independent La only depends on position → DXF=0 - San For later rdô d's back and forth are the same amont of Work this is perpendicular to the force so the only the radial part of the motion dot product would be Zero contributes to the work so only radial position watters

How do we handle multph charges

 $q_3 = \overline{F}_{31} + \overline{F}_{32}$

Gz

So the total work is:

W_ = W21 + W31 + W32

Wr = kg,g2 + kg,g3 + kg2g3

(32

So I have done work to build this charge distribution. $W_3 = \int \overrightarrow{F_3} \cdot d\overrightarrow{r}$ $W_3 = \int (\overrightarrow{F_{32}} + \overrightarrow{F_{31}}) \cdot d\overrightarrow{r}$ $W_3 = \int \overrightarrow{F_{32}} \cdot d\overrightarrow{r} + \int \overrightarrow{F_{31}} \cdot d\overrightarrow{r}$

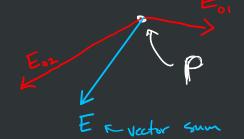
W3= W32 + W31

Potential Energy is in the system. Vext = - Wents independent of the order that the charges
were assumbled Back to two charges: U=-kg.gz -> plot this -> (,2 | U=0, ~,2→6

Electric Field > form per unit of charge

$$\vec{E} = \vec{F} \Rightarrow \vec{F} = q_2 \vec{E}$$

$$\widehat{E}(x,y,z) = \frac{1}{4\pi\epsilon_0} \sum_{j=1}^{N} \frac{q_j \hat{c}_{ij}}{r_{ij}^2}$$



How do we generalize to a continuous distribution of charge?

Charge density
$$\Rightarrow dq = p dV$$

"rho"

 $E(x,y,z) = \frac{1}{4\pi\epsilon_0} \sum_{j=1}^{N} \frac{q_j \hat{r}_j}{r_j^2}$
 $E(x,y,z) = \frac{1}{4\pi\epsilon_0} \int_{r_2}^{r_2} \frac{dq}{r_2} \hat{r}$
 $E(x,y,z) = \frac{1}{4\pi\epsilon_0} \int_{r_2}^{r_2} \frac{dq}{r_2} \hat{r}$

$$\frac{dV = dr(rd\theta)dz}{dV = rdrd\phi dz}$$

$$\frac{dV = dr(rd\theta)(rd\theta d\phi)}{dV = r^2 \sin\theta drd\theta d\phi}$$

HW: 35,36,40,42,49,63c,65,77

35) Me= 9.10³¹ kg

Fa= m.a weight

Fa= 9.10³¹ kg. 9.8 N = Kg

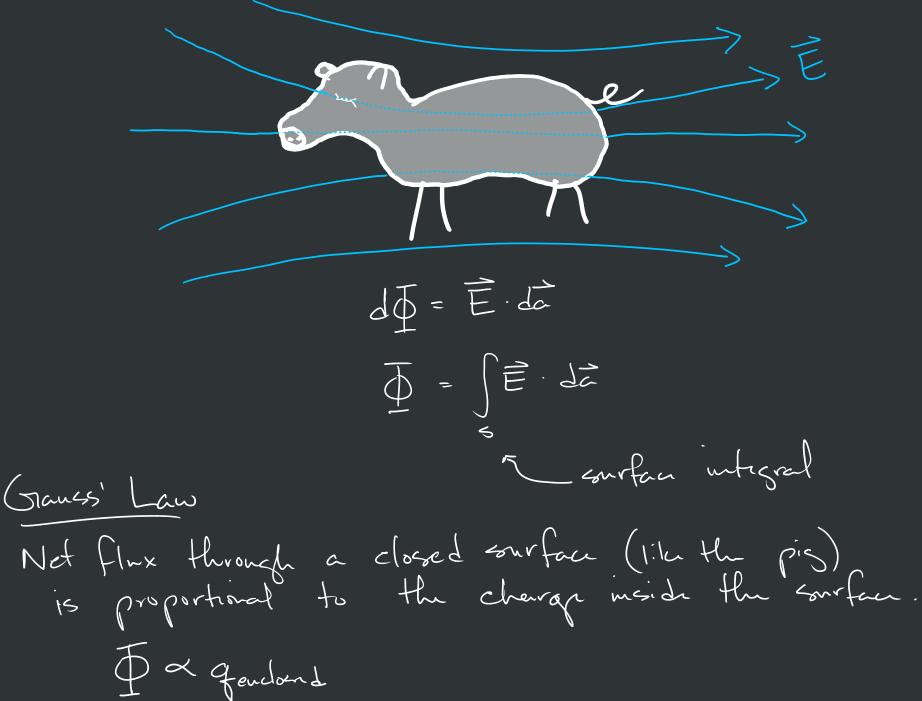
F= kggz

Flux

rector field-function that outputs a vector

| = = = a

| dot product



Pagendond

F = gencland

Go

Lets check! w/ a point charge Ë= 90 γ Sphinial coordinates

4πεο Γ² W/ 90 at the origin do rsiddo $\Phi = \int_{C} \vec{E} \cdot d\vec{e} d\vec{e}$ Janessian Ganessian $\overline{\Phi} = \left(\frac{q}{4\pi c}, \frac{dc}{2}\right)$ D= Go J 2TT R UTTEO J J ZZ SINO 2010 D da = da r È.da = qor ATTESTZ. dar T= Go Sinododo

T= Go Sinodo 27 UTEO Sinodo do Solo SETOKZ -cost = 2T - COST - - COS D -(-1) - -(+1)MYDIPOT point cherrys U O YX limited to This is not endond 7 gend = PdV endond gender endond W

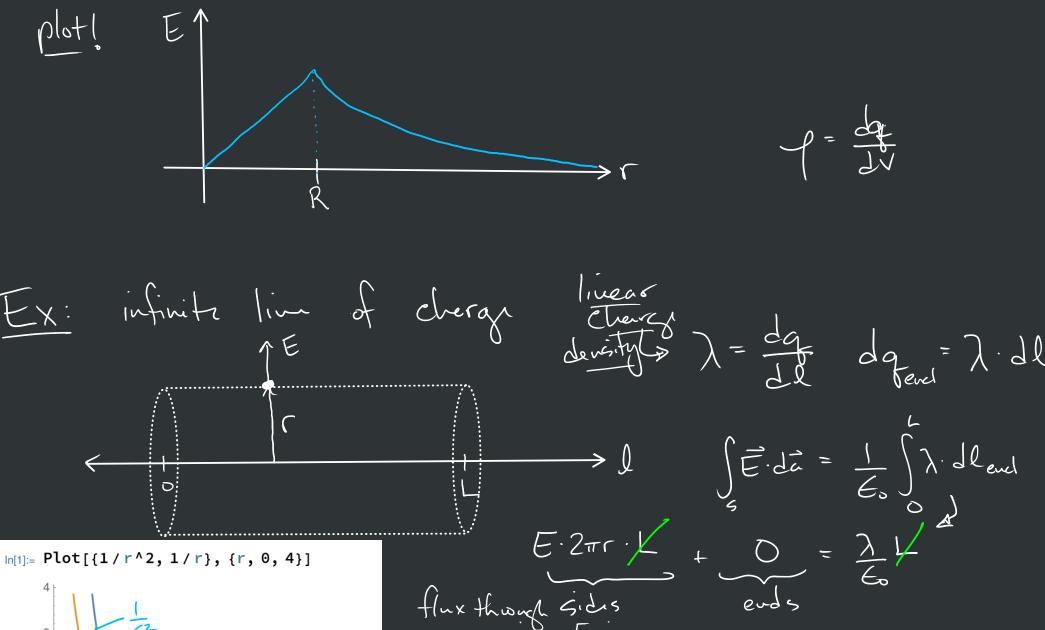
we have a sphen of uniform thuran density what is the electric field inside to outside the outside the sphere: r>R Sphere

E. ATTZ = P J Dend = PV 4TR3

E. ATT = 7. 4TR Inside the sphen: (rLR)

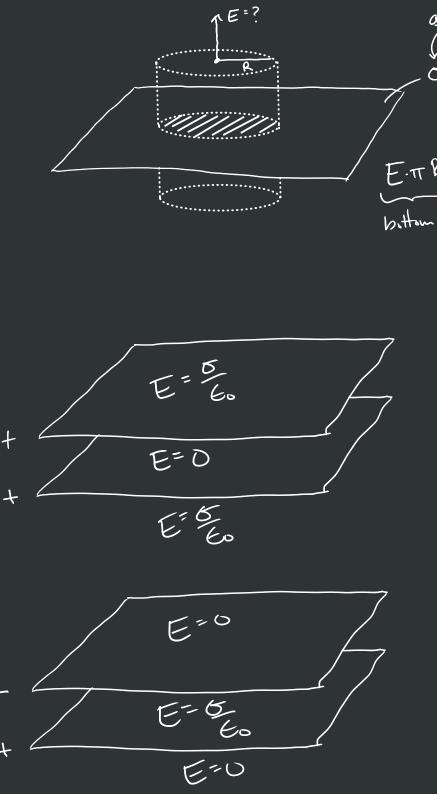
JE. dà = 1 Spellend E. At 52 = 2 43 11/3 E = 36. E= fr 36. (2 E. ATT = Qend Eo

E=Q ATE 12



flux through sides accommende E is I to the sides

E =
$$\frac{\lambda}{2\pi\epsilon_0}$$

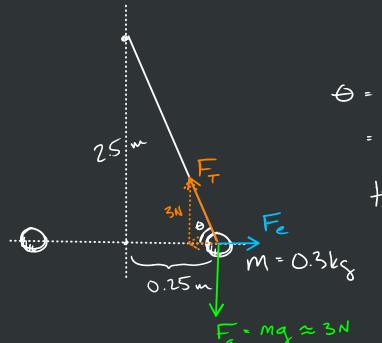


$$E \cdot \pi \ell^2 + E \cdot \pi \ell^2 + O = \frac{\sigma}{\varepsilon} \pi \ell^2$$
bithom
$$E \cdot 2\pi \ell^2 = \frac{\sigma}{\varepsilon} \pi \ell^2$$

$$E \cdot 2\pi \ell^2 = \frac{\sigma}{\varepsilon} \pi \ell^2$$

$$E = \frac{\sigma}{2\varepsilon} = \frac{\sigma}{2\varepsilon} \pi \ell^2$$

Homework



$$\Theta = \tan^{1}\left(\frac{2.5}{0.25}\right)$$

$$= 84 \text{ ish}^{\circ}$$

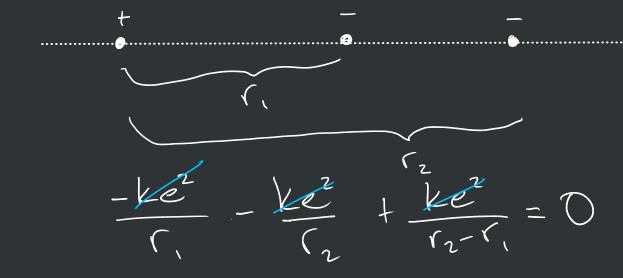
$$+ \text{cm } 84 \text{ ish} =$$

$$F_{e} = \frac{kq^{2}}{r^{2}}$$

$$0.32N = \frac{kq^{2}}{(0.5)^{2}}$$

$$Q = \frac{0.32N(0.5)^{2}}{9.10^{5}}$$

$$Q = \frac{3.10^{6}C}{3mC}$$



$$-\frac{1}{r_1} - \frac{1}{r_2} + \frac{1}{r_2 - r_1} = 0$$

$$\frac{1}{r_2 - r_1} = \frac{1}{r_1(r_2)} \frac{1}{r_2(r_1)}$$

$$\frac{1}{r_2 - r_1} = \frac{r_2}{r_1(r_2)} + \frac{r_1}{r_1(r_2)} = \frac{r_2 + r_1}{r_1(r_2)}$$

$$\frac{1}{r_2 - r_1} = \frac{r_2 + r_1}{r_1(r_2)}$$

$$\frac{1}{r_1(r_2)} = \frac{r_2}{r_1(r_2)}$$

$$\frac{1}{r_1(r_2)} = \frac{r_2}{r_1(r_2)}$$

$$\frac{r_1(r_2)}{r_1(r_2)} = \frac{r_2}{r_1(r_2)}$$

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$$\frac{r_1(r_2)}{r_1(r_2)} = \frac{r_2}{r_1(r_2)}$$

HINT:
$$\ln(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \dots$$

$$-\frac{2 ke^2}{a} + \frac{ke^2}{2a} - \frac{ke^2}{3a} + \frac{ke^2}{2a} - \frac{ke^2}{a}$$

$$\frac{U = -ke^{2}}{N} \left(\frac{N-1}{1} - \frac{N-2}{2} + \frac{N-3}{3} - \frac{N-4}{4} + \dots \right)$$

$$= -\frac{|Ce^{2}|}{Nc} \left(\frac{N-1}{1} - \frac{N}{2} + \frac{2}{2} + \frac{N}{3} - \frac{3}{3} - \frac{N}{4} + \frac{4}{4} + \dots \right)$$

$$= -\frac{ke^{2}}{a} \left(1 - \frac{1}{2} + \frac{1}{3} - \frac{1}{4} + \dots \right)$$

$$= -\frac{ke^{2}}{a} \left(1 - \frac{1}{2} + \frac{1}{3} - \frac{1}{4} + \dots \right)$$

$$= -\frac{1}{2} + \frac{1}{3} - \frac{1}{4} + \dots$$

HINT:
$$\ln(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \dots$$

$$\frac{U}{N} = -\frac{kc^2}{a} \ln(2)$$

$$\alpha = \frac{dy}{dt}$$

$$Q = \frac{dv}{dr} \frac{dr}{dt}$$

$$\frac{a}{V} = \frac{dv}{dr}$$

$$a dr = V dv$$

$$\int_{\infty}^{R} dr = \int_{\infty}^{R} v dv$$

$$= \frac{1}{2}v^{2} |_{\infty}$$

$$= \frac{1}{2}v^{2}$$

$$= \frac{1}{2}v^{2}$$