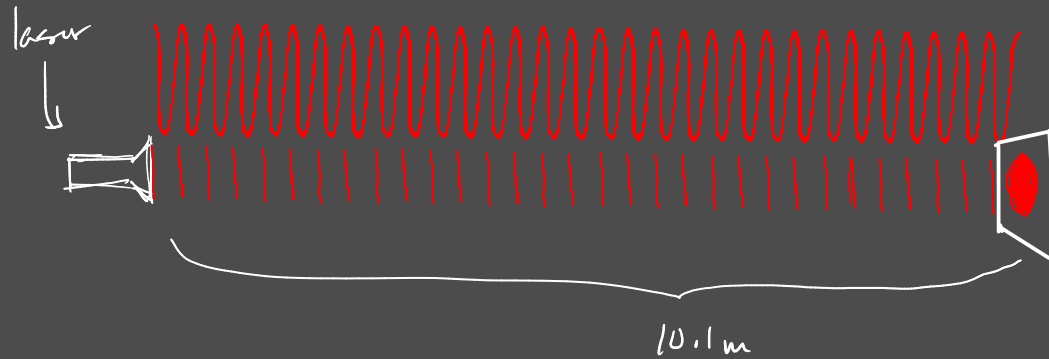


Diffraction and Interference - Chapter 7

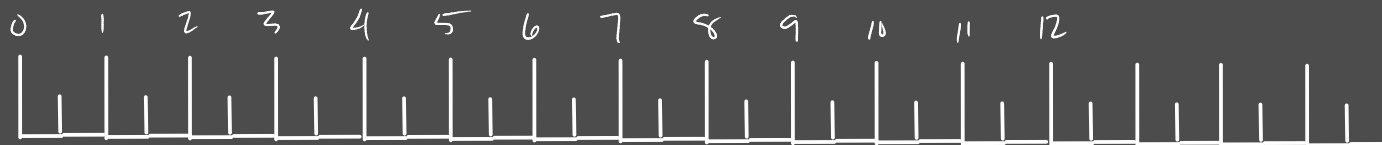
coherent light - single wavelength
- every part of the beam is "in phase" or lined up with itself

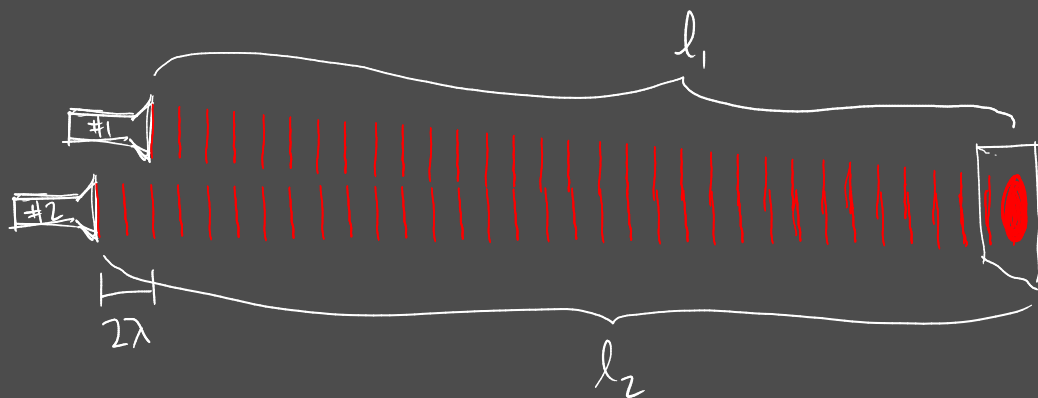
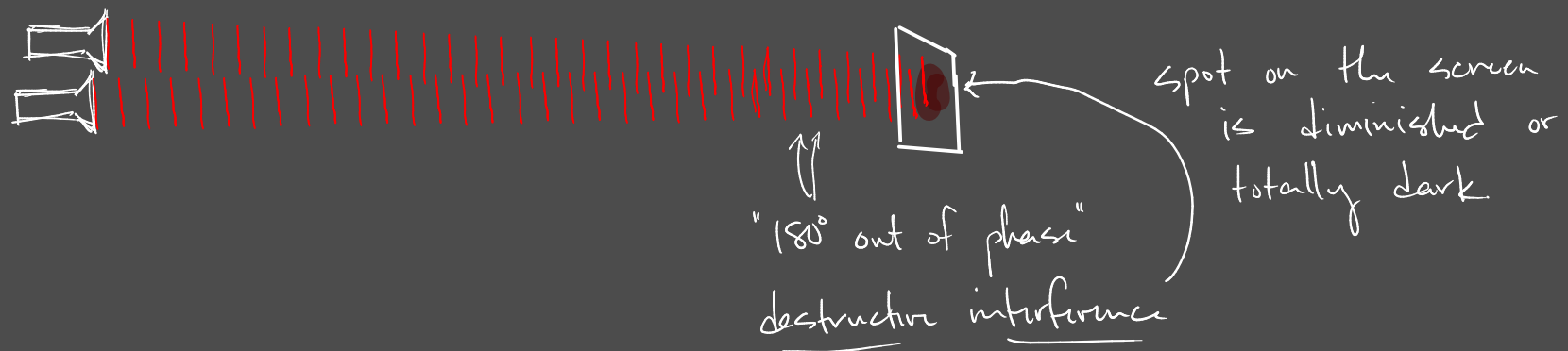
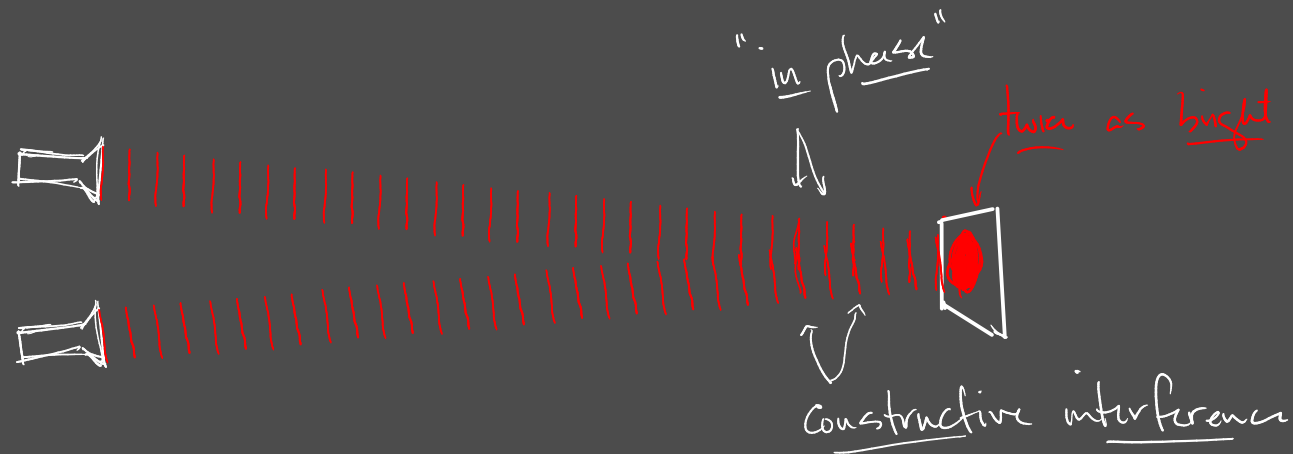


$$\lambda = 0.33 \text{ m}$$

How many λ 's fit bet the laser & the screen?

$$\frac{\text{total distance}}{\text{a wavelength}} = \# \text{ of wavelengths} = \frac{10.1 \text{ m}}{0.33 \text{ m}} = \underline{\underline{30.6}} \approx 31 \leftarrow \text{Counted}$$





Constructive interference

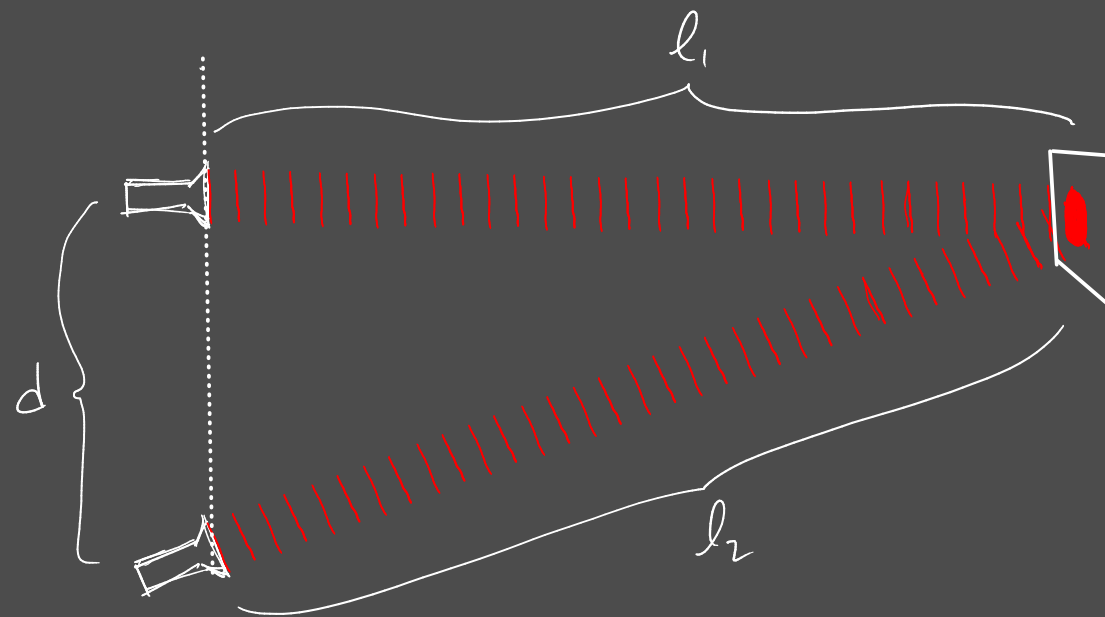
$$\Delta l = l_2 - l_1 = m \cdot \lambda$$

$$m = 0, 1, 2, 3, \dots$$

destructive interference

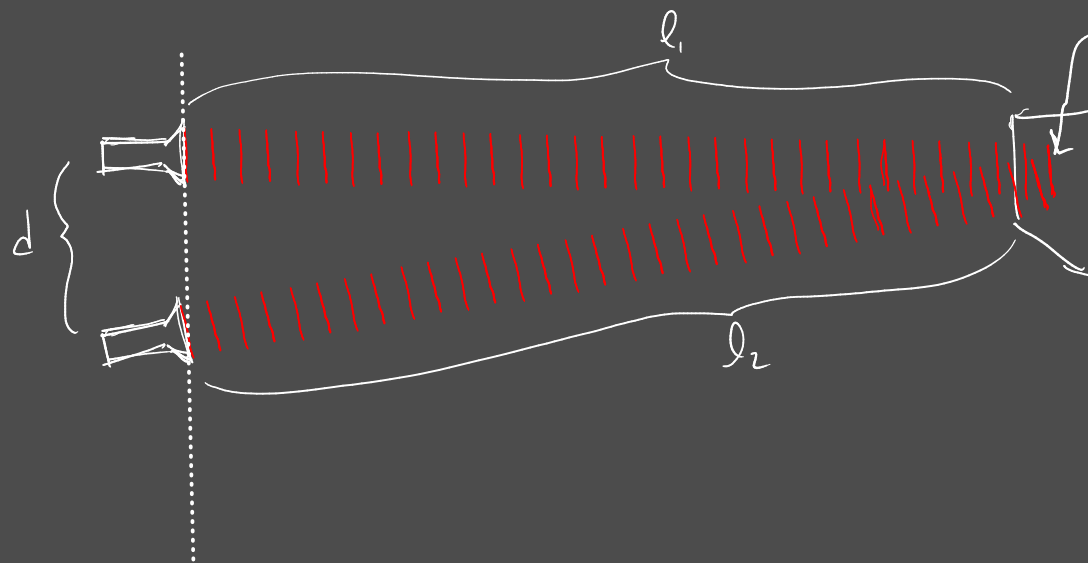
$$\Delta l = l_2 - l_1 = (m + \frac{1}{2}) \cdot \lambda$$

$$m = 0, 1, 2, 3, \dots$$



constructive interference

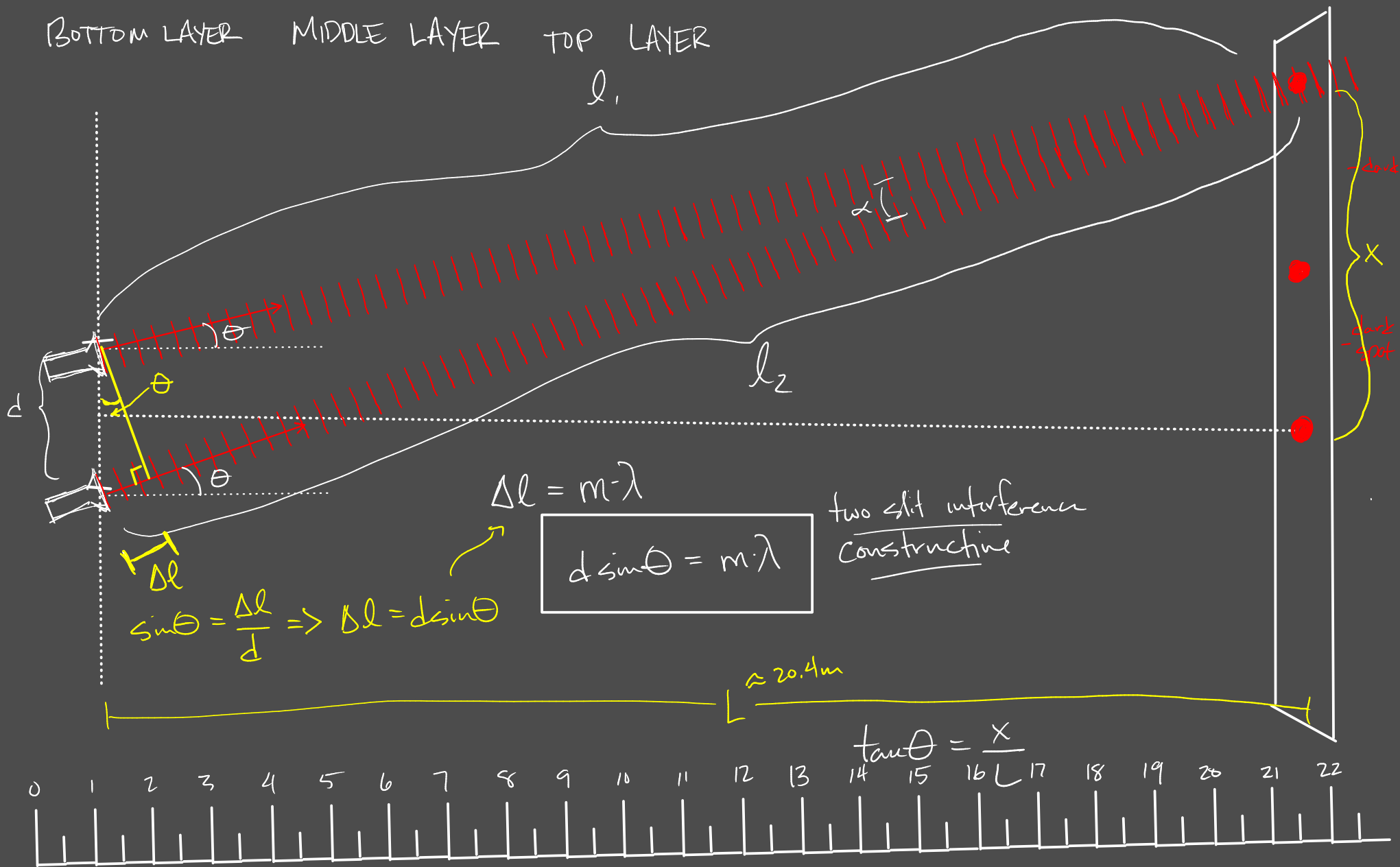
$$l_2 - l_1 = m \cdot \lambda$$



destructive interference

$$l_1 - l_2 = (m + \frac{1}{2}) \lambda$$

BOTTOM LAYER MIDDLE LAYER TOP LAYER



$$\Delta l = m \cdot \lambda$$

$$d \sin \theta = m \cdot \lambda$$

two slit interference
Constructive

$$\sin \theta = \frac{\Delta l}{d} \Rightarrow \Delta l = d \sin \theta$$

$$\tan \theta = \frac{X}{L}$$

$$X = L \tan \theta$$

$$X = 20.4 \tan(15.3^\circ)$$

$$X = 5.6\text{m} \approx 5.9\text{m}$$

$$\sin \theta = \frac{m \lambda}{d}$$

$$\theta = \sin^{-1}\left(\frac{2 \cdot 0.33\text{m}}{2.5\text{m}}\right) = 15.3^\circ$$

$$l_1 = 20.8\text{m}$$

$$l_2 = 21.5$$

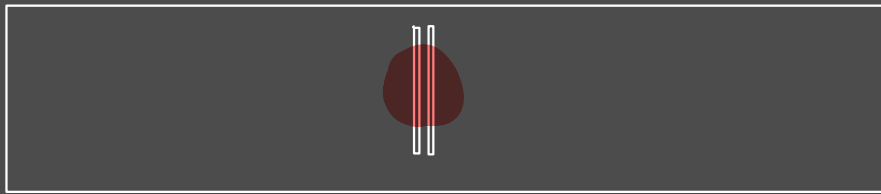
$$l_2 - l_1 = 0.7\text{m} \stackrel{?}{=} 2 \cdot \lambda$$

$$3\lambda = 1\text{m}$$

$$\lambda = \frac{1}{3}\text{m} = \underline{\underline{0.33}}$$

$$0.7 \approx 0.67$$

double slit



constructive interference

$$d \sin \theta = m \lambda$$

$$\tan \theta = \frac{x}{L}$$

small angle approximation

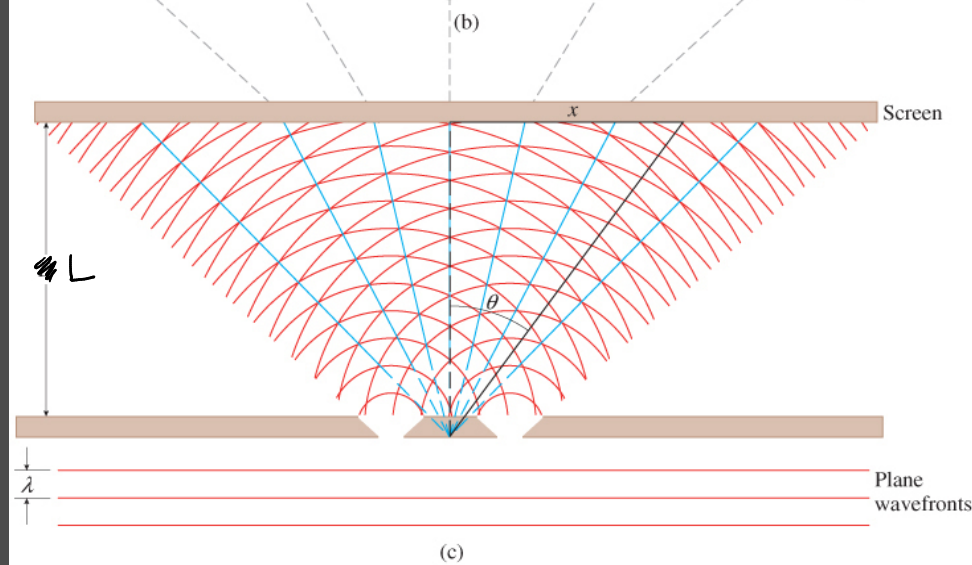
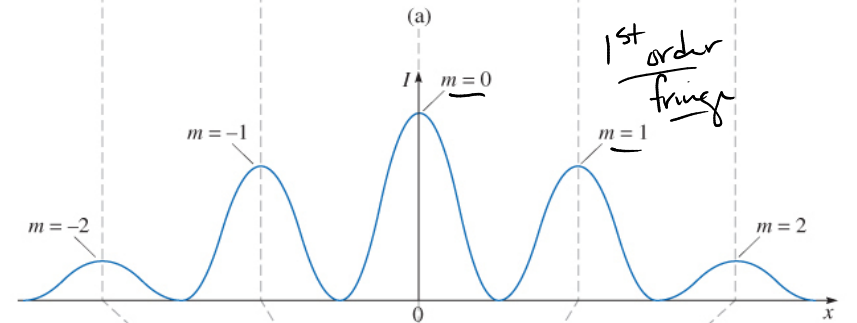
when θ is small

$$\tan \theta \approx \sin \theta \approx \theta$$

$$d \sin \theta = m \lambda$$

$$d \cdot \frac{x}{L} = m \lambda$$

double slit constructive interference
small angle approximation



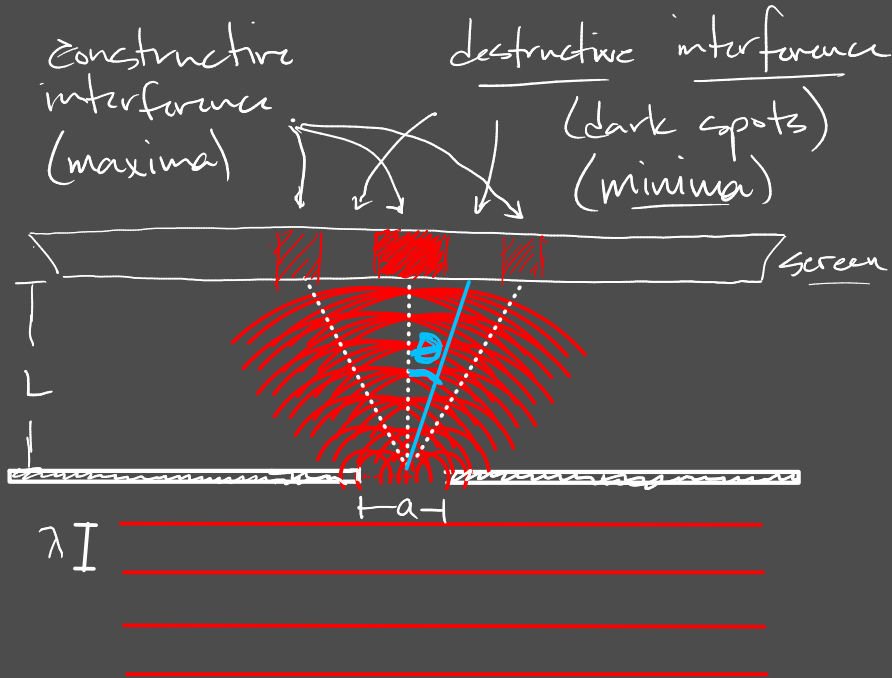
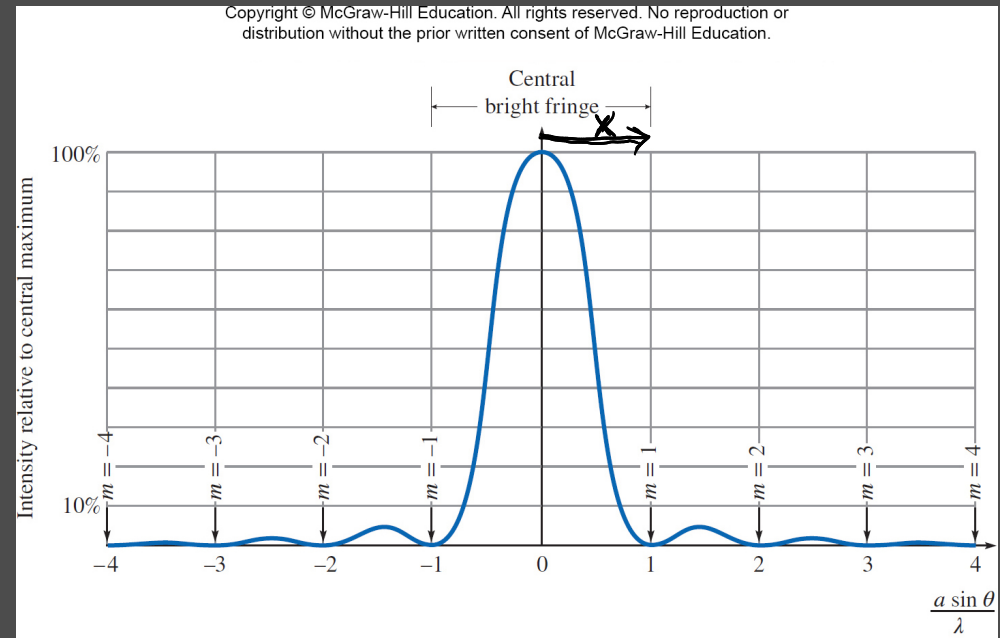
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Single Slit Diffraction / Interference

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locations of the minima:

location from central axis to minima

$a \sin \theta = m \lambda$

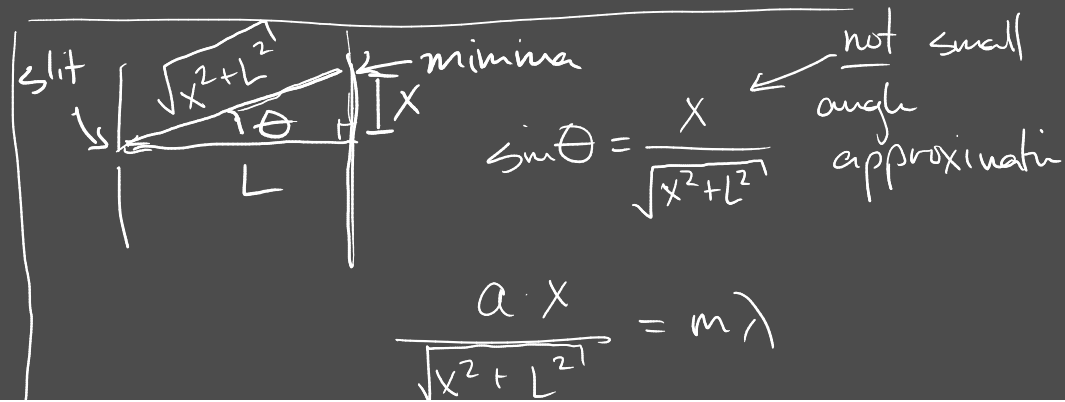
\rightarrow slit width

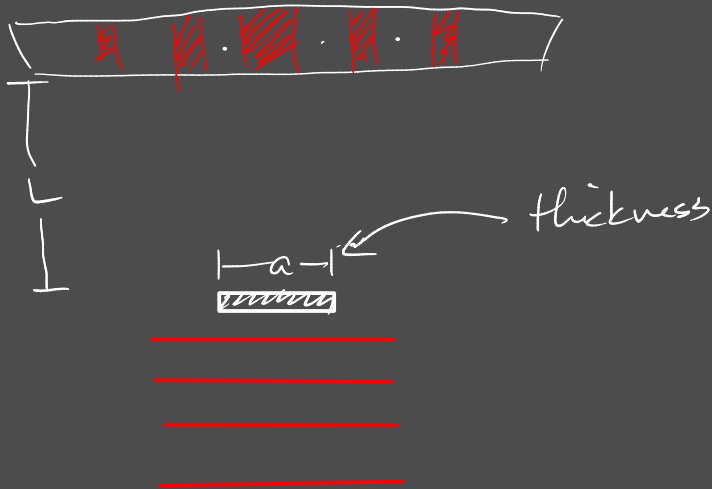
\rightarrow fringe from the center

This pattern also results from a small obstruction to the light beam

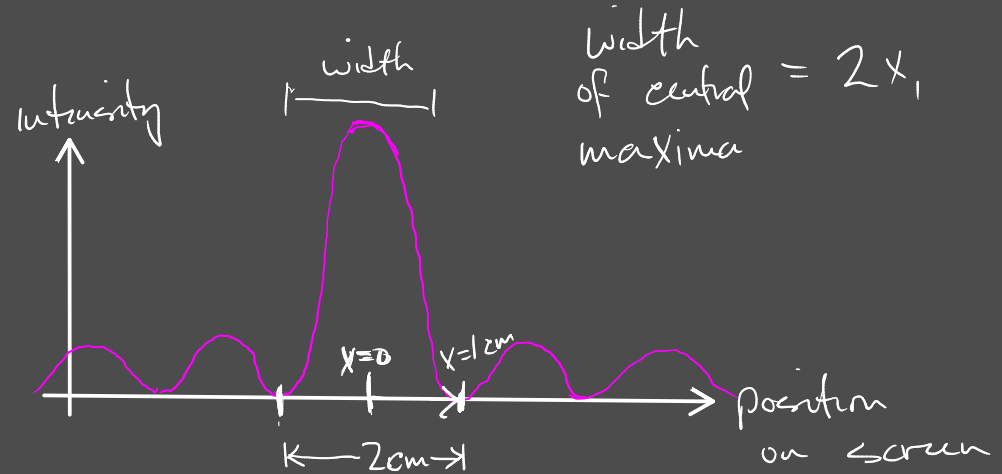
small angle approximation

$$\sin \theta = \frac{x}{L} \quad \left\{ \quad \frac{a x}{L} = m \lambda \right.$$





© The diffraction pattern from a single slit is viewed on a distant screen. Using violet light, the width of the central maximum is 2.0 cm. (a) Would the central maximum be narrower or wider if red light is used instead? (b) If the violet light has wavelength $0.43 \mu\text{m}$ and the red light has wavelength $0.70 \mu\text{m}$, what is the width of the central maximum when red light is used?



$$\frac{ax}{L} = m\lambda$$

$$x = \frac{m\lambda \cdot L}{a}$$

location of minima

$$\text{width} \propto x \propto \lambda$$

from violet to red
 λ increases
 $400 \text{ nm} \rightarrow 700 \text{ nm}$

$$w \propto x \propto \lambda$$

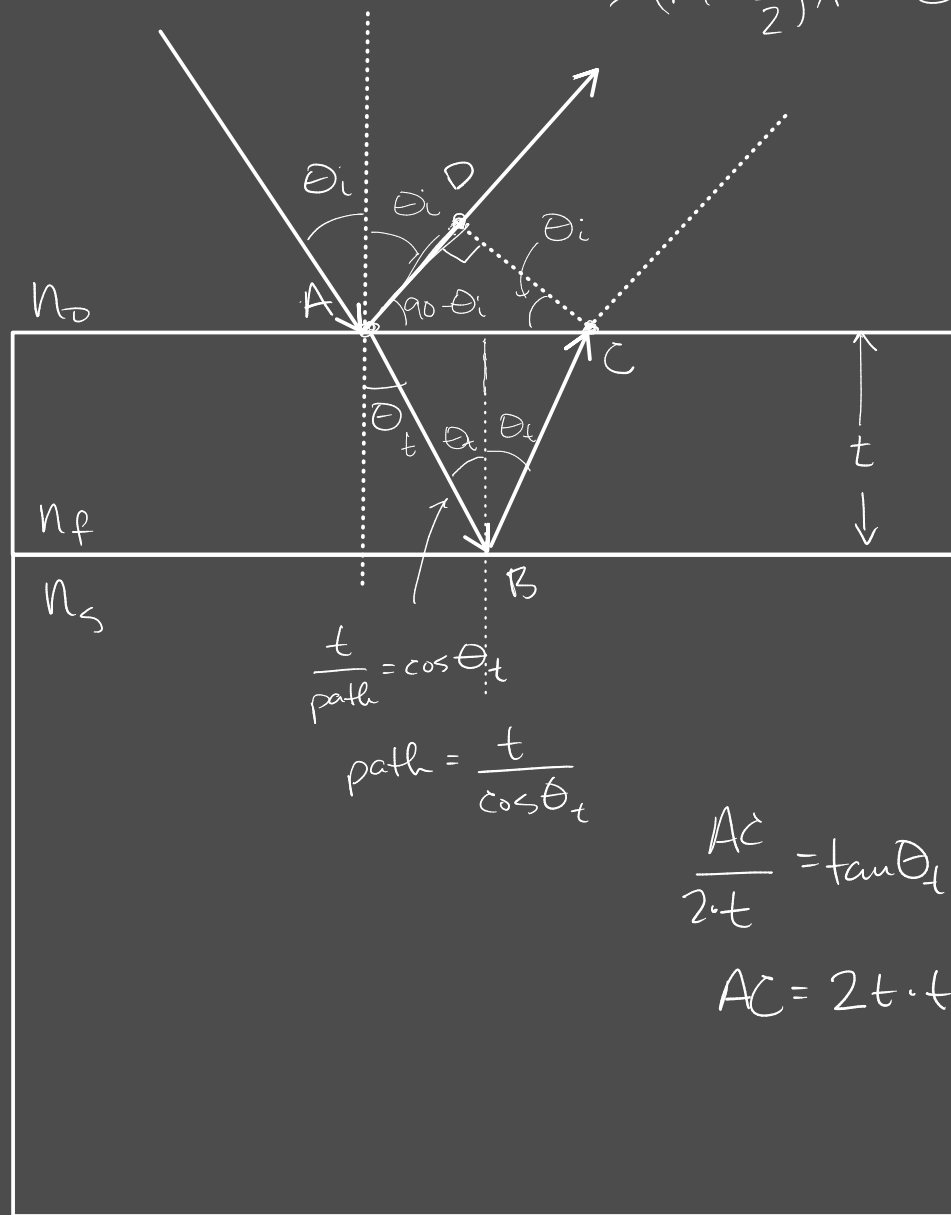
$$w \propto \lambda$$

$$\frac{w_{\text{red}}}{w_{\text{v}}} = \frac{\lambda_{\text{red}}}{\lambda_{\text{v}}}$$

$$w_{\text{red}} = 2.0 \text{ cm} \cdot \left(\frac{0.70 \mu\text{m}}{0.43 \mu\text{m}} \right)$$

$$w_{\text{red}} = 3.2 \text{ cm}$$

path length difference $\rightarrow m\lambda$ constructive interference
 $\rightarrow (m + \frac{1}{2})\lambda$ destructive interference



optical path length $\rightarrow n \cdot l$

$$\Delta \text{path length} = n \left(\frac{2t}{\cos \theta_t} \right) - n_0 (AD)$$

$$AD = AC \sin \theta_i$$

$$\text{Snell's} \rightarrow n_0 \sin \theta_i = n_f \sin \theta_t$$

$$\sin \theta_i = \frac{n_f}{n_0} \sin \theta_t$$

$$AD = AC \frac{n_f}{n_0} \sin \theta_t$$

$$AD = \frac{n_f}{n_0} \cdot 2t \cdot \sin \theta_t \tan \theta_t$$

$$AD = \frac{n_f}{n_0} \cdot 2t \cdot \frac{\sin^2 \theta_t}{\cos \theta_t}$$

$$\Delta = \frac{2n_f t}{\cos \theta_t} - n_0 \left(\frac{n_f}{n_0} \cdot 2t \cdot \frac{\sin^2 \theta_t}{\cos \theta_t} \right)$$

$$\Delta = \frac{2n_f t}{\cos \theta_t} \underbrace{\left(1 - \sin^2 \theta_t\right)}_{\cos^2 \theta_t}$$

optical path
length difference

$$\Delta = 2nt \cos \theta_t$$

BUT WAIT!

• $\frac{\lambda}{2} \rightarrow$ ~~path~~ phase shift

from reflection
higher index to
a lower index
material

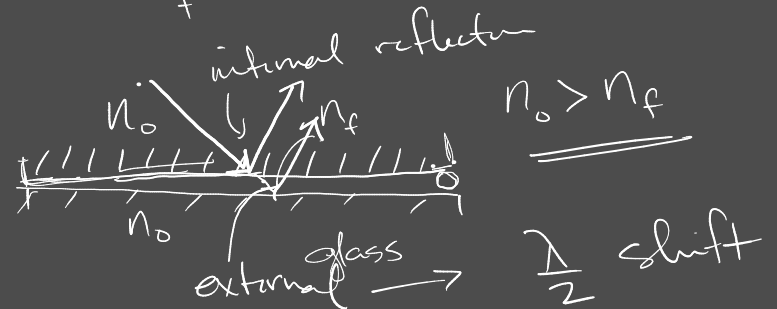
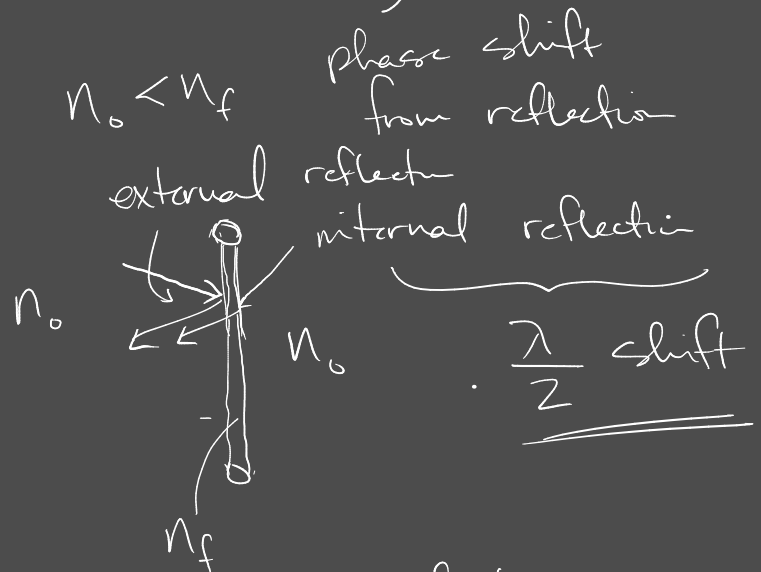
• $\pi \rightarrow$ phase shift (relative)
from internal and
external reflections

$$\sin(k(x-vt) + \phi_R)$$

$$\sin(kx - \omega t + \phi_R)$$

$$\phi_R = \pi \rightarrow$$

$$\Delta_P + \Delta_R = \begin{cases} m\lambda & \text{constructive} \\ (m + \frac{1}{2})\lambda & \text{destructive} \end{cases}$$



$$\sin(kx - \omega t + \pi)$$

\nwarrow
 $\frac{k}{k} \leftarrow \frac{2\pi}{\lambda}$

$$\sin(kx - \omega t + \frac{k\cancel{\pi}\lambda}{\cancel{2\pi}})$$

$$\sin(k(x + \frac{\lambda}{2}) - \omega t)$$

