Chapter 2 - 2nd Law of Thermodynamics Lo heat spontaneously flows from high temp to low temp Huaconda python inestall Monty Python Einstein Solid Ideal Gas

Entropy (mbinatorics 5 coins one coin
P(heads) = 1 microstatus HHTTH — 3H Z macrostates
THHHH — 4H Z multiple coins how many microstates are in a macrostate?

Notificity $\Omega(n) = \frac{5!}{n!(5-n)!} |\Omega(1) = \frac{5!}{1!(5-1)!}$ $P(n) = \frac{n}{N}$ number of heals $P(3 \text{ heads}) = \frac{\Omega(3)}{\Omega(all)}$ 2 microstati of 3 = 5.4.3.2.4 1.4.3.X.X Q(1) = 5 all of the microsfates Q(2) = 10 S2(3)=10 $\Omega(2) = \frac{5!}{2!3!} = 10$ SL(4) = 5 SL(5)=1

$$\Omega(N,n) = \frac{N!}{n!(N-n)!} = Notation: (N)$$
of coinc

10 atoms each w1 0 or 1 packets of energy (energy unit)
How many possible ways are there to distribute 4 energy units

0 0 0 0 0 0 0 0 0 microstate $\Omega(10,4) = \frac{10!}{4! \ 6!} = 210$ 4 energy pulats = macrostate

What if an atom can have more than one energy packet at a time?

4 energy packets & macrostate

This model of a collection of Arma w/ equal size energy quanta distributed among them is the Einstein Solid.

Democratical Debye Model

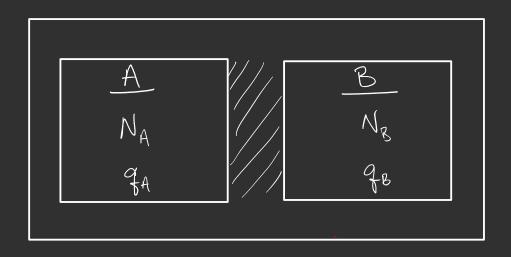
I hf 3kx²

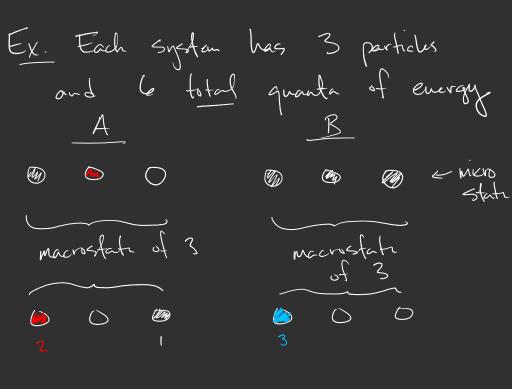
$$f = \frac{1}{2\pi} \sqrt{\frac{k}{m}}$$

E Large Mumber -> addition of small numbers is not important $10^{23} + 23 = 10^{23}$

Stirling's Approximation $N! \approx N^N e^N \sqrt{2\pi N} = \frac{N^N}{e^N} \sqrt{2\pi N}$ Very large numbers $\ln N! \approx N \ln N - N$ we leave this off

Two Systems





$$q_A \text{ mult}_A \quad q_B \text{ mult}_B \quad \text{mult}_{\text{total}}$$
 $0 \quad 1 \quad 6 \quad 28 \quad 28$
 $1 \quad 3 \quad 5 \quad 21 \quad 63 \quad \text{macroslate} \quad \text{microslate}$
 $2 \quad 6 \quad 4 \quad 15 \quad 90 \quad \text{the most}$
 $4 \quad 15 \quad 2 \quad 6 \quad 90 \quad \text{fotal number} \quad \text{macroslate} \quad \text{of microslate}$
 $5 \quad 21 \quad 1 \quad 3 \quad 63 \quad \text{for microslate}$
 $6 \quad 28 \quad 0 \quad 1 \quad 28 \quad 462 \quad \text{for microslate}$

manufate of 1
$$2(3,1)=3$$

macroslate of 5 Q(3,5) $=\frac{7!}{5!2!}=2!$

Fundamental Assumption of Stat Mich: all microstatis are possible and equally probable But that does not mean that every microstate will occur. Not all macrostates are equally probable.

Pala = Itola (ga)

We could find the total # of microsifatics:
$$\int [(b, b)] = \frac{(b \cdot b - 1)}{6!(b-1)!} = 462$$
N q

So lets apply Stirling's Approx to Multiplicity
$$[l_N N] = N l_N N - N$$

$$Q(N,q) = \frac{(q+N-1)!}{q!(N-1)!} \approx \frac{(q+N)!}{q!N!}$$

$$\ln \Omega = \ln(q+N)! - (\ln q! - (\ln N!) \rightarrow N \ln N - N)$$

$$\ln(q+N)! = (q+N) \ln(q+N) - (q+N)$$

high temperature limit -> q>> N

$$\ln \Omega = (q+N) \ln(q+N) - q \ln q - N \ln N$$

$$= q \ln(q+N) + N \ln(q+N) - q \ln q - N \ln N$$

$$= \ln q + \ln(1+\frac{N}{q})$$

$$= \ln q + \ln(1+\frac{N}{q})$$

$$= \ln q + \frac{N}{q} \approx \ln(q+N)$$

$$\ln \Omega = q \ln q + N + N \ln q + \frac{N^2}{q} - q \ln q - N \ln N$$

$$= N \ln \left(\frac{q}{N}\right) + N + \frac{N^2}{q}$$

$$= \ln \left(\frac{q}{N}\right) + N + \frac{N^2}{q}$$

$$\Omega(q>N) = e^{N \ln(\frac{q}{N}) + N} = e^{N \ln(\frac{q}{N})} = e^{N \ln(\frac{q})} = e^{N \ln(\frac{q}{N})} = e^{N \ln(\frac{q}{N})} = e^{N \ln(\frac{q}{N})} = e$$



