Chapter 2 - 2nd Law of Thermodynamics Lo heat spontaneously flows from high temp to low temp Huaconda python
inestall
Monty Python Einstein Sold Ideal Gas

Entropy (mbinatorics 5 coins one coin
P(heads) = 1 microstatus HHTTH — 3H Z macrostates
THHHH — 4H Z multiple coins how many microstates are in a macrostate?

Notificity $\Omega(n) = \frac{5!}{n!(5-n)!} |\Omega(1) = \frac{5!}{1!(5-1)!}$ $P(n) = \frac{n}{N}$ number of heals $P(3 \text{ heads}) = \frac{\Omega(3)}{\Omega(all)}$ 2 microstati of 3 = 5.4.3.2.4 1.4.3.X.X Q(1) = 5 all of the microsfates Q(2) = 10 S2(3)=10 $\Omega(2) = \frac{5!}{2!3!} = 10$ SL(4) = 5 SL(5)=1

$$\Omega(N,n) = \frac{N!}{n!(N-n)!} = Notation: (N)$$
of coinc

10 atoms each w1 0 or 1 packets of energy (energy unit)
How many possible ways are there to distribute 4 energy units

0 0 0 0 0 0 0 0 0 microstate $\Omega(10,4) = \frac{10!}{4! \ 6!} = 210$ 4 energy pulats = macrostate

What if an atom can have more than one energy packet at a time?

4 energy packets & macrostate

This model of a collection of Arma w/ equal size energy quanta distributed among them is the Einstein Solid.

Democratical Debye Model

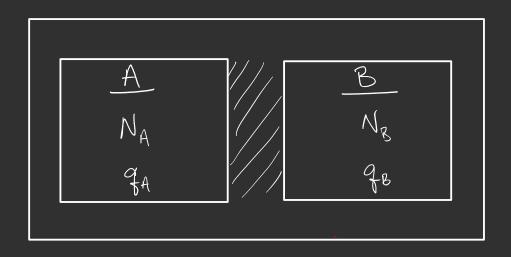
I hf 3kx²

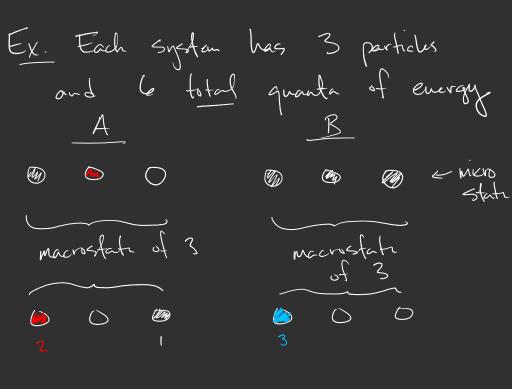
$$f = \frac{1}{2\pi} \sqrt{\frac{k}{m}}$$

E Large Mumber -> addition of small numbers is not important $10^{23} + 23 = 10^{23}$

Stirling's Approximation $N! \approx N^N e^N \sqrt{2\pi N} = \frac{N^N}{e^N} \sqrt{2\pi N}$ Very large numbers $\ln N! \approx N \ln N - N$ we leave this off

Two Systems





$$q_A \text{ mult}_A \quad q_B \text{ mult}_B \quad \text{mult}_{\text{total}}$$
 $0 \quad 1 \quad 6 \quad 28 \quad 28$
 $1 \quad 3 \quad 5 \quad 21 \quad 63 \quad \text{macroslate} \quad \text{microslate}$
 $2 \quad 6 \quad 4 \quad 15 \quad 90 \quad \text{the most}$
 $4 \quad 15 \quad 2 \quad 6 \quad 90 \quad \text{fotal number} \quad \text{macroslate} \quad \text{of microslate}$
 $5 \quad 21 \quad 1 \quad 3 \quad 63 \quad \text{for microslate}$
 $6 \quad 28 \quad 0 \quad 1 \quad 28 \quad 462 \quad \text{for microslate}$

manufate of 1
$$2(3,1)=3$$

macroslate of 5 Q(3,5) $=\frac{7!}{5!2!}=2!$

Fundamental Assumption of Stat Mich: all microstatis are possible and equally probable But that does not mean that every microstate will occur. Not all macrostates are equally probable.

Pala = Itola (ga)

We could find the total # of microsifatics:
$$\int [(b, b)] = \frac{(b \cdot b - 1)}{6!(b-1)!} = 462$$
N q

So lets apply Stirling's Approx to Multiplicity
$$[l_N N] = N l_N N - N$$

$$Q(N,q) = \frac{(q+N-1)!}{q!(N-1)!} \approx \frac{(q+N)!}{q!N!}$$

$$\ln \Omega = \ln(q+N)! - (\ln q! - (\ln N!) \rightarrow N \ln N - N)$$

$$\ln(q+N)! = (q+N) \ln(q+N) - (q+N)$$

high temperature limit -> q>> N

$$\ln \Omega = (q+N) \ln(q+N) - q \ln q - N \ln N$$

$$= q \ln(q+N) + N \ln(q+N) - q \ln q - N \ln N$$

$$= \ln q + \ln(1+\frac{N}{q})$$

$$= \ln q + \ln(1+\frac{N}{q})$$

$$= \ln q + \frac{N}{q} \approx \ln(q+N)$$

$$\ln \Omega = q \ln q + N + N \ln q + \frac{N^2}{q} - q \ln q - N \ln N$$

$$= N \ln \left(\frac{q}{N}\right) + N + \frac{N^2}{q}$$

$$= \ln \left(\frac{q}{N}\right) + N + \frac{N^2}{q}$$

$$\Omega(q>N) = e^{N \ln(\frac{q}{N}) + N} = e^{N \ln(\frac{q}{N})} = e^{N \ln(\frac{q})} = e^{N \ln(\frac{q}{N})} = e^{N \ln(\frac{q}{N})} = e^{N \ln(\frac{q}{N})} = e$$

2 Einstein solids (Inich temperature limit) (q>>N)

$$Q_{A} = \begin{pmatrix} eq_{1}N_{A} \\ N_{A} \end{pmatrix}$$
 $Q_{B} = \begin{pmatrix} eq_{1}N_{A} \\ N_{B} \end{pmatrix}$
 $Q_{B} = \begin{pmatrix} eq_{1}N_{A} \\ N_{A} \end{pmatrix}$

Entropy + the 2rd Law: Any large system in equilibrium will be found in the macrostate with the greatest multiplicity 2nd Law of Thermodynamics Multiplicity tends to increase. Multiplicities are very large! Take the natural log of them. entropy -> S = Kig In I

> S KB = INSL

$$Q = (eg)^{N} \qquad q >> N \quad \text{Einstein solid}$$

$$N = 10^{23} \qquad q = 10^{25}$$

$$S = k_{B} \ln \left((eg)^{N} \right) = N \cdot k_{B} \ln \left((eg)^{N} \right) =$$

$$= 1.38 (1 + ln(10^{2}))$$
4.6



















