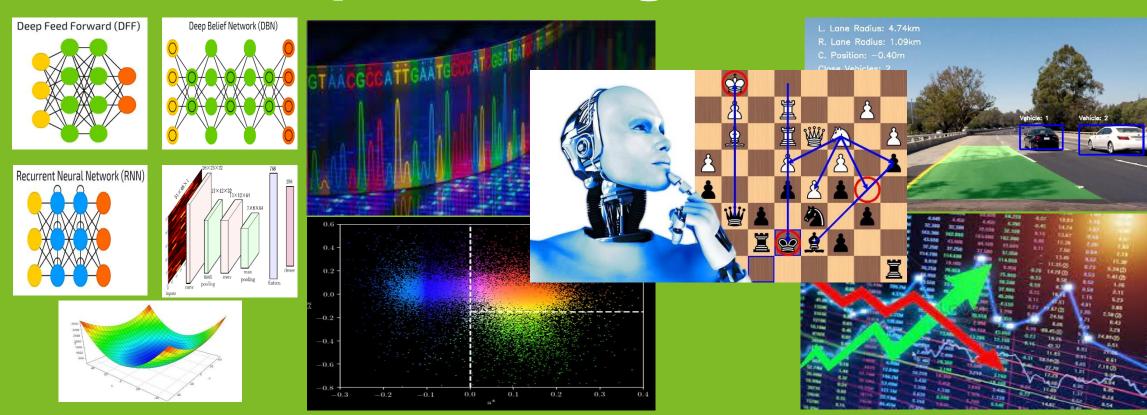
Deep Learning CSI_7_DEL



Week 9:Deep Belief Networks



Deep Belief Networks

- Probabilistic generative model.
- Introduced by Hinton et al in 2006.
- Non-linear dimensionality reduction.
- Captures correlations between the activities of the hidden features in the preceding layers.
- A Greedy layer-by-layer unsupervised training (Vanishing gradient?)



Deep Belief Networks: Characteristics

- Generative: DBN can produce randomly created values for the input values. Some research paper refer to this as dreaming.
- Probabilistic: DBNs are used for classification tasks. The output is the probability that certain input belongs a particular class.
- Multi-layered: like other neural networks, DBN is made up of multiple layers.
- Stochastic latent variables: Since DBN is made up of stacked RBMs, it produces random (*stochastic*) values that can not be directly observed (*latent*).

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DBN vs Feedforward Neural Networks

Deep Belief Networks	Feedforward Neural Networks
Input must be Binary	Input can be decimal or binary
The output is a class to which the input belongs	The output can be a class or a numeric prediction
Can generate plausible input based on a given outcome	Can not perform like DBN



DBN Applications

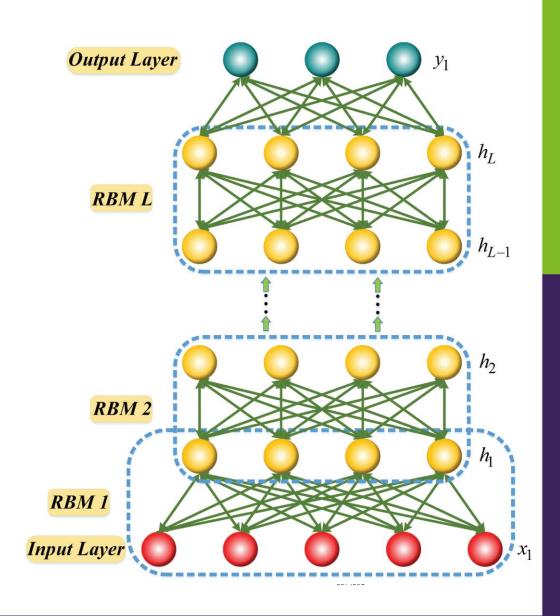
- Generating and reconstructing images (Hinton et al 2007)
- Collaborative filtering for recommender system(Salakhutdinov et al., <u>2007</u>).
- Motion-capture data (Taylor et. al. 2007).
- Images and information retrieval and reconstruction. (Gehler et al. <u>2006</u>)



DBN Architecture

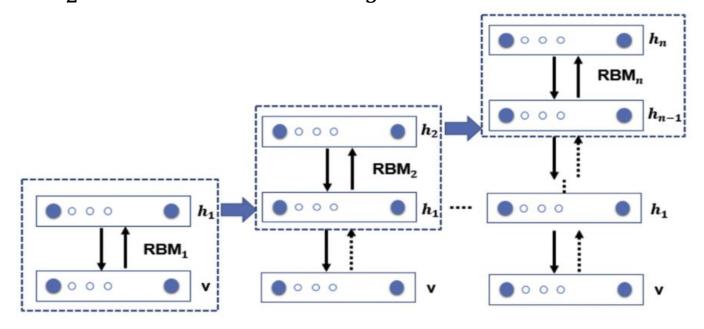
- Input fed to the DBN network passes through a series of layers.
- DBN is made up of stacked RBM
- The hidden units become the output to the next layers
- Adding additional RBMs causes deeper DBN.
- Even though RBMs are unsupervised, the desired outcome in DBN is supervised.
- A final logistic regression layer is included to associate the given input to an output class.

Source: https://www.mdpi.com/2072-4292/14/6/1484/htm



DBN Architecture: Stacked RBMs

- Each RBM has visible layer v and a single layer h.
- RBM_1 is trained using the visible neurons
- The hidden layer h_2 of RBM_2 is trained using the previously trained layer h_1 .
- The output of h_2 is used to train RBM_3 and son on.

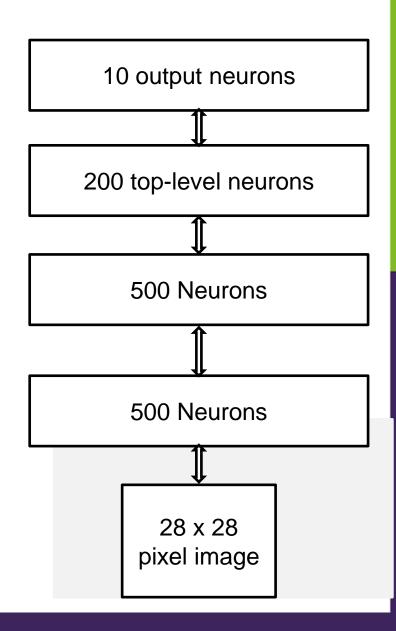




Source: https://www.sciencedirect.com/science/article/pii/B9780128154809000116

Early DBN: Hinton's 2006 Experiment

- First DBN network was trained by Hinton in 2006
- The input was a 28X28 pixels or 784 single bit vector
- Monochrome and single channel (black & white)
- 3 layers of stacked RBMs
- L1= 500 neurons, L2= 500 neurons, L3= 200 neurons
- The output neurons here are 10 digits.



DBN Dreaming of Digits

- The following digits have been created using DBN and were taking from Hinton's (2006) deep learning paper
- The first row shows zeros generated by DBN using contrastive divergence by Gibbs sampling.





Source: Hinton et al 2006

Energy function / Cost function

- Low energy translates to high probability (High accuracy).
- In the case of DBN, there is an energy function for each RBM layer.
- The total energy of the joint configuration of the visible and hidden neurons can be formulated:

$$E(v,h) = -\sum_{i} a_i v_i - \sum_{j} b_j h_j - \sum_{i,j} w_{ij} v_i h_j$$
$$= -a^T v - b^T h - v^T W h$$

• Where a_i , b_i are biases, weights represents w_{ji} and v_i , b_j are the corresponding visible and hidden units.

Recap: RBM: Hidden and Visible units

• In For any hidden unit h_i , he probability P that h_i can be turn on can be computed as follow:

$$P(h_i=1)=rac{1}{1-e^{-z_i}}$$
 (a sigmoid basically also called partition function)

 z_i represents the sum of all input combinations:

$$z_{i} = \sum_{i} w_{ji} v_{i} + b_{i}$$

Where w_{ji} is the weight connection between the visible and the hidden neurons and b_i is the bias added to the visible neuron.

• Similarly, for any hidden unit v_i , he probability P that v_i can be turn on can be computed as follow:

$$P(v_i = 1) = \frac{1}{1 - e^{-y_i}}$$
Where $y_i = \sum_i w_{ii} v_i + b_i$

 Once this output is calculated, it gets passed on the next layer as input



DBN Training

- DBN is pretrained using an algorithm called Greedy layer-wise training.
- Each RBM layer is trained separately with gradient descent.
- The purpose of this algorithm is to produce binary vector to feed into the contrastive divergence algorithm.
- The weights for each layer are updated using:

$$w_{ij}(t+1) = w_{ij}(t) + \eta \frac{\partial \log p(v)}{\partial w_{ij}}$$

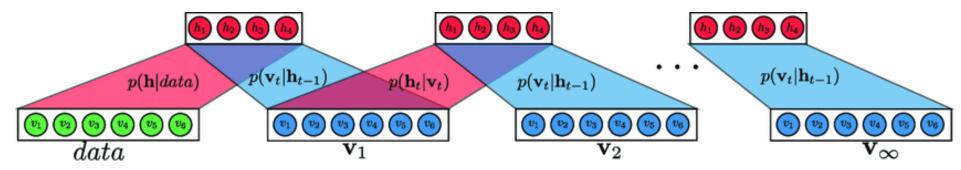
$$\frac{\partial \log p(v)}{\partial w_{ij}} = \langle v_i h_j \rangle^0 - \langle v_i h_j \rangle^\infty$$

• Where $\langle v_i h_i \rangle$ is the average over many generated samples



DBN Training:

- Several steps of Gibbs sampling executed on each RBM layer.
- The logistic layer is trained using backpropagation.
- The whole network weights are adjusted in a single passed (fine-tuning)





Contrastive Divergence by Gibbs sampling

- RBMs layers in DBN are pretrained using CD.
- The CD algorithm works as follow:

Step 1: Initialise the visible units using a random training vector

Step 2: Start Gibb Sampling and repeat for N step:

Step 2.1: Update the hidden neurons given the visible neuron $p(h_j = 1|V) = \sigma(b_j + \sum_i v_i w_{ij})$

Step 2.2: Update the visible neurons given the hidden neuron $p(v_i = 1|H) = \sigma(a_i + \sum_j h_j w_{ij})$

Step 2.3: Re—update the hidden neurons given the constructed visible neurons using equation

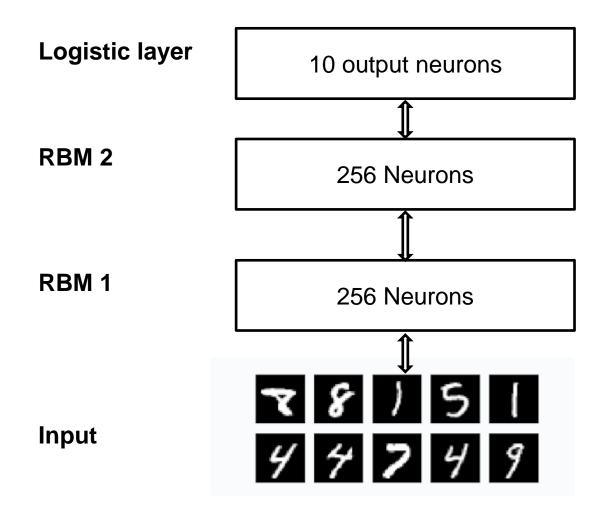
in 2.1

Step 2.4: Update the weight $W_{new} = W_{old} + \Delta W$

 Once this is done, DBN feeds the output of the current RBM hidden layer to the next RBM input layer as an input.



Example: MNIST Dataset





Example: Greedy Algorithm Training

Layer-by-layer Greedy Training

```
[BernoulliRBM] Iteration 1, pseudo-likelihood = -26.72, time = 0.07s
[BernoulliRBM] Iteration 2, pseudo-likelihood = -26.19, time = 0.10s
[BernoulliRBM] Iteration 3, pseudo-likelihood = -24.22, time = 0.10s
[BernoulliRBM] Iteration 4, pseudo-likelihood = -23.68, time = 0.11s
[BernoulliRBM] Iteration 5, pseudo-likelihood = -22.78, time = 0.11s
[BernoulliRBM] Iteration 6, pseudo-likelihood = -22.26, time = 0.12s
[BernoulliRBM] Iteration 7, pseudo-likelihood = -22.44, time = 0.10s
[BernoulliRBM] Iteration 8, pseudo-likelihood = -22.40, time = 0.11s
[BernoulliRBM] Iteration 9, pseudo-likelihood = -21.67, time = 0.12s
[BernoulliRBM] Iteration 10, pseudo-likelihood = -21.30, time = 0.13s
[BernoulliRBM] Iteration 1, pseudo-likelihood = -45.36, time = 0.11s
[BernoulliRBM] Iteration 2, pseudo-likelihood = -44.76, time = 0.20s
[BernoulliRBM] Iteration 3, pseudo-likelihood = -43.70, time = 0.17s
[BernoulliRBM] Iteration 4, pseudo-likelihood = -44.89, time = 0.18s
[BernoulliRBM] Iteration 5, pseudo-likelihood = -43.69, time = 0.18s
[BernoulliRBM] Iteration 6, pseudo-likelihood = -42.48, time = 0.17s
[BernoulliRBM] Iteration 7, pseudo-likelihood = -43.42, time = 0.17s
[BernoulliRBM] Iteration 8, pseudo-likelihood = -43.12, time = 0.17s
[BernoulliRBM] Iteration 9, pseudo-likelihood = -43.96, time = 0.16s
[BernoulliRBM] Iteration 10, pseudo-likelihood = -44.07, time = 0.16s
```

RBM 1 training

RBM 2 training



Example: Model performance

Model performance:				
	precision	recall	f1-score	support
e	1.00	1.00	1.00	27
1	0.93	0.74	0.83	35
2	0.79	0.86	0.83	36
3	0.86	0.83	0.84	29
4	0.97	0.97	0.97	30
5	0.97	0.97	0.97	40
6	1.00	1.00	1.00	44
7	0.93	0.97	0.95	39
8	0.85	0.85	0.85	39
9	0.82	0.88	0.85	41
accuracy	,		0.91	360
macro avg	0.91	0.91	0.91	360
weighted avg	0.91	0.91	0.91	360
	-	-	<u> </u>	-



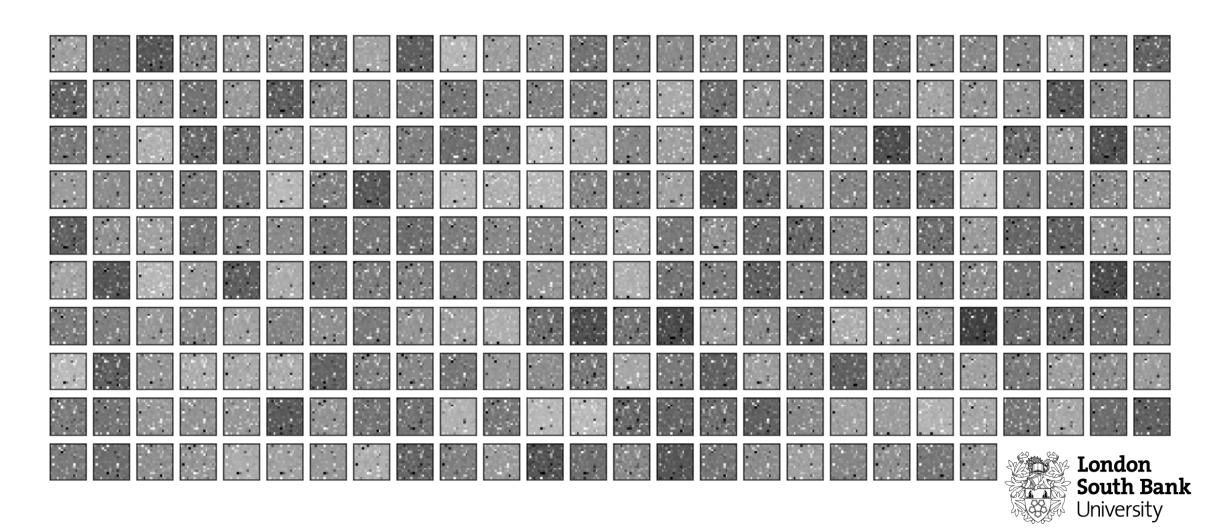
Example: RBM 1 Components

256 components extracted by RBM 1



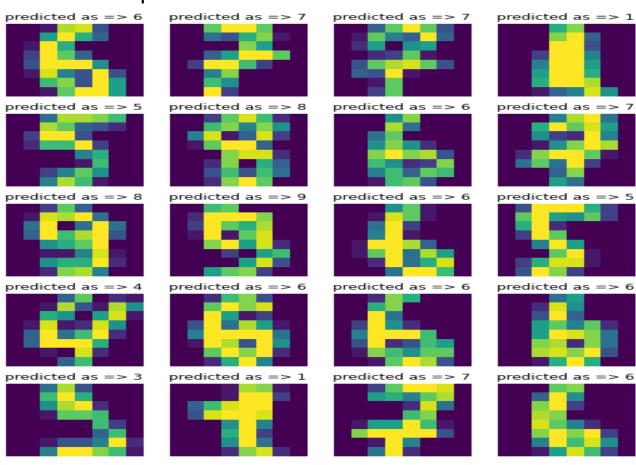
Example: RBM 2 components

256 components extracted by RBM 2



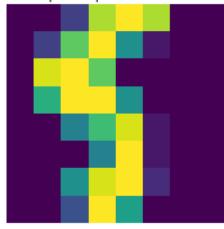
Example: Logistic Classification

Multi input classification results



Single classification result

This shape was predicted as number 5





DBN Limitations

- Very restrictive!
- Sometimes slow to train given the number of samples.
- The input can only be binary and not continuous.
- DBNs can only be used for classification and not for regression



Summary

- A DBN network undergo unsupervised and supervised training.
- During the unsupervised training, DBN does not use the output labels.
- During the supervised training, on training data with labels is used.
- Once the unsupervised phase is finished, the output from the layers is refined with supervised logistic regression.
- The logistic function layer is used for classification task.



Questions & Answers



