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# GFLIB User's Guide

ARM® Cortex® M7F

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# Chapter 1

## Library

### 1.1 Introduction

#### 1.1.1 Overview

This user's guide describes the General Functions Library (GFLIB) for the family of ARM Cortex M7F core-based microcontrollers. This library contains optimized functions.

#### 1.1.2 Data types

GFLIB supports several data types: (un)signed integer, fractional, and accumulator, and floating point. The integer data types are useful for general-purpose computation; they are familiar to the MPU and MCU programmers. The fractional data types enable powerful numeric and digital-signal-processing algorithms to be implemented. The accumulator data type is a combination of both; that means it has the integer and fractional portions. The floating-point data types are capable of storing real numbers in wide dynamic ranges. The type is represented by binary digits and an exponent. The exponent allows scaling the numbers from extremely small to extremely big numbers. Because the exponent takes part of the type, the overall resolution of the number is reduced when compared to the fixed-point type of the same size.

The following list shows the integer types defined in the libraries:

- [Unsigned 16-bit integer](#) —<0 ; 65535> with the minimum resolution of 1
- [Signed 16-bit integer](#) —<-32768 ; 32767> with the minimum resolution of 1
- [Unsigned 32-bit integer](#) —<0 ; 4294967295> with the minimum resolution of 1
- [Signed 32-bit integer](#) —<-2147483648 ; 2147483647> with the minimum resolution of 1

- **Unsigned 64-bit integer** — $\langle 0 ; 18446744073709551615 \rangle$  with the minimum resolution of 1
- **Signed 64-bit integer** — $\langle -9223372036854775808 ; 9223372036854775807 \rangle$  with the minimum resolution of 1

The following list shows the fractional types defined in the libraries:

- **Fixed-point 16-bit fractional** — $\langle -1 ; 1 - 2^{-15} \rangle$  with the minimum resolution of  $2^{-15}$
- **Fixed-point 32-bit fractional** — $\langle -1 ; 1 - 2^{-31} \rangle$  with the minimum resolution of  $2^{-31}$

The following list shows the accumulator types defined in the libraries:

- **Fixed-point 16-bit accumulator** — $\langle -256.0 ; 256.0 - 2^{-7} \rangle$  with the minimum resolution of  $2^{-7}$
- **Fixed-point 32-bit accumulator** — $\langle -65536.0 ; 65536.0 - 2^{-15} \rangle$  with the minimum resolution of  $2^{-15}$

The following list shows the floating-point types defined in the libraries:

- **Floating point 32-bit single precision** — $\langle -3.40282 \cdot 10^{38} ; 3.40282 \cdot 10^{38} \rangle$  with the minimum resolution of  $2^{-23}$

### 1.1.3 API definition

GFLIB uses the types mentioned in the previous section. To enable simple usage of the algorithms, their names use set prefixes and postfixes to distinguish the functions' versions. See the following example:

```
f32Result = MLIB_Mac_F32lss(f32Accum, f16Mult1, f16Mult2);
```

where the function is compiled from four parts:

- **MLIB**—this is the library prefix
- **Mac**—the function name—Multiply-Accumulate
- **F32**—the function output type
- **lss**—the types of the function inputs; if all the inputs have the same type as the output, the inputs are not marked

The input and output types are described in the following table:

**Table 1-1. Input/output types**

Type	Output	Input
<code>frac16_t</code>	F16	s

*Table continues on the next page...*

**Table 1-1. Input/output types (continued)**

Type	Output	Input
<code>frac32_t</code>	F32	l
<code>acc32_t</code>	A32	a
<code>float_t</code>	FLT	f

### 1.1.4 Supported compilers

GFLIB for the ARM Cortex M7F core is written in C. The library is built and tested using the following compilers:

- Kinetis Design Studio
- IAR Embedded Workbench
- Keil  $\mu$ Vision

For the Kinetis Design Studio, the library is delivered in the *gflib.a* file.

For the IAR Embedded Workbench, the library is delivered in the *gflib.a* file.

For the Keil  $\mu$ Vision, the library is delivered in the *gflib.lib* file.

The interfaces to the algorithms included in this library are combined into a single public interface include file, *gflib.h*. This is done to lower the number of files required to be included in your application.

### 1.1.5 Special issues

1. The equations describing the algorithms are symbolic. If there is positive 1, the number is the closest number to 1 that the resolution of the used fractional type allows. If there are maximum or minimum values mentioned, check the range allowed by the type of the particular function version.
2. The library functions that round the result (the API contains Rnd) round to nearest (half up).

## 1.2 Library integration into project (Kinetis Design Studio)

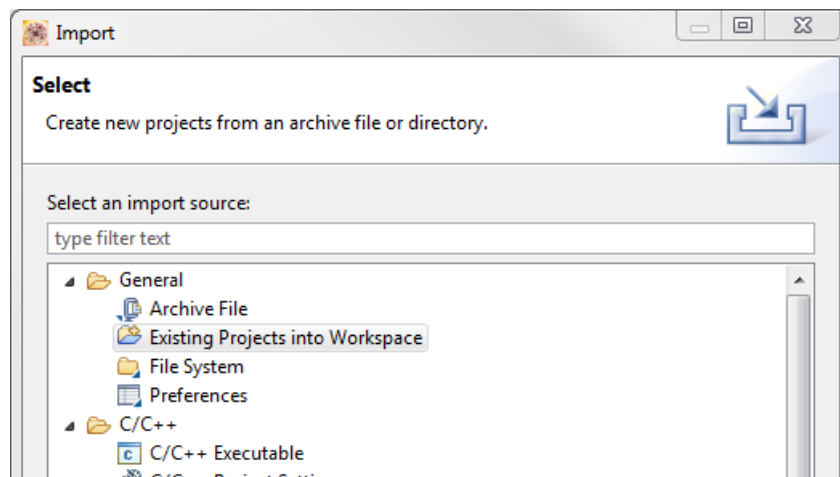
This section provides a step-by-step guide on how to quickly and easily include GFLIB into an empty project or any SDK example or demo application projects using Kinetis Design Studio. This example uses the default installation path (C:\NXP\RTCESL

\CM7F\_RTCESL\_4.3\_KDS). If you have a different installation path, use that path instead. If you want to use an existing SDK project (for example the hello\_world project) see [Library path variable](#). If not, continue with the next section.

### 1.2.1 New project (without SDK)

To start working on an application, create a new project. If the project already exists and is opened, skip to the next section. Follow these steps to create a new project:

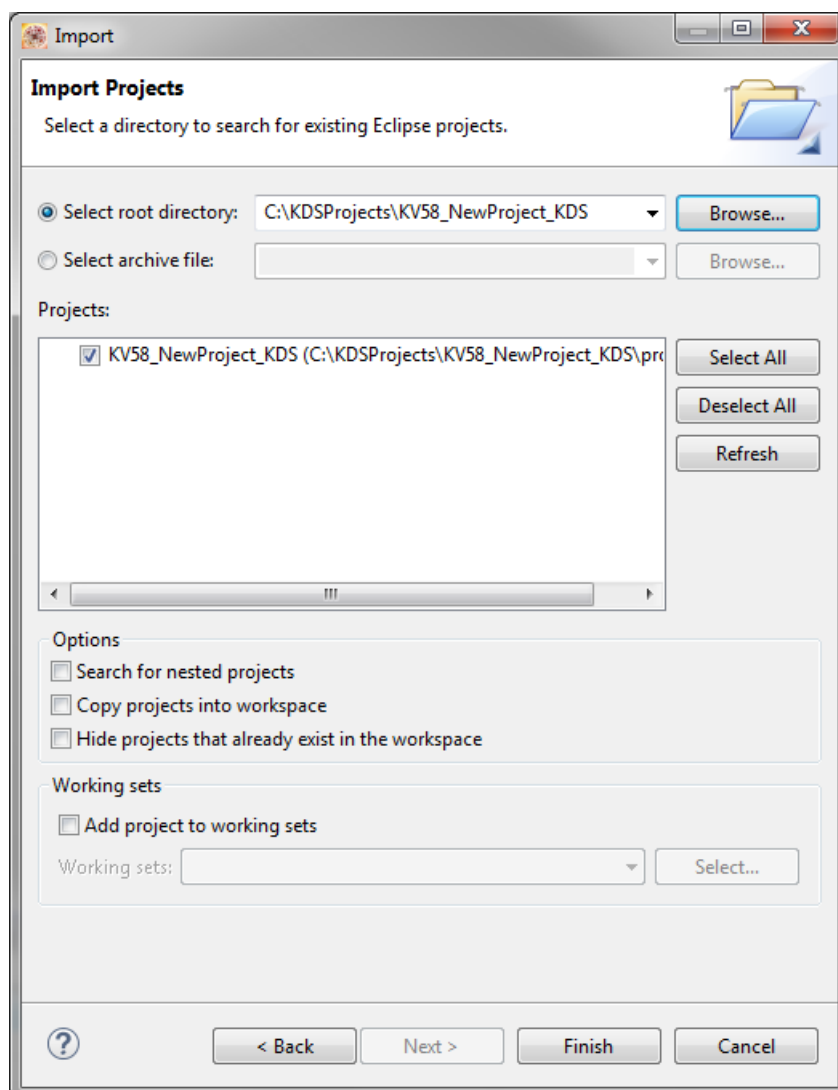
1. Because Kinetis Design Studio does not have any stationary for Kinetis CM7-based platforms, the library installation comes with an empty project for the KV5x family (the empty project is not attached if NXP Kinetis Expert was used for RTCESL download). Copy the existing empty project folder KV58\_NewProject\_KDS (located in the library installation sub-folder Projects) to your projects folder (for example, C:\KDSProjects).
2. Launch Kinetis Design Studio.
3. Select File > Import... so that the Import dialog appears. See [Figure 1-1](#).



**Figure 1-1. Project import**

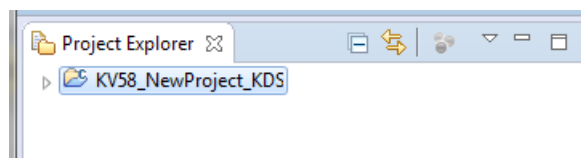
4. Select the General > Existing Projects into Workspace node and click Next.
5. In the Select root directory box, type the path to which you copied the project (C:\KDSProjects\KV58\_NewProject\_KDS), or look for it by clicking Browse. See [Figure 1-2](#).





**Figure 1-2. Project import folder**

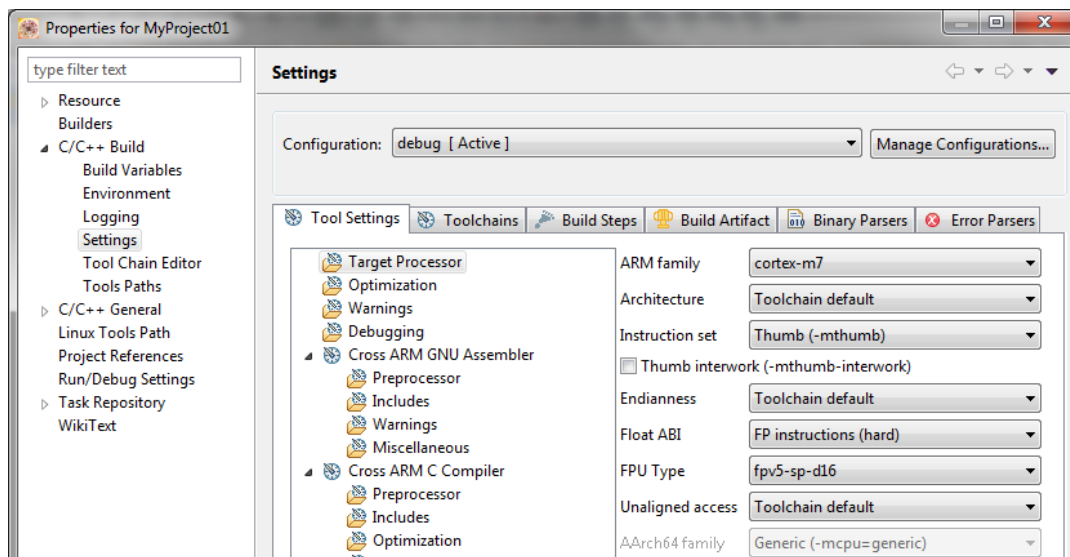
6. In the Projects dialog, tick the right project and then click Finish.
7. In the Project Explorer dialog, right-click the newly-imported project KV58\_NewProject\_KDS and select Rename. See [Figure 1-3](#).



**Figure 1-3. Project Explorer**

8. In the next dialog, type the name of your project (for example MyProject01) and click OK.
9. Right-click the MyProject01 node, click Properties in the Project Explorer, or select Project > Properties from the menu. A project properties dialog appears.
10. Expand the C/C++ Build node and select Settings.

11. In the right-hand part, set the Float ABI as FP instructions (hard) and the FPU type as fpv5\_sp\_d16. See [Figure 1-4](#).



**Figure 1-4. FPU setting**

## 1.2.2 Library path variable

To make the library integration easier, create a variable that will hold the information about the library path.

1. Right-click the MyProject01 or SDK project name node in the left-hand part and click Properties, or select Project > Properties from the menu. A project properties dialog appears.
2. Expand the Resource node and click Linked Resources. See [Figure 1-5](#).

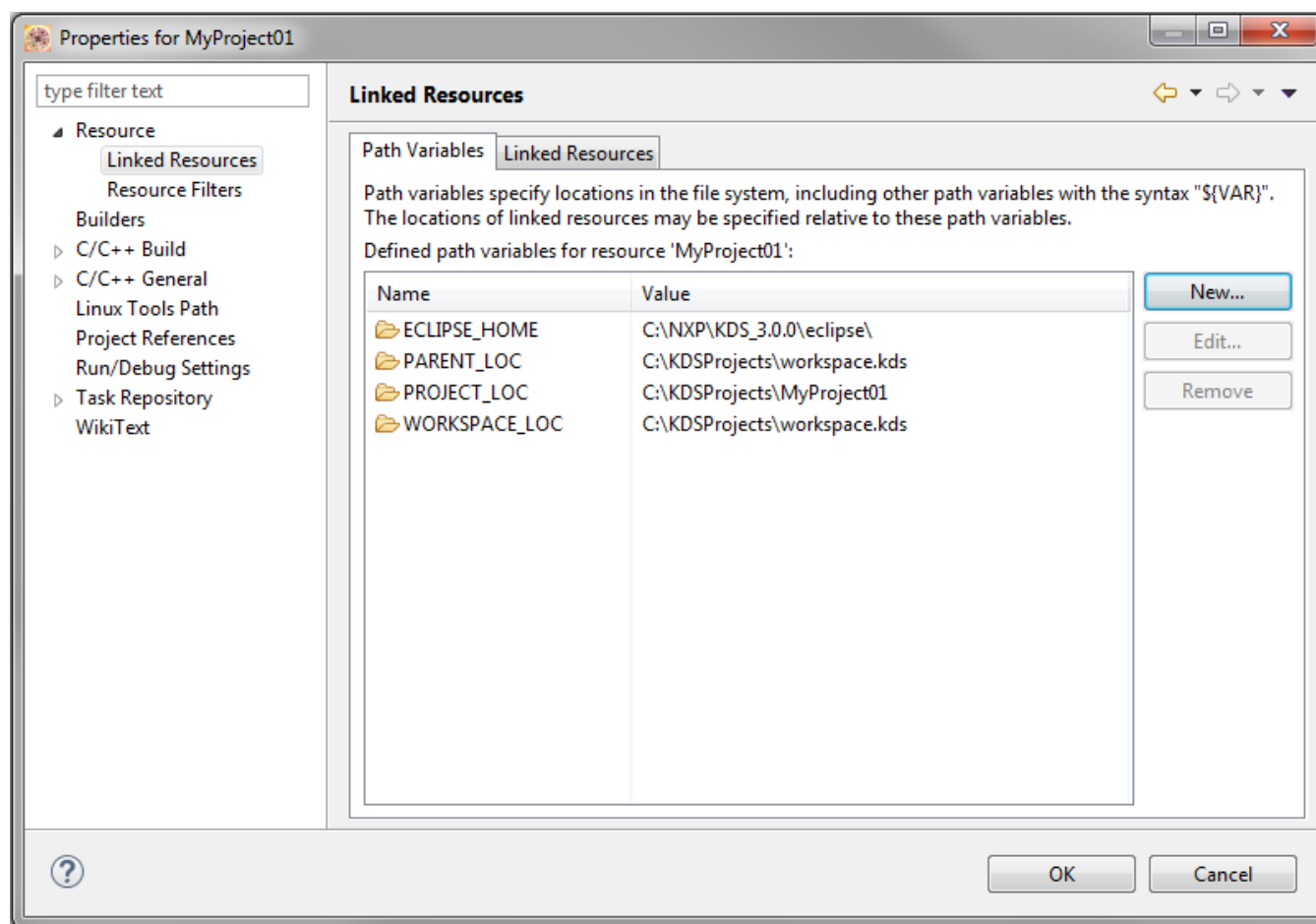


Figure 1-5. Project properties

3. Click the New... button in the right-hand side.
4. In the dialog that appears (see Figure 1-6), type this variable name into the Name box: RTCESL\_LOC.
5. Select the library parent folder by clicking Folder..., or just type the following path into the Location box: C:\NXP\RTCESL\CM7F\_RTCESEL\_4.3\_KDS. Click OK.

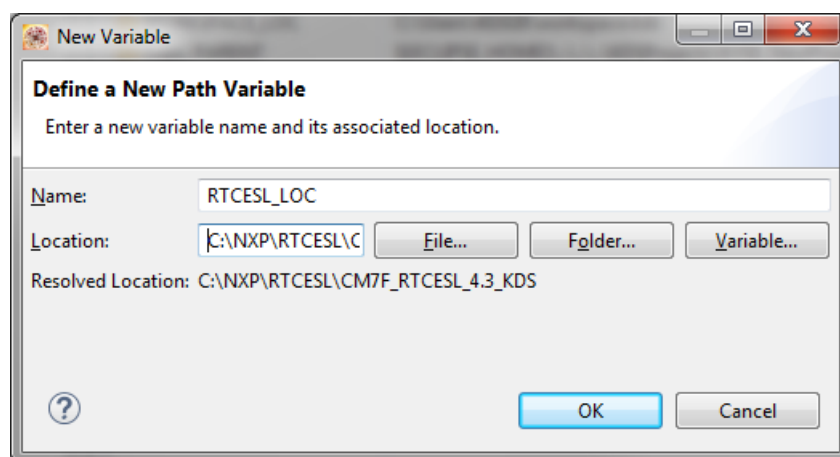


Figure 1-6. New variable

6. Create such variable for the environment. Expand the C/C++ Build node and click Environment.
7. Click the Add... button in the right-hand side.
8. In the dialog that appears (see [Figure 1-7](#)), type this variable name into the Name box: RTCESL\_LOC.
9. Type the library parent folder path into the Value box: C:\NXP\RTCESL\CM7F\_RTCESEL\_4.3\_KDS.
10. Tick the Add to all configurations box to use this variable in all configurations. See [Figure 1-7](#).
11. Click OK.
12. In the previous dialog, click OK.

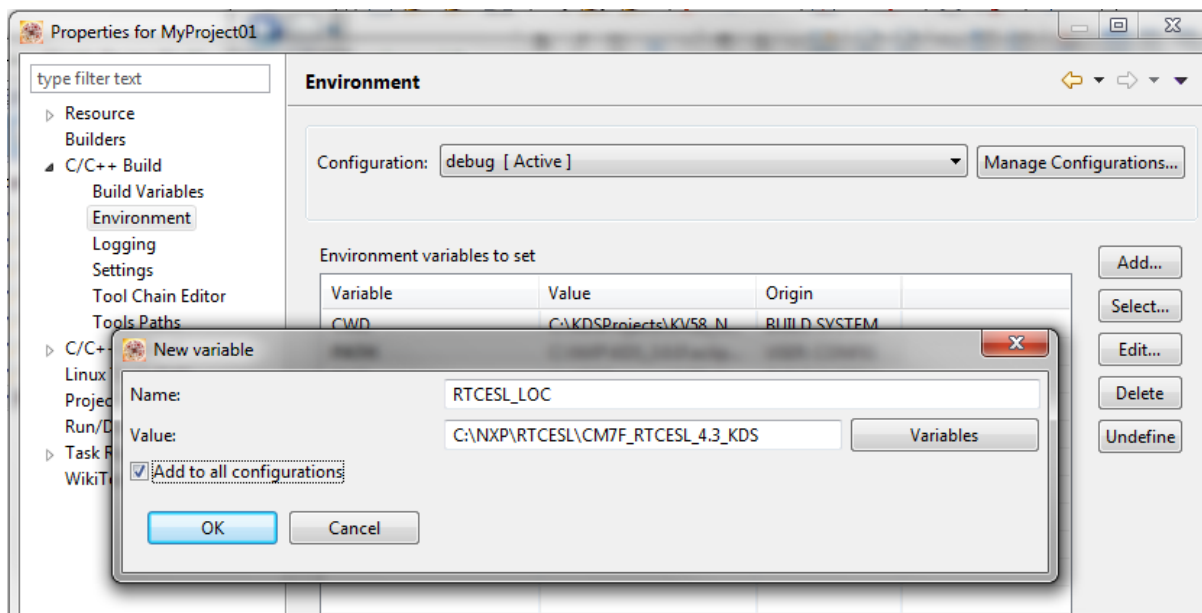


Figure 1-7. Environment variable

### 1.2.3 Library folder addition

To use the library, add it into the Project tree dialog.

1. Right-click the MyProject01 or SDK project name node in the left-hand part and click New > Folder, or select File > New > Folder from the menu. A dialog appears.
2. Click Advanced to show the advanced options.
3. To link the library source, select the option Link to alternate location (Linked Folder).
4. Click Variables..., select the RTCESL\_LOC variable in the dialog, click OK, and/or type the variable name into the box. See [Figure 1-8](#).
5. Click Finish, and you will see the library folder linked in the project. See [Figure 1-9](#).

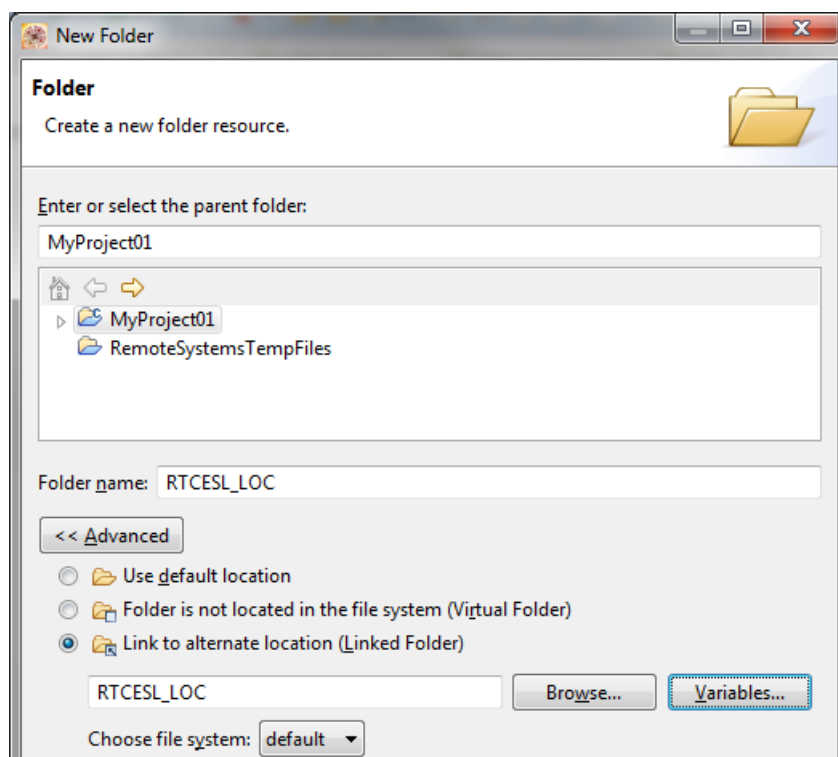


Figure 1-8. Folder link

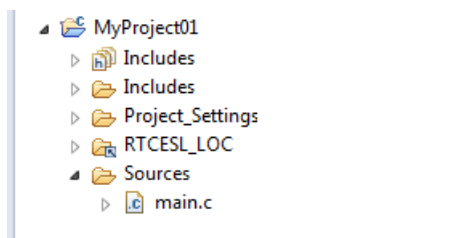


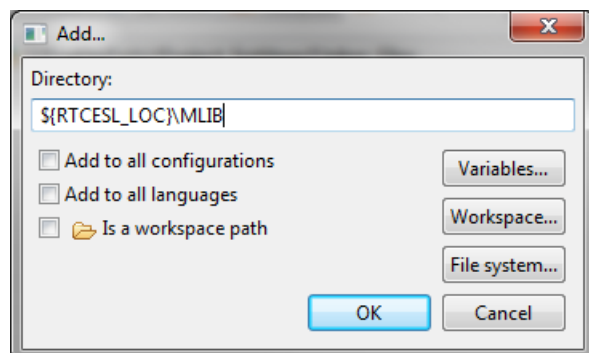
Figure 1-9. Projects libraries paths

## 1.2.4 Library path setup

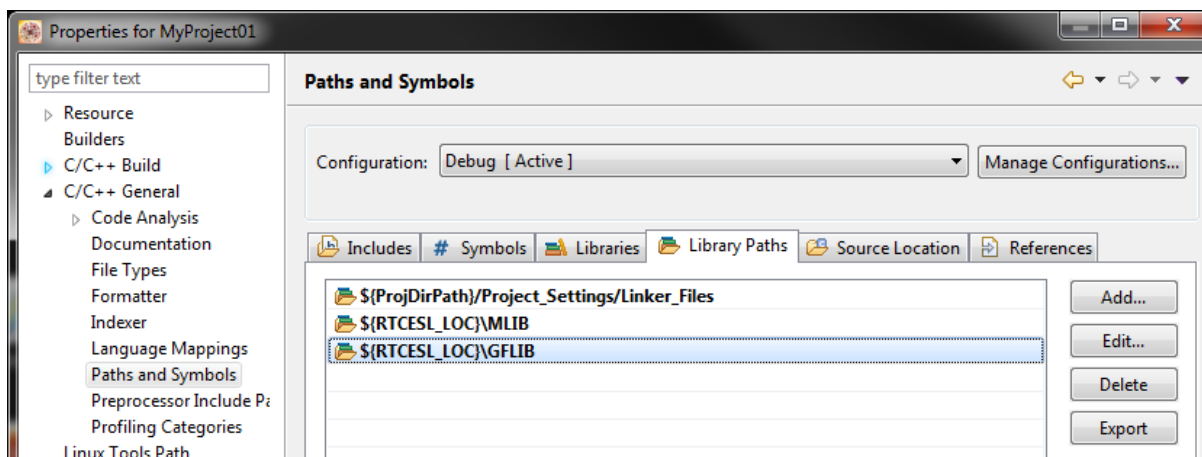
GFLIB requires MLIB to be included too. These steps show how to include all dependent modules:

1. Right-click the MyProject01 or SDK project name node in the left-hand part and click Properties, or select Project > Properties from the menu. A project properties dialog appears.
2. Expand the C/C++ General node, and click Paths and Symbols.
3. In the right-hand dialog, select the Library Paths tab. See [Figure 1-11](#).
4. Click the Add... button on the right, and a dialog appears.
5. Look for the RTCESL\_LOC variable by clicking Variables..., and then finish the path in the box by adding the following (see [Figure 1-10](#)): `${RTCESL_LOC}\MLIB`.

6. Click OK, and then click the Add... button.
7. Look for the RTCESL\_LOC variable by clicking Variables..., and then finish the path in the box by adding the following: \${RTCESL\_LOC}\GFLIB.
8. Click OK, and the paths will be visible in the list. See [Figure 1-11](#).



**Figure 1-10. Library path inclusion**



**Figure 1-11. Library paths**

9. After adding the library paths, add the library files. Click the Libraries tab. See [Figure 1-13](#).
10. Click the Add... button on the right, and a dialog appears.
11. Type the following into the File text box (see [Figure 1-12](#)): :mlib.a
12. Click OK, and then click the Add... button.
13. Type the following into the File text box: :gflib.a
14. Click OK, and you will see the libraries added in the list. See [Figure 1-13](#).

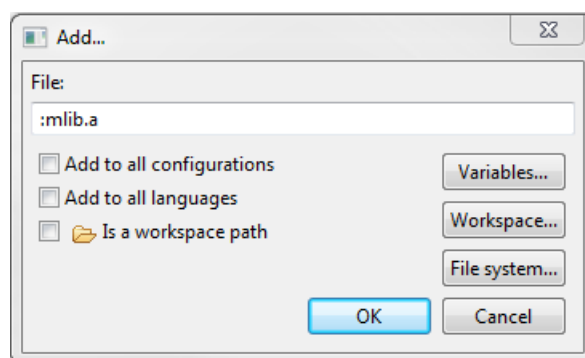


Figure 1-12. Library file inclusion

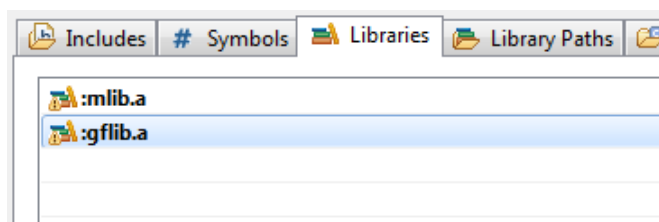


Figure 1-13. Libraries

15. In the right-hand dialog, select the Includes tab, and click GNU C in the Languages list. See [Figure 1-15](#).
16. Click the Add... button on the right, and a dialog appears. See [Figure 1-14](#).
17. Look for the RTCESL\_LOC variable by clicking Variables..., and then finish the path in the box to be: \${RTCESL\_LOC}\MLIB\Include
18. Click OK, and then click the Add... button.
19. Look for the RTCESL\_LOC variable by clicking Variables..., and then finish the path in the box to be: \${RTCESL\_LOC}\GFLIB\Include
20. Click OK, and you will see the paths added in the list. See [Figure 1-15](#). Click OK.

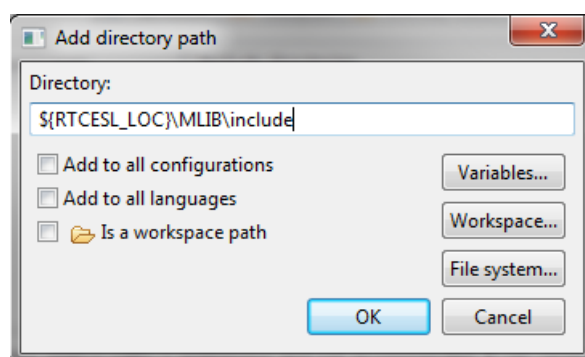


Figure 1-14. Library include path addition

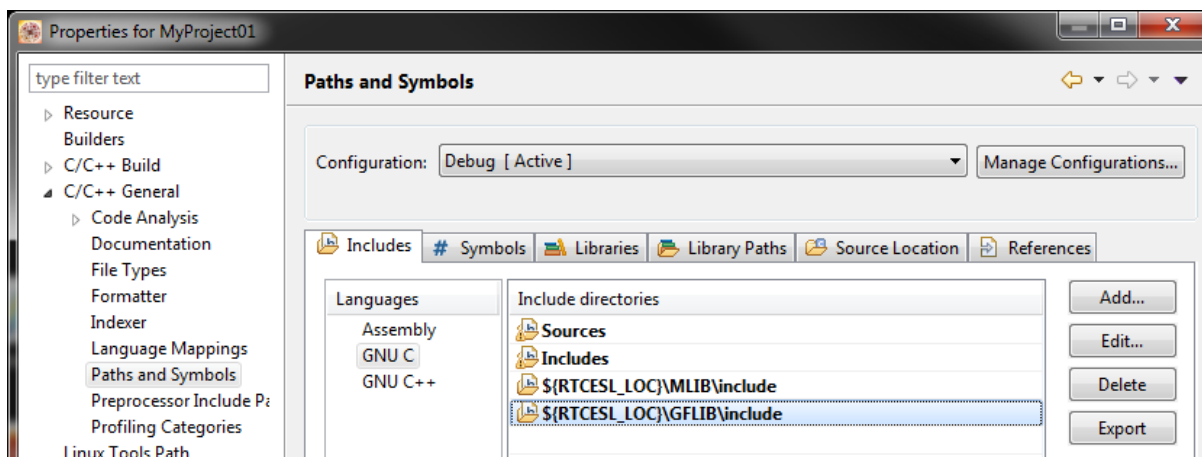


Figure 1-15. Compiler setting

Type the `#include` syntax into the code. Include the library into the *main.c* file. In the left-hand dialog, open the Sources folder of the project, and double-click the *main.c* file. After the *main.c* file opens up, include the following lines in the `#include` section:

```
#include "mlib_fp.h"
#include "gflib_fp.h"
```

When you click the Build icon (hammer), the project will be compiled without errors.

## 1.3 Library integration into project (Keil µVision)

This section provides a step-by-step guide on how to quickly and easily include GFLIB into an empty project or any SDK example or demo application projects using Keil µVision. This example uses the default installation path (C:\NXP\RTCESL\CM7F\_RTCESL\_4.3\_KEIL). If you have a different installation path, use that path instead. If any SDK project is intended to use (for example hello\_world project) go to [Linking the files into the project](#) chapter otherwise read next chapter.

### 1.3.1 NXP pack installation for new project (without SDK)

This example uses the NXP MKV58F1M0xxx22 part, and the default installation path (C:\NXP\RTCESL\CM7F\_RTCESL\_4.3\_KEIL) is supposed. If the compiler has never been used to create any NXP MCU-based projects before, check whether the NXP MCU pack for the particular device is installed. Follow these steps:

1. Launch Keil µVision.
2. In the main menu, go to Project > Manage > Pack Installer....



3. In the left-hand dialog (under the Devices tab), expand the All Devices > Freescale (NXP) node.
4. Look for a line called "KVxx Series" and click it.
5. In the right-hand dialog (under the Packs tab), expand the Device Specific node.
6. Look for a node called "Keil::Kinetis\_KVxx\_DFP." If there are the Install or Update options, click the button to install/update the package. See [Figure 1-16](#).
7. When installed, the button has the "Up to date" title. Now close the Pack Installer.

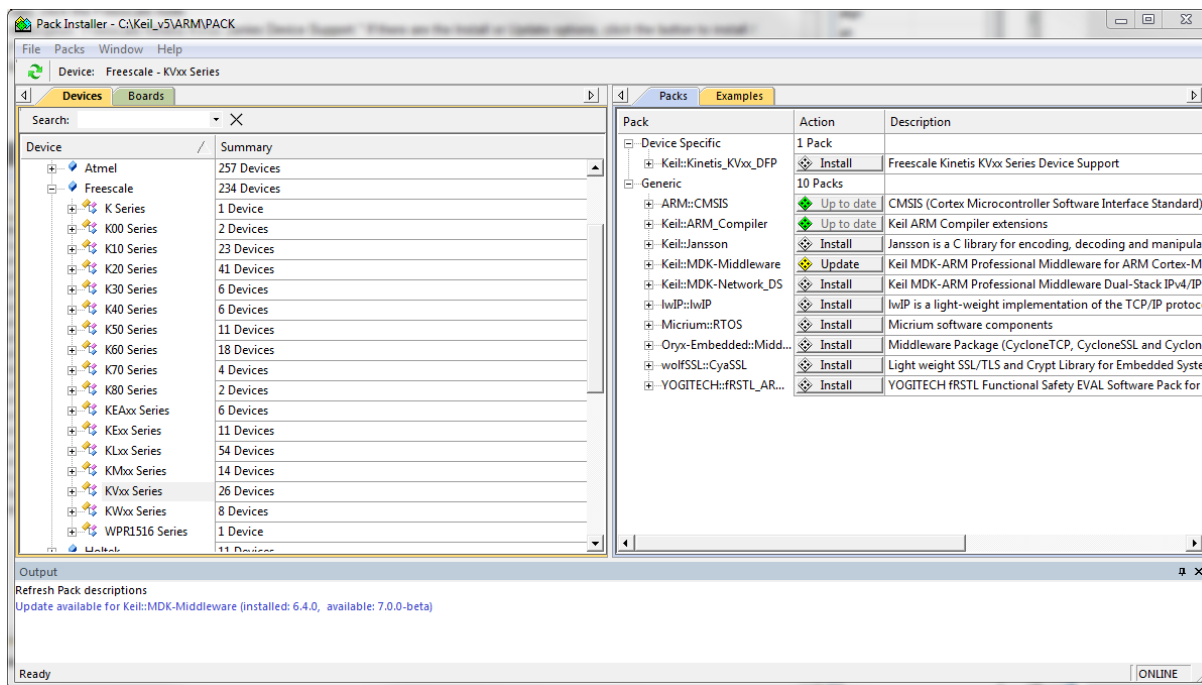
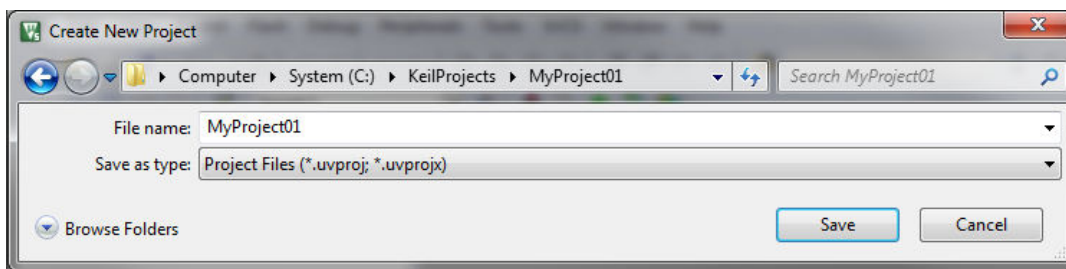


Figure 1-16. Pack Installer

### 1.3.2 New project (without SDK)

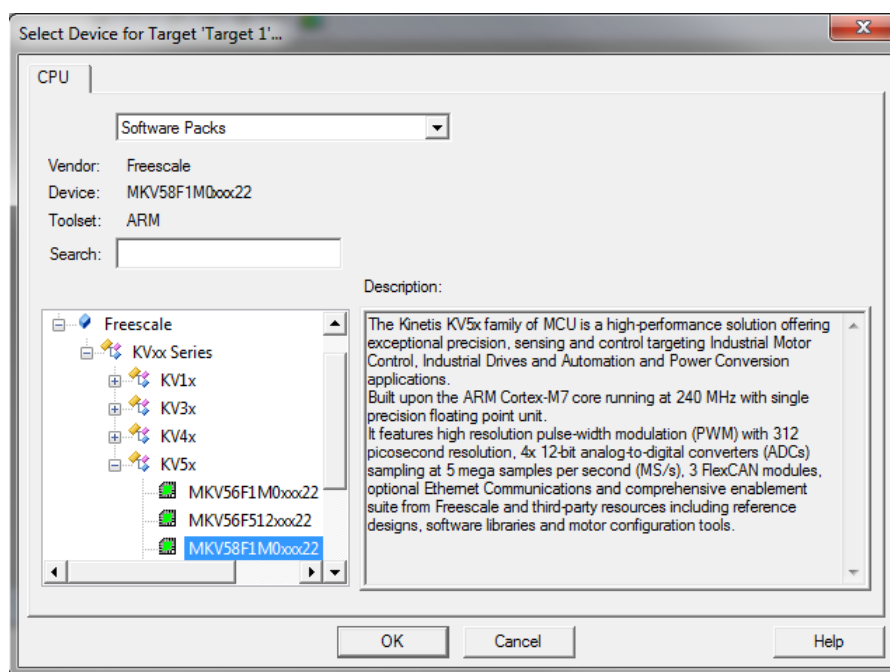
To start working on an application, create a new project. If the project already exists and is opened, skip to the next section. Follow these steps to create a new project:

1. Launch Keil  $\mu$ Vision.
2. In the main menu, select Project > New  $\mu$ Vision Project..., and the Create New Project dialog appears.
3. Navigate to the folder where you want to create the project, for example C:\KeilProjects\MyProject01. Type the name of the project, for example MyProject01. Click Save. See [Figure 1-17](#).



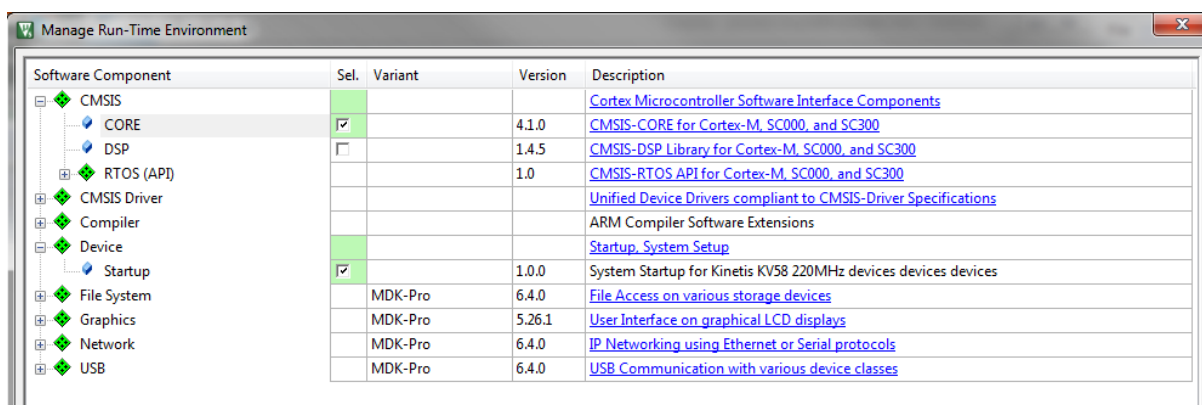
**Figure 1-17. Create New Project dialog**

4. In the next dialog, select the Software Packs in the very first box.
5. Type " into the Search box, so that the device list is reduced to the devices.
6. Expand the node.
7. Click the MKV58F1M0xxx22 node, and then click OK. See [Figure 1-18](#).



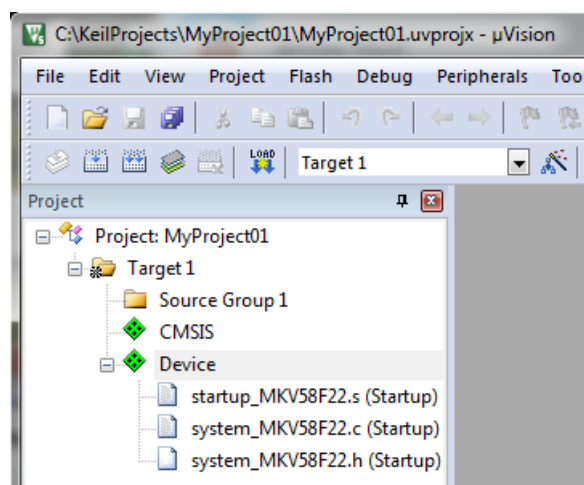
**Figure 1-18. Select Device dialog**

8. In the next dialog, expand the Device node, and tick the box next to the Startup node. See [Figure 1-19](#).
9. Expand the CMSIS node, and tick the box next to the CORE node.



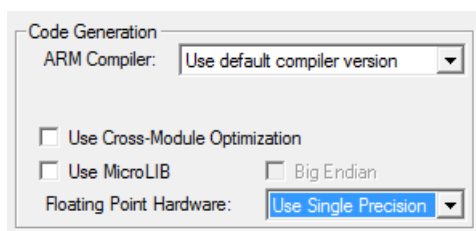
**Figure 1-19. Manage Run-Time Environment dialog**

10. Click OK, and a new project is created. The new project is now visible in the left-hand part of Keil  $\mu$ Vision. See [Figure 1-20](#).



**Figure 1-20. Project**

11. In the main menu, go to Project > Options for Target 'Target1'..., and a dialog appears.
12. Select the Target tab.
13. Select Use Single Precision in the Floating Point Hardware option. See [Figure 1-20](#).



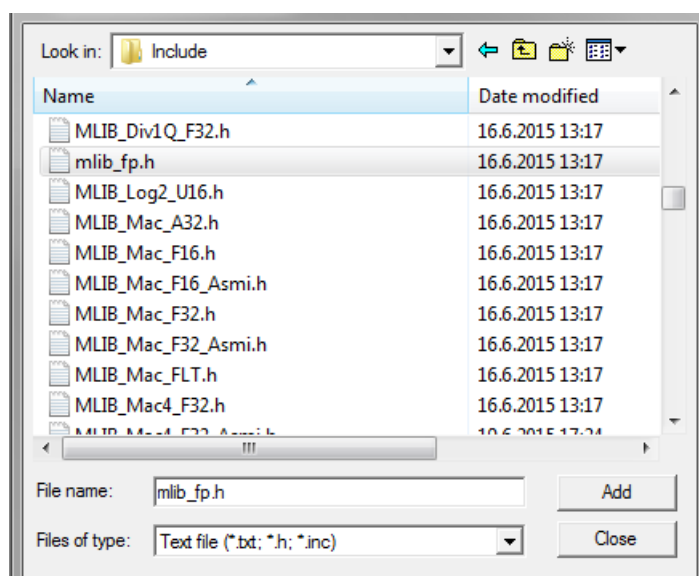
**Figure 1-21. FPU**

### 1.3.3 Linking the files into the project

GFLIB requires MLIB to be included too. The following steps show how to include all dependent modules.

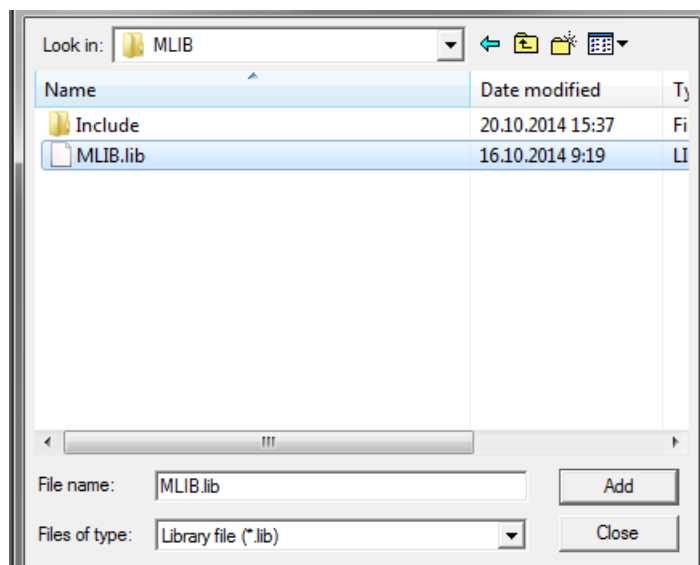
To include the library files in the project, create groups and add them.

1. Right-click the Target 1 node in the left-hand part of the Project tree, and select Add Group... from the menu. A new group with the name New Group is added.
2. Click the newly created group, and press F2 to rename it to RTCESL.
3. Right-click the RTCESL node, and select Add Existing Files to Group 'RTCESL'... from the menu.
4. Navigate into the library installation folder C:\NXP\RTCESL\CM7F\_RTCESL\_4.3\_KEIL\MLIB\Include, and select the *mllib\_fp.h* file. If the file does not appear, set the Files of type filter to Text file. Click Add. See [Figure 1-22](#).



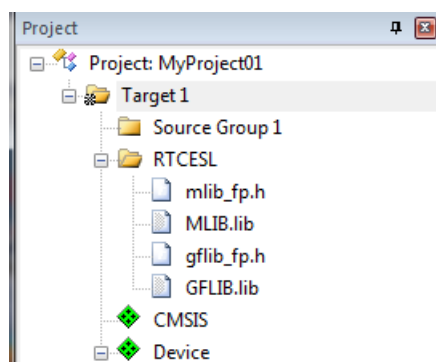
**Figure 1-22. Adding .h files dialog**

5. Navigate to the parent folder C:\NXP\RTCESL\CM7F\_RTCESL\_4.3\_KEIL\MLIB, and select the *mllib.lib* file. If the file does not appear, set the Files of type filter to Library file. Click Add. See [Figure 1-23](#).



**Figure 1-23. Adding .lib files dialog**

6. Navigate into the library installation folder C:\NXP\RTCESL\CM7F\_RTCESL\_4.3\_KEIL\GFLIB\Include, and select the *gflib\_fp.h* file. If the file does not appear, set the Files of type filter to Text file. Click Add.
7. Navigate to the parent folder C:\NXP\RTCESL\CM7F\_RTCESL\_4.3\_KEIL\GFLIB, and select the *gflib.lib* file. If the file does not appear, set the Files of type filter to Library file. Click Add.
8. Now, all necessary files are in the project tree; see [Figure 1-24](#). Click Close.



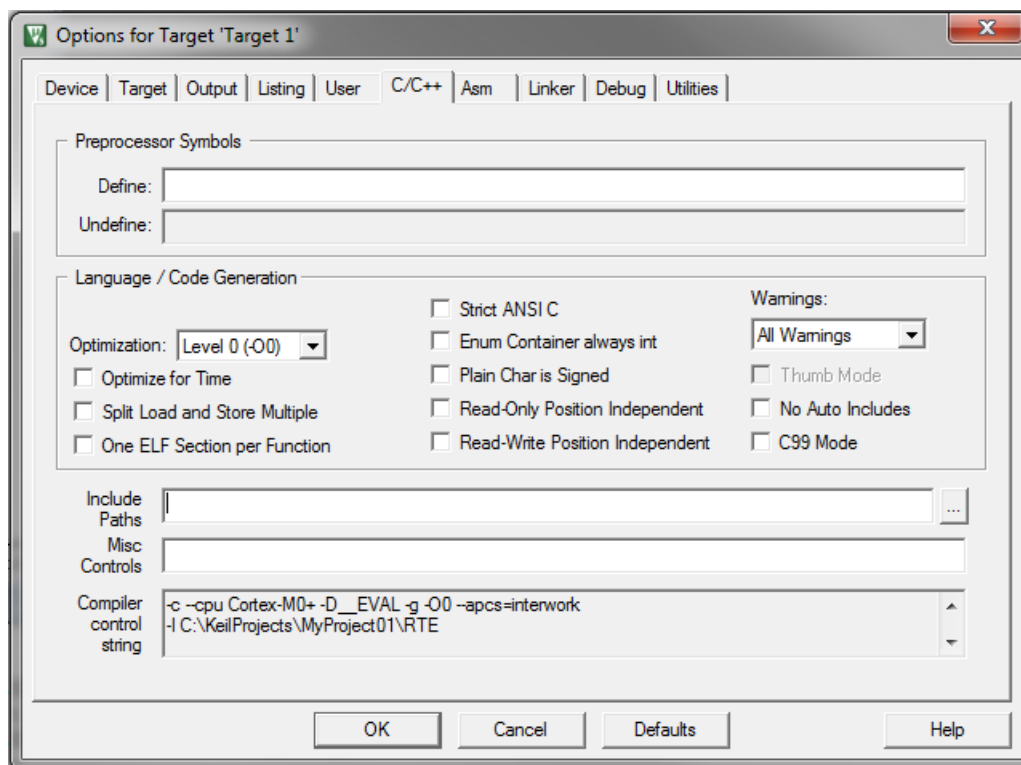
**Figure 1-24. Project workspace**

### 1.3.4 Library path setup

The following steps show the inclusion of all dependent modules.

1. In the main menu, go to Project > Options for Target 'Target1'..., and a dialog appears.
2. Select the C/C++ tab. See [Figure 1-25](#).

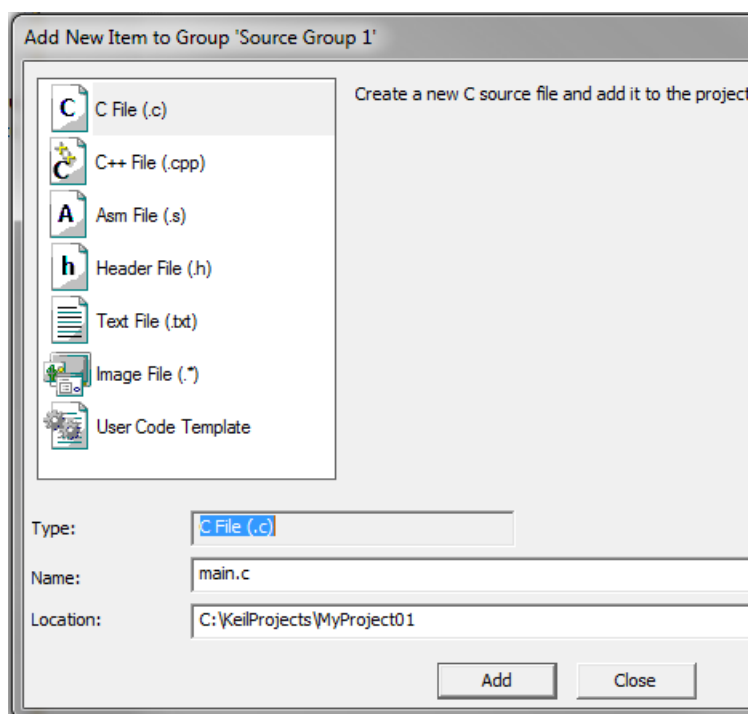
3. In the Include Paths text box, type the following paths (if there are more paths, they must be separated by ';') or add them by clicking the ... button next to the text box:
  - "C:\NXP\RTCESL\CM7F\_RTCSL\_4.3\_KEIL\MLIB\Include"
  - "C:\NXP\RTCESL\CM7F\_RTCSL\_4.3\_KEIL\GFLIB\Include"
4. Click OK.
5. Click OK in the main dialog.



**Figure 1-25. Library path addition**

Type the #include syntax into the code. Include the library into a source file. In the new project, it is necessary to create a source file:

1. Right-click the Source Group 1 node, and Add New Item to Group 'Source Group 1'... from the menu.
2. Select the C File (.c) option, and type a name of the file into the Name box, for example 'main.c'. See [Figure 1-26](#).



**Figure 1-26. Adding new source file dialog**

3. Click Add, and a new source file is created and opened up.
4. In the opened source file, include the following lines into the #include section, and create a main function:

```
#include "mlib_fp.h"
#include "gflib_fp.h"

int main(void)
{
    while(1);
}
```

When you click the Build (F7) icon, the project will be compiled without errors.

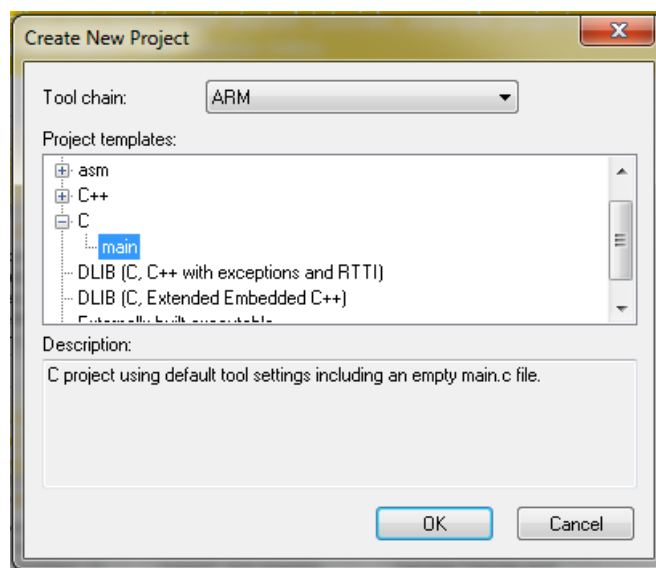
## 1.4 Library integration into project (IAR Embedded Workbench)

This section provides a step-by-step guide on how to quickly and easily include the GFLIB into an empty project or any SDK example or demo application projects using IAR Embedded Workbench. This example uses the default installation path (C:\NXP\RTCESL\CM7F\_RTCESL\_4.3\_IAR). If you have a different installation path, use that path instead. If any SDK project is intended to use (for example hello\_world project) go to [Linking the files into the project](#) chapter otherwise read next chapter.

### 1.4.1 New project (without SDK)

This example uses the NXP MKV58F1M0xxx22 part, and the default installation path (C:\NXP\RTCESL\CM7F\_RTCESL\_4.3\_IAR) is supposed. To start working on an application, create a new project. If the project already exists and is opened, skip to the next section. Perform these steps to create a new project:

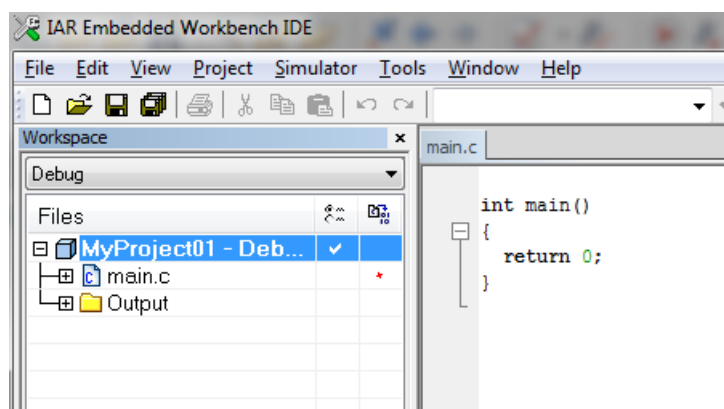
1. Launch IAR Embedded Workbench.
2. In the main menu, select Project > Create New Project... so that the "Create New Project" dialog appears. See [Figure 1-27](#).



**Figure 1-27. Create New Project dialog**

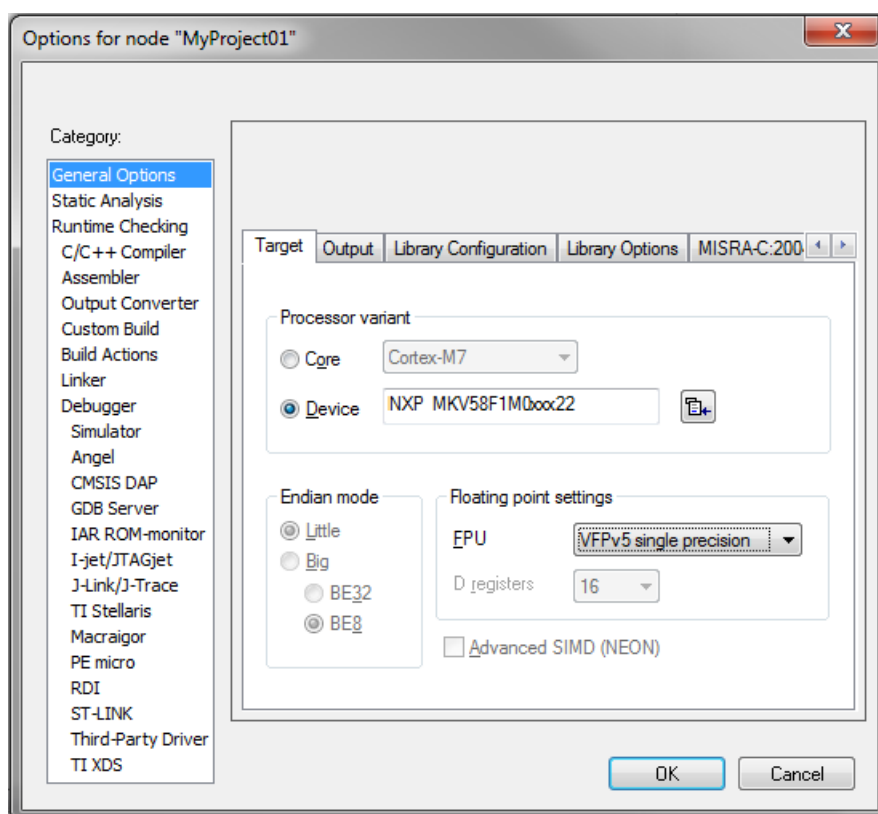
3. Expand the C node in the tree, and select the "main" node. Click OK.
4. Navigate to the folder where you want to create the project, for example, C:\IARProjects\MyProject01. Type the name of the project, for example, MyProject01. Click Save, and a new project is created. The new project is now visible in the left-hand part of IAR Embedded Workbench. See [Figure 1-28](#).





**Figure 1-28. New project**

5. In the main menu, go to Project > Options..., and a dialog appears.
6. In the Target tab, select the Device option, and click the button next to the dialog to select the MCU. In this example, select NXP > KV5x > NXP MKV58F1M0xxx22. Select VFPv5 single precision in the FPU option. Click OK. See [Figure 1-29](#).

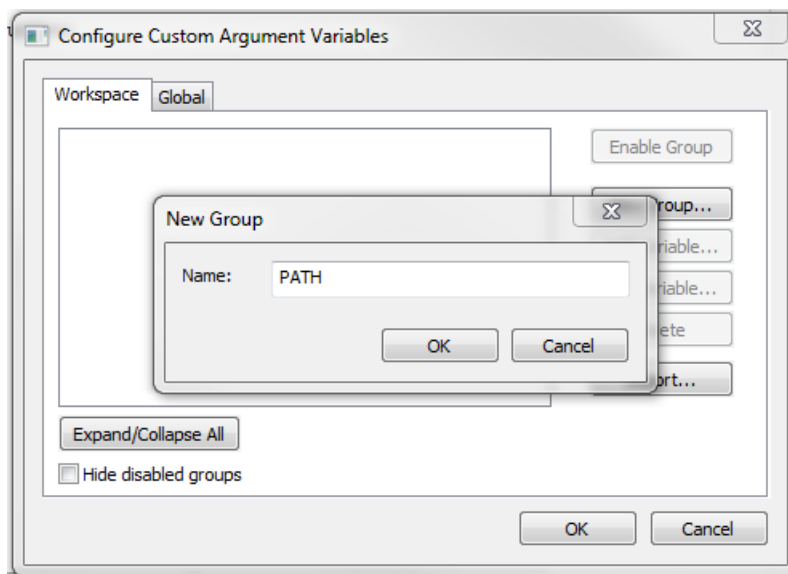


**Figure 1-29. Options dialog**

## 1.4.2 Library path variable

To make the library integration easier, create a variable that will hold the information about the library path.

1. In the main menu, go to Tools > Configure Custom Argument Variables..., and a dialog appears.
2. Click the New Group button, and another dialog appears. In this dialog, type the name of the group PATH, and click OK. See [Figure 1-30](#).



**Figure 1-30. New Group**

3. Click on the newly created group, and click the Add Variable button. A dialog appears.
4. Type this name: RTCESL\_LOC
5. To set up the value, look for the library by clicking the '...' button, or just type the installation path into the box: C:\NXP\RTCESL\CM7F\_RTCESL\_4.3\_IAR. Click OK.
6. In the main dialog, click OK. See [Figure 1-31](#).

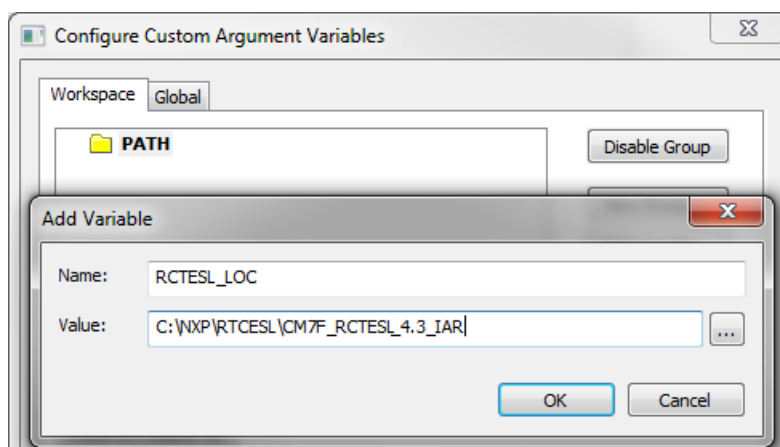


Figure 1-31. New variable

### 1.4.3 Linking the files into the project

GFLIB requires MLIB to be included too. The following steps show the inclusion of all dependent modules.

To include the library files into the project, create groups and add them.

1. Go to the main menu Project > Add Group...
2. Type RTCESL, and click OK.
3. Click on the newly created node RTCESL, go to Project > Add Group..., and create a MLIB subgroup.
4. Click on the newly created node MLIB, and go to the main menu Project > Add Files... See [Figure 1-33](#).
5. Navigate into the library installation folder C:\NXP\RTCESL\CM7F\_RTCESEL\_4.3\_IAR\MLIB\Include, and select the *mlib\_fp.h* file. (If the file does not appear, set the file-type filter to Source Files.) Click Open. See [Figure 1-32](#).
6. Navigate into the library installation folder C:\NXP\RTCESL\CM7F\_RTCESEL\_4.3\_IAR\MLIB, and select the *mlib.a* file. If the file does not appear, set the file-type filter to Library / Object files. Click Open.

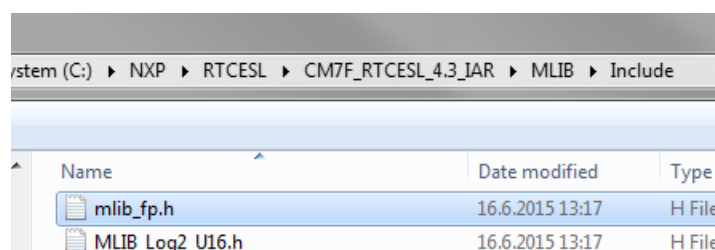
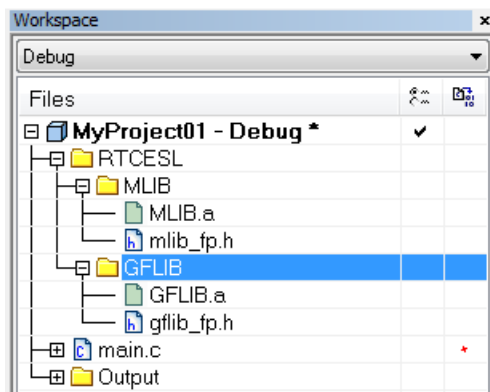


Figure 1-32. Add Files dialog

7. Click on the RTCESL node, go to Project > Add Group..., and create a GFLIB subgroup.

8. Click on the newly created node GFLIB, and go to the main menu Project > Add Files....
9. Navigate into the library installation folder C:\NXP\RTCESL\CM7F\_RTCESL\_4.3\_IAR\GFLIB\Include, and select the *gflib\_fp.h* file. (If the file does not appear, set the file-type filter to Source Files.) Click Open.
10. Navigate into the library installation folder C:\NXP\RTCESL\CM7F\_RTCESL\_4.3\_IAR\GFLIB, and select the *gflib.a* file. If the file does not appear, set the file-type filter to Library / Object files. Click Open.
11. Now you will see the files added in the workspace. See [Figure 1-33](#).

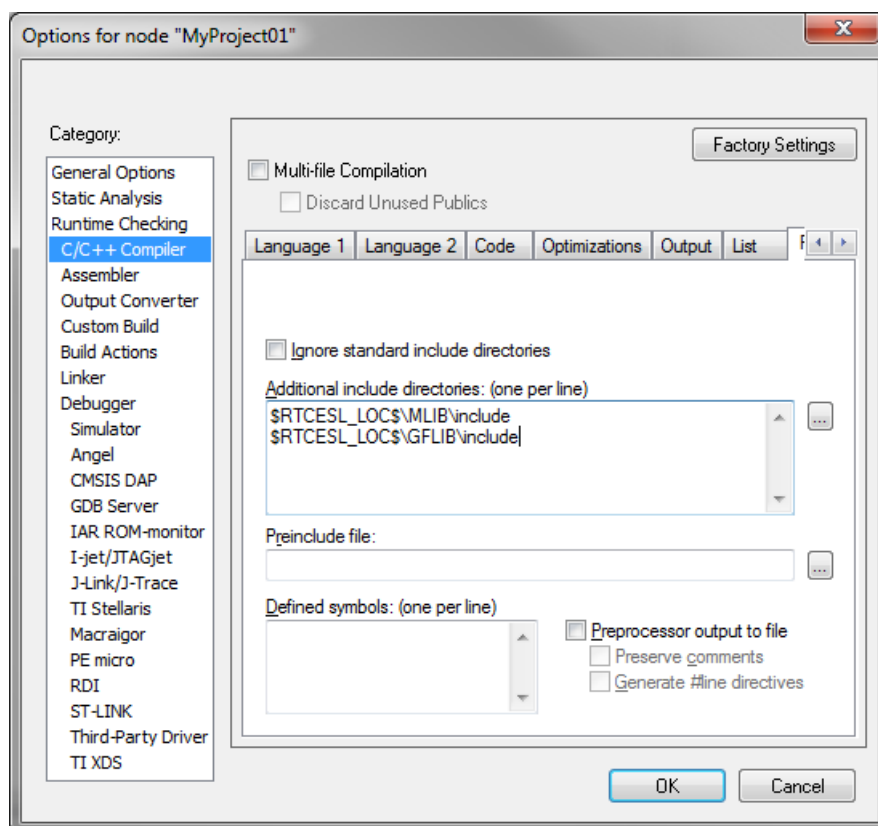


**Figure 1-33. Project workspace**

## 1.4.4 Library path setup

The following steps show the inclusion of all dependent modules:

1. In the main menu, go to Project > Options..., and a dialog appears.
2. In the left-hand column, select C/C++ Compiler.
3. In the right-hand part of the dialog, click on the Preprocessor tab (it can be hidden in the right; use the arrow icons for navigation).
4. In the text box (at the Additional include directories title), type the following folder (using the created variable):
  - \$RTCESL\_LOC\$\MLIB\Include
  - \$RTCESL\_LOC\$\GFLIB\Include
5. Click OK in the main dialog. See [Figure 1-34](#).



**Figure 1-34. Library path addition**

Type the `#include` syntax into the code. Include the library included into the *main.c* file. In the workspace tree, double-click the *main.c* file. After the *main.c* file opens up, include the following lines into the `#include` section:

```
#include "mlib_fp.h"
#include "gflib_fp.h"
```

When you click the Make icon, the project will be compiled without errors.



## Chapter 2

# Algorithms in detail

### 2.1 GFLIB\_Sin

The [GFLIB\\_Sin](#) function implements the polynomial approximation of the sine function. It provides a computational method for the calculation of a standard trigonometric sine function  $\sin(x)$ , using the 9<sup>th</sup> order Taylor polynomial approximation. The Taylor polynomial approximation of a sine function is expressed as follows:

$$\sin(x) = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \frac{x^9}{9!}$$

**Equation 1.**

$$\sin(x) = x(d_1 + x^2(d_3 + x^2(d_5 + x^2(d_7 + x^2d_9))))$$

**Equation 2.**

where the constants are:

$$d_1 = 1$$

$$d_3 = -\frac{1}{3!}$$

$$d_5 = \frac{1}{5!}$$

$$d_7 = -\frac{1}{7!}$$

$$d_9 = \frac{1}{9!}$$

The fractional arithmetic is limited to the range  $<-1 ; 1)$ , so the input argument can only be within this range. The input argument is the multiplier of  $\pi$ :  $\sin(\pi \cdot x)$ , where the user passes the  $x$  argument. Example: if the input is  $-0.5$ , it corresponds to  $-0.5\pi$ .

The fractional function  $\sin(\pi \cdot x)$  is expressed using the 9<sup>th</sup> order Taylor polynomial as follows:

$$\sin(\pi \cdot x) = x(c_1 + x^2(c_3 + x^2(c_5 + x^2(c_7 + x^2c_9))))$$

**Equation 3.**

where:

$$c_1 = d_1 \pi^1 = \pi$$

$$c_3 = d_3 \pi^3 = -\frac{\pi^3}{3!}$$

$$c_5 = d_5 \pi^5 = \frac{\pi^5}{5!}$$

$$c_7 = d_7 \pi^7 = -\frac{\pi^7}{7!}$$

$$c_9 = d_9 \pi^9 = \frac{\pi^9}{9!}$$

## 2.1.1 Available versions

The function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range <-1 ; 1). The result may saturate.
- Floating-point output - the output is the floating-point result within the range <-1.0 ; 1.0>.
- Floating-point output with accumulator input - the output is the floating-point result within the range <-1.0 ; 1.0>. The input is the accumulator angle in radians divided by  $\pi$ .

The available versions of the [GFLIB\\_Sin](#) function are shown in the following table:

**Table 2-1. Function versions**

Function name	Input type	Result type	Description
GFLIB_Sin_F16	<a href="#">frac16_t</a>	<a href="#">frac16_t</a>	Calculation of the $\sin(\pi \cdot x)$ , where the input argument is a 16-bit fractional value normalized to the range <-1 ; 1) that represents an angle in radians within the range < $-\pi$ ; $\pi$ ). The output is a 16-bit fractional value within the range <-1 ; 1).
GFLIB_Sin_FLT	<a href="#">float_t</a>	<a href="#">float_t</a>	Calculation of the $\sin(x)$ , where the input argument is a 32-bit single precision floating-point value in radians within the range < $-\pi$ ; $\pi$ ). The output is a 32-bit single precision floating-point value within the range <-1.0 ; 1.0>.
GFLIB_Sin_FLTa	<a href="#">acc32_t</a>	<a href="#">float_t</a>	Calculation of the $\sin(\pi \cdot x)$ , where the input argument is a 32-bit accumulator value where the fractional part <-1 ; 1) represents the angle within the range < $-\pi$ ; $\pi$ ). The output is a 32-bit single precision floating-point value within the range <-1.0 ; 1.0>.

## 2.1.2 Declaration

The available [GFLIB\\_Sin](#) functions have the following declarations:

```

frac16\_t GFLIB_Sin_F16(frac16\_t fl6Angle)
float\_t GFLIB_Sin_FLT(float\_t fltAngle)
float\_t GFLIB_Sin_FLTa(acc32\_t a32Angle)

```



## 2.1.3 Function use

The use of the [GFLIB\\_Sin](#) function is shown in the following example:

```
#include "gflib.h"

static frac16_t f16Result;
static frac16_t f16Angle;

void main(void)
{
    f16Angle = FRAC16(0.333333);          /* f16Angle = 0.333333 [60°] */
    /* f16Result = sin(f16Angle); (π * f16Angle[rad]) = deg * (π / 180) */
    f16Result = GFLIB_Sin_F16(f16Angle);
}
```

## 2.2 GFLIB\_Cos

The [GFLIB\\_Cos](#) function implements the polynomial approximation of the cosine function. This function computes the  $\cos(x)$  using the ninth-order Taylor polynomial approximation of the sine function, and its equation is as follows:

$$\cos(x) = \sin\left[\frac{\pi}{2} + |x|\right]$$

**Equation 4.**

Because the fractional arithmetic is limited to the range  $<-1 ; 1)$ , the input argument can only be within this range. The input argument is the multiplier of  $\pi$ :  $\cos(\pi \cdot x)$ , where the user passes the  $x$  argument. For example, if the input is  $-0.5$ , it corresponds to  $-0.5\pi$ .

### 2.2.1 Available versions

This function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range  $<-1 ; 1)$ . The result may saturate.
- Floating-point output - the output is the floating-point result within the range  $<-1.0 ; 1.0>$ .
- Floating-point output with accumulator input - the output is the floating-point result within the range  $<-1.0 ; 1.0>$ . The input is the accumulator angle in radians divided by  $\pi$ .

The available versions of the [GFLIB\\_Cos](#) function are shown in the following table:

**Table 2-2. Function versions**

Function name	Input type	Result type	Description
GFLIB_Cos_F16	<a href="#">frac16_t</a>	<a href="#">frac16_t</a>	Calculation of $\cos(\pi \cdot x)$ , where the input argument is a 16-bit fractional value, normalized to the range $<-1 ; 1)$ that represents an angle in radians within the range $<-\pi ; \pi)$ . The output is a 16-bit fractional value within the range $<-1 ; 1)$ .
GFLIB_Cos_FLT	<a href="#">float_t</a>	<a href="#">float_t</a>	Calculation of $\cos(x)$ , where the input argument is a 32-bit single precision floating-point value in radians within the range $<-\pi ; \pi)$ . The output is a 32-bit single precision floating-point value within the range $<-1.0 ; 1.0>$ .
GFLIB_Cos_FLTa	<a href="#">acc32_t</a>	<a href="#">float_t</a>	Calculation of the $\cos(\pi \cdot x)$ , where the input argument is a 32-bit accumulator value where the fractional part $<-1 ; 1)$ represents the angle within the range $<-\pi ; \pi)$ . The output is a 32-bit single precision floating-point value within the range $<-1.0 ; 1.0>$ .

## 2.2.2 Declaration

The available [GFLIB\\_Cos](#) functions have the following declarations:

```
frac16_t GFLIB_Cos_F16(frac16_t f16Angle)
float_t GFLIB_Cos_FLT(float_t fltAngle)
float_t GFLIB_Cos_FLTa(acc32_t a32Angle)
```

## 2.2.3 Function use

The use of the [GFLIB\\_Cos](#) function is shown in the following example:

```
#include "gflib.h"

static frac16_t f16Result;
static frac16_t f16Angle;

void main(void)
{
    f16Angle = FRAC16(0.333333);          /* f16Angle = 0.333333 [60°] */

    /* f16Result = cos(f16Angle); (π * f16Angle[rad]) = deg * (π / 180) */
    f16Result = GFLIB_Cos_F16(f16Angle);
}
```

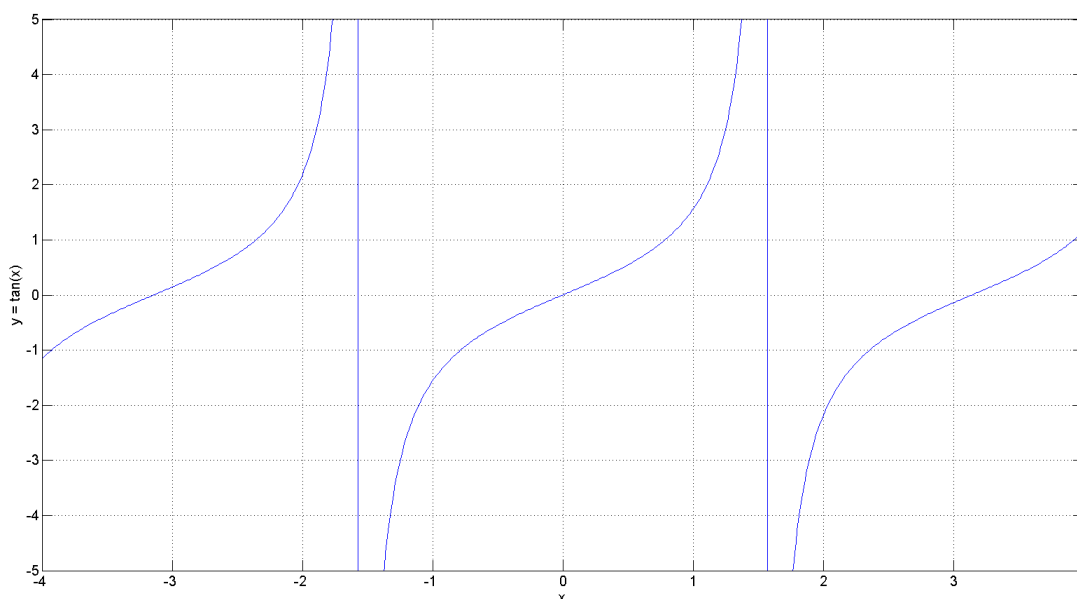
## 2.3 GFLIB\_Tan

The **GFLIB\_Tan** function provides a computational method for calculation of a standard trigonometric tangent function  $\tan(x)$ , using the piece-wise polynomial approximation. Function  $\tan(x)$  takes an angle and returns the ratio of two sides of a right-angled triangle. The ratio is the length of the side opposite the angle divided by the length of the side adjacent to the angle.

$$\tan(x) = \frac{\sin(x)}{\cos(x)}$$

### Equation 5.

Because both  $\sin(x)$  and  $\cos(x)$  are defined in interval  $[-\pi; \pi]$ , the function  $\tan(x)$  is equal to zero when  $\sin(x)=0$  and is equal to infinity when  $\cos(x)=0$ . The graph of  $\tan(x)$  is shown in the following figure:



**Figure 2-1. Course of the function GFLIB\_Tan**

The fractional arithmetic is limited to the range  $[-1; 1]$  so the input argument can only be within this range. The input argument is the multiplier of  $\pi$ :  $\tan(\pi \cdot x)$  where you pass the  $x$  argument. Example: if the input is  $-0.5$ , it corresponds to  $-0.5\pi$ . The output of the function is limited to the range  $[-1; 1]$  for the fractional arithmetic. For the points where the function is not defined, the output is fractional  $-1$ .

## 2.3.1 Available versions

The function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range  $<-1 ; 1$ ). The result may saturate.
- Floating-point output - the output is the floating-point result.
- Floating-point output with accumulator input - the output is the floating-point result. The input is the accumulator angle in radians divided by  $\pi$ .

The available versions of the [GFLIB\\_Tan](#) function are shown in the following table:

**Table 2-3. Function versions**

Function name	Input type	Result type	Description
GFLIB_Tan_F16	<a href="#">frac16_t</a>	<a href="#">frac16_t</a>	Calculation of the $\tan(\pi \cdot x)$ where the input argument is a 16-bit fractional value normalized to the range $<-1 ; 1$ ) that represents an angle in radians within the range $<-\pi ; \pi$ ). The output is a 16-bit fractional value within the range $<-1 ; 1$ ).
GFLIB_Tan_FLT	<a href="#">float_t</a>	<a href="#">float_t</a>	Calculation of the $\tan(x)$ where the input argument is a 32-bit single precision floating-point value in radians within the range $<-\pi ; \pi$ ). The output is a 32-bit single precision floating-point value within the full range.
GFLIB_Tan_FLTa	<a href="#">acc32_t</a>	<a href="#">float_t</a>	Calculation of the $\tan(\pi \cdot x)$ , where the input argument is a 32-bit accumulator value where the fractional part $<-1 ; 1$ ) represents the angle within the range $<-\pi ; \pi$ ). The output is a 32-bit single precision floating-point value within the full range.

## 2.3.2 Declaration

The available [GFLIB\\_Tan](#) functions have the following declarations:

```

frac16\_t GFLIB_Tan_F16(frac16\_t f16Angle)
float\_t GFLIB_Tan_FLT(float\_t fltAngle)
float\_t GFLIB_Tan_FLTa(acc32\_t a32Angle)

```

## 2.3.3 Function use

The use of the [GFLIB\\_Tan](#) function is shown in the following example:

```

#include "gflib.h"

static frac16\_t f16Result;
static frac16\_t f16Angle;

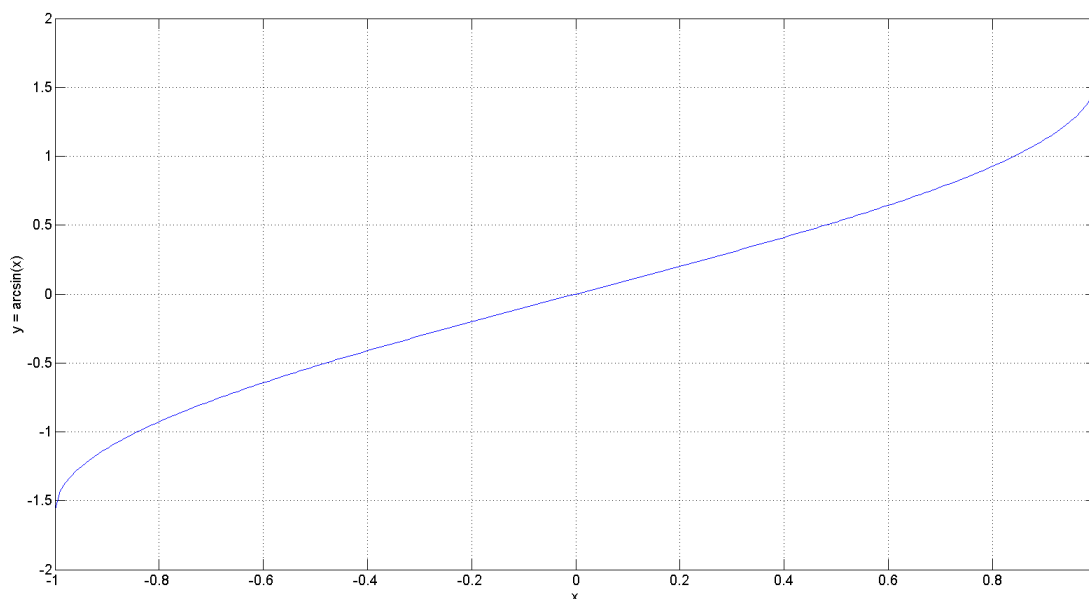
void main(void)
{
    f16Angle = FRAC16(0.1);          /* f16Angle = 0.1 [18°] */

    /* f16Result = tan(f16Angle); (π * f16Angle[rad]) = deg * (π / 180) */
    f16Result = GFLIB_Tan_F16(f16Angle);
}

```

## 2.4 GFLIB\_Asin

The [GFLIB\\_Asin](#) function provides a computational method for calculation of a standard inverse trigonometric arcsine function  $\arcsin(x)$ , using the piece-wise polynomial approximation. Function  $\arcsin(x)$  takes the ratio of the length of the opposite side to the length of the hypotenuse and returns the angle.



**Figure 2-2. Course of the function GFLIB\_Asin**

The fractional arithmetic is limited by the range  $<-1;1)$  so the output can only be within this range. This range corresponds to the angle  $<-1;1)$ . Example: if the output is -0.5 it corresponds to  $-0.5\pi$ .

### 2.4.1 Available versions

The function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range  $<-1;1)$ . The result may saturate.
- Floating point output - the output is the floating point result within the range  $<-\pi;\pi>$ .

The available versions of the [GFLIB\\_Asin](#) function are shown in the following table:

**Table 2-4. Function versions**

Function name	Input type	Result type	Description
GFLIB_Asin_F16	<a href="#">frac16_t</a>	<a href="#">frac16_t</a>	Calculation of the $\arcsin(x) / \pi$ where the input argument is a 16-bit fractional within the range $<-1;1>$ . The output is a 16-bit fractional value within the range $<-1;1>$ that represents an angle in radians within the range $<-\pi;\pi>$ .
GFLIB_Asin_FLT	<a href="#">float_t</a>	<a href="#">float_t</a>	Calculation of the $\arcsin(x)$ where the input argument is a 32-bit single precision floating point value within the range $<-1;1>$ . The output is a 32-bit single precision floating point value within the range $<-\pi;\pi>$ .

## 2.4.2 Declaration

The available [GFLIB\\_Asin](#) functions have the following declarations:

```
frac16\_t GFLIB_Asin_F16(frac16\_t f16Val)
float\_t GFLIB_Asin_FLT(float\_t fltVal)
```

## 2.4.3 Function use

The use of the [GFLIB\\_Asin](#) function is shown in the following example:

```
#include "gflib.h"

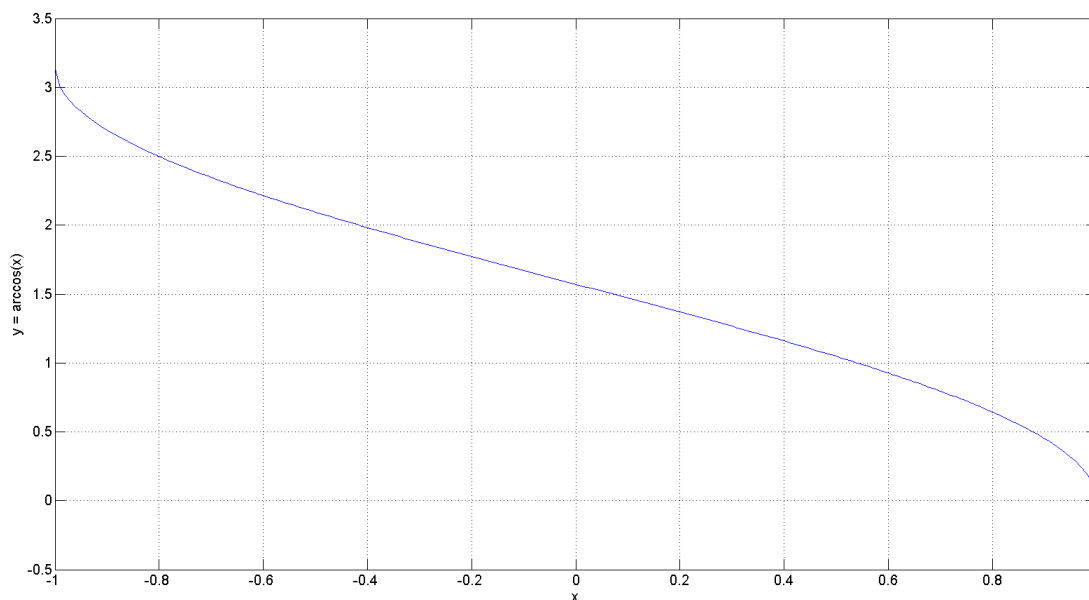
static frac16\_t f16Result;
static frac16\_t f16Value;

void main(void)
{
    f16Value = FRAC16(0.5);          /* f16Value = 0.5 */

    /* f16Result = arcsin(f16Value); */
    f16Result = GFLIB_Asin_F16(f16Value);
}
```

## 2.5 GFLIB\_Acos

The [GFLIB\\_Acos](#) function provides a computational method for calculation of a standard inverse trigonometric arccosine function  $\arccos(x)$ , using the piece-wise polynomial approximation. Function  $\arccos(x)$  takes the ratio of the length of the adjacent side to the length of the hypotenuse and returns the angle.



**Figure 2-3. Course of the function GFLIB\_Acos**

The fractional arithmetic is limited by the range  $<-1;1)$  so the output can only be within this range. This range corresponds to the angle  $<-1;1)$ . Example: if the output is -0.5 it corresponds to  $-0.5\pi$ .

## 2.5.1 Available versions

The function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range  $<-1;1)$ . The result may saturate.
- Floating point output - the output is the floating point result within the range  $<-\pi;\pi>$ .

The available versions of the [GFLIB\\_Acos](#) function are shown in the following table:

**Table 2-5. Function versions**

Function name	Input type	Result type	Description
GFLIB_Acos_F16	<a href="#">frac16_t</a>	<a href="#">frac16_t</a>	Calculation of the $\arccos(x) / \pi$ where the input argument is a 16-bit fractional within the range $<-1;1)$ . The output is a 16-bit fractional value within the range $<-1;1)$ that represents an angle in radians within the range $<-\pi;\pi)$ .
GFLIB_Acos_FLT	<a href="#">float_t</a>	<a href="#">float_t</a>	Calculation of the $\arccos(x)$ where the input argument is a 32-bit single precision floating point value within the range $<-1;1>$ . The output is a 32-bit single precision floating point value within the range $<-\pi;\pi>$ .

## 2.5.2 Declaration

The available [GFLIB\\_Acos](#) functions have the following declarations:

```
frac16_t GFLIB_Acos_F16(frac16_t f16Val)
float_t GFLIB_Acos_FLT(float_t fltVal)
```

## 2.5.3 Function use

The use of the [GFLIB\\_Acos](#) function is shown in the following example:

```
#include "gflib.h"

static frac16_t f16Result;
static frac16_t f16Value;

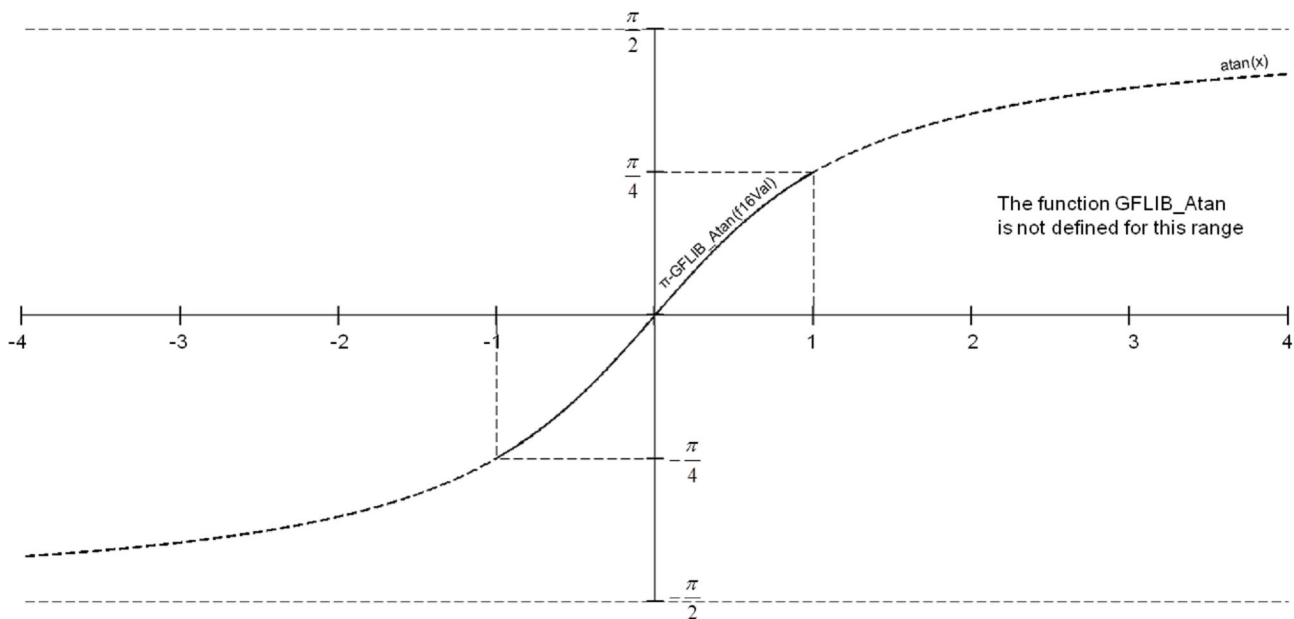
void main(void)
{
    f16Value = FRAC16(0.5);          /* f16Value = 0.5 */

    /* f16Result = arcscos(f16Value); */
    f16Result = GFLIB_Acos_F16(f16Value);
}
```

## 2.6 GFLIB\_Atan

The [GFLIB\\_Atan](#) function implements the polynomial approximation of the arctangent function. It provides a computational method for calculating the standard trigonometric arctangent function  $\arctan(x)$ , using the piece-wise minimax polynomial approximation. Function  $\arctan(x)$  takes a ratio, and returns the angle of two sides of a right-angled triangle. The ratio is the length of the side opposite to the angle divided by the length of the side adjacent to the angle. The graph of the  $\arctan(x)$  is shown in the following figure:





**Figure 2-4. Course of the GFLIB\_Atan function**

The fractional arithmetic version of the [GFLIB\\_Atan](#) function is limited to a certain range of inputs  $<-1 ; 1)$ . Because the arctangent values are the same, with just an opposite sign for the input ranges  $<-1 ; 0)$  and  $<0 ; 1)$ , the approximation of the arctangent function over the entire defined range of input ratios can be simplified to the approximation for a ratio in the range  $<0 ; 1)$ . After that, the result will be negated, depending on the input ratio.

## 2.6.1 Available versions

The function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range  $<-0.25 ; 0.25)$ , which corresponds to the angle  $<-\pi / 4 ; \pi / 4)$ .
- Floating-point output - the output is the floating-point result within the range  $<-\pi / 2 ; \pi / 2>$ .
- Accumulator output with floating-point input - the output is the accumulator angle within the range  $(-0.5 ; 0.5)$ , which corresponds to the angle  $(-\pi / 2 ; \pi / 2)$ . The input is the floating-point value.

The available versions of the [GFLIB\\_Atan](#) function are shown in the following table:

**Table 2-6. Function versions**

Function name	Input type	Result type	Description
GFLIB_Atan_F16	<a href="#">frac16_t</a>	<a href="#">frac16_t</a>	Input argument is a 16-bit fractional value within the range $[-1; 1]$ . The output is the arctangent of the input as a 16-bit fractional value, normalized within the range $[-0.25; 0.25]$ , which represents an angle (in radians) in the range $[-\pi/4; \pi/4]$ $[-45^\circ; 45^\circ]$ .
GFLIB_Atan_FLT	<a href="#">float_t</a>	<a href="#">float_t</a>	Input argument is a 32-bit single precision floating-point value within the full type's range. The output is the arctangent of the input as a 32-bit single precision floating-point value in radians.
GFLIB_Atan_A32f	<a href="#">float_t</a>	<a href="#">acc32_t</a>	Input argument is a 32-bit single precision floating-point value within the full type's range. The output is the arctangent of the input as a 32-bit accumulator value, normalized within the range $[-0.5; 0.5]$ , which represents an angle (in radians) in the range $[-\pi/2; \pi/2]$ $[-90^\circ; 90^\circ]$ .

## 2.6.2 Declaration

The available [GFLIB\\_Atan](#) functions have the following declarations:

```
frac16\_t GFLIB_Atan_F16(frac16\_t f16Val)
float\_t GFLIB_Atan_FLT(float\_t fltVal)
acc32\_t GFLIB_Atan_A32f(float\_t fltVal)
```

## 2.6.3 Function use

The use of the [GFLIB\\_Atan](#) function is shown in the following example:

```
#include "gflib.h"

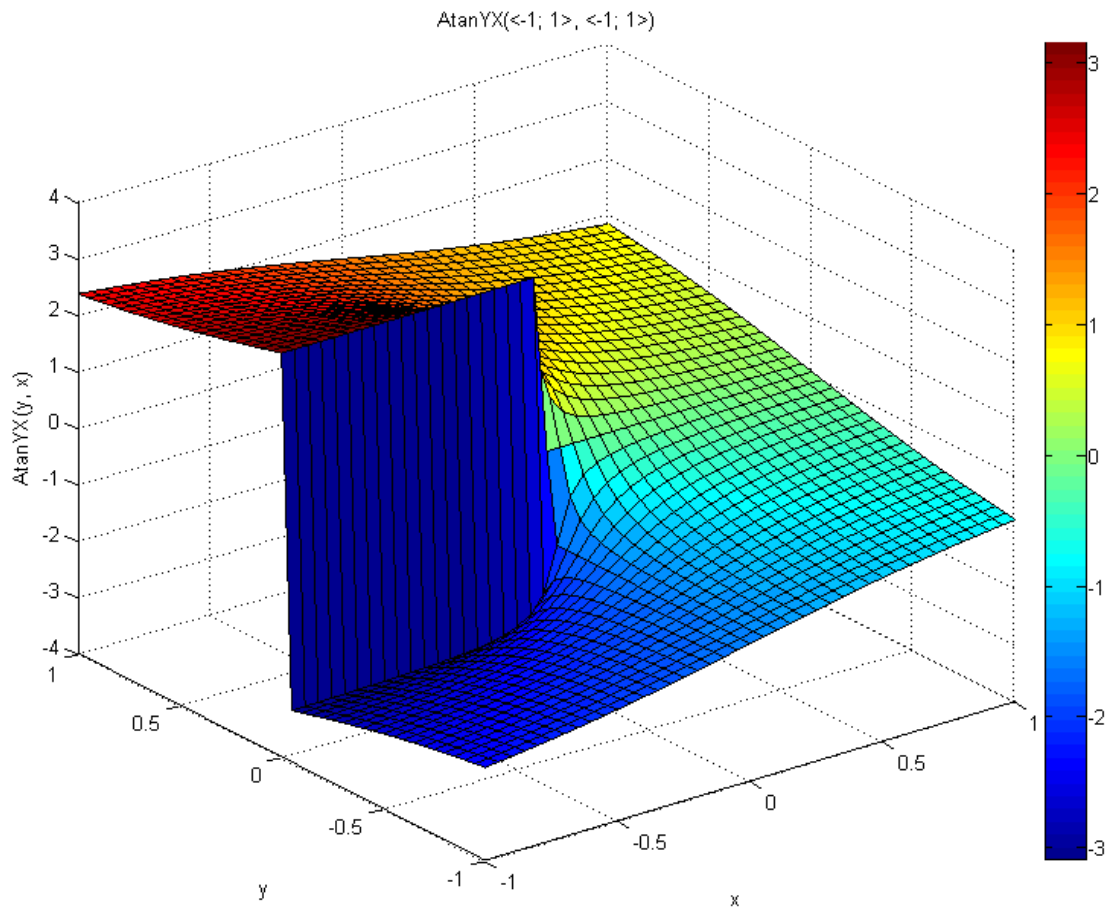
static frac16\_t f16Result;
static frac16\_t f16Val;

void main(void)
{
    f16Val = FRAC16(0.57735026918962576450914878050196);    /* f16Val = tan(30°) */

    /* f16Result = atan(f16Val); f16Result * 180 => angle[degree] */
    f16Result = GFLIB_Atan_F16(f16Val);
}
```

## 2.7 GFLIB\_AtanYX

The [GFLIB\\_AtanYX](#) function computes the angle, where its tangent is  $y / x$  (see the figure below). This calculation is based on the input argument division ( $y$  divided by  $x$ ), and the piece-wise polynomial approximation.



**Figure 2-5. Course of the GFLIB\_AtanYX function**

The first parameter  $Y$  is the ordinate (the  $x$  coordinate), and the second parameter  $X$  is the abscissa (the  $x$  coordinate). The counter-clockwise direction is assumed to be positive, and thus a positive angle is computed if the provided ordinate ( $Y$ ) is positive. Similarly, a negative angle is computed for the negative ordinate. The calculations are performed in several steps. In the first step, the angle is positioned within the correct half-quarter of the circumference of a circle by dividing the angle into two parts: the integral multiple of  $45^\circ$  (half-quarter), and the remaining offset within the  $45^\circ$  range. Simple geometric properties of the Cartesian coordinate system are used to calculate the coordinates of the vector with the calculated angle offset. In the second step, the vector ordinate is divided by the vector abscissa ( $y / x$ ) to obtain the tangent value of the angle offset. The angle offset is computed by applying the [GFLIB\\_Atana](#) function. The sum of the integral multiple of half-quarters and the angle offset within a single halfquarter form the angle is computed.

The function returns 0 if both input arguments equal 0, and sets the output error flag; in other cases, the output flag is cleared. When compared to the [GFLIB\\_Atan](#) function, the [GFLIB\\_AtanYX](#) function places the calculated angle correctly within the fractional range  $<-\pi ; \pi>$ .

In the fractional arithmetic, both input parameters are assumed to be in the fractional range  $<-1 ; 1>$ . The output is within the range  $<-1 ; 1>$ , which corresponds to the real range  $<-\pi ; \pi>$ .

## 2.7.1 Available versions

This function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range  $<-1 ; 1>$ , which corresponds to the angle  $<-\pi ; \pi>$ .
- Floating-point output - the output is the floating-point result within the range  $<-\pi ; \pi>$ .
- Accumulator output with floating-point input - the output is the accumulator angle within the range  $<-1 ; 1>$ , which corresponds to the angle  $<-\pi ; \pi>$ . The input is the floating-point value.

The available versions of the [GFLIB\\_AtanYX](#) function are shown in the following table:

**Table 2-7. Function versions**

Function name	Input type		Output type	Result type
	Y	X	Error flag	
GFLIB_AtanYX_F16	<a href="#">frac16_t</a>	<a href="#">frac16_t</a>	<a href="#">bool_t</a> *	<a href="#">frac16_t</a>
	The first input argument is a 16-bit fractional value that contains the ordinate of the input vector (y coordinate). The second input argument is a 16-bit fractional value that contains the abscissa of the input vector (x coordinate). The result is the arctangent of the input arguments as a 16-bit fractional value within the range $<-1 ; 1>$ , which corresponds to the real angle range $<-\pi ; \pi>$ . The function sets the boolean error flag pointed to by the output parameter if both inputs are zero; in other cases, the output flag is cleared.			
GFLIB_AtanYX_FLT	<a href="#">float_t</a>	<a href="#">float_t</a>	<a href="#">bool_t</a> *	<a href="#">float_t</a>
	The first input argument is a 32-bit single precision floating-point value, which contains the ordinate of the input vector (y coordinate). The second input argument is a 32-bit single precision floating-point value, which contains the abscissa of the input vector (x coordinate). The result is the arctangent of the input arguments as a 32-bit single precision floating-point value within the range $<-\pi ; \pi>$ . The function sets the boolean error flag pointed to by the output parameter if both inputs are zero; in other cases, the output flag is cleared.			
GFLIB_AtanYX_A32ff	<a href="#">float_t</a>	<a href="#">float_t</a>	<a href="#">bool_t</a> *	<a href="#">acc32_t</a>
	The first input argument is a 32-bit single precision floating-point value, which contains the ordinate of the input vector (y coordinate). The second input argument is a 32-bit single precision floating-point value, which contains the abscissa of the input vector (x coordinate). The result is the arctangent of the input arguments as a 32-bit accumulator value within the range $<-1 ; 1>$ , which corresponds to the real angle range $<-\pi ; \pi>$ . The function sets the boolean error flag pointed to by the output parameter if both inputs are zero; in other cases, the output flag is cleared.			

## 2.7.2 Declaration

The available [GFLIB\\_AtanYX](#) functions have the following declarations:

```
frac16_t GFLIB_AtanYX_F16(frac16_t f16Y, frac16_t f16X, bool_t *pbErrFlag)
float_t GFLIB_AtanYX_FLT(float_t fltY, float_t fltX, bool_t *pbErrFlag)
acc32_t GFLIB_AtanYX_a32ff(float_t fltY, float_t fltX, bool_t *pbErrFlag)
```

## 2.7.3 Function use

The use of the [GFLIB\\_AtanYX](#) function is shown in the following example:

```
#include "gflib.h"

static frac16_t f16Result;
static frac16_t f16Y, f16X;
static bool_t bErrFlag;

void main(void)
{
    f16Y = FRAC16(0.9);          /* f16Y = 0.9 */
    f16X = FRAC16(0.3);          /* f16X = 0.3 */

    /* f16Result = atan(f16Y / f16X); f16Result * 180 => angle [degree] */
    f16Result = GFLIB_AtanYX_F16(f16Y, f16X, &bErrFlag);
}
```

## 2.8 GFLIB\_Sqrt

The [GFLIB\\_Sqrt](#) function returns the square root of the input value. The input must be a non-negative number, otherwise the function returns undefined results. See the following equation:

$$\text{GFLIB\_Sqrt}(x) = \begin{cases} \sqrt{x}, & x \geq 0 \\ \text{undefined}, & x < 0 \end{cases}$$

**Equation 6. Algorithm formula**

### 2.8.1 Available versions

This function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range  $<0 ; 1$ ). The function is only defined for non-negative inputs. The function returns undefined results out of this condition.
- Floating-point output - the output is the floating-point non-negative result. The function is only defined for non-negative inputs. The function returns undefined results out of this condition.

The available versions of the [GFLIB\\_Sqrt](#) function are shown in the following table:

**Table 2-8. Function versions**

Function name	Input type	Result type	Description
GFLIB_Sqrt_F16	<a href="#">frac16_t</a>	<a href="#">frac16_t</a>	The input value is a 16-bit fractional value, limited to the range $<0 ; 1$ ). The function is not defined out of this range. The output is a 16-bit fractional value within the range $<0 ; 1$ ).
GFLIB_Sqrt_F16l	<a href="#">frac32_t</a>	<a href="#">frac16_t</a>	The input value is a 32-bit fractional value, limited to the range $<0 ; 1$ ). The function is not defined out of this range. The output is a 16-bit fractional value within the range $<0 ; 1$ ).
GFLIB_Sqrt_FLT	<a href="#">float_t</a>	<a href="#">float_t</a>	The input value is a 32-bit single precision floating-point non-negative value. The function is not defined for the negative inputs. The output is a 32-bit single precision floating-point non-negative value.

## 2.8.2 Declaration

The available [GFLIB\\_Sqrt](#) functions have the following declarations:

```
frac16_t GFLIB_Sqrt_F16(frac16_t f16Val)
frac16_t GFLIB_Sqrt_F16l(frac32_t f32Val)
float_t GFLIB_Sqrt_FLT(float_t f16Val)
```

## 2.8.3 Function use

The use of the [GFLIB\\_Sqrt](#) function is shown in the following example:

```
#include "gflib.h"

static frac16_t f16Result;
static frac16_t f16Val;

void main(void)
{
    f16Val = FRAC16(0.5);          /* f16Val = 0.5 */

    /* f16Result = sqrt(f16Val) */
    f16Result = GFLIB_Sqrt_F16(f16Val);
}
```

## 2.9 GFLIB\_Limit

The [GFLIB\\_Limit](#) function returns the value limited by the upper and lower limits. See the following equation:

$$\text{GFLIB\_Limit}(x, \min, \max) = \begin{cases} \min, & x < \min \\ \max, & x > \max \\ x, & \text{else} \end{cases}$$

**Equation 7. Algorithm formula**

### 2.9.1 Available versions

This function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range <-1 ; 1). The result may saturate.
- Floating-point output - the output is the floating-point result within the type's full range.

The available versions of the [GFLIB\\_Limit](#) functions are shown in the following table:

**Table 2-9. Function versions**

Function name	Input type			Result type	Description
	Input	Lower limit	Upper limit		
GFLIB_Limit_F16	<a href="#">frac16_t</a>	<a href="#">frac16_t</a>	<a href="#">frac16_t</a>	<a href="#">frac16_t</a>	The inputs are 16-bit fractional values within the range <-1 ; 1). The function returns a 16-bit fractional value in the range <f16LLim ; f16ULim>.
GFLIB_Limit_F32	<a href="#">frac32_t</a>	<a href="#">frac32_t</a>	<a href="#">frac32_t</a>	<a href="#">frac32_t</a>	The inputs are 32-bit fractional values within the range <-1 ; 1). The function returns a 32-bit fractional value in the range <f32LLim ; f32ULim>.
GFLIB_Limit_FLT	<a href="#">float_t</a>	<a href="#">float_t</a>	<a href="#">float_t</a>	<a href="#">float_t</a>	The inputs are 32-bit single precision floating-point values within the full range. The function returns a 32-bit single precision floating-point value in the range <fltLLim ; fltULim>.

### 2.9.2 Declaration

The available [GFLIB\\_Limit](#) functions have the following declarations:

```
frac16_t GFLIB_Limit_F16(frac16_t f16Val, frac16_t f16LLim, frac16_t f16ULim)
frac32_t GFLIB_Limit_F32(frac32_t f32Val, frac32_t f32LLim, frac32_t f32ULim)
float_t GFLIB_Limit_FLT(float_t fltVal, float_t fltLLim, float_t fltULim)
```

## 2.9.3 Function use

The use of the [GFLIB\\_Limit](#) function is shown in the following example:

```
#include "gflib.h"

static frac16_t f16Val, f16ULim, f16LLim, f16Result;

void main(void)
{
    f16ULim = FRAC16(0.8);
    f16LLim = FRAC16(-0.3);
    f16Val = FRAC16(0.9);

    f16Result = GFLIB_Limit_F16(f16Val, f16LLim, f16ULim);
}
```

## 2.10 GFLIB\_LowerLimit

The [GFLIB\\_LowerLimit](#) function returns the value limited by the lower limit. See the following equation:

$$\text{GFLIB\_LowerLimit}(x, \min) = \begin{cases} \min, & x < \min \\ x, & \text{else} \end{cases}$$

**Equation 8. Algorithm formula**

### 2.10.1 Available versions

This function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range <-1 ; 1). The result may saturate.
- Floating-point output - the output is the floating-point result within the type's full range.



The available versions of the [GFLIB\\_LowerLimit](#) functions are shown in the following table:

**Table 2-10. Function versions**

Function name	Input type		Result type	Description
	Input	Lower limit		
GFLIB_LowerLimit_F16	<a href="#">frac16_t</a>	<a href="#">frac16_t</a>	<a href="#">frac16_t</a>	The inputs are 16-bit fractional values within the range <-1 ; 1). The function returns a 16-bit fractional value in the range <f16LLim ; 1).
GFLIB_LowerLimit_F32	<a href="#">frac32_t</a>	<a href="#">frac32_t</a>	<a href="#">frac32_t</a>	The inputs are 32-bit fractional values within the range <-1 ; 1). The function returns a 32-bit fractional value in the range <f32LLim ; 1).
GFLIB_LowerLimit_FLT	<a href="#">float_t</a>	<a href="#">float_t</a>	<a href="#">float_t</a>	The inputs are 32-bit single precision floating-point values within the full range. The function returns a 32-bit single precision floating-point value greater than or equal to fltLLim.

## 2.10.2 Declaration

The available [GFLIB\\_LowerLimit](#) functions have the following declarations:

```
frac16\_t GFLIB_LowerLimit_F16(frac16\_t f16Val, frac16\_t f16LLim)
frac32\_t GFLIB_LowerLimit_F32(frac32\_t f32Val, frac32\_t f32LLim)
float\_t GFLIB_LowerLimit_FLT(float\_t fltVal, float\_t fltLLim)
```

## 2.10.3 Function use

The use of the [GFLIB\\_LowerLimit](#) function is shown in the following example:

```
#include "gflib.h"

static frac16\_t f16Val, f16LLim, f16Result;

void main(void)
{
    f16LLim = FRAC16(0.3);
    f16Val = FRAC16(0.1);

    f16Result = GFLIB_LowerLimit_F16(f16Val, f16LLim);
}
```

## 2.11 GFLIB\_UpperLimit

The [GFLIB\\_UpperLimit](#) function returns the value limited by the upper limit. See the following equation:

$$\text{GFLIB\_UpperLimit}(x, \text{max}) = \begin{cases} \text{max}, & x > \text{max} \\ x, & \text{else} \end{cases}$$

**Equation 9. Algorithm formula**

## 2.11.1 Available versions

This function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range <-1 ; 1). The result may saturate.
- Floating-point output - the output is the floating-point result within the type's full range.

The available versions of the [GFLIB\\_UpperLimit](#) functions are shown in the following table:

**Table 2-11. Function versions**

Function name	Input type		Result type	Description
	Input	Upper limit		
GFLIB_UpperLimit_F16	<a href="#">frac16_t</a>	<a href="#">frac16_t</a>	<a href="#">frac16_t</a>	The inputs are 16-bit fractional values within the range <-1 ; 1). The function returns a 16-bit fractional value in the range <-1 ; f16ULim>.
GFLIB_UpperLimit_F32	<a href="#">frac32_t</a>	<a href="#">frac32_t</a>	<a href="#">frac32_t</a>	The inputs are 32-bit fractional values within the range <-1 ; 1). The function returns a 32-bit fractional value in the range <-1 ; f32ULim>.
GFLIB_UpperLimit_FLT	<a href="#">float_t</a>	<a href="#">float_t</a>	<a href="#">float_t</a>	The inputs are 32-bit single precision floating-point values within the full range. The function returns a 32-bit single precision floating-point value, which is lower or equal to fltULim.

## 2.11.2 Declaration

The available [GFLIB\\_UpperLimit](#) functions have the following declarations:

```
frac16\_t GFLIB_UpperLimit_F16(frac16\_t f16Val, frac16\_t f16ULim)
frac32\_t GFLIB_UpperLimit_F32(frac32\_t f32Val, frac32\_t f32ULim)
float\_t GFLIB_UpperLimit_FLT(float\_t fltVal, float\_t fltULim)
```

### 2.11.3 Function use

The use of the [GFLIB\\_UpperLimit](#) function is shown in the following example:

```
#include "gflib.h"

static frac16_t f16Val, f16ULim, f16Result;

void main(void)
{
    f16ULim = FRAC16(0.3);
    f16Val = FRAC16(0.9);

    f16Result = GFLIB_UpperLimit_F16(f16Val, f16ULim);
}
```

### 2.12 GFLIB\_VectorLimit

The [GFLIB\\_VectorLimit](#) function returns the limited vector by an amplitude. This limitation is calculated to achieve the zero angle error.

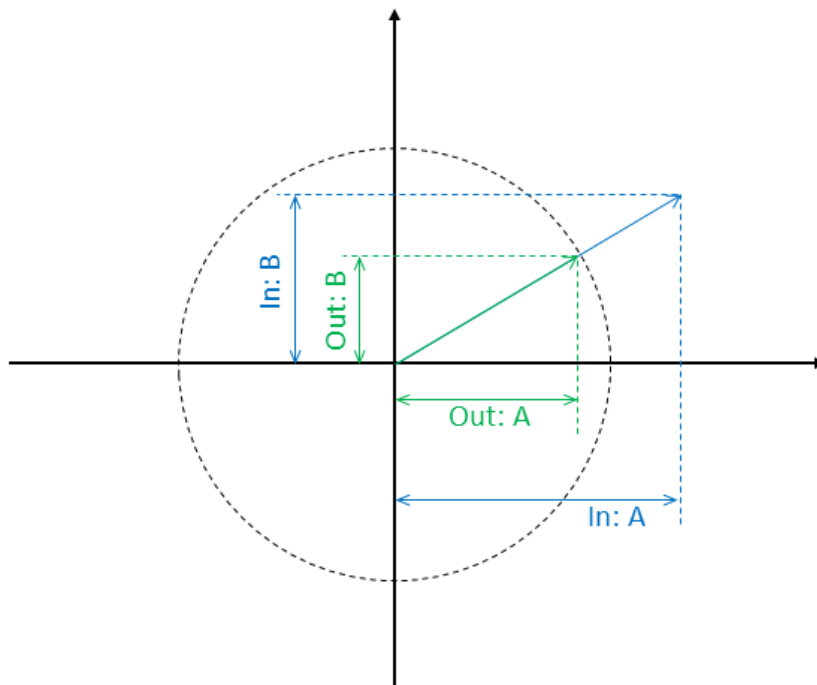


Figure 2-6. Input and related output

The [GFLIB\\_VectorLimit](#) function limits the amplitude of the input vector. The input vector  $a$ ,  $b$  components, are passed into the function as the input arguments. The resulting limited vector is transformed back into the  $a$ ,  $b$  components. The limitation is performed according to the following equations:

$$a^* = \begin{cases} a, & \sqrt{a^2 + b^2} \leq \text{lim} \\ a \cdot \frac{\text{lim}}{\sqrt{a^2 + b^2}}, & \text{else} \end{cases}$$

**Equation 10. Algorithm formulas**

$$b^* = \begin{cases} b, & \sqrt{a^2 + b^2} \leq \text{lim} \\ b \cdot \frac{\text{lim}}{\sqrt{a^2 + b^2}}, & \text{else} \end{cases}$$

**Equation 11**

where:

- $a$ ,  $b$  are the vector coordinates
- $a^*$ ,  $b^*$  are the vector coordinates after limitation
- $\text{lim}$  is the maximum amplitude

The relationship between the input and limited output vectors is obvious from [Figure 2-6](#).

If the amplitude of the input vector is greater than the input Lim value, the function calculates the new coordinates from the Lim value; otherwise the function copies the input values to the output.

## 2.12.1 Available versions

The function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range  $[-1;1]$ . The result may saturate.
- Floating point output - the output is the floating point result within the type's full range.

The available versions of the [GFLIB\\_VectorLimit](#) functions are shown in the following table:

**Table 2-12. Function versions**

Function name	Input type		Output type	Result type
	Input	Limit		
GFLIB_VectorLimit_F16	<a href="#">GFLIB_VECTORLIMIT_T_F16</a> *	<a href="#">frac16_t</a>	<a href="#">GFLIB_VECTORLIMIT_T_F16</a> *	void

*Table continues on the next page...*

Table 2-12. Function versions (continued)

Function name	Input type		Output type	Result type
	Input	Limit		
	Limitation of a two-component 16-bit fractional vector within the range <-1;1) with a 16-bit fractional limitation amplitude. The function returns a two-component 16-bit fractional vector.			
GFLIB_VectorLimit_FLT	GFLIB_VECTORLIMIT_T_FLT *	float_t	GFLIB_VECTORLIMIT_T_FLT *	void
	Limitation of a two-component 32-bit single precision floating point vector within the full range with a 32-bit single precision floating point limitation amplitude. The function returns a two-component 32-bit single precision floating point vector.			

## 2.12.2 GFLIB\_VECTORLIMIT\_T\_F16 type description

Variable name	Input type	Description
f16A	frac16_t	A-component; 16-bit fractional type.
f16B	frac16_t	B-component; 16-bit fractional type

## 2.12.3 GFLIB\_VECTORLIMIT\_T\_FLT type description

Variable name	Input type	Description
fltA	float_t	A-component; 32-bit single precision floating point type.
fltB	float_t	B-component; 32-bit single precision floating point type.

## 2.12.4 Declaration

The available [GFLIB\\_VectorLimit](#) functions have the following declarations:

```
frac16_t GFLIB_VectorLimit_F16(const GFLIB_VECTORLIMIT_T_F16 *psVectorIn, frac16_t f16Lim,
GFLIB_VECTORLIMIT_T_F16 *psVectorOut)
float_t GFLIB_VectorLimit_FLT(const GFLIB_VECTORLIMIT_T_FLT *psVectorIn, float_t fltLim,
GFLIB_VECTORLIMIT_T_FLT *psVectorOut)
```

## 2.12.5 Function use

The use of the [GFLIB\\_VectorLimit](#) function is shown in the following example:

## GFLIB\_VectorLimit1

```
#include "gflib.h"

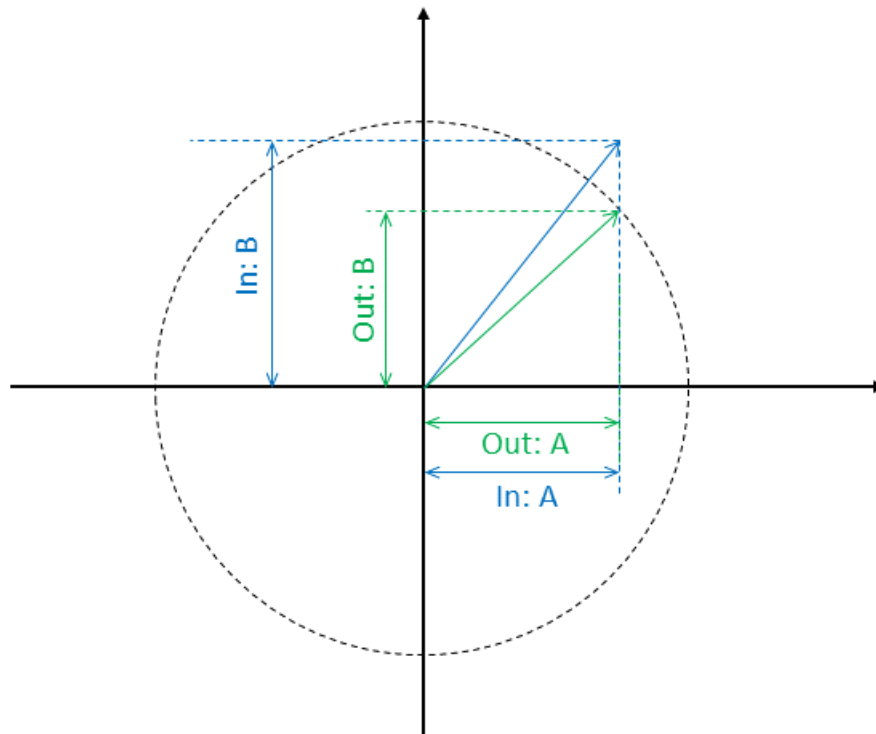
static GFLIB_VECTORLIMIT_T_F16 sVector, sResult;
static frac16_t f16MaxAmpl;

void main(void)
{
    f16MaxAmpl = FRAC16(0.8);
    sVector.f16A = FRAC16(-0.79);
    sVector.f16B = FRAC16(0.86);

    GFLIB_VectorLimit_F16(&sVector, f16MaxAmpl, &sResult);
}
```

## 2.13 GFLIB\_VectorLimit1

The [GFLIB\\_VectorLimit1](#) function returns the limited vector by an amplitude. This limitation is calculated to achieve that the first component remains unchanged (if the limitation factor allows).



**Figure 2-7. Input and related output**

The [GFLIB\\_VectorLimit1](#) function limits the amplitude of the input vector. The input vector  $a$ ,  $b$  components are passed to the function as the input arguments. The resulting limited vector is transformed back into the  $a$ ,  $b$  components. The limitation is performed according to the following equations:

$$\alpha^* = \begin{cases} a, & |a| \leq \text{lim} \\ \text{lim} \cdot \text{sgn}(a), & \text{else} \end{cases}$$

**Equation 12**

$$b^* = \begin{cases} b, & |b| \leq \sqrt{\text{lim}^2 - a^{*2}} \\ \sqrt{\text{lim}^2 - a^{*2}} \cdot \text{sgn}(b), & \text{else} \end{cases}$$

**Equation 13**

where:

- a, b are the vector coordinates
- a\*, b\* are the vector coordinates after limitation
- lim is the maximum amplitude

The relationship between the input and limited output vectors is shown in [Figure 2-7](#).

If the amplitude of the input vector is greater than the input Lim value, the function calculates the new coordinates from the Lim value; otherwise the function copies the input values to the output.

### 2.13.1 Available versions

The function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range <-1 ; 1). The result may saturate.
- Floating-point output - the output is the floating-point result within the type's full range.

The available versions of the [GFLIB\\_VectorLimit1](#) function are shown in the following table:

**Table 2-13. Function versions**

Function name	Input type		Output type	Result type
	Input	Limit		
GFLIB_VectorLimit1_F16	<a href="#">GFLIB_VECTORLIMIT_T_F16</a> *	<a href="#">frac16_t</a>	<a href="#">GFLIB_VECTORLIMIT_T_F16</a> *	void
	Limitation of a two-component 16-bit fractional vector within the range <-1 ; 1) with a 16-bit fractional limitation amplitude. The function returns a two-component 16-bit fractional vector.			
GFLIB_VectorLimit1_FLT	<a href="#">GFLIB_VECTORLIMIT_T_FLT</a> *	<a href="#">float_t</a>	<a href="#">GFLIB_VECTORLIMIT_T_FLT</a> *	void
	Limitation of a two-component 32-bit single precision floating-point vector within the full range with a 32-bit single precision floating-point limitation amplitude. The function returns a two-component 32-bit single precision floating-point vector.			

## 2.13.2 GFLIB\_VECTORLIMIT\_T\_F16 type description

Variable name	Input type	Description
f16A	<a href="#">frac16_t</a>	A-component; 16-bit fractional type.
f16B	<a href="#">frac16_t</a>	B-component; 16-bit fractional type.

## 2.13.3 GFLIB\_VECTORLIMIT\_T\_FLT type description

Variable name	Input type	Description
fltA	<a href="#">float_t</a>	A-component; 32-bit single precision floating-point type.
fltB	<a href="#">float_t</a>	B-component; 32-bit single precision floating-point type.

## 2.13.4 Declaration

The available [GFLIB\\_VectorLimit1](#) functions have the following declarations:

```
frac16_t GFLIB_VectorLimit1_F16(const GFLIB\_VECTORLIMIT\_T\_F16 *psVectorIn, frac16\_t f16Lim,
GFLIB\_VECTORLIMIT\_T\_F16 *psVectorOut)
float_t GFLIB_VectorLimit1_FLT(const GFLIB\_VECTORLIMIT\_T\_FLT *psVectorIn, float\_t fltLim,
GFLIB\_VECTORLIMIT\_T\_FLT *psVectorOut)
```

## 2.13.5 Function use

The use of the [GFLIB\\_VectorLimit1](#) function is shown in the following example:

```
#include "gflib.h"

static GFLIB\_VECTORLIMIT\_T\_F16 sVector, sResult;
static frac16\_t f16MaxAmpl;

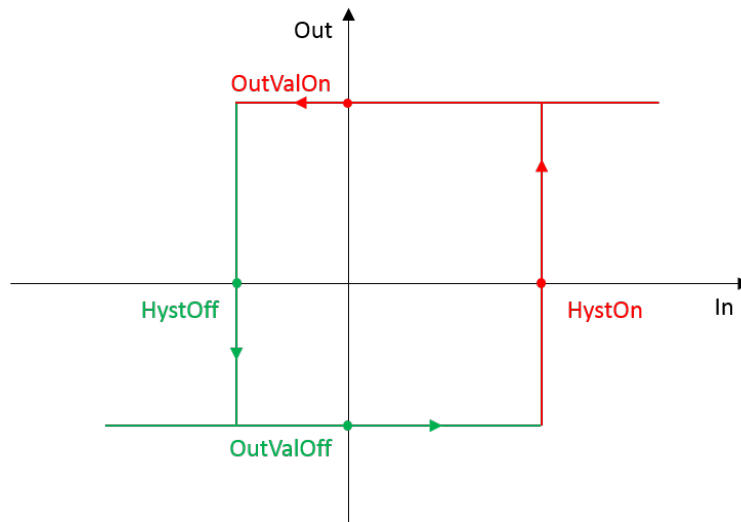
void main(void)
{
    f16MaxAmpl = FRAC16(0.5);
    sVector.f16A = FRAC16(-0.4);
    sVector.f16B = FRAC16(0.2);

    GFLIB_VectorLimit1_F16(&sVector, f16MaxAmpl, &sResult);
}
```



## 2.14 GFLIB\_Hyst

The [GFLIB\\_Hyst](#) function represents a hysteresis (relay) function. The function switches the output between two predefined values. When the input is higher than the upper threshold, the output is high; when the input is lower than the lower threshold, the output is low. When the input is between the two thresholds, the output retains its value. See the following figure:



**Figure 2-8. GFLIB\_Hyst functionality**

The four points in the figure are to be set up in the parameters structure of the function. For a proper functionality, the HystOn point must be greater than the HystOff point.

### 2.14.1 Available versions

This function is available in the following versions:

- Fractional output - the output is the fractional portion of the result, and the result is within the range  $-1 ; 1$ ).
- Floating-point output - the output is the floating-point result within the type's full range.

The available versions of the [GFLIB\\_Hyst](#) function are shown in the following table.

**Table 2-14. Function versions**

Function name	Input type	Parameters	Result type	Description
GFLIB_Hyst_F16	<a href="#">frac16_t</a>	<a href="#">GFLIB_HYST_T_F16</a> *	<a href="#">frac16_t</a>	The input is a 16-bit fractional value within the range $<-1 ; 1$ ). The output is a two-state 16-bit fractional value.
GFLIB_Hyst_FLT	<a href="#">float_t</a>	<a href="#">GFLIB_HYST_T_FLT</a> *	<a href="#">float_t</a>	The input is a 32-bit single precision floating-point value within its full range. The output is a two-state 32-bit single precision floating-point value.

## 2.14.2 GFLIB\_HYST\_T\_F16

Variable name	Input type	Description
f16HystOn	<a href="#">frac16_t</a>	The point where the output sets the output to the f16OutValOn value when the input rises. Set by the user.
f16HystOff	<a href="#">frac16_t</a>	The point where the output sets the output to the f16OutValOff value when the input falls. Set by the user.
f16OutValOn	<a href="#">frac16_t</a>	The ON value. Set by the user.
f16OutValOff	<a href="#">frac16_t</a>	The OFF value. Set by the user.
f16OutState	<a href="#">frac16_t</a>	The output state. Set by the algorithm. Must be initialized by the user.

## 2.14.3 GFLIB\_HYST\_T\_FLT

Variable name	Input type	Description
fltHystOn	<a href="#">float_t</a>	The point where the output sets the output to the fltOutValOn value when the input rises. Set by the user.
fltHystOff	<a href="#">float_t</a>	The point where the output sets the output to the fltOutValOff value when the input falls. Set by the user.
fltOutValOn	<a href="#">float_t</a>	The ON value. Set by the user.
fltOutValOff	<a href="#">float_t</a>	The OFF value. Set by the user.
fltOutState	<a href="#">float_t</a>	The output state. Set by the algorithm. Must be initialized by the user.

## 2.14.4 Declaration

The available [GFLIB\\_Hyst](#) functions have the following declarations:

```
frac16_t GFLIB_Hyst_F16(frac16_t f16Val, GFLIB_HYST_T_F16 *psParam)
float_t GFLIB_Hyst_FLT(float_t fltVal, GFLIB_HYST_T_FLT *psParam)
```

## 2.14.5 Function use

The use of the [GFLIB\\_Hyst](#) function is shown in the following example:

```
#include "gflib.h"

static frac16_t f16Result, f16InVal;
static GFLIB_HYST_T_F16 sParam;

void main(void)
{
    f16InVal = FRAC16(-0.11);
    sParam.f16HystOn = FRAC16(0.5);
    sParam.f16HystOff = FRAC16(-0.1);
    sParam.f16OutValOn = FRAC16(0.7);
    sParam.f16OutValOff = FRAC16(0.3);
    sParam.f16OutState = FRAC16(0.0);

    f16Result = GFLIB_Hyst_F16(f16InVal, &sParam);
}
```

## 2.15 GFLIB\_Lut1D

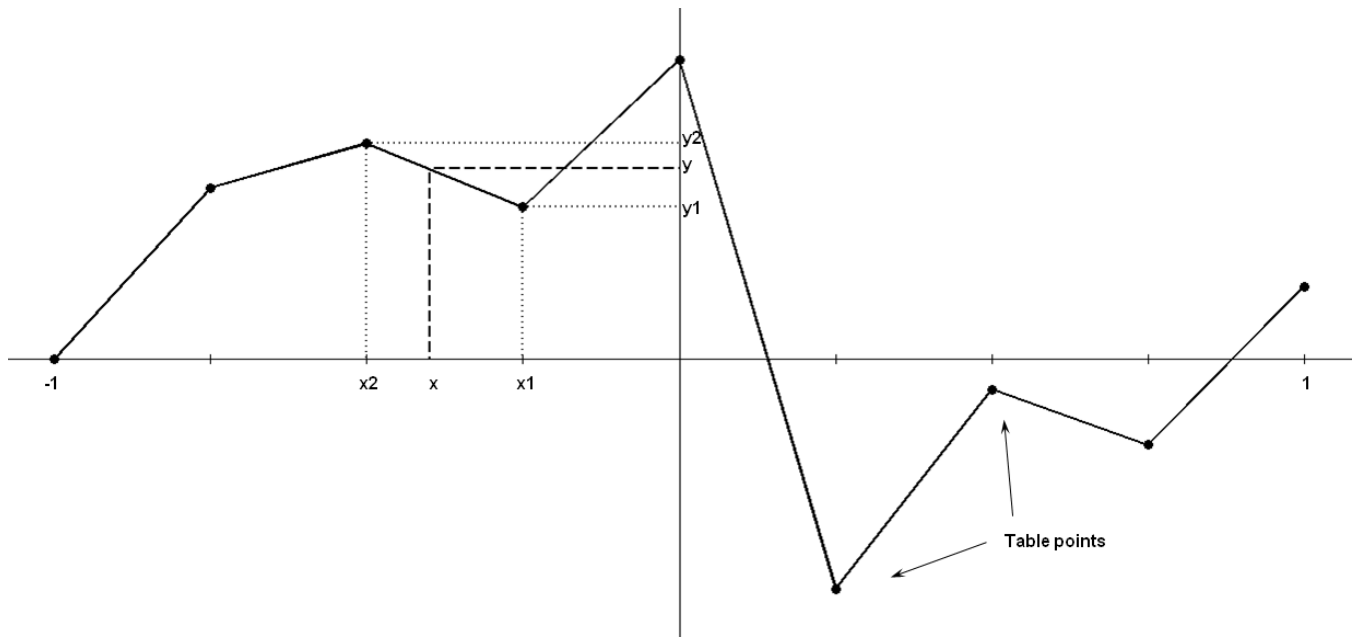
The [GFLIB\\_Lut1D](#) function implements the one-dimensional look-up table.

$$y = y_1 + \frac{y_2 - y_1}{x_2 - x_1}(x - x_1)$$

**Equation 14.**

where:

- y is the interpolated value
- y<sub>1</sub> and y<sub>2</sub> are the ordinate values at the beginning and end of the interpolating interval, respectively
- x<sub>1</sub> and x<sub>2</sub> are the abscissa values at the beginning and end of the interpolating interval, respectively
- x is the input value provided to the function in the X input argument



**Figure 2-9. Algorithm diagram - fractional version**

The [GFLIB\\_Lut1D](#) fuses a table of the precalculated function points. These points are selected with a fixed step.

The fractional version of the algorithm has a defined interval of inputs within the range  $<-1 ; 1>$ . The number of points must be  $2^n + 1$ , where  $n$  can range from 1 through to 15.

The floating-point version of the algorithm has a defined interval of inputs within the range  $<\text{min} ; \text{max}>$ , where the min and max values are the parameters of the algorithms. The number of points is within the range  $<2 ; 65535>$ , where the first point lies at the min position, and the last point lies at the max position.

The function finds two nearest precalculated points of the input argument, and calculates the output value using the linear interpolation between these two points.

### 2.15.1 Available versions

The function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range  $<-1 ; 1>$ .
- Floating-point output - the output is the floating-point result within the type's full range. The input values are defined by the minimum and maximum.

The available versions of the [GFLIB\\_Lut1D](#) function are shown in the following table:

**Table 2-15. Function versions**

Function name	Input type	Parameters		Result type
		Table	Table size	
GFLIB_Lut1D_F16	<a href="#">frac16_t</a>	<a href="#">frac16_t</a> *	<a href="#">uint16_t</a>	<a href="#">frac16_t</a>
	The input arguments are the 16-bit fractional value that contains the abscissa for which the 1-D interpolation is performed, the pointer to a structure which contains the 16-bit fractional values of the look-up table, and the size of the look-up table. The table size parameter can be in the range <1 ; 15> (that means the parameter is $\log_2$ of the number of points - 1). The output is the interpolated 16-bit fractional value computed from the look-up table.			
GFLIB_Lut1D_FLT	<a href="#">float_t</a>	<a href="#">float_t</a> *	<a href="#">GFLIB_LUT1D_T_FLT</a> *	<a href="#">float_t</a>
	The input arguments are the 32-bit single precision floating-point value that contains the abscissa for which the 1-D interpolation is performed, the pointer to a structure which contains the 32-bit single precision floating-point values of the look-up table, and the pointer a to structure that contains the size of the look-up table together with the minimum and maximum borders of the input interval. The table size parameter can be in the range <2 ; 65535>. The first value of the table is located at the fltMin position, and the last value of the table is located at the fltMax position. The output is the interpolated 32-bit single precision floating-point value computed from the look-up table.			

## 2.15.2 GFLIB\_LUT1D\_T\_FLT type description

Variable name	Input type	Description
u16TableSize	<a href="#">uint16_t</a>	Size of the table; a 16-bit unsigned integer type within the range <2 ; 65535>. Set by the user.
fltMin	<a href="#">float_t</a>	The minimum of the look-up table x-coordinate; a 32-bit single precision floating-point type. Set by the user.
fltMax	<a href="#">float_t</a>	The maximum of the look-up table x-coordinate; a 32-bit single precision floating-point type. Set by the user.

## 2.15.3 Declaration

The available [GFLIB\\_Lut1D](#) functions have the following declarations:

```
frac16\_t GFLIB_Lut1D_F16(frac16\_t f16X, const frac16\_t *pf16Table, uint16\_t u16TableSize)
float\_t GFLIB_Lut1D_FLT(float\_t fltX, const float\_t *pfltTable, const GFLIB\_LUT1D\_T\_FLT
*psParam)
```

## 2.15.4 Function use

The use of the [GFLIB\\_Lut1D](#) function is shown in the following example:

```
#include "gflib.h"

static frac16_t f16Result, f16X;
static uint16_t ul6TableSize;
static frac16_t f16Table[9] = {FRAC16(0.8), FRAC16(0.1), FRAC16(-0.2), FRAC16(0.7),
FRAC16(0.2), FRAC16(-0.3), FRAC16(-0.8), FRAC16(0.91), FRAC16(0.99)};

void main(void)
{
    ul6TableSize = 3;                                /* size of table = 2 ^ 3 + 1 */
    f16X = FRAC16(0.625);                             /* f16X = 0.625 */

    /* f16Result = value from look-up table between 7th and 8th position */
    f16Result = GFLIB_Lut1D_F16(f16X, f16Table, ul6TableSize);
}
```

## 2.16 GFLIB\_LutPer1D

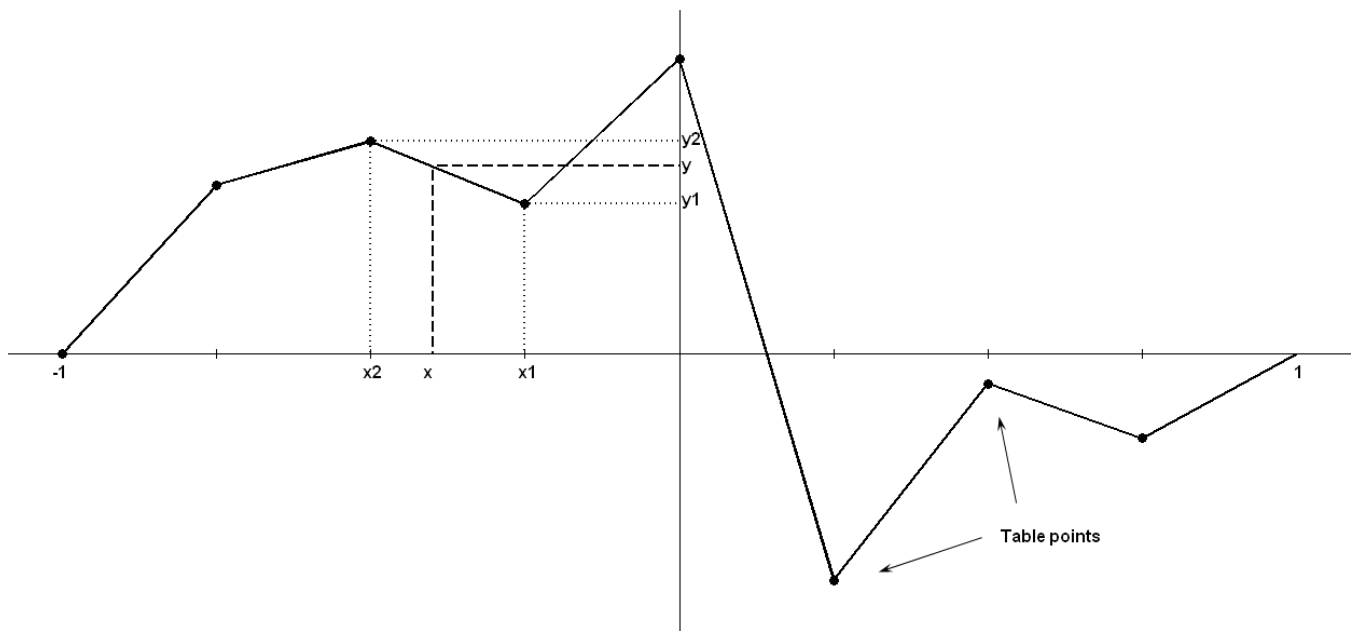
The [GFLIB\\_LutPer1D](#) function approximates the one-dimensional arbitrary user function using the interpolation look-up method. It is periodic.

$$y = y_1 + \frac{y_2 - y_1}{x_2 - x_1}(x - x_1)$$

**Equation 15.**

where:

- y is the interpolated value
- y<sub>1</sub> and y<sub>2</sub> are the ordinate values at the beginning and end of the interpolating interval, respectively
- x<sub>1</sub> and x<sub>2</sub> are the abscissa values at the beginning and end of the interpolating interval, respectively
- x is the input value provided to the function in the X input argument



**Figure 2-10. Algorithm diagram - fractional version**

The [GFLIB\\_LutPer1D](#) fuses a table of the precalculated function points. These points are selected with a fixed step.

The fractional version of the algorithm has a defined interval of inputs within the range  $<-1 ; 1>$ . The number of points must be  $2^n$ , where  $n$  can range from 1 through to 15.

The floating-point version of the algorithm has a defined interval of inputs within the range  $<\text{min} ; \text{max}>$ , where the min and max values are parameters of the algorithms. The number of points is within the range  $<2 ; 65535>$ , where the first point lies at the min position, and the last point lies at the max position.

The function finds two nearest precalculated points of the input argument, and calculates the output value using the linear interpolation between these two points. This algorithm serves for periodical functions, that means if the input argument lies behind the last precalculated point of the function, the interpolation is calculated between the last and first points of the table.

### 2.16.1 Available versions

This function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range  $<-1 ; 1>$ .
- Floating-point output - the output is the floating-point result within the type's full range.

The available versions of the [GFLIB\\_LutPer1D](#) function are shown in the following table:

**Table 2-16. Function versions**

Function name	Input type	Parameters		Result type
		Table	Table size	
GFLIB_LutPer1D_F16	<a href="#">frac16_t</a>	<a href="#">frac16_t *</a>	<a href="#">uint16_t</a>	<a href="#">frac16_t</a>
	The input arguments are the 16-bit fractional value that contains the abscissa for which the 1-D interpolation is performed, the pointer to a structure which contains the 16-bit fractional values of the look-up table, and the size of the look-up table. The table size parameter can be in the range <1 ; 15> (that means the parameter is $\log_2$ of the number of points). The output is the interpolated 16-bit fractional value computed from the look-up table.			
GFLIB_LutPer1D_FLT	<a href="#">float_t</a>	<a href="#">float_t *</a>	<a href="#">GFLIB_LUTPER1D_T_FLT *</a>	<a href="#">float_t</a>
	The input arguments are the 32-bit single precision floating-point value that contains the abscissa for which the 1-D interpolation is performed, the pointer to a structure which contains the 32-bit single precision floating-point values of the look-up table, and the pointer a to structure that contains the size of the look-up table together with the minimum and maximum borders of the input interval. The table size parameter can be in the range <2 ; 65535>. The first value of the table is located at the fltMin position, and the last value of the table is located at the fltMax position. The output is the interpolated 32-bit single precision floating-point value computed from the look-up table.			

## 2.16.2 GFLIB\_LUTPER1D\_T\_FLT type description

Variable name	Input type	Description
u16TableSize	<a href="#">uint16_t</a>	Size of the table; a 16-bit unsigned integer type within the range <2 ; 65535>. Set by the user.
fltMin	<a href="#">float_t</a>	Minimum of the look-up table x-coordinate; a 32-bit single precision floating-point type. Set by the user.
fltMax	<a href="#">float_t</a>	Maximum of the look-up table x-coordinate; a 32-bit single precision floating-point type. Set by the user.

## 2.16.3 Declaration

The available [GFLIB\\_LutPer1D](#) functions have the following declarations:

```
frac16_t GFLIB_LutPer1D_F16(frac16_t f16X, const frac16_t *pf16Table, uint16_t u16TableSize)
float_t GFLIB_LutPer1D_FLT(float_t fltX, const float_t *pfltTable, const
GFLIB_LUTPER1D_T_FLT *psParam)
```



## 2.16.4 Function use

The use of the [GFLIB\\_LutPer1D](#) function is shown in the following example:

```
#include "gflib.h"

static frac16_t f16Result, f16X;
static uint16_t u16TableSize;
static frac16_t f16Table[8] = {FRAC16(0.8), FRAC16(0.1), FRAC16(-0.2), FRAC16(0.7),
FRAC16(0.2), FRAC16(-0.3), FRAC16(-0.8), FRAC16(0.91)};

void main(void)
{
    u16TableSize = 3;                /* size of table = 2 ^ 3 */
    f16X = FRAC16(0.25);             /* f16X = 0.25 */

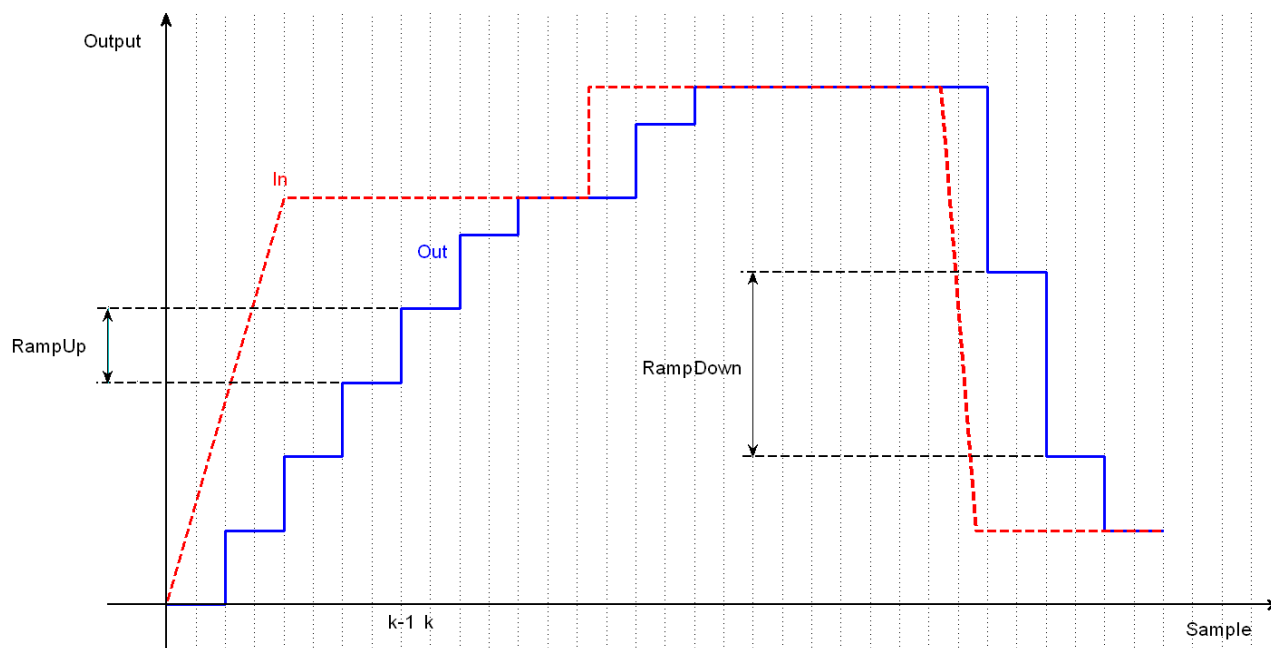
    /* f16Result = value from look-up table at 6th position */
    f16Result = GFLIB_LutPer1D_F16(f16X, f16Table, u16TableSize);
}
```

## 2.17 GFLIB\_Ramp

The [GFLIB\\_Ramp](#) function calculates the up / down ramp with the defined fixed-step increment / decrement. These two parameters must be set by the user.

For a proper use, it is recommended that the algorithm is initialized by the [GFLIB\\_RampInit](#) function, before using the [GFLIB\\_Ramp](#) function. The [GFLIB\\_RampInit](#) function initializes the internal state variable of the [GFLIB\\_Ramp](#) algorithm with a defined value. You must call the init function when you want the ramp to be initialized.

The use of the [GFLIB\\_Ramp](#) function is as follows: If the target value is greater than the ramp state value, the function adds the ramp-up value to the state output value. The output will not trespass the target value, that means it will stop at the target value. If the target value is lower than the state value, the function subtracts the ramp-down value from the state value. The output is limited to the target value, that means it will stop at the target value. This function returns the actual ramp output value. As time passes, it is approaching the target value by step increments defined in the algorithm parameters' structure. The functionality of the implemented ramp algorithm is explained in the next figure:



### Figure 2-11. GFLIB\_Ramp functionality

### 2.17.1 Available versions

This function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range  $[-1; 1)$ . The result may saturate.
- Floating-point output - the output is the floating-point result within the type's full range.

The available versions of the GFLIB\_RampInit functions are shown in the following table:

### Table 2-17. Init function versions

Function name	Input type	Parameters	Result type	Description
GFLIB_RampInit_F16	<a href="#">frac16_t</a>	<a href="#">GFLIB_RAMP_T_F16</a> *	void	Input argument is a 16-bit fractional value that represents the initialization value. The parameters' structure is pointed to by a pointer. The input data value is in the range <-1 ; 1).
GFLIB_RampInit_F32	<a href="#">frac32_t</a>	<a href="#">GFLIB_RAMP_T_F32</a> *	void	Input argument is a 32-bit fractional value that represents the initialization value. The parameters' structure is pointed to by a pointer. The input data value is in the range <-1 ; 1).

*Table continues on the next page...*

Table 2-17. Init function versions (continued)

Function name	Input type	Parameters	Result type	Description
GFLIB_Ramplnit_FLT	float_t	GFLIB_RAMP_T_FLT *	void	Input argument is a 32-bit single precision floating-point value that represents the initialization value. The parameters' structure is pointed to by a pointer. The input value is within the full 32-bit single-point floating-point range.

The available versions of the [GFLIB\\_Ramp](#) functions are shown in the following table:

Table 2-18. Function versions

Function name	Input type	Parameters	Result type	Description
GFLIB_Ramp_F16	frac16_t	GFLIB_RAMP_T_F16 *	frac16_t	Input argument is a 16-bit fractional value that represents the target output value. The parameters' structure is pointed to by a pointer. The function returns a 16-bit fractional value, which represents the actual ramp output value. The input data value is in the range <-1 ; 1), and the output data value is in the range <-1 ; 1).
GFLIB_Ramp_F32	frac32_t	GFLIB_RAMP_T_F32 *	frac32_t	Input argument is a 32-bit fractional value that represents the target output value. The parameters' structure is pointed to by a pointer. The function returns a 32-bit fractional value, which represents the actual ramp output value. The input data value is in the range <-1 ; 1), and the output data value is in the range <-1 ; 1).
GFLIB_Ramp_FLT	float_t	GFLIB_RAMP_T_FLT *	float_t	Input argument is a 32-bit single precision floating-point value that represents the target output value. The parameters' structure is pointed to by a pointer. The function returns a 32-bit single precision floating-point value, which represents the actual ramp output value. The input and output values are within the full 32-bit single-point floating-point range.

## 2.17.2 GFLIB\_RAMP\_T\_F16

Variable name	Type	Description
f16State	frac16_t	Actual value - controlled by the algorithm.
f16RampUp	frac16_t	Value of the ramp-up increment. The data value is in the range <0 ; 1). Set by the user.
f16RampDown	frac16_t	Value of the ramp-down increment. The data value is in the range <0 ; 1). Set by the user.

## 2.17.3 GFLIB\_RAMP\_T\_F32

Variable name	Type	Description
f32State	<a href="#">frac32_t</a>	Actual value - controlled by the algorithm.
f32RampUp	<a href="#">frac32_t</a>	Value of the ramp-up increment. The data value is in the range <0 ; 1). Set by the user.
f32RampDown	<a href="#">frac32_t</a>	Value of the ramp-down increment. The data value is in the range <0 ; 1). Set by the user.

## 2.17.4 GFLIB\_RAMP\_T\_FLT

Variable name	Type	Description
fltState	<a href="#">float_t</a>	Actual value - controlled by the algorithm.
fltRampUp	<a href="#">float_t</a>	Value of the ramp-up increment. The data value is within the full 32-bit single precision floating point. Set by the user as non- negative value.
fltRampDown	<a href="#">float_t</a>	Value of the ramp-down increment. The data value is within the full 32-bit single precision floating point. Set by the user as non- negative value.

## 2.17.5 Declaration

The available GFLIB\_RampInit functions have the following declarations:

```
void GFLIB_RampInit_F16(frac16\_t f16InitVal, GFLIB\_RAMP\_T\_F16 *psParam)
void GFLIB_RampInit_F32(frac32\_t f32InitVal, GFLIB\_RAMP\_T\_F32 *psParam)
void GFLIB_RampInit_FLT(float\_t fltInitVal, GFLIB\_RAMP\_T\_FLT *psParam)
```

The available [GFLIB\\_Ramp](#) functions have the following declarations:

```
frac16\_t GFLIB_Ramp_F16(frac16\_t f16Target, GFLIB\_RAMP\_T\_F16 *psParam)
frac32\_t GFLIB_Ramp_F32(frac32\_t f32Target, GFLIB\_RAMP\_T\_F32 *psParam)
float\_t GFLIB_Ramp_FLT(float\_t fltTarget, GFLIB\_RAMP\_T\_FLT *psParam)
```

## 2.17.6 Function use

The use of the GFLIB\_RampInit and [GFLIB\\_Ramp](#) functions is shown in the following example:

```
#include "gflib.h"

static frac16\_t f16InitVal;
static GFLIB\_RAMP\_T\_F16 sParam;
static frac16\_t f16Target, f16Result;

void Isr(void);
```

```

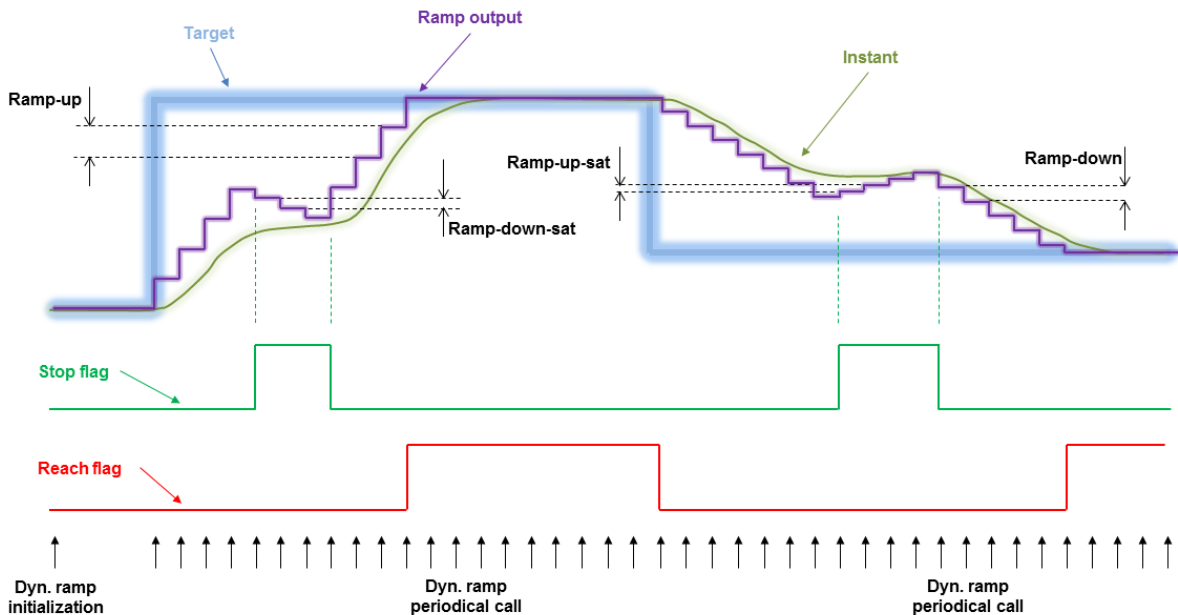
void main(void)
{
    sParam.f16RampUp = FRAC16(0.1);
    sParam.f16RampDown = FRAC16(0.02);
    f16Target = FRAC16(0.75);
    f16InitVal = FRAC16(0.9);
    GFLIB_RampInit_F16(f16InitVal, &sParam);
}

/* periodically called function */
void Isr()
{
    f16Result = GFLIB_Ramp_F16(f16Target, &sParam);
}

```

## 2.18 GFLIB\_DRamp

The [GFLIB\\_DRamp](#) function calculates the up / down ramp with the defined step increment / decrement. The algorithm approaches the target value when the stop flag is not set, and/or returns to the instant value when the stop flag is set.



**Figure 2-12. GFLIB\_DRamp functionality**

For a proper use, it is recommended that the algorithm is initialized by the [GFLIB\\_DRampInit](#) function, before using the [GFLIB\\_DRamp](#) function. This function initializes the internal state variable of [GFLIB\\_DRamp](#) algorithm with the defined value. You must call this function when you want the ramp to be initialized.

The [GFLIB\\_DRamp](#) function calculates a ramp with a different set of up / down parameters, depending on the state of the stop flag. If the stop flag is cleared, the function calculates the ramp of the actual state value towards the target value, using the up or down increments contained in the parameters' structure. If the stop flag is set, the function calculates the ramp towards the instant value, using the up or down saturation increments.

If the target value is greater than the state value, the function adds the ramp-up value to the state value. The output cannot be greater than the target value (case of the stop flag being cleared), nor lower than the instant value (case of the stop flag being set).

If the target value is lower than the state value, the function subtracts the ramp-down value from the state value. The output cannot be lower than the target value (case of the stop flag being cleared), nor greater than the instant value (case of the stop flag being set).

If the actual internal state reaches the target value, the reach flag is set.

## 2.18.1 Available versions

The function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range  $<-1 ; 1$ ). The result may saturate.
- Floating-point output - the output is the floating-point result within the type's full range.

The available versions of the GFLIB\_DRampInit function are shown in the following table:

**Table 2-19. Init function versions**

Function name	Input type	Parameters	Result type	Description
GFLIB_DRampInit_F16	<a href="#">frac16_t</a>	<a href="#">GFLIB_DRAMP_T_F16</a> *	void	Input argument is a 16-bit fractional value that represents the initialization value. The parameters' structure is pointed to by a pointer. The input data value is in the range $<-1 ; 1$ ).
GFLIB_DRampInit_F32	<a href="#">frac32_t</a>	<a href="#">GFLIB_DRAMP_T_F32</a> *	void	Input argument is a 32-bit fractional value that represents the initialization value. The parameters' structure is pointed to by a pointer. The input data value is in the range $<-1 ; 1$ ).

*Table continues on the next page...*

**Table 2-19. Init function versions (continued)**

Function name	Input type	Parameters	Result type	Description
GFLIB_DRampInit_FLT	float_t	GFLIB_DRAMP_T_FLT *	void	Input argument is a 32-bit single precision floating-point value that represents the initialization value. The parameters' structure is pointed to by a pointer. The input value is within the full 32-bit single-point floating-point range.

The available versions of the [GFLIB\\_DRamp](#) function are shown in the following table:

**Table 2-20. Function versions**

Function name	Input type			Parameters	Result type
	Target	Instant	Stop flag		
GFLIB_DRamp_F16	frac16_t	frac16_t	bool_t *	GFLIB_DRAMP_T_F16 *	frac16_t
	The target and instant arguments are 16-bit fractional values. The parameters' structure is pointed to by a pointer. The function returns a 16-bit fractional value, which represents the actual ramp output value. The input data values are in the range $<-1 ; 1$ ), the Stop flag parameter is a pointer to a boolean value, and the output data value is in the range $<-1 ; 1$ ).				
GFLIB_DRamp_F32	frac32_t	frac32_t	bool_t *	GFLIB_DRAMP_T_F32 *	frac32_t
	The target and instant arguments are 32-bit fractional values. The parameters' structure is pointed to by a pointer. The function returns a 32-bit fractional value, which represents the actual ramp output value. The input data values are in the range $<-1 ; 1$ ), the Stop flag parameter is a pointer to a boolean value, and the output data value is in the range $<-1 ; 1$ ).				
GFLIB_DRamp_FLT	float_t	float_t	bool_t *	GFLIB_DRAMP_T_FLT *	float_t
	The target and instant arguments are 32-bit single precision floating-point values. The parameters' structure is pointed to by a pointer. The function returns a 32-bit single precision floating-point value, which represents the actual ramp output value. The input and output values are within the full 32-bit single-point floating-point range, the Stop flag parameter is a pointer to a boolean value.				

## 2.18.2 GFLIB\_DRAMP\_T\_F16

Variable name	Type	Description
f16State	frac16_t	Actual value - controlled by the algorithm.
f16RampUp	frac16_t	Value of non-saturation ramp-up increment. The data value is in the range $<0 ; 1$ ). Set by the user.
f16RampDown	frac16_t	Value of non-saturation ramp-down increment. The data value is in the range $<0 ; 1$ ). Set by the user.
f16RampUpSat	frac16_t	Value of saturation ramp-up increment. The data value is in the range $<0 ; 1$ ). Set by the user.
f16RampDownSat	frac16_t	Value of saturation ramp-down increment. The data value is in the range $<0 ; 1$ ). Set by the user.
bReachFlag	bool_t	If the actual state value reaches the target value, this flag is set, otherwise, it is cleared. Set by the algorithm.

## 2.18.3 GFLIB\_DRAMP\_T\_F32

Variable name	Type	Description
f32State	<a href="#">frac32_t</a>	Actual value - controlled by the algorithm.
f32RampUp	<a href="#">frac32_t</a>	Value of non-saturation ramp-up increment. The data value is in the range <0 ; 1). Set by the user.
f32RampDown	<a href="#">frac32_t</a>	Value of non-saturation ramp-down increment. The data value is in the range <0 ; 1). Set by the user.
f32RampUpSat	<a href="#">frac32_t</a>	Value of saturation ramp-up increment. The data value is in the range <0 ; 1). Set by the user.
f32RampDownSat	<a href="#">frac32_t</a>	Value of saturation ramp-down increment. The data value is in the range <0 ; 1). Set by the user.
bReachFlag	<a href="#">bool_t</a>	If the actual state value reaches the target value, this flag is set, otherwise, it is cleared. Set by the algorithm.

## 2.18.4 GFLIB\_DRAMP\_T\_FLT

Variable name	Type	Description
fltState	<a href="#">float_t</a>	Actual value - controlled by the algorithm.
fltRampUp	<a href="#">float_t</a>	Value of non-saturation ramp-up increment. The data value is within the full 32-bit single precision floating point. Set by the user as non- negative value.
fltRampDown	<a href="#">float_t</a>	Value of non-saturation ramp-down increment. The data value is within the full 32-bit single precision floating point. Set by the user as non- negative value.
fltRampUpSat	<a href="#">float_t</a>	Value of saturation ramp-up increment. The data value is within the full 32-bit single precision floating point. Set by the user as non- negative value.
fltRampDownSat	<a href="#">float_t</a>	Value of saturation ramp-down increment. The data value is within the full 32-bit single precision floating point. Set by the user as non- negative value.
bReachFlag	<a href="#">bool_t</a>	If the actual state value reaches the target value, this flag is set, otherwise, it is cleared. Set by the algorithm.

## 2.18.5 Declaration

The available GFLIB\_DRampInit functions have the following declarations:

```
void GFLIB_DRampInit_F16(frac16\_t f16InitVal, GFLIB\_DRAMP\_T\_F16 *psParam)
void GFLIB_DRampInit_F32(frac32\_t f32InitVal, GFLIB\_DRAMP\_T\_F32 *psParam)
void GFLIB_DRampInit_FLT(float\_t fltInitVal, GFLIB\_DRAMP\_T\_FLT *psParam)
```

The available [GFLIB\\_DRamp](#) functions have the following declarations:



```

frac16_t GFLIB_DRamp_F16(frac16_t f16Target, frac16_t f16Instant, const bool_t *pbStopFlag,
GFLIB_DRAMP_T_F16 *psParam)
frac32_t GFLIB_DRamp_F32(frac32_t f32Target, frac32_t f32Instant, const bool_t *pbStopFlag,
GFLIB_DRAMP_T_F32 *psParam)
float_t GFLIB_DRamp_FLT(float_t fltTarget, float_t fltInstant, const bool_t *pbStopFlag,
GFLIB_DRAMP_T_FLT *psParam)

```

## 2.18.6 Function use

The use of the GFLIB\_DRampInit and GFLIB\_DRamp functions is shown in the following example:

```

#include "gflib.h"

static frac16_t f16InitVal, f16Target, f16Instant, f16Result;
static GFLIB_DRAMP_T_F16 sParam;
static bool_t bStopFlag;

void Isr(void);

void main(void)
{
    sParam.f16RampUp = FRAC16(0.05);
    sParam.f16RampDown = FRAC16(0.02);
    sParam.f16RampUpSat = FRAC16(0.025);
    sParam.f16RampDownSat = FRAC16(0.01);
    f16Target = FRAC16(0.7);
    f16InitVal = FRAC16(0.3);
    f16Instant = FRAC16(0.6);
    bStopFlag = FALSE;

    GFLIB_DRampInit_F16(f16InitVal, &sParam);
}

/* periodically called function */
void Isr()
{
    f16Result = GFLIB_DRamp_F16(f16Target, f16Instant, &bStopFlag, &sParam);
}

```

## 2.19 GFLIB\_FlexRamp

The GFLIB\_FlexRamp function calculates the up/down ramp with a fixed-step increment that is calculated according to the required speed change per a defined duration. These parameters must be set by the user.

The GFLIB\_FlexRamp algorithm consists of three functions that must be used for a proper functionality of the algorithm:

- GFLIB\_FlexRampInit - this function initializes the state variable with a defined value and clears the reach flag

- GFLIB\_FlexRampCalcIncr - this function calculates the increment and clears the reach flag
- GFLIB\_FlexRamp - this function calculates the ramp in the periodically called loop

For a proper use, it is recommended to initialize the algorithm by the GFLIB\_FlexRampInit function. The GFLIB\_FlexRampInit function initializes the internal state variable of the algorithm with a defined value and clears the reach flag. Call the init function when you want to initialize the ramp.

To calculate the increment, use the GFLIB\_FlexRampCalcIncr function. This function is called at the point when you want to change the ramp output value. This function's inputs are the target value and duration. The target value is the destination value that you want to get to. The duration is the time required to change the ramp output from the actual state to the target value. To be able to calculate the ramp increment, fill the control structure with the sample time, that means the period of the loop where the [GFLIB\\_FlexRamp](#) function is called. The structure also contains a variable which determines the maximum value of the increment. It is necessary to set it up too. The equation for the increment calculation is as follows:

$$I = \frac{V_t - V_s}{T} \cdot T_s$$

**Equation 16.**

where:

- I is the increment
- $V_t$  is the target value
- $V_s$  is the state (actual) value (in the structure)
- T is the duration of the ramp (to reach the target value starting at the state value)
- $T_s$  is the sample time, that means the period of the loop where the ramp algorithm is called (set in the structure)

If the increment is greater than the maximum increment (set in the structure), the increment uses the maximum increment value.

As soon as the new increment is calculated, call the [GFLIB\\_FlexRamp](#) algorithm in the periodical control loop. The function works as follows: The function adds the increment to the state value (from the previous step), which results in a new state. The new state is returned by the function. As the time passes, the algorithm is approaching the target value. If the new state trespasses the target value, that new state is limited to the target value and the reach flag is set. The functionality of the implemented algorithm is shown in this figure:

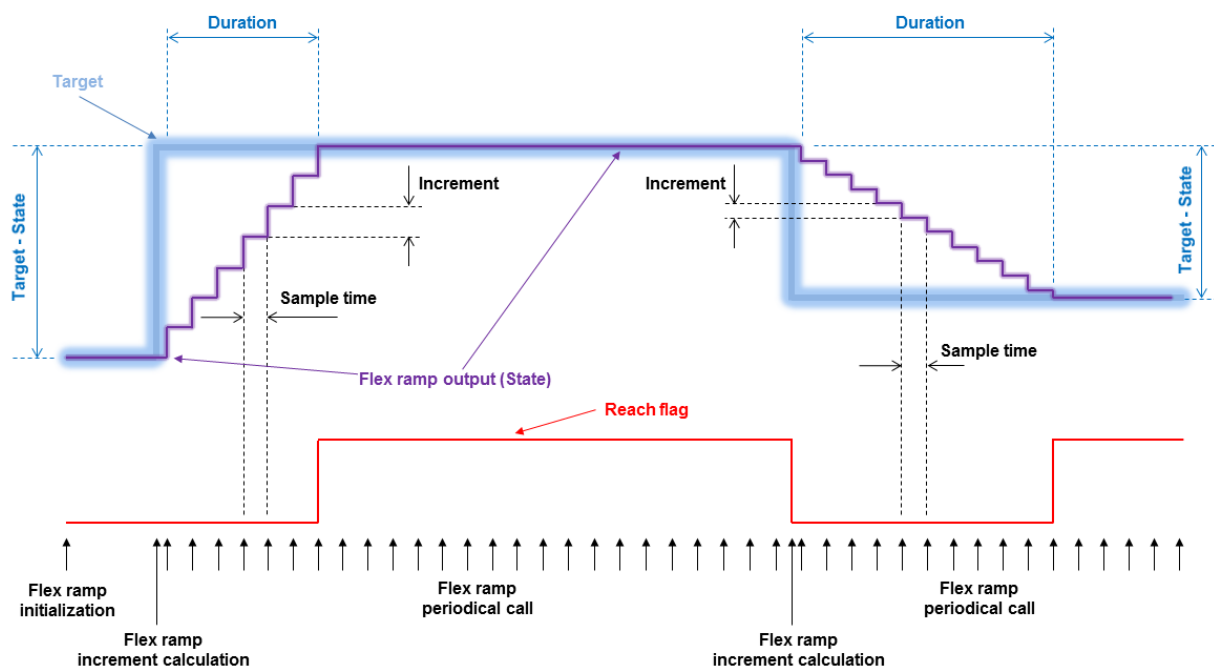


Figure 2-13. GFLIB\_FlexRamp functionality

### 2.19.1 Available versions

This function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range  $-1 ; 1$ ). The input parameters are the fractional and accumulator types.
- Floating-point output - the output is the floating-point result within the type's full range.

The available versions of the GFLIB\_FlexRampInit function are shown in the following table:

Table 2-21. Init function versions

Function name	Input type	Parameters	Result type	Description
GFLIB_FlexRampInit_F16	frac16_t	GFLIB_FLEXRAMP_T_F32 *	void	The input argument is a 16-bit fractional value that represents the initialization value. The parameters' structure is pointed to by a pointer. The input data value is in the range $-1 ; 1$ ).

Table continues on the next page...

**Table 2-21. Init function versions (continued)**

Function name	Input type	Parameters	Result type	Description
GFLIB_FlexRampInit_FLT	float_t	GFLIB_FLEXRAMP_T_FLT *	void	The input argument is a 32-bit single precision floating-point value that represents the initialization value. The parameters' structure is pointed to by a pointer. The input value is within the full 32-bit single-point floating-point range.

The available versions of the [GFLIB\\_FlexRamp](#) function are shown in the following table:

**Table 2-22. Increment calculation function versions**

Function name	Input type		Parameters	Result type
	Target	Duration		
GFLIB_FlexRampCalcIncr_F16	frac16_t	acc32_t	GFLIB_FLEXRAMP_T_F32 *	void
	The input arguments are a 16-bit fractional value in the range <-1 ; 1) that represents the target output value and a 32-bit accumulator value in the range (0 ; 65536.0) that represents the duration of the ramp (in seconds) to reach the target value. The parameters' structure is pointed to by a pointer.			
GFLIB_FlexRampCalcIncr_FLT	float_t	float_t	GFLIB_FLEXRAMP_T_FLT *	void
	The input arguments are 32-bit single precision floating-point values that represent the target output value and the duration of the ramp (in seconds, except zero value) to reach the target value. The parameters' structure is pointed to by a pointer. The target argument is within the full range; the duration argument is a non-negative value.			

**Table 2-23. Function versions**

Function name	Parameters	Result type	Description
GFLIB_FlexRamp_F16	GFLIB_FLEXRAMP_T_F32 *	frac16_t	The parameters' structure is pointed to by a pointer. The function returns a 16-bit fractional value, which represents the actual ramp output value. The output data value is in the range <-1 ; 1).
GFLIB_FlexRamp_FLT	GFLIB_FLEXRAMP_T_FLT *	float_t	The parameters' structure is pointed to by a pointer. The function returns a 32-bit single precision floating-point value, which represents the actual ramp output value. The output value is within the full 32-bit single-point floating-point range.

## 2.19.2 GFLIB\_FLEXRAMP\_T\_F32

Variable name	Type	Description
f32State	<a href="#">frac32_t</a>	The actual value. Controlled by the GFLIB_FlexRampInit_F16 and GFLIB_FlexRamp_F16 algorithms.
f32Incr	<a href="#">frac32_t</a>	The value of the flex ramp increment. Controlled by the GFLIB_FlexRampCalcIncr_F16 algorithm.
f32Target	<a href="#">frac32_t</a>	The target value of the flex ramp algorithm. Controlled by the GFLIB_FlexRampCalcIncr_F16 algorithm.
f32Ts	<a href="#">frac32_t</a>	The sample time, that means the period of the loop where the GFLIB_FlexRamp_F16 algorithms are periodically called. The data value (in seconds) is in the range (0 ; 1). Set by the user.
f32IncrMax	<a href="#">frac32_t</a>	The maximum value of the flex ramp increment. The data value is in the range (0 ; 1). Set by the user.
bReachFlag	<a href="#">bool_t</a>	The reach flag. This flag is controlled by the GFLIB_FlexRamp_F16 algorithm. It is cleared by the GFLIB_FlexRampInit_F16 and GFLIB_FlexRampCalcIncr_F16 algorithms.

## 2.19.3 GFLIB\_FLEXRAMP\_T\_FLT

Variable name	Type	Description
fltState	<a href="#">float_t</a>	The actual value. Controlled by the GFLIB_FlexRampInit_FLT and GFLIB_FlexRamp_FLT algorithms.
fltIncr	<a href="#">float_t</a>	The value of the flex ramp increment. Controlled by the GFLIB_FlexRampCalcIncr_FLT algorithm.
fltTarget	<a href="#">float_t</a>	The target value of the flex ramp algorithm. Controlled by the GFLIB_FlexRampCalcIncr_FLT algorithm.
fltTs	<a href="#">float_t</a>	The sample time, that means the period of the loop where the GFLIB_FlexRamp_FLT algorithm is periodically called. The data value (in seconds, except zero value) is a non-negative value. Set by the user.
fltIncrMax	<a href="#">float_t</a>	The maximum value of the flex ramp increment. The data is a positive value. Set by the user.
bReachFlag	<a href="#">bool_t</a>	The reach flag. This flag is controlled by the GFLIB_FlexRamp_FLT algorithm. It is cleared by the GFLIB_FlexRampInit_FLT and GFLIB_FlexRampCalcIncr_FLT algorithms.

## 2.19.4 Declaration

The available GFLIB\_FlexRampInit functions have the following declarations:

```
void GFLIB_FlexRampInit_F16(frac16\_t f16InitVal, GFLIB\_FLEXRAMP\_T\_F32 *psParam)
void GFLIB_FlexRampInit_FLT(float\_t fltInitVal, GFLIB\_FLEXRAMP\_T\_FLT *psParam)
```

The available GFLIB\_FlexRampCalcIncr functions have the following declarations:

## GFLIB\_DFlexRamp

```
void GFLIB_FlexRampCalcIncr_F16(frac16_t f16Target, acc32_t a32Duration,
GFLIB_FLEXRAMP_T_F32 *psParam)
void GFLIB_FlexRampCalcIncr_FLT(float_t fltTarget, float_t fltDuration, GFLIB_FLEXRAMP_T_FLT
*psParam)
```

The available [GFLIB\\_FlexRamp](#) functions have the following declarations:

```
frac16_t GFLIB_FlexRamp_F16(GFLIB_FLEXRAMP_T_F32 *psParam)
float_t GFLIB_FlexRamp_FLT(GFLIB_FLEXRAMP_T_FLT *psParam)
```

### 2.19.5 Function use

The use of the [GFLIB\\_FlexRampInit](#), [GFLIB\\_FlexRampCalcIncr](#), and [GFLIB\\_FlexRamp](#) functions is shown in the following example:

```
#include "gflib.h"

static frac16_t f16InitVal;
static GFLIB_FLEXRAMP_T_F32 sFlexRamp;
static frac16_t f16Target, f16RampResult;
static acc32_t a32RampDuration;

void Isr(void);

void main(void)
{
    /* Control loop period is 0.002 s; maximum increment value is 0.15 */
    sFlexRamp.f32Ts = FRAC32(0.002);
    sFlexRamp.f32IncrMax = FRAC32(0.15);

    /* Initial value to 0 */
    f16InitVal = FRAC16(0.0);

    /* Flex ramp initialization */
    GFLIB_FlexRampInit_F16(f16InitVal, &sFlexRamp);

    /* Target value is 0.7 in duration of 5.3 s */
    f16Target = FRAC16(0.7);
    a32RampDuration = ACC32(5.3);

    /* Flex ramp increment calculation */
    GFLIB_FlexRampCalcIncr_F16(f16Target, a32RampDuration, &sFlexRamp);
}

/* periodically called control loop with a period of 2 ms */
void Isr()
{
    f16RampResult = GFLIB_FlexRamp_F16(&sFlexRamp);
}
```

## 2.20 GFLIB\_DFlexRamp

The [GFLIB\\_DFLEXRamp](#) function calculates the up/down ramp with a fixed-step increment that is calculated according to the required speed change per a defined duration. These parameters must be set by the user. The algorithm has stop flags. If none of them is set, the ramp behaves normally. If one of them is set, the ramp can run in the opposite direction.

The [GFLIB\\_DFLEXRamp](#) algorithm consists of three functions that must be used for a proper functionality of the algorithm:

- [GFLIB\\_DFLEXRampInit](#) - this function initializes the state variable with a defined value and clears the reach flag
- [GFLIB\\_DFLEXRampCalcIncr](#) - this function calculates the increment and clears the reach flag
- [GFLIB\\_DFLEXRamp](#) - this function calculates the ramp in the periodically called loop

For a proper use, initialize the algorithm by the [GFLIB\\_DFLEXRampInit](#) function. The [GFLIB\\_DFLEXRampInit](#) function initializes the internal state variable of the algorithm with a defined value and clears the reach flag. Call the init function when you want to initialize the ramp.

To calculate the increment, use the [GFLIB\\_DFLEXRampCalcIncr](#) function. Call this function when you want to change the ramp output value. This function's inputs are the target value and duration, and the ramp increments for motoring and generating saturation modes. The target value is the destination value that you want to get to. The duration is the time required to change the ramp output from the actual state to the target value. To calculate the ramp increment, fill the control structure with the sample time, that means the period of the loop where the [GFLIB\\_DFLEXRamp](#) function is called. The structure also contains a variable which determines the maximum value of the increment. It is necessary to set it up too. The equation for the increment calculation is as follows:

$$I = \frac{V_t - V_s}{T} \cdot T_s$$

**Equation 17.**

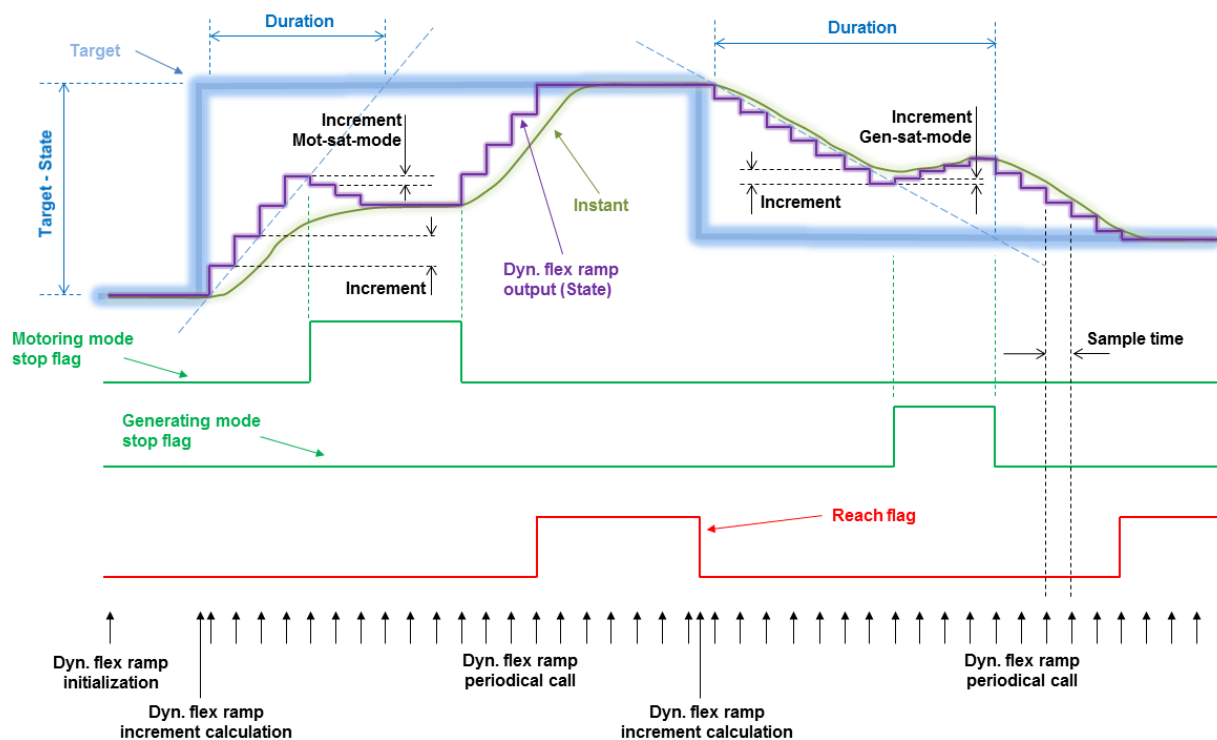
where:

- I is the increment
- $V_t$  is the target value
- $V_s$  is the state (actual) value (in the structure)
- T is the duration of the ramp (to reach the target value starting at the state value)
- $T_s$  is the sample time, that means the period of the loop where the ramp algorithm is called (set in the structure)

If the increment is greater than the maximum increment (set in the structure), the increment uses the maximum increment value.

The state, target, and instant values must have the same sign, otherwise the saturation modes don't work properly.

As soon as the new increment is calculated, you can call the [GFLIB\\_DFlexRamp](#) algorithm in the periodical control loop. If none of the stop flags is set, the function works as follows: The function adds the increment to the state value (from the previous step), which results in a new state. The new state is returned by the function. As time passes, the algorithm is approaching the target value. If the new state trespasses the target value that new state is limited to, the target value and the reach flag are set. The functionality of the implemented algorithm is shown in the following figure:



**Figure 2-14. GFLIB\_DFlexRamp functionality**

If the motoring mode stop flag is set and the absolute value of the target value is greater than the absolute value of the state value, the function uses the increment for the motoring saturation mode to return to the instant value. Use case: when the application is in the saturation mode and cannot supply more power to increase the speed, then a saturation (motoring mode) flag is generated. To get out of the saturation, the ramp output value is being reduced.



If the generating mode stop flag is set and the absolute value of the target value is lower than the absolute value of the state value, the function uses the increment for the generating saturation mode to return to the instant value. Use case: when the application is braking a motor and voltage increases on the DC-bus capacitor, then a saturation (generating mode) flag is generated. To avoid trespassing the DC-bus safe voltage limit, the speed requirement is increasing to dissipate the energy of the capacitor.

## 2.20.1 Available versions

This function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range  $-1 ; 1$ ). The input parameters are the fractional and accumulator types.

The available versions of the GFLIB\_DFLEXRampInit functions are shown in the following table:

**Table 2-24. Init function versions**

Function name	Input type	Parameters	Result type	Description
GFLIB_FlexRampInit_F16	<a href="#">frac16_t</a>	<a href="#">GFLIB_DFLEXRAMP_T_F32</a> *	void	The input argument is a 16-bit fractional value that represents the initialization value. The parameters' structure is pointed to by a pointer. The input data value is in the range $-1 ; 1$ ).
GFLIB_FlexRampInit_FLT	<a href="#">float_t</a>	<a href="#">GFLIB_DFLEXRAMP_T_FLT</a> *	void	The input argument is a 32-bit single precision floating-point value that represents the initialization value. The parameters' structure is pointed to by a pointer. The input value is within the full 32-bit single-point floating-point range.

The available versions of the [GFLIB\\_DFLEXRamp](#) functions are shown in the following table:

**Table 2-25. Increment calculation function versions**

Function name	Input type				Parameters	Result type
	Target	Duration	Incr. sat-mot	Incr. sat-gen		
GFLIB_DFLEXRampCalcIncr_F16	<a href="#">frac16_t</a>	<a href="#">acc32_t</a>	<a href="#">frac32_t</a>	<a href="#">frac32_t</a>	<a href="#">GFLIB_DFLEXRAMP_T_F32</a> *	void

*Table continues on the next page...*

**Table 2-25. Increment calculation function versions (continued)**

Function name	Input type				Parameters	Result type
	Target	Duration	Incr. sat-mot	Incr. sat-gen		
	The input arguments are 16-bit fractional values in the range <-1 ; 1) that represent the target output value and a 32-bit accumulator value in the range (0 ; 65536.0) that represents the duration (in seconds) of the ramp to reach the target value. The other two arguments are increments for the saturation mode when in the motoring and generating modes. The parameters' structure is pointed to by a pointer.					
GFLIB_DFlexRampCalcIncr_FLT	float_t	float_t	float_t	float_t	GFLIB_DFLEXRAMP_T_FLT *	void
	The input arguments are 32-bit single precision floating-point values that represent the target output value and the duration of the ramp (in seconds, except zero value) to reach the target value. The other two arguments are increments for the saturation mode when in the motoring and generating modes. The parameters' structure is pointed to by a pointer. The target argument is within the full range; the duration argument is a non-negative value.					

**Table 2-26. Function versions**

Function name	Input type			Parameters	Result type
	Instant	Stop flag-mot	Stop flag-gen		
GFLIB_DFlexRamp_F16	frac16_t	bool_t *	bool_t *	GFLIB_DFLEXRAMP_T_F32 *	frac16_t
	The input argument is a 16-bit fractional value in the range <-1 ; 1) that represents the measured instant value. The stop flags are pointers to the bool_t types. The parameters' structure is pointed to by a pointer. The function returns a 16-bit fractional value, which represents the actual ramp output value. The output data value is in the range <-1 ; 1).				
GFLIB_DFlexRamp_FLT	float_t	bool_t *	bool_t *	GFLIB_DFLEXRAMP_T_FLT *	float_t
	The input arguments are 32-bit single precision floating-point values that represent the measured instant value. The stop flags are pointers to bool_t types. The parameters' structure is pointed to by a pointer. The function returns a 32-bit single precision floating-point value, which represents the actual ramp output value. The output value is within the full 32-bit single-point floating-point range.				

## 2.20.2 GFLIB\_DFLEXRAMP\_T\_F32

Variable name	Type	Description
f32State	frac32_t	The actual value. Controlled by the GFLIB_FlexRampInit_F16 and GFLIB_FlexRamp_F16 algorithms.
f32Incr	frac32_t	The value of the dyn. flex ramp increment. Controlled by the GFLIB_FlexRampCalcIncr_F16 algorithm.
f32IncrSatMot	frac32_t	The value of the dyn. flex ramp increment when in the motoring saturation mode. Controlled by the GFLIB_DFlexRampCalcIncr_F16 algorithm.

Table continues on the next page...

Variable name	Type	Description
f32IncrSatGen	<a href="#">frac32_t</a>	The value of the dyn. flex ramp increment when in the generating saturation mode. Controlled by the GFLIB_DFflexRampCalcIncr_F16 algorithm.
f32Target	<a href="#">frac32_t</a>	The target value of the flex ramp algorithm. Controlled by the GFLIB_DFflexRampCalcIncr_F16 algorithm.
f32Ts	<a href="#">frac32_t</a>	The sample time, that means the period of the loop where the GFLIB_DFflexRamp_F16 algorithm is periodically called. The data value (in seconds) is in the range (0 ; 1). Set by the user.
f32IncrMax	<a href="#">frac32_t</a>	The maximum value of the flex ramp increment. The data value is in the range (0 ; 1). Set by the user.
bReachFlag	<a href="#">bool_t</a>	Reach flag. This flag is controlled by the GFLIB_DFflexRamp_F16 algorithm. It is cleared by the GFLIB_DFflexRampInit_F16 and GFLIB_DFflexRampCalcIncr_F16 algorithms.

### 2.20.3 GFLIB\_DFLEXRAMP\_T\_FLT

Variable name	Type	Description
fltState	<a href="#">float_t</a>	The actual value. Controlled by the GFLIB_DFflexRampInit_FLT and GFLIB_DFflexRamp_FLT algorithms.
fltIncr	<a href="#">float_t</a>	The value of the flex ramp increment. Controlled by the GFLIB_DFflexRampCalcIncr_FLT algorithm.
fltIncrSatMot	<a href="#">float_t</a>	The value of the dyn. flex ramp increment when in the motoring saturation mode. Controlled by the GFLIB_DFflexRampCalcIncr_FLT algorithm.
fltIncrSatGen	<a href="#">float_t</a>	The value of the dyn. flex ramp increment when in the generating saturation mode. Controlled by the GFLIB_DFflexRampCalcIncr_FLT algorithm.
fltTarget	<a href="#">float_t</a>	The target value of the flex ramp algorithm. Controlled by the GFLIB_DFflexRampCalcIncr_FLT algorithm.
fltTs	<a href="#">float_t</a>	The sample time, that means the period of the loop where the GFLIB_DFflexRamp_FLT algorithm is periodically called. The data value (in seconds, except zero value) is a non-negative value. Set by the user.
fltIncrMax	<a href="#">float_t</a>	The maximum value of the flex ramp increment. The data is a positive value. Set by the user.
bReachFlag	<a href="#">bool_t</a>	The reach flag. This flag is controlled by the GFLIB_DFflexRamp_FLT algorithm. It is cleared by the GFLIB_DFflexRampInit_FLT and GFLIB_DFflexRampCalcIncr_FLT algorithms.

### 2.20.4 Declaration

The available GFLIB\_DFflexRampInit functions have the following declarations:

```
void GFLIB_DFflexRampInit_F16(frac16\_t f16InitVal, GFLIB\_DFLEXRAMP\_T\_F32 *psParam)
void GFLIB_DFflexRampInit_FLT(float\_t fltInitVal, GFLIB\_DFLEXRAMP\_T\_FLT *psParam)
```

The available GFLIB\_DFflexRampCalcIncr functions have the following declarations:

## GFLIB\_DFlexRamp

```
void GFLIB_DFlexRampCalcIncr_F16(frac16_t f16Target, acc32_t a32Duration, frac32_t
f32IncrSatMot, frac32_t f32IncrSatGen, GFLIB_DFLEXRAMP_T_F32 *psParam)
void GFLIB_DFlexRampCalcIncr_FLT(float_t fltTarget, float_t fltDuration, float_t
f32IncrSatMot, float_t f32IncrSatGen, GFLIB_DFLEXRAMP_T_FLT *psParam)
```

The available [GFLIB\\_DFlexRamp](#) functions have the following declarations:

```
frac16_t GFLIB_DFlexRamp_F16(frac16_t f16Instant, const bool_t *pbStopFlagMot, const bool_t
*pbStopFlagGen, GFLIB_DFLEXRAMP_T_F32 *psParam)
float_t GFLIB_DFlexRamp_FLT(float_t fltInstant, const bool_t *pbStopFlagMot, const bool_t
*pbStopFlagGen, GFLIB_DFLEXRAMP_T_FLT *psParam)
```

## 2.20.5 Function use

The use of the [GFLIB\\_DFlexRampInit](#), [GFLIB\\_DFlexRampCalcIncr](#), and [GFLIB\\_DFlexRamp](#) functions is shown in the following example:

```
#include "gflib.h"

static frac16_t f16InitVal;
static GFLIB_DFLEXRAMP_T_F32 sDFlexRamp;
static frac16_t f16Target, f16RampResult, f16Instant;
static acc32_t a32RampDuration;
static frac32_t f32IncrSatMotMode, f32IncrSatGenMode;
static bool_t bSatMot, bSatGen;

void Isr(void);

void main(void)
{
    /* Control loop period is 0.002 s; maximum increment value is 0.15 */
    sDFlexRamp.f32Ts = FRAC32(0.002);
    sDFlexRamp.f32IncrMax = FRAC32(0.15);

    /* Initial value to 0 */
    f16InitVal = FRAC16(0.0);

    /* Dyn. flex ramp initialization */
    GFLIB_FlexRampInit_F16(f16InitVal, &sDFlexRamp);

    /* Target value is 0.7 in duration of 5.3 s */
    f16Target = FRAC16(0.7);
    a32RampDuration = ACC32(5.3);

    /* Saturation increments */
    f32IncrSatMotMode = FRAC32(0.000015);
    f32IncrSatGenMode = FRAC32(0.00002);

    /* Saturation flags init */
    bSatMot = FALSE;
    bSatGen = FALSE;

    /* Dyn. flex ramp increment calculation */
    GFLIB_DFlexRampCalcIncr_F16(f16Target, a32RampDuration, f32IncrSatMotMode,
f32IncrSatGenMode, &sDFlexRamp);
}

/* periodically called control loop with a period of 2 ms */
void Isr()
{
```

```
f16RampResult = GFLIB_DFlexRamp_F16(f16Instant, &bSatMot, &bSatGen, &sDFlexRamp);
}
```

## 2.21 GFLIB\_FlexSRamp

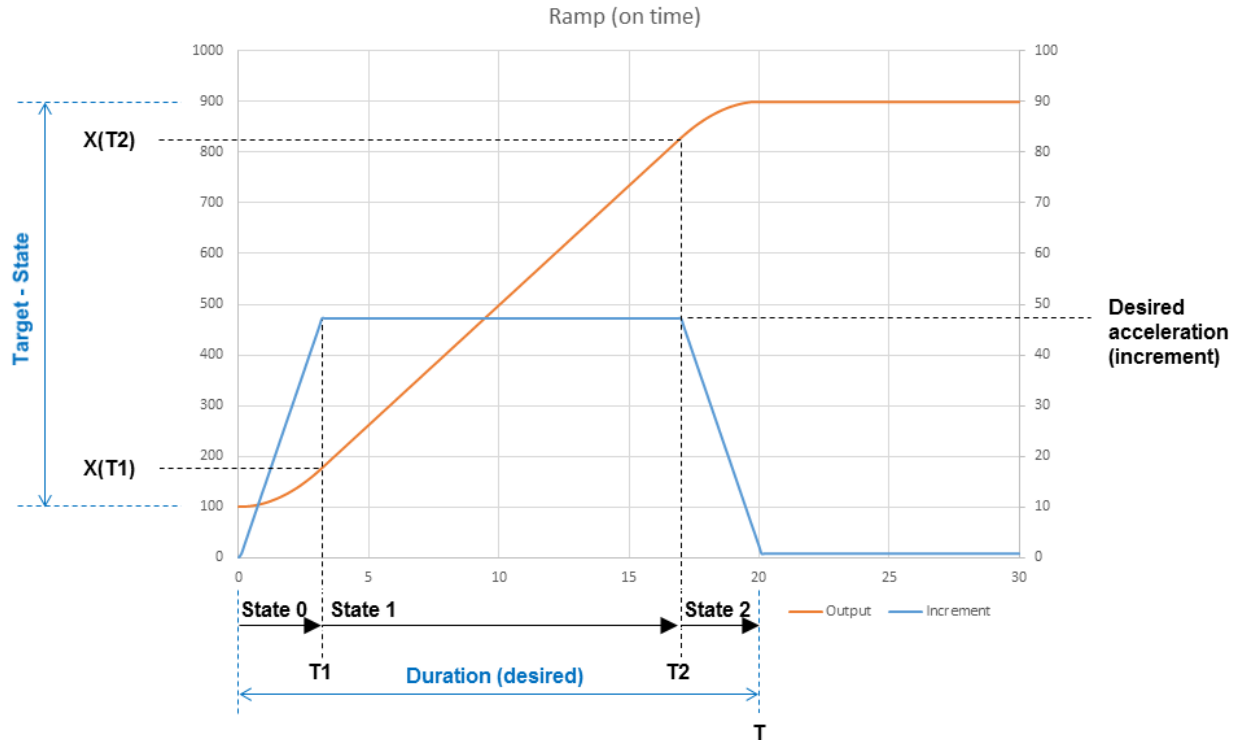
The [GFLIB\\_FlexSRamp](#) function calculates the up/down ramp with a variable increment that is calculated according to the required speed change per a defined duration. These parameters must be set by the user. The variable increment is profiled to reach the S-profile of the resulting ramp.

The [GFLIB\\_FlexSRamp](#) algorithm consists of three functions that must be used for a proper functionality of the algorithm:

- [GFLIB\\_FlexSRampInit](#) - this function initializes the state variable with a defined value, resets the acceleration increment to zero, sets the acceleration state to zero, and clears the reach flag
- [GFLIB\\_FlexSRampCalcIncr](#) - this function calculates the desired acceleration, two points of the speed where the acceleration changes from a variable to a constant and vice-versa, acceleration (derivative) increment, resets the increment to zero, sets the acceleration state to zero, and clears the reach flag
- [GFLIB\\_FlexSRamp](#) - this function calculates the ramp in the periodically called loop

For a proper use, initialize the algorithm by the [GFLIB\\_FlexSRampInit](#) function. The [GFLIB\\_FlexSRampInit](#) function initializes the internal state variable of the algorithm with a defined value, resets the acceleration increment to zero, sets the acceleration state to zero, and clears the reach flag. This function does not affect the other parameters of the ramp. Call the init function to initialize the ramp.

To calculate the profile of the ramp, use the [GFLIB\\_FlexSRampCalcIncr](#) function. This function is called when you want to change the ramp output value. This function's inputs are the target value and duration. The target value is the destination value that you want to get to. The duration is the time required to change the ramp output from the actual state to the target value. To calculate the ramp increment, fill the control structure with the sample time, that means the period of the loop where the [GFLIB\\_FlexSRamp](#) function is called. Set up the desirable acceleration derivative that is necessary for the acceleration and deceleration states. The structure also contains a variable that determines the maximum value of the increment (acceleration). It is necessary to set it up too. The equations for the ramp calculation are derived from the following figure:



**Figure 2-15. GFLIB\_FlexSRamp profile**

For the ramp output change in each state, these equations apply:

$$\Delta x_1 = x(T_1) - x(0)$$

**Equation 18.**

$$\Delta x_2 = x(T_2) - x(T_1)$$

**Equation 19.**

$$\Delta x_3 = \Delta x_1$$

**Equation 20.**

where:

- $x$  is the ramp output
- $\Delta x_1$  is the ramp change in state 0
- $\Delta x_2$  is the ramp change in state 1
- $\Delta x_3$  is the ramp change in state 2
- $T_1$  is the instant when the desired acceleration is reached and becomes constant
- $T_2$  is the instant when the desired acceleration starts to decrease

To get the full ramp change between the actual state value and the target value, this equation applies:

$$\Delta x = \Delta x_1 + \Delta x_2 + \Delta x_3 = 2 \cdot \Delta x_1 + \Delta x_2$$

**Equation 21.**

The value of the desired acceleration that is reached by the integration of the acceleration derivative along the time within state 0 is:

$$a_{des} = a(T_1) = \int_0^{T_1} dA \cdot dt = dA \cdot T_1$$

**Equation 22.**

where:

- $a_{des}$  is the desired acceleration
- $dA$  is the derivative of the acceleration

Similarly, the  $\Delta x_1$  and  $\Delta x_2$  values are given by integrating the acceleration in time:

$$\Delta x_1 = \int_0^{T_1} dA \cdot t \cdot dt = \frac{1}{2} dA \cdot T_1^2$$

**Equation 23.**

$$\Delta x_2 = \int_{T_1}^{T_2} a_{des} \cdot dt = a_{des} \cdot (T_2 - T_1)$$

**Equation 24.**

Because the ramp is symmetrical, time  $T_2$  is expressed as:

$$T_2 = T - T_1$$

**Equation 25.**

where:

- $T$  is the duration of the ramp

Using the equations for  $a_{des}$  and  $T_2$ , [Equation 24 on page 87](#) is rewritten as:

$$\Delta x_2 = dA \cdot T_1 \cdot (T - 2T_1)$$

**Equation 26.**

Putting [Equation 26 on page 87](#) and [Equation 26 on page 87](#) into [Equation 21 on page 87](#), the following equation is reached:

$$\Delta x = 2 \cdot \frac{1}{2} \cdot dA \cdot T_1^2 + dA \cdot T_1 \cdot (T - 2T_1) = -dA \cdot T_1^2 + dA \cdot T \cdot T_1$$

**Equation 27.**

Having normalized the previous equation, a quadrature equation is reached:

$$T_1^2 - T \cdot T_1 + \frac{\Delta x}{dA} = 0$$

**Equation 28.**

One root of this quadrature equation is  $T_1$ :

$$T_1 = \frac{T - \sqrt{T^2 - 4 \cdot \frac{\Delta x}{dA}}}{2}$$

**Equation 29.**

Using [Equation 22 on page 87](#), the desired acceleration is expressed as:

$$a_{des} = \frac{dA \cdot T - \sqrt{dA^2 \cdot T^2 - 4 \cdot dA \cdot \Delta x}}{2}$$

**Equation 30.**

This equation has a solution within the range of real numbers only if the square root argument is not negative, so this condition must be met:

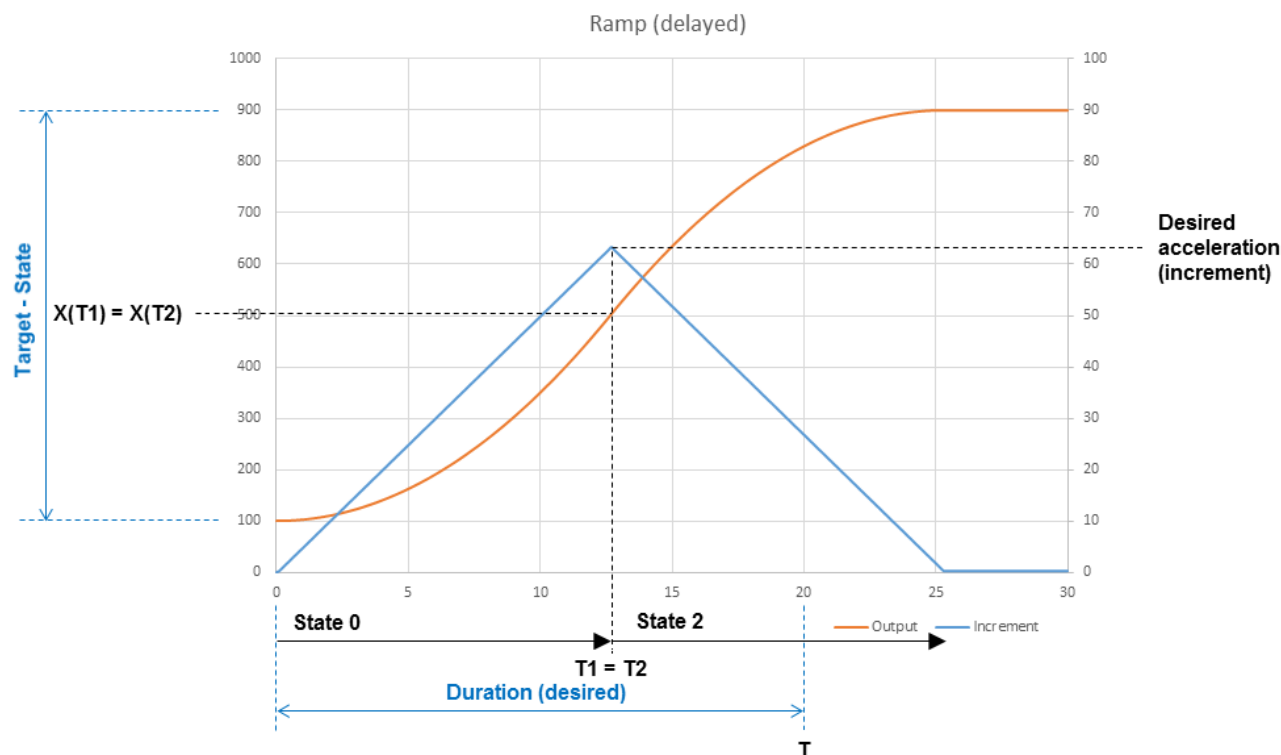
$$dA^2 \cdot T^2 \geq 4 \cdot dA \cdot \Delta x$$

**Equation 31.**

If this condition is met and the desired acceleration is not greater than the maximum increment (set in the structure), the ramp is achievable within the defined duration and the function's output flag is *TRUE*. If the acceleration is greater than the maximum increment, the function uses the maximum increment value and then the ramp is not achieved on time, the output flag is *FALSE*.

If the condition given by [Equation 31 on page 88](#) is not met, the ramp is not achievable within the defined duration and the function returns the flag *FALSE*. In such case, the ramp skips state 1 (where the acceleration is constant) and goes directly from state 0 to state 2. The following figure shows the ramp profile:





**Figure 2-16. GFLIB\_FlexSRamp delayed profile**

This ramp takes longer time than desirable duration. In this case,  $\Delta x_I$  is exactly a half of the full ramp change output. The  $T_I$  instant is derived from Equation 23 on page 87 as:

$$T_I = \sqrt{\frac{2 \cdot \Delta x_I}{dA}} = \sqrt{\frac{\Delta x}{dA}}$$

**Equation 32.**

The desired acceleration is given by Equation 22 on page 87 as:

$$a_{des} = dA \cdot \sqrt{\frac{\Delta x}{dA}} = \sqrt{\Delta x \cdot dA}$$

**Equation 33.**

Similarly to the previous case (when the ramp is achievable within the desired time), the desired acceleration cannot be greater than the maximum increment, otherwise the function uses the maximum increment value. If the desired acceleration is trimmed, the ramp is in state 1 with a constant acceleration.

In both cases, the desired acceleration could have been reduced to the maximum increment value, therefore it is necessary to adjust the  $T_I$  value using Equation 22 on page 87 :

$$T_1 = \frac{a_{des}}{dA}$$

**Equation 34.**

where:

- $a_{des}$  can be changed to the maximum increment

By putting  $T_1$  into [Equation 23 on page 87](#), the  $\Delta x_I$  value is given as:

$$\Delta x_1 = \frac{1}{2} dA \cdot \left( \frac{a_{des}}{dA} \right)^2 = \frac{1}{2} \cdot \frac{a_{des}^2}{dA}$$

**Equation 35.**

Because the ramp output profile is now symmetrical, the ramp output value in time  $T_1$  is given by adding (or subtracting) the  $\Delta x_I$  value to the state value. Similarly, the ramp output value in time  $T_2$  is given by subtracting (or adding) the  $\Delta x_I$  value from the target value. These two values are returned within the function structure together with the desired acceleration value.

Another parameter that must be calculated is the acceleration increment. The increment uses the derivative of acceleration  $dA$  and the sample time of the application. This must apply:

$$dA = \frac{da}{dt} = \frac{d^2x}{dt^2} \approx \frac{A_{incr}}{T_s^2}$$

**Equation 36.**

where:

- $A_{incr}$  is the acceleration increment
- $T_s$  is the sample time

The acceleration increment needed for the algorithm is:

$$A_{incr} = T_s^2 \cdot dA$$

**Equation 37.**

As soon as the necessary parameters are calculated, call the [GFLIB\\_FlexSRamp](#) algorithm in the periodical control loop. The function works in these three states:

- State 0 - acceleration rises from 0 towards the desired acceleration
- State 1 - acceleration is constant
- State 2 - acceleration is falling from the desired acceleration towards zero

In state 0, the function adds the acceleration increment to the increment. In the first step, it only adds half of the acceleration increment (to form the trapezoidal integration). The resulting increment is added to or subtracted from the state value (from the previous step), which results in a new state. The new state is returned by the function. After the  $X(T_1)$  value is reached, the function switches to state 1. At the same time, the function checks whether the condition  $X(T_2)$  value is reached. In such case, the function goes directly to state 2.

In state 1, the function does not change the increment; it stays constant from the last value in state 0. The increment is added to or subtracted from the state value (from the previous step), which results in a new state. The new state is returned by the function. When the  $X(T_2)$  value is reached, the function switches to state 2.

In state 2, the function subtracts the acceleration increment from the increment. The resulting increment is added to or subtracted from the state value (from the previous step), which results in a new state. The new state is returned by the function. If the new state trespasses the target value, it is trimmed to the target value. It can happen that the function output does not reach the target value before the increment returns to zero. If the increment is zero before reaching the target value, the output stops before the target value. This can happen because the function does not work with the continuous time. The incrementation depends on the sampling time and the arithmetic accuracy used. To ensure that the function always reaches the target value, the function checks if the increment is not lower than the half of the acceleration increment. If the resulting increment is lower than half of the acceleration increment, the increment is set to a half of the acceleration increment. Using this approach, the function always reaches the target value. As soon as the target value is reached, the reach flag is set.

The functionality of the implemented algorithm is shown in this figure:

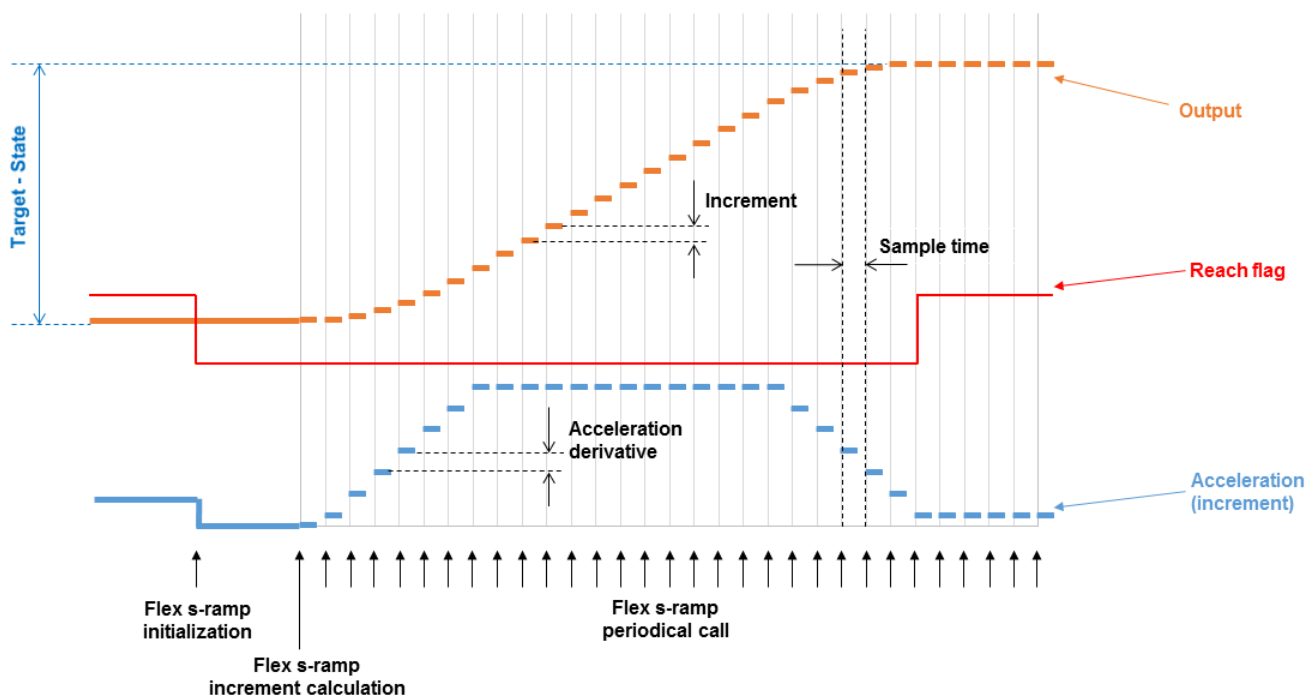


Figure 2-17. GFLIB\_FlexSRamp functionality

## 2.21.1 Available versions

This function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range  $-1 ; 1$ ). The input parameters are the fractional and accumulator types.

The available versions of the GFLIB\_FlexSRampInit function are shown in the following table:

Table 2-27. Init function versions

Function name	Input type	Parameters	Result type	Description
GFLIB_FlexSRampInit_F16	<a href="#">frac16_t</a>	<a href="#">GFLIB_FLEXSRAMP_T_F32</a> *	void	The input argument is a 16-bit fractional value that represents the initialization value. The parameters' structure is pointed to by a pointer. The input data value is in the range $-1 ; 1$ ).
GFLIB_FlexRampInit_FLT	<a href="#">float_t</a>	<a href="#">GFLIB_FLEXSRAMP_T_FLT</a> *	void	The input argument is a 32-bit single precision floating-point value that represents the initialization value. The

**Table 2-27. Init function versions**

Function name	Input type	Parameters	Result type	Description
				parameters' structure is pointed to by a pointer. The input value is within the full 32-bit single-point floating-point range.

The available versions of the [GFLIB\\_FlexSRamp](#) function are shown in the following table:

**Table 2-28. Increment calculation function versions**

Function name	Input type		Parameters	Result type
	Target	Duration		
GFLIB_FlexSRampCalcIncr_F16	<a href="#">frac16_t</a>	<a href="#">acc32_t</a>	<a href="#">GFLIB_FLEXSRAMP_T_F32</a> *	<a href="#">bool_t</a>
	The input arguments are a 16-bit fractional value in the range <-1 ; 1) that represents the target output value and a 32-bit accumulator value in the range (0 ; 1/ f16DA) that represents the duration of the ramp (in seconds) to reach the target value. The parameters' structure is pointed to by a pointer. The function returns TRUE if the ramp is achievable within the defined duration; if it is not achievable, it returns FALSE. The parameters are calculated, but the ramp takes longer.			
GFLIB_FlexRampCalcIncr_FLT	<a href="#">float_t</a>	<a href="#">float_t</a>	<a href="#">GFLIB_FLEXSRAMP_T_FLT</a> *	<a href="#">bool_t</a>
	The input arguments are 32-bit single precision floating-point values that represent the target output value and the duration of the ramp (in seconds, except zero value) to reach the target value. The parameters' structure is pointed to by a pointer. The target argument is within the full range; the duration argument is a non-negative value. The function returns TRUE if the ramp is achievable within the defined duration; if it is not achievable, it returns FALSE. The parameters are calculated, but the ramp takes longer.			

**Table 2-29. Function versions**

Function name	Parameters	Result type	Description
GFLIB_FlexSRamp_F16	<a href="#">GFLIB_FLEXSRAMP_T_F32</a> *	<a href="#">frac16_t</a>	The parameters' structure is pointed to by a pointer. The function returns a 16-bit fractional value, which represents the actual ramp output value. The output data value is in the range <-1 ; 1).
GFLIB_FlexRamp_FLT	<a href="#">GFLIB_FLEXSRAMP_T_FLT</a> *	<a href="#">float_t</a>	The parameters' structure is pointed to by a pointer. The function returns a 32-bit single precision floating-point value, which represents the actual ramp output value. The output value is within the full 32-bit single-point floating-point range.

## 2.21.2 GFLIB\_FLEXSRAMP\_T\_F32

Variable name	Type	Description
f32State	<a href="#">frac32_t</a>	The actual value. Controlled by the GFLIB_FlexSRampInit_F16 and GFLIB_FlexSRamp_F16 algorithms.
f32Incr	<a href="#">frac32_t</a>	The value of the flex s-ramp increment. Controlled by the GFLIB_FlexSRamp_F16 algorithm. It is reset to zero by the GFLIB_FlexSRampInit_F16 and GFLIB_FlexSRampCalcIncr_F16 algorithms.
f32AIincr	<a href="#">frac32_t</a>	The value of the flex s-ramp acceleration increment. Controlled by the GFLIB_FlexSRampCalcIncr_F16 algorithm.
f32ADes	<a href="#">frac32_t</a>	The value of the flex s-ramp desired acceleration. Controlled by the GFLIB_FlexSRampCalcIncr_F16 algorithm.
f32Target	<a href="#">frac32_t</a>	The target value of the flex s-ramp algorithm. Controlled by the GFLIB_FlexSRampCalcIncr_F16 algorithm.
f32Ts	<a href="#">frac32_t</a>	The sample time, that means the period of the loop where the GFLIB_FlexSRamp_F16 algorithms are periodically called. The data value (in seconds) is in the range (0 ; 1). Set by the user.
f32IncrMax	<a href="#">frac32_t</a>	The maximum value of the flex s-ramp increment. The data value is in the range (0 ; 1). Set by the user.
f32XT1	<a href="#">frac32_t</a>	The flex s-ramp value of the point where the increment must stop incrementing. Controlled by the GFLIB_FlexSRampCalcIncr_F16 algorithm.
f32XT2	<a href="#">frac32_t</a>	The flex s-ramp value of the point where the increment must start decrementing. Controlled by the GFLIB_FlexSRampCalcIncr_F16 algorithm.
f16DA	<a href="#">frac16_t</a>	The acceleration derivative. The data value (in acceleration change per second or ramp output value change per square second) is in the range <0 ; 0.5). Set by the user.
u16AccState	<a href="#">uint_16_t</a>	The acceleration state of the function: 0 - acceleration rises; 1 - acceleration is constant; 2 - acceleration falls. Controlled by the GFLIB_FlexSRamp_F16 algorithm. It is reset to zero by the GFLIB_FlexSRampInit_F16 and GFLIB_FlexSRampCalcIncr_F16 algorithms.
bReachFlag	<a href="#">bool_t</a>	Reach flag. This flag is controlled by the GFLIB_FlexSRamp_F16 algorithm. It is cleared by the GFLIB_FlexSRampInit_F16 and GFLIB_FlexSRampCalcIncr_F16 algorithms.

## 2.21.3 GFLIB\_FLEXSRAMP\_T\_FLT

Variable name	Type	Description
fltState	<a href="#">float_t</a>	The actual value. Controlled by the GFLIB_FlexSRampInit_FLT and GFLIB_FlexSRamp_FLT algorithms.
fltIncr	<a href="#">float_t</a>	The value of the flex s-ramp increment. Controlled by the GFLIB_FlexSRamp_FLT algorithm. It is reset to zero by the GFLIB_FlexSRampInit_FLT and GFLIB_FlexSRampCalcIncr_FLT algorithms.
fltAIincr	<a href="#">float_t</a>	The value of the flex s-ramp acceleration increment. Controlled by the GFLIB_FlexSRampCalcIncr_FLT algorithm.
fltADes	<a href="#">float_t</a>	The value of the flex s-ramp desired acceleration. Controlled by the GFLIB_FlexSRampCalcIncr_FLT algorithm.
fltTarget	<a href="#">float_t</a>	The target value of the flex s-ramp algorithm. Controlled by the GFLIB_FlexSRampCalcIncr_FLT algorithm.

*Table continues on the next page...*

Variable name	Type	Description
fltTs	float_t	The sample time, that means the period of the loop where the GFLIB_FlexSRamp_FLT algorithms are periodically called. The data value (in seconds, except zero value) is in the 32-bit single precision floating-point range. Set by the user.
fltIncrMax	float_t	The maximum value of the flex s-ramp increment. The data value is in the 32-bit single precision floating-point range. Set by the user.
fltXT1	float_t	The flex s-ramp value of the point where the increment must stop incrementing. Controlled by the GFLIB_FlexSRampCalcIncr_FLT algorithm.
fltXT2	float_t	The flex s-ramp value of the point where the increment must start decrementing. Controlled by the GFLIB_FlexSRampCalcIncr_FLT algorithm.
fltDA	float_t	The acceleration derivative. The data value (in acceleration change per second or ramp output value change per square second) is in the range $<0 ; 1$ ). Set by the user.
u16AccState	uint_16_t	The acceleration state of the function: 0 - acceleration rises; 1 - acceleration is constant; 2 - acceleration falls. Controlled by the GFLIB_FlexSRamp_FLT algorithm. It is reset to zero by the GFLIB_FlexSRampInit_FLT and GFLIB_FlexSRampCalcIncr_FLT algorithms.
bReachFlag	bool_t	The reach flag. This flag is controlled by the GFLIB_FlexSRamp_FLT algorithm. It is cleared by the GFLIB_FlexSRampInit_FLT and GFLIB_FlexSRampCalcIncr_FLT algorithms.

## 2.21.4 Declaration

The available GFLIB\_FlexSRampInit functions have the following declarations:

```
void GFLIB_FlexSRampInit_F16(frac16_t f16InitVal, GFLIB_FLEXSRAMP_T_F32 *psParam)
void GFLIB_FlexSRampInit_FLT(float_t fltInitVal, GFLIB_FLEXSRAMP_T_FLT *psParam)
```

The available GFLIB\_FlexSRampCalcIncr functions have the following declarations:

```
bool_t GFLIB_FlexSRampCalcIncr_F16(frac16_t f16Target, acc32_t a32Duration,
GFLIB_FLEXSRAMP_T_F32 *psParam)
bool_t GFLIB_FlexSRampCalcIncr_FLT(float_t fltTarget, float_t fltDuration,
GFLIB_FLEXSRAMP_T_FLT *psParam)
```

The available GFLIB\_FlexSRamp functions have the following declarations:

```
frac16_t GFLIB_FlexSRamp_F16(GFLIB_FLEXSRAMP_T_F32 *psParam)
float_t GFLIB_FlexSRamp_FLT(GFLIB_FLEXSRAMP_T_FLT *psParam)
```

## 2.21.5 Function use

The use of the GFLIB\_FlexSRampInit, GFLIB\_FlexRampSCalcIncr, and GFLIB\_FlexSRamp functions is shown in the following example:

A ramp with a profile as in [Figure 2-15](#) is generated. The ramp must change the speed from 100 RPM to 900 RPM in 20 s. The speed scale is 5000 RPM. The ramp must change the speed in 20 s. The acceleration derivative is  $15 \text{ RPM} / \text{s}^2$ . The sample time is 0.1 s. The maximum acceleration is  $50 \text{ RPM} / \text{s}$ .

```

#include "gflib.h"

static frac16_t f16InitVal;
static GFLIB_FLEXSRAMP_T_F32 sFlexSRamp;
static frac16_t f16Target, f16RampResult;
static acc32_t a32RampDuration;
static bool_t bFlexSRampFlag;

void Isr(void);

void main(void)
{
    /* Control loop period is 0.1 s */
    sFlexSRamp.f32Ts = FRAC32(0.1);

    /* Maximum increment value is 50 RPM / s */
    sFlexSRamp.f32IncrMax = FRAC32(50.0 / 5000.0 * 0.1);

    /* Desired acceleration derivative 15 RPM / s ^ 2 */
    sFlexSRamp.f16DA = FRAC16(15.0 / 5000.0);

    /* Initial value to 100 RPM */
    f16InitVal = FRAC16(100.0 / 5000.0);

    /* Flex ramp initialization */
    GFLIB_FlexSRampInit_F16(f16InitVal, &sFlexSRamp);

    /* Target value is 900 RPM in duration of 20 s */
    f16Target = FRAC16(900.0 / 5000.0);
    a32RampDuration = ACC32(20.0);

    /* Flex s-ramp parameters calculation */
    bFlexSRampFlag = GFLIB_FlexSRampCalcIncr_F16(f16Target, a32RampDuration, &sFlexSRamp);
}

/* periodically called control loop with a period of 100 ms */
void Isr()
{
    f16RampResult = GFLIB_FlexSRamp_F16(&sFlexSRamp);
}

```

## 2.22 GFLIB\_Integrator

The [GFLIB\\_Integrator](#) function calculates a discrete implementation of the integrator (sum), discretized using a trapezoidal rule in Tustin's method (bi-linear transformation).

The continuous time domain representation of the integrator is defined as follows:

$$u(t) = \int e(t) dt$$

**Equation 38.**

In a continuous time domain, the transfer function for this integrator is described using the Laplace transformation as follows:



$$H(s) = \frac{U(s)}{E(s)} = \frac{1}{s}$$

**Equation 39.**

Transforming the above equation into a digital time domain using the bi-linear transformation leads to the following transfer function:

$$Z\{H(s)\} = \frac{U(z)}{E(z)} = \frac{T_s + T_s z^{-1}}{2 - 2z^{-1}}$$

**Equation 40.**

where  $T_s$  is the sampling period of the system. The discrete implementation of the digital transfer function in the above equation is expressed as follows:

$$u(k) = u(k-1) + e(k) \frac{T_s}{2} + e(k-1) \frac{T_s}{2}$$

**Equation 41.**

Considering integrator gain  $K_I$ , the transfer function leads to the following equation:

$$u_I(k) = u_I(k-1) + e(k) \cdot \frac{K_I T_s}{2} + e(k-1) \frac{K_I T_s}{2}$$

**Equation 42.**

where:

- $u_I(k)$  is the integrator's output in the actual step
- $u_I(k-1)$  is the integrator's output from the previous step
- $e(k)$  is the integrator's input in the actual step
- $e(k-1)$  is the integrator's input from the previous step
- $K_I$  is the integrator's gain coefficient
- $T_s$  is the sampling period of the system

[Equation 42 on page 97](#) can be used in the fractional arithmetic as follows:

$$u_{Isc}(k) \cdot u_{max} = u_{Isc}(k-1) \cdot u_{max} + K_I T_s \cdot \frac{e_{sc}(k) + e_{sc}(k-1)}{2} \cdot e_{max}$$

**Equation 43.**

where:

- $u_{max}$  is the integrator output scale
- $u_{Isc}(k)$  is the scaled integrator output in the actual step
- $u_{Isc}(k-1)$  is the scaled integrator output from the previous step
- $e_{max}$  is the integrator input scale
- $e_{sc}(k)$  is the scaled integrator input in the actual step
- $e_{sc}(k-1)$  is the scaled integrator input in the previous step

For a proper use of this function, it is recommended to initialize the function's data by the GFLIB\_IntegratorInit functions, before using the [GFLIB\\_Integrator](#) function. You must call the init function when you want the integrator to be initialized.

## 2.22.1 Available versions

This function is available in the following versions:

- Fractional output - the output is the fractional portion of the result, the result is within the range  $<-1 ; 1)$ , and it may overflow. The parameters use the accumulator types.
- Floating-point output - the output is the floating-point result within the type's full range, with defined upper and lower limits. The result may overflow from one limit to the other.

The available versions of the GFLIB\_IntegratorInit function are shown in the following table:

**Table 2-30. Init function versions**

Function name	Input type	Parameters	Result type	Description
GFLIB_IntegratorInit_F16	<a href="#">frac16_t</a>	<a href="#">GFLIB_INTEGRATOR_T_A32</a> *	void	The inputs are a 16-bit fractional initial value and a pointer to the integrator parameters' structure.
GFLIB_IntegratorInit_FLT	<a href="#">float_t</a>	<a href="#">GFLIB_INTEGRATOR_T_FLT</a> *	void	The inputs are a 32-bit single precision floating-point initial value and a pointer to the integrator parameters' structure.

The available versions of the [GFLIB\\_Integrator](#) function are shown in the following table:

**Table 2-31. Function versions**

Function name	Input type	Parameters	Result type	Description
GFLIB_Integrator_F16	<a href="#">frac16_t</a>	<a href="#">GFLIB_INTEGRATOR_T_A32</a> *	<a href="#">frac16_t</a>	The inputs are a 16-bit fractional value to be integrated and a pointer to the integrator parameters' structure. The output is limited to range $<-1 ; 1>$ . When the integrator reaches the limit, it overflows to the other limit.
GFLIB_Integrator_FLT	<a href="#">float_t</a>	<a href="#">GFLIB_INTEGRATOR_T_FLT</a> *	<a href="#">float_t</a>	The inputs are a 32-bit single precision floating-point value to be integrated and a pointer to the integrator parameters' structure. The

Table 2-31. Function versions

Function name	Input type	Parameters	Result type	Description
				output is limited to range <fltLowerLim ; fltUpperLim>. When the integrator reaches the limit, it overflows to the other limit.

## 2.22.2 GFLIB\_INTEGRATOR\_T\_A32

Variable name	Input type	Description
a32Gain	acc32_t	Integrator gain is set up according to <a href="#">Equation 43 on page 97</a> as follows: $K_I T_s \cdot \frac{e_{max}}{u_{max}}$ The parameter is a 32-bit accumulator type within the range <-65536.0 ; 65536.0>. Set by the user.
f32IAccK_1	frac32_t	Integral portion in the step k - 1. Controlled by the algorithm.
f16InValK_1	frac16_t	Input value in the step k - 1. Controlled by the algorithm.

## 2.22.3 GFLIB\_INTEGRATOR\_T\_FLT

Variable name	Input type	Description
fltGain	float_t	Integrator gain is set up according to <a href="#">Equation 42 on page 97</a> as $K_I T_s$ . The parameter is a 32-bit single precision floating-point type within the full range. Set by the user.
fltIAccK_1	float_t	Integral portion in the step k - 1. Controlled by the algorithm.
fltInValK_1	float_t	Input value in the step k - 1. Controlled by the algorithm.
fltUpperLim	float_t	Upper limit. This parameter must be greater than fltLowerLim. Set by the user.
fltLowerLim	float_t	Lower limit. This parameter must be lower than fltUpperLim. Set by the user.

## 2.22.4 Declaration

The available GFLIB\_IntegratorInit functions have the following declarations:

```
void GFLIB_IntegratorInit_F16(frac16_t f16InitVal, GFLIB_INTEGRATOR_T_A32 *psParam)
void GFLIB_IntegratorInit_FLT(float_t fltInitVal, GFLIB_INTEGRATOR_T_FLT *psParam)
```

The available [GFLIB\\_Integrator](#) functions have the following declarations:

```
frac16_t GFLIB_Integrator_F16(frac16_t f16InVal, GFLIB_INTEGRATOR_T_A32 *psParam)
float_t GFLIB_Integrator_FLT(float_t fltInVal, GFLIB_INTEGRATOR_T_FLT *psParam)
```

## 2.22.5 Function use

The use of the GFLIB\_IntegratorInit and [GFLIB\\_Integrator](#) functions is shown in the following example:

```
#include "gflib.h"

static frac16_t f16Result, f16InVal, f16InitVal;
static GFLIB_INTEGRATOR_T_A32 sParam;

void Isr(void);

void main(void)
{
    f16InVal = FRAC16(-0.4);
    sParam.a32Gain = ACC32(0.1);

    f16InitVal = FRAC16(0.1);

    GFLIB_IntegratorInit_F16(f16InitVal, &sParam);
}

/* periodically called function */
void Isr()
{
    f16Result = GFLIB_Integrator_F16(f16InVal, &sParam);
}
```

## 2.23 GFLIB\_CtrlPIpAW

The [GFLIB\\_CtrlPIpAW](#) function calculates the parallel form of the Proportional-Integral (PI) controller with implemented integral anti-windup functionality.

The PI controller attempts to correct the error between the measured process variable and the desired set-point by calculating a corrective action that can adjust the process accordingly. The [GFLIB\\_CtrlPIpAW](#) function calculates the PI algorithm according to the equations below. The PI algorithm is implemented in the parallel (non-interacting) form, allowing the user to define the P and I parameters independently and without interaction. The controller output is limited and the limit values (upper limit and lower limit) are defined by the user.

The PI controller algorithm also returns a limitation flag, which indicates that the controller's output is at the limit. If the PI controller output reaches the upper or lower limit, then the limit flag is set to 1, otherwise it is 0 (integer values).

An anti-windup strategy is implemented by limiting the integral portion. The integral state is limited by the controller limits in the same way as the controller output. The integration can be stopped by a flag that is pointed to by the function's API.

The PI algorithm in the continuous time domain can be expressed as follows:

$$u(t) = e(t) \cdot K_P + K_I \int e(t) dt$$

**Equation 44.**

where:

- $u(t)$  is the controller output in the continuous time domain
- $e(t)$  is the input error in the continuous time domain
- $K_P$  is the proportional gain
- $K_I$  is the integral gain

[Equation 44 on page 101](#) can be expressed using the Laplace transformation as follows:

$$H(s) = \frac{U(s)}{E(s)} = K_P + \frac{K_I}{s}$$

**Equation 45.**

The proportional part ( $u_P$ ) of [Equation 44 on page 101](#) is transformed into the discrete time domain as follows:

$$u_P(k) = K_P \cdot e(k)$$

**Equation 46.**

where:

- $u_P(k)$  is the proportional action in the actual step
- $e(k)$  is the error in the actual step
- $K_P$  is the proportional gain coefficient

[Equation 46 on page 101](#) can be used in the fractional arithmetic as follows:

$$u_{Psc}(k) \cdot u_{max} = K_P \cdot e_{sc}(k) \cdot e_{max}$$

**Equation 47.**

where:

- $u_{max}$  is the action output scale
- $u_{Psc}(k)$  is the scaled proportional action in the actual step
- $e_{max}$  is the error input scale
- $e_{sc}(k)$  is the scale error in the actual step

Transforming the integral part ( $u_I$ ) of [Equation 44 on page 101](#) into a discrete time domain using the bi-linear method, also known as the trapezoidal approximation, is as follows:

$$u_I(k) = u_I(k-1) + e(k) \cdot \frac{K_I T_s}{2} + e(k-1) \frac{K_I T_s}{2}$$

**Equation 48.**

where:

- $u_I(k)$  is the integral action in the actual step
- $u_I(k-1)$  is the integral action from the previous step
- $e(k)$  is the error in the actual step
- $e(k-1)$  is the error in the previous step
- $T_s$  is the sampling period of the system
- $K_I$  is the integral gain coefficient

[Equation 48 on page 102](#) can be used in the fractional arithmetic as follows:

$$u_{Isc}(k) \cdot u_{max} = u_{Isc}(k-1) \cdot u_{max} + K_I T_s \cdot \frac{e_{sc}(k) + e_{sc}(k-1)}{2} \cdot e_{max}$$

**Equation 49.**

where:

- $u_{max}$  is the action output scale
- $u_{Isc}(k)$  is the scaled integral action in the actual step
- $u_{Isc}(k-1)$  is the scaled integral action from the previous step
- $e_{max}$  is the error input scale
- $e_{sc}(k)$  is the scaled error in the actual step
- $e_{sc}(k-1)$  is the scaled error in the previous step

The output signal limitation is implemented in this controller. The actual output  $u(k)$  is bounded not to exceed the given limit values UpperLimit and LowerLimit. This is due to either the bounded power of the actuator or due to the physical constraints of the plant.

$$u(k) = \begin{cases} UpperLimit & u(k) \geq UpperLimit \\ LowerLimit & u(k) \leq LowerLimit \\ u(k) & else \end{cases}$$

**Equation 50.**

The bounds are described by a limitation element, as shown in [Equation 50 on page 102](#). When the bounds are exceeded, the nonlinear saturation characteristic will take effect and influence the dynamic behavior. The described limitation is implemented on the integral

part accumulator (limitation during the calculation) and on the overall controller output. Therefore, if the limitation occurs, the controller output is clipped to its bounds, and the wind-up occurrence of the accumulator portion is avoided by saturating the actual sum.

For a proper use of this function, it is recommended to initialize the function data by the GFLIB\_CtrlPIpAInit functions, before using the [GFLIB\\_CtrlPIpAW](#) function. You must call this function when you want the PI controller to be initialized.

## 2.23.1 Available versions

This function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range  $<-1 ; 1)$ . The parameters use the accumulator types.
- Floating-point output - the output is the floating-point result within the type's full range.

The available versions of the GFLIB\_CtrlPIpAInit function are shown in the following table:

**Table 2-32. Init function versions**

Function name	Input type	Parameters	Result type	Description
GFLIB_CtrlPIpAInit_F16	<a href="#">frac16_t</a>	<a href="#">GFLIB_CTRL_PI_P_AW_T_A32</a> *	void	The inputs are a 16-bit fractional initial value and a pointer to the controller's parameters structure.
GFLIB_CtrlPIpAInit_FLT	<a href="#">float_t</a>	<a href="#">GFLIB_CTRL_PI_P_AW_T_FLT</a> *	void	The inputs are a 32-bit single precision floating-point initial value and a pointer to the controller's parameters structure.

The available versions of the [GFLIB\\_CtrlPIpAW](#) function are shown in the following table:

**Table 2-33. Function versions**

Function name	Input type		Parameters	Result type
	Error	Stop flag		
GFLIB_CtrlPIpAW_F16	<a href="#">frac16_t</a>	<a href="#">bool_t</a> *	<a href="#">GFLIB_CTRL_PI_P_AW_T_A32</a> *	<a href="#">frac16_t</a>
The error input is a 16-bit fractional value within the range $<-1 ; 1)$ . The integration of the PI controller is suspended if the stop flag is set. When it is cleared, the integration continues. The parameters are pointed to by an input pointer. The function returns a 16-bit fractional value in the range $<f16LowerLim ; f16UpperLim>$ .				

*Table continues on the next page...*

**Table 2-33. Function versions (continued)**

Function name	Input type		Parameters	Result type
	Error	Stop flag		
GFLIB_CtrlPipAW_FLT	float_t	bool_t *	GFLIB_CTRL_PI_P_AW_T_FLT *	float_t
The error input is a 32-bit single precision floating-point value within the full type's range. The integration of the PI controller is suspended if the stop flag is set. When it is cleared, the integration continues. The parameters are pointed to by an input pointer. The function returns a 32-bit single precision floating-point value in the range <fltLowerLim ; fltUpperLim>.				

## 2.23.2 GFLIB\_CTRL\_PI\_P\_AW\_T\_A32

Variable name	Input type	Description
a32PGain	acc32_t	Proportional gain is set up according to <a href="#">Equation 47 on page 101</a> as follows: $K_P \cdot \frac{e_{max}}{u_{max}}$ The parameter is a 32-bit accumulator type within the range <0 ; 65536.0>. Set by the user.
a32IGain	acc32_t	Integral gain is set up according to <a href="#">Equation 49 on page 102</a> as follows: $K_I T_s \cdot \frac{e_{max}}{u_{max}}$ The parameter is a 32-bit accumulator type within the range <0 ; 65536.0>. Set by the user.
f32IAccK_1	frac32_t	State variable of the internal accumulator (integrator). Controlled by the algorithm.
f16InErrK_1	frac16_t	Input error at the step k - 1. Controlled by the algorithm.
f16UpperLim	frac16_t	Upper limit of the controller's output and the internal accumulator (integrator). This parameter must be greater than f16LowerLim. Set by the user.
f16LowerLim	frac16_t	Lower limit of the controller's output and the internal accumulator (integrator). This parameter must be lower than f16UpperLim. Set by the user.
bLimFlag	bool_t	Limitation flag, which identifies that the controller's output reached the limits. 1 - the limit is reached; 0 - the output is within the limits. Controlled by the application.

## 2.23.3 GFLIB\_CTRL\_PI\_P\_AW\_T\_FLT

Variable name	Input type	Description
fltPGain	float_t	Proportional gain is set up according to <a href="#">Equation 46 on page 101</a> as $K_P$ . The parameter is a 32-bit single precision floating-point type non-negative value. Set by the user.
fltIGain	float_t	Integral gain is set up according to <a href="#">Equation 48 on page 102</a> as $K_I T_s$ . The parameter is a 32-bit single precision floating-point type non-negative value. Set by the user.

Table continues on the next page...



Variable name	Input type	Description
fltAccK_1	float_t	State variable of the internal accumulator (integrator). Controlled by the algorithm.
fltInErrK_1	float_t	Input error at the step k - 1. Controlled by the algorithm.
fltUpperLim	float_t	Upper limit of the controller's output and the internal accumulator (integrator). This parameter must be greater than fltLowerLim. Set by the user.
fltLowerLim	float_t	Lower limit of the controller's output and the internal accumulator (integrator). This parameter must be lower than fltUpperLim. Set by the user.
bLimFlag	bool_t	Limitation flag, which identifies that the controller's output reached the limits. 1 - the limit is reached; 0 - the output is within the limits. Controlled by the application.

## 2.23.4 Declaration

The available GFLIB\_CtrlPIpAWInit functions have the following declarations:

```
void GFLIB_CtrlPIpAWInit_F16(frac16_t f16InitVal, GFLIB_CTRL_PI_P_AW_T_A32 *psParam)
void GFLIB_CtrlPIpAWInit_FLT(float_t fltInitVal, GFLIB_CTRL_PI_P_AW_T_FLT *psParam)
```

The available GFLIB\_CtrlPIpAW functions have the following declarations:

```
frac16_t GFLIB_CtrlPIpAW_F16(frac16_t f16InErr, const bool_t *pbStopIntegFlag,
GFLIB_CTRL_PI_P_AW_T_A32 *psParam)
float_t GFLIB_CtrlPIpAW_FLT(float_t fltInErr, const bool_t *pbStopIntegFlag,
GFLIB_CTRL_PI_P_AW_T_FLT *psParam)
```

## 2.23.5 Function use

The use of the GFLIB\_CtrlPIpAWInit and GFLIB\_CtrlPIpAW functions is shown in the following example:

```
#include "gflib.h"

static frac16_t f16Result, f16InitVal, f16InErr;
static bool_t bStopIntegFlag;
static GFLIB_CTRL_PI_P_AW_T_A32 sParam;

void Isr(void);

void main(void)
{
    f16InErr = FRAC16(-0.4);
    sParam.a32PGain = ACC32(0.1);
    sParam.a32IGain = ACC32(0.2);
    sParam.f16UpperLim = FRAC16(0.9);
    sParam.f16LowerLim = FRAC16(-0.9);
    bStopIntegFlag = FALSE;

    f16InitVal = FRAC16(0.0);

    GFLIB_CtrlPIpAWInit_F16(f16InitVal, &sParam);
}
```

```

/* periodically called function */
void Isr()
{
    f16Result = GFLIB_CtrlPIpAW_F16(f16InErr, &bStopIntegFlag, &sParam);
}

```

## 2.24 GFLIB\_CtrlPIDpAW

The [GFLIB\\_CtrlPIDpAW](#) function calculates the parallel form of the Proportional-Integral-Derivative (PID) controller with implemented integral anti-windup functionality.

The PID controller attempts to correct the error between the measured process variable and the desired set-point by calculating a corrective action that can adjust the process accordingly. The [GFLIB\\_CtrlPIDpAW](#) function calculates the PID algorithm according to the equations below. The PID algorithm is implemented in the parallel (non-interacting) form, allowing the user to define the P, I, and D parameters independently and without interaction. The controller output is limited, and the limit values (upper limit and lower limit) are defined by the user.

The algorithm has two error inputs: one for the P and I calculation, and the other for the D calculation. This allows the user to apply different filters on both inputs.

The PID controller algorithm also returns a limitation flag, which indicates that the controller's output is at the limit. If the PID controller output reaches the upper or lower limit, then the limit flag is set to 1, otherwise it is 0 (integer values).

An anti-windup strategy is implemented by limiting the integral portion. The integral state is limited by the controller limits in the same way as the controller output. The integration can be stopped by a flag, which is pointed to by the function's API.

The PID algorithm in the continuous time domain can be expressed as follows:

$$u(t) = e(t) \cdot K_P + K_I \int e(t) dt + K_D \frac{d}{dt} e_D(t)$$

**Equation 51.**

where

- $u(t)$  is the controller output in the continuous time domain
- $e(t)$  is the input error for the proportional and integral calculation in the continuous time domain
- $e_D(t)$  is the input error for the derivative calculation in the continuous time domain
- $K_P$  is the proportional gain
- $K_I$  is the integral gain
- $K_D$  is the derivative gain

Equation 51 on page 106 can be expressed using the Laplace transformation as follows:

$$H(s) = \frac{U(s)}{E(s)} = K_P + \frac{K_I}{s} + K_d \cdot s$$

**Equation 52.**

The proportional part ( $u_P$ ) of Equation 52 on page 107 is transformed into the discrete time domain as follows:

$$u_P(k) = K_P \cdot e(k)$$

**Equation 53.**

where:

- $u_P(k)$  is the proportional action in the actual step
- $e(k)$  is the error in the actual step
- $K_P$  is the proportional gain coefficient

Equation 53 on page 107 can be used in the fractional arithmetic as follows:

$$u_{Psc}(k) \cdot u_{max} = K_P \cdot e_{sc}(k) \cdot e_{max}$$

**Equation 54.**

where:

- $u_{max}$  is the action output scale
- $u_{Psc}(k)$  is the scaled proportional action in the actual step
- $e_{max}$  is the error input scale
- $e_{sc}(k)$  is the scale error in the actual step

Transforming the integral part ( $u_I$ ) of Equation 52 on page 107 into a discrete time domain using the bi-linear method, also known as the trapezoidal approximation, is as follows:

$$u_I(k) = u_I(k-1) + e(k) \cdot \frac{K_I T_s}{2} + e(k-1) \cdot \frac{K_I T_s}{2}$$

**Equation 55.**

where:

- $u_I(k)$  is the integral action in the actual step
- $u_I(k-1)$  is the integral action from the previous step
- $e(k)$  is the error in the actual step
- $e(k-1)$  is the error in the previous step
- $T_s$  is the sampling period of the system
- $K_I$  is the integral gain coefficient

[Equation 55 on page 107](#) can be used in the fractional arithmetic as follows:

$$u_{Isc}(k) \cdot u_{max} = u_{Isc}(k-1) \cdot u_{max} + K_I T_s \cdot \frac{e_{sc}(k) + e_{sc}(k-1)}{2} \cdot e_{max}$$

**Equation 56.**

where:

- $u_{max}$  is the action output scale
- $u_{Isc}(k)$  is the scaled integral action in the actual step
- $u_{Isc}(k-1)$  is the scaled integral action from the previous step
- $e_{max}$  is the error input scale
- $e_{sc}(k)$  is the scaled error in the actual step
- $e_{sc}(k-1)$  is the scaled error in the previous step

The derivative part ( $u_D$ ) of [Equation 51 on page 106](#) is transformed into the discrete time domain as follows:

$$u_D(k) = \frac{K_D}{T_s} \cdot [e_D(k) - e_D(k-1)]$$

**Equation 57.**

where:

- $u_D(k)$  is the proportional action in the actual step
- $e_D(k)$  is the error used for the derivative input in the actual step
- $e_D(k-1)$  is the error used for the derivative input in the previous step
- $K_D$  is the proportional gain coefficient

[Equation 53 on page 107](#) can be used in the fractional arithmetic as follows:

$$u_{Dsc}(k) \cdot u_{max} = \frac{K_D}{T_s} \cdot [e_{Dsc}(k) - e_{Dsc}(k-1)] \cdot e_{max}$$

**Equation 58.**

where:

- $u_{max}$  is the action output scale
- $u_{Dsc}(k)$  is the scaled derivative action in the actual step
- $e_{max}$  is the error input scale
- $e_{Dsc}(k)$  is the scaled error for the derivative input in the actual step
- $e_{Dsc}(k-1)$  is the scaled error for the derivative input in the previous step

The output signal limitation is implemented in this controller. The actual output  $u(k)$  is bounded to not exceed the given limit values - UpperLimit and LowerLimit. This is due to either the bounded power of the actuator, or due to the physical constraints of the plant.

$$u(k) = \begin{cases} UpperLimit & u(k) \geq UpperLimit \\ LowerLimit & u(k) \leq LowerLimit \\ u(k) & else \end{cases}$$

**Equation 59.**

The bounds are described by a limitation element, as shown in [Equation 59 on page 109](#). When the bounds are exceeded, the non-linear saturation characteristic will take effect, and influence the dynamic behavior. The described limitation is implemented in the integral part accumulator (limitation during the calculation) and in the overall controller output. Therefore, if the limitation occurs, the controller output is clipped to its bounds, and the wind-up occurrence of the accumulator portion is avoided by saturating the actual sum.

For a proper use of this function, it is recommended to initialize the function data by the GFLIB\_CtrlPIDpAWInit functions, before using the [GFLIB\\_CtrlPIDpAW](#) function. You must call this function, when you want the PID controller to be initialized.

### 2.24.1 Available versions

This function is available in the following versions:

- Fractional output - the output is the fractional portion of the result; the result is within the range <-1 ; 1). The parameters use the accumulator types.
- Floating-point output - the output is the floating-point result within the type's full range.

The available versions of the GFLIB\_CtrlPIDpAWInit function are shown in the following table:

**Table 2-34. Init function versions**

Function name	Input type	Parameters	Result type	Description
GFLIB_CtrlPIDpAWInit_F16	<a href="#">frac16_t</a>	<a href="#">GFLIB_CTRL_PID_P_AW_T_A32</a> *	void	The inputs are a 16-bit fractional initial value and a pointer to the controller's parameters structure.
GFLIB_CtrlPIDpAWInit_FLT	<a href="#">float_t</a>	<a href="#">GFLIB_CTRL_PID_P_AW_T_FLT</a> *	void	The inputs are a 32-bit single precision floating-point initial value and a pointer to the controller's parameters structure.

The available versions of the [GFLIB\\_CtrlPIDpAW](#) function are shown in the following table:

**Table 2-35. Function versions**

Function name	Input type			Parameters	Result type
	PI error	D error	Stop flag		
GFLIB_CtrlPIDpAW_F16	<a href="#">frac16_t</a>	<a href="#">frac16_t</a>	<a href="#">bool_t</a> *	<a href="#">GFLIB_CTRL_PID_P_AW_T_A32</a> *	<a href="#">frac16_t</a>
	The error inputs are 16-bit fractional values within the range <-1 ; 1>. The integration of the PID controller is suspended if the stop flag is set. When it is cleared, the integration continues. The parameters are pointed to by an input pointer. The function returns a 16-bit fractional value in the range <f16LowerLim ; f16UpperLim>.				
GFLIB_CtrlPIDpAW_FLT	<a href="#">float_t</a>	<a href="#">float_t</a>	<a href="#">bool_t</a> *	<a href="#">GFLIB_CTRL_PID_P_AW_T_FLT</a> *	<a href="#">float_t</a>
	The error inputs are 32-bit single precision floating-point values within the full type's range. The integration of the PID controller is suspended if the stop flag is set. When it is cleared, the integration continues. The parameters are pointed to by an input pointer. The function returns a 32-bit single precision floating-point value in the range <fltLowerLim ; fltUpperLim>.				

## 2.24.2 GFLIB\_CTRL\_PID\_P\_AW\_T\_A32

Variable name	Input type	Description
a32PGain	<a href="#">acc32_t</a>	Proportional gain is set up according to <a href="#">Equation 54 on page 107</a> as follows: $K_P \cdot \frac{e_{max}}{u_{max}}$ The parameter is a 32-bit accumulator type within the range <0 ; 65536.0>. Set by the user.
a32IGain	<a href="#">acc32_t</a>	Integral gain is set up according to <a href="#">Equation 56 on page 108</a> as follows: $K_I T_s \cdot \frac{e_{max}}{u_{max}}$ The parameter is a 32-bit accumulator type within the range <0 ; 65536.0>. Set by the user.
a32DGain	<a href="#">acc32_t</a>	Derivative gain is set up according to <a href="#">Equation 58 on page 108</a> as follows: $\frac{K_D}{T_s} \cdot \frac{e_{max}}{u_{max}}$ The parameter is a 32-bit accumulator type within the range <0 ; 65536.0>. Set by the user.
f32IAccK_1	<a href="#">frac32_t</a>	State variable of the internal accumulator (integrator). Controlled by the algorithm.
f16InErrK_1	<a href="#">frac16_t</a>	Input error in the step k - 1. Controlled by the algorithm.
f16UpperLim	<a href="#">frac16_t</a>	Upper limit of the controller's output and the internal accumulator (integrator). This parameter must be greater than f16LowerLim. Set by the user.
f16LowerLim	<a href="#">frac16_t</a>	Lower limit of the controller's output and the internal accumulator (integrator). This parameter must be lower than f16UpperLim. Set by the user.
f16InErrDK_1	<a href="#">frac16_t</a>	Input error for the derivative calculation in the step k - 1. Controlled by the algorithm.
bLimFlag	<a href="#">bool_t</a>	Limitation flag, which identifies that the controller's output reached the limits. 1 - the limit is reached; 0 - the output is within the limits. Controlled by the application.

### 2.24.3 GFLIB\_CTRL\_PID\_P\_AW\_T\_FLT

Variable name	Input type	Description
fltPGain	float_t	Proportional gain is set up according to <a href="#">Equation 53 on page 107</a> as $K_P$ . The parameter is a 32-bit single precision floating-point type non-negative value. Set by the user.
fltIGain	float_t	Integral gain is set up according to <a href="#">Equation 55 on page 107</a> as $K_I T_s$ . The parameter is a 32-bit single precision floating-point type non-negative value. Set by the user.
fltDGain	float_t	Derivative gain is set up according to <a href="#">Equation 57 on page 108</a> as $K_D / T_s$ . The parameter is a 32-bit single precision floating-point type non-negative value. Set by the user.
fltAccK_1	float_t	State variable of the internal accumulator (integrator). Controlled by the algorithm.
fltInErrK_1	float_t	Input error in the step $k - 1$ . Controlled by the algorithm.
fltUpperLim	float_t	Upper limit of the controller's output and the internal accumulator (integrator). This parameter must be greater than fltLowerLim. Set by the user.
fltLowerLim	float_t	Lower limit of the controller's output and the internal accumulator (integrator). This parameter must be lower than fltUpperLim. Set by the user.
fltInErrDK_1	float_t	Input error for the derivative calculation in the step $k - 1$ . Controlled by the algorithm.
bLimFlag	bool_t	Limitation flag, which identifies that the controller's output reached the limits. 1 - the limit is reached; 0 - the output is within the limits. Controlled by the application.

### 2.24.4 Declaration

The available GFLIB\_CtrlPIDpAWInit functions have the following declarations:

```
void GFLIB_CtrlPIDpAWInit_F16(frac16_t f16InitVal, GFLIB_CTRL_PID_P_AW_T_A32 *psParam)
void GFLIB_CtrlPIDpAWInit_FLT(float_t fltInitVal, GFLIB_CTRL_PID_P_AW_T_FLT *psParam)
```

The available [GFLIB\\_CtrlPIDpAW](#) functions have the following declarations:

```
frac16_t GFLIB_CtrlPIDpAW_F16(frac16_t f16InErr, frac16_t f16InErrD, const bool_t
*pbStopIntegFlag, GFLIB_CTRL_PID_P_AW_T_A32 *psParam)
float_t GFLIB_CtrlPIDpAW_FLT(float_t fltInErr, float_t fltInErrD, const bool_t
*pbStopIntegFlag, GFLIB_CTRL_PID_P_AW_T_FLT *psParam)
```

### 2.24.5 Function use

The use of the GFLIB\_CtrlPIDpAWInit and [GFLIB\\_CtrlPIDpAW](#) functions is shown in the following example:

## GFLIB\_CtrlPIDpAW

```
#include "gflib.h"

static frac16_t f16Result, f16InitVal, f16InErr, f16InErrD;
static bool_t bStopIntegFlag;
static GFLIB_CTRL_PID_P_AW_T_A32 sParam;

void Isr(void);

void main(void)
{
    f16InErr = FRAC16(-0.4);
    f16InErr = f16InErrD;
    sParam.a32PGain = ACC32(0.1);
    sParam.a32IGain = ACC32(0.2);
    sParam.a32DGain = ACC32(0.001);
    sParam.f16UpperLim = FRAC16(0.9);
    sParam.f16LowerLim = FRAC16(-0.9);
    bStopIntegFlag = FALSE;

    f16InitVal = FRAC16(0.0);

    GFLIB_CtrlPIDpAWInit_F16(f16InitVal, &sParam);
}

/* periodically called function */
void Isr()
{
    f16Result = GFLIB_CtrlPIDpAW_F16(f16InErr, f16InErrD, &bStopIntegFlag, &sParam);
}
```



# Appendix A

## Library types

### A.1 bool\_t

The `bool_t` type is a logical 16-bit type. It is able to store the boolean variables with two states: TRUE (1) or FALSE (0). Its definition is as follows:

```
typedef unsigned short bool_t;
```

The following figure shows the way in which the data is stored by this type:

**Table A-1. Data storage**

	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
Value	Unused															Logical
TRUE	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1
	0				0				0				1			
FALSE	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	0				0				0				0			

To store a logical value as `bool_t`, use the `FALSE` or `TRUE` macros.

### A.2 uint8\_t

The `uint8_t` type is an unsigned 8-bit integer type. It is able to store the variables within the range <0 ; 255>. Its definition is as follows:

```
typedef unsigned char uint8_t;
```

The following figure shows the way in which the data is stored by this type:

Table A-2. Data storage

	7	6	5	4	3	2	1	0
Value	Integer							
255	1	1	1	1	1	1	1	1
	F				F			
11	0	0	0	0	1	0	1	1
	0				B			
124	0	1	1	1	1	1	0	0
	7				C			
159	1	0	0	1	1	1	1	1
	9				F			

A.3 uint16\_t

The [uint16\\_t](#) type is an unsigned 16-bit integer type. It is able to store the variables within the range <0 ; 65535>. Its definition is as follows:

```
typedef unsigned short uint16_t;
```

The following figure shows the way in which the data is stored by this type:

Table A-3. Data storage

	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
Value	Integer															
65535	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
	F				F				F				F			
5	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	1
	0				0				0				5			
15518	0	0	1	1	1	1	0	0	1	0	0	1	1	1	1	0
	3				C				9				E			
40768	1	0	0	1	1	1	1	1	0	1	0	0	0	0	0	0
	9				F				4				0			

A.4 uint32\_t

The `uint32_t` type is an unsigned 32-bit integer type. It is able to store the variables within the range  $\langle 0 ; 4294967295 \rangle$ . Its definition is as follows:

```
typedef unsigned long uint32_t;
```

The following figure shows the way in which the data is stored by this type:

**Table A-4. Data storage**

	31	24	23	16	15	8	7	0
Value	Integer							
4294967295	F	F	F	F	F	F	F	F
2147483648	8	0	0	0	0	0	0	0
55977296	0	3	5	6	2	5	5	0
3451051828	C	D	B	2	D	F	3	4

## A.5 uint64\_t

The `uint64_t` type is an unsigned 64-bit integer type. It is able to store the variables within the range  $\langle 0 ; 2^{64} - 1 \rangle$ . Its definition is as follows:

```
typedef unsigned long long uint64_t;
```

The following figure shows the way in which the data is stored by this type:

**Table A-5. Data storage**

	63	48	47	32	31	16	15	0
Value	Integer							
18446744073709551315	F F	F F	F F	F F	F F	F F	F E	D 3
9223372036854775808	8 0	0 0	0 0	0 0	0 0	0 0	0 0	0 0
5971730530807955574	5 2	D F	D 9	4 7	3 7	2 9	C 0	7 6
18080213425565777426	F A	E 9	D 2	5 1	4 6	1 8	B E	1 2

## A.6 int8\_t

The `int8_t` type is a signed 8-bit integer type. It is able to store the variables within the range  $\langle -128 ; 127 \rangle$ . Its definition is as follows:

```
typedef char int8_t;
```

The following figure shows the way in which the data is stored by this type:

**Table A-6. Data storage**

	7	6	5	4	3	2	1	0
Value	Sign	Integer						
127	0	1	1	1	1	1	1	1
	7				F			
-128	1	0	0	0	0	0	0	0
	8				0			
60	0	0	1	1	1	1	0	0
	3				C			
-97	1	0	0	1	1	1	1	1
	9				F			

## A.7 int16\_t

The `int16_t` type is a signed 16-bit integer type. It is able to store the variables within the range  $\langle -32768 ; 32767 \rangle$ . Its definition is as follows:

```
typedef short int16_t;
```

The following figure shows the way in which the data is stored by this type:

**Table A-7. Data storage**

	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
Value	Sign	Integer														
32767	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
	7				F				F				F			
-32768	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	8				0				0				0			
15518	0	0	1	1	1	1	0	0	1	0	0	1	1	1	1	0
	3				C				9				E			
-24768	1	0	0	1	1	1	1	1	0	1	0	0	0	0	0	0
	9				F				4				0			

## A.8 int32\_t

The `int32_t` type is a signed 32-bit integer type. It is able to store the variables within the range  $\langle -2147483648 ; 2147483647 \rangle$ . Its definition is as follows:

```
typedef long int32_t;
```

The following figure shows the way in which the data is stored by this type:

**Table A-8. Data storage**

	31	24	23	16	15	8	7	0
Value	S	Integer						
2147483647	7	F	F	F	F	F	F	F
-2147483648	8	0	0	0	0	0	0	0
55977296	0	3	5	6	2	5	5	0
-843915468	C	D	B	2	D	F	3	4

## A.9 int64\_t

The `int64_t` type is a signed 64-bit integer type. It is able to store the variables within the range  $\langle -2^{63} ; 2^{63}-1 \rangle$ . Its definition is as follows:

```
typedef long long int64_t;
```

The following figure shows the way in which the data is stored by this type:

**Table A-9. Data storage**

	63	48	47	32	31	16	15	0
Value	S	Integer						
$2^{63}-1$	7	F	F	F	F	F	F	F
$-2^{63}$	8	0	0	0	0	0	0	0
5971730530807955574	5	2	D	F	D	9	4	7
-366530648143774190	F	A	E	9	D	2	5	1

A.10 frac8\_t

The `frac8_t` type is a signed 8-bit fractional type. It is able to store the variables within the range <-1 ; 1). Its definition is as follows:

```
typedef char frac8_t;
```

The following figure shows the way in which the data is stored by this type:

Table A-10. Data storage

	7	6	5	4	3	2	1	0
Value	Sign	Fractional						
0.99219	0	1	1	1	1	1	1	1
	7				F			
-1.0	1	0	0	0	0	0	0	0
	8				0			
0.46875	0	0	1	1	1	1	0	0
	3				C			
-0.75781	1	0	0	1	1	1	1	1
	9				F			

To store a real number as `frac8_t`, use the `FRAC8` macro.

A.11 frac16\_t

The `frac16_t` type is a signed 16-bit fractional type. It is able to store the variables within the range <-1 ; 1). Its definition is as follows:

```
typedef short frac16_t;
```

The following figure shows the way in which the data is stored by this type:

Table A-11. Data storage

	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
Value	Sign	Fractional														
0.99997	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
	7				F				F				F			
-1.0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Table continues on the next page...

**Table A-11. Data storage (continued)**

0.47357  -0.75586	8				0				0				0			
	0	0	1	1	1	1	0	0	1	0	0	1	1	1	1	0
	3				C				9				E			
	1	0	0	1	1	1	1	1	0	1	0	0	0	0	0	0
	9				F				4				0			

To store a real number as `frac16_t`, use the `FRAC16` macro.

## A.12 `frac32_t`

The `frac32_t` type is a signed 32-bit fractional type. It is able to store the variables within the range  $<-1 ; 1$ ). Its definition is as follows:

```
typedef long frac32_t;
```

The following figure shows the way in which the data is stored by this type:

**Table A-12. Data storage**

	31	24 23		16 15		8 7		0	
Value	S	Fractional							
0.9999999995	7	F	F	F	F	F	F	F	
-1.0	8	0	0	0	0	0	0	0	
0.02606645970	0	3	5	6	2	5	5	0	
-0.3929787632	C	D	B	2	D	F	3	4	

To store a real number as `frac32_t`, use the `FRAC32` macro.

## A.13 `acc16_t`

The `acc16_t` type is a signed 16-bit fractional type. It is able to store the variables within the range  $<-256 ; 256$ ). Its definition is as follows:

```
typedef short acc16_t;
```

The following figure shows the way in which the data is stored by this type:

**Table A-13. Data storage**

	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0	
Value	Sign	Integer								Fractional							
255.9921875	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
	7				F				F				F				
-256.0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	8				0				0				0				
1.0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	
	0				0				8				0				
-1.0	1	1	1	1	1	1	1	1	1	0	0	0	0	0	0	0	
	F				F				8				0				
13.7890625	0	0	0	0	0	1	1	0	1	1	1	0	0	1	0	1	
	0				6				E				5				
-89.71875	1	1	0	1	0	0	1	1	0	0	1	0	0	1	0	0	
	D				3				2				4				

To store a real number as `acc16_t`, use the `ACC16` macro.

## A.14 `acc32_t`

The `acc32_t` type is a signed 32-bit accumulator type. It is able to store the variables within the range <-65536 ; 65536). Its definition is as follows:

```
typedef long acc32_t;
```

The following figure shows the way in which the data is stored by this type:

**Table A-14. Data storage**

	31	24 23		16 15		8 7		0	
Value	S	Integer				Fractional			
65535.999969	7	F	F	F	F	F	F	F	
-65536.0	8	0	0	0	0	0	0	0	
1.0	0	0	0	0	8	0	0	0	
-1.0	F	F	F	F	8	0	0	0	
23.789734	0	0	0	B	E	5	1	6	
-1171.306793	F	D	B	6	5	8	B	C	

To store a real number as `acc32_t`, use the `ACC32` macro.



## A.15 float t

The `float_t` type is a signed 32-bit single precision floating-point type, defined by IEEE 754. It is able to store the full precision (normalized) finite variables within the range  $[-3.40282 \cdot 10^{38} ; 3.40282 \cdot 10^{38}]$  with the minimum resolution of  $2^{-23}$ . The smallest normalized number is  $\pm 1.17549 \cdot 10^{-38}$ . Nevertheless, the denormalized numbers (with reduced precision) reach yet lower values, from  $\pm 1.40130 \cdot 10^{-45}$  to  $\pm 1.17549 \cdot 10^{-38}$ . The standard also defines the additional values:

- Negative zero
- Infinity
- Negative infinity
- Not a number

The 32-bit type is composed of:

- Sign (bit 31)
- Exponent (bits 23 to 30)
- Mantissa (bits 0 to 22)

The conversion of the number is straightforward. The sign of the number is stored in bit 31. The binary exponent is decoded as an integer from bits 23 to 30 by subtracting 127. The mantissa (fraction) is stored in bits 0 to 22. An invisible leading bit (it is not actually stored) with value 1.0 is placed in front; therefore, bit 23 has a value of 0.5, bit 22 has a value 0.25, and so on. As a result, the mantissa has a value between 1.0 and 2. If the exponent reaches -127 (binary 00000000), the leading 1.0 is no longer used to enable the gradual underflow.

The `float_t` type definition is as follows:

```
typedef float float t;
```

The following figure shows the way in which the data is stored by this type:

**Table A-15. Data storage - normalized values**

	31	24 23							16 15							8 7							0																			
Value	S	Exponent							Mantissa																																	
$(2.0 - 2^{-23}) \cdot 2^{127}$	0	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1														
$\approx 3.40282 \cdot 10^{38}$	7							F							7							F							F							F						
$-(2.0 - 2^{-23}) \cdot 2^{127}$	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1														
$\approx -3.40282 \cdot 10^{38}$	F							F							7							F							F							F						

*Table continues on the next page...*

**Table A-15. Data storage - normalized values (continued)**

$2^{-126}$ $\approx 1.17549 \cdot 10^{-38}$	0	0 0 0 0 0 0 0 0 1	0 0
	0	0	8 0 0 0 0 0 0 0
$-2^{-126}$ $\approx -1.17549 \cdot 10^{-38}$	1	0 0 0 0 0 0 0 0 1	0 0
	8	0	8 0
1.0	0	0 1 1 1 1 1 1 1 1	0 0
	3	F	8 0
-1.0	1	0 1 1 1 1 1 1 1 1	0 0
	B	F	8 0
$\pi$ $\approx 3.1415927$	0	1 0 0 0 0 0 0 0 0	1 0 0 1 0 0 1 0 0 0 0 0 1 1 1 1 1 1 1 0 1 1 0 1 1 1 1 0 1 1 0 1 1
	4	0	4 9 0 F D B
-20810.086	1	1 0 0 0 1 1 0 1	0 1 0 0 0 1 0 1 0 0 1 0 1 0 0 0 0 1 0 1 0 1 1 0 0 0 0 1 0 1 1 0 0
	C	6	A 2 9 4 2 C

**Table A-16. Data storage - denormalized values**

	31	24 23	16 15	8 7	0																					
Value	S	Exponent	Mantissa																							
0.0	0	0 0 0 0 0 0 0 0	0 0																							
		0 0	0 0	0 0	0 0																					
-0.0	1	0 0 0 0 0 0 0 0	0 0																							
		8 0	0 0	0 0	0 0																					
$(1.0 - 2^{-23}) \cdot 2^{-126}$ $\approx 1.17549 \cdot 10^{-38}$	0	0 0 0 0 0 0 0 0	1 1																							
		0 0	7 F	F F	F F																					
$-(1.0 - 2^{-23}) \cdot 2^{-126}$ $\approx -1.17549 \cdot 10^{-38}$	1	0 0 0 0 0 0 0 0	1 1																							
		8 0	7 F	F F	F F																					
$2^{-1} \cdot 2^{-126}$ $\approx 5.87747 \cdot 10^{-39}$	0	0 0 0 0 0 0 0 0	1 0																							
		0 0	4 0	0 0	0 0																					
$-2^{-1} \cdot 2^{-126}$ $\approx -5.87747 \cdot 10^{-39}$	1	0 0 0 0 0 0 0 0	1 0																							
		8 0	4 0	0 0	0 0																					
$2^{-23} \cdot 2^{-126}$ $\approx 1.40130 \cdot 10^{-45}$	0	0 0 0 0 0 0 0 0	0 1																							
		0 0	0 0	0 0	0 1																					
$-2^{-23} \cdot 2^{-126}$ $\approx -1.40130 \cdot 10^{-45}$	1	0 0 0 0 0 0 0 0	0 1																							
		8 0	0 0	0 0	0 1																					

**Table A-17. Data storage - special values**

[illegible]

**A.16 FALSE**

The `FALSE` macro serves to write a correct value standing for the logical FALSE value of the `bool t` type. Its definition is as follows:

```
#define FALSE      ((bool_t)0)

#include "mlib.h"

static bool_t bVal;

void main(void)
{
    bVal = FALSE;                                /* bVal = FALSE */
}
```

**A.17 TRUE**

The `TRUE` macro serves to write a correct value standing for the logical TRUE value of the `bool_t` type. Its definition is as follows:

```
#define TRUE      ((bool_t)1)

#include "mlib.h"

static bool_t bVal;

void main(void)
{
    bVal = TRUE;                                /* bVal = TRUE */
}
```

## A.18 FRAC8

The **FRAC8** macro serves to convert a real number to the `frac8_t` type. Its definition is as follows:

```
#define FRAC8(x) ((frac8_t)((x) < 0.9921875 ? ((x) >= -1 ? (x)*0x80 : 0x80) : 0x7F))
```

The input is multiplied by 128 ( $=2^7$ ). The output is limited to the range `<0x80 ; 0x7F>`, which corresponds to `<-1.0 ; 1.0-2-7>`.

```
#include "mlib.h"

static frac8_t f8Val;

void main(void)
{
    f8Val = FRAC8(0.187);          /* f8Val = 0.187 */
}
```

## A.19 FRAC16

The **FRAC16** macro serves to convert a real number to the `frac16_t` type. Its definition is as follows:

```
#define FRAC16(x) ((frac16_t)((x) < 0.999969482421875 ? ((x) >= -1 ? (x)*0x8000 : 0x8000) : 0x7FFF))
```

The input is multiplied by 32768 ( $=2^{15}$ ). The output is limited to the range `<0x8000 ; 0x7FFF>`, which corresponds to `<-1.0 ; 1.0-2-15>`.

```
#include "mlib.h"

static frac16_t f16Val;

void main(void)
{
    f16Val = FRAC16(0.736);        /* f16Val = 0.736 */
}
```

## A.20 FRAC32

The **FRAC32** macro serves to convert a real number to the `frac32_t` type. Its definition is as follows:

```
#define FRAC32(x) ((frac32_t)((x) < 1 ? ((x) >= -1 ? (x)*0x80000000 : 0x80000000) : 0x7FFFFFFF))
```

The input is multiplied by 2147483648 ( $=2^{31}$ ). The output is limited to the range  $\langle 0x80000000 ; 0x7FFFFFFF \rangle$ , which corresponds to  $\langle -1.0 ; 1.0 \cdot 2^{-31} \rangle$ .

```
#include "mlib.h"

static frac32_t f32Val;

void main(void)
{
    f32Val = FRAC32(-0.1735667);          /* f32Val = -0.1735667 */
}
```

## A.21 ACC16

The **ACC16** macro serves to convert a real number to the `acc16_t` type. Its definition is as follows:

```
#define ACC16(x) ((acc16_t)((x) < 255.9921875 ? ((x) >= -256 ? (x)*0x80 : 0x8000) : 0x7FFF))
```

The input is multiplied by 128 ( $=2^7$ ). The output is limited to the range  $\langle 0x8000 ; 0x7FFF \rangle$  that corresponds to  $\langle -256.0 ; 255.9921875 \rangle$ .

```
#include "mlib.h"

static acc16_t a16Val;


void main(void)
{
    a16Val = ACC16(19.45627);          /* a16Val = 19.45627 */
}
```

## A.22 ACC32

The **ACC32** macro serves to convert a real number to the `acc32_t` type. Its definition is as follows:

```
#define ACC32(x) ((acc32_t)((x) < 65535.999969482421875 ? ((x) >= -65536 ? (x)*0x8000 : 0x80000000) : 0x7FFFFFFF))
```

The input is multiplied by 32768 ( $=2^{15}$ ). The output is limited to the range  $\langle 0x80000000 ; 0x7FFFFFFF \rangle$ , which corresponds to  $\langle -65536.0 ; 65536.0 \cdot 2^{-15} \rangle$ .



```
#include "mlib.h"

static acc32_t a32Val;

void main(void)
{
    a32Val = ACC32(-13.654437);          /* a32Val = -13.654437 */
}
```

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