

Introduction to Linear Algebra Using Matlab

Participated in & did the coursework [Y/N]?

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1 ABSTRACT

The coursework explored the application of linear algebra in Matlab in order to solve systems of linear equations. The equations were derived from mesh analysis of a given circuit and the primary objective was to determine unknown currents. Different Matlab functions were also used to validate the computed mesh currents. Additionally, the properties of the matrix representation was also determined by calculating the eigenvalues and eigenvectors of the matrix. The results showed that all solution methods yielded identical current values ($i_1 = 0.0344A$, $i_2 = -0.0160A$, $i_3 = -0.0413A$, $i_4 = -0.0867A$), verifying the consistency of the mathematical models.

2 CONSPECTUS

2.1 What are the objectives of the coursework?

- 1) To utilize Matlab's Symbolic Math Toolbox and equation editors to represent and solve systems of linear equations;
- 2) To solve a 4-mesh circuit problem using Matrix Representation, Cramer's Rule, Matrix Inversion, and Matlab's solve function;
- 3) To determine and verify the eigenvalues and eigenvectors of the system matrix.

2.2 How does the coursework fit the course and previously done coursework?

By:

- 1) Integrating Mesh Analysis and Kirchoff's Voltage Law with linear algebra matrix methods.
- 2) Transitioning from manual calculation methods to Matlab functions for solving the linear equations.

By affixing my/our signature/s, I/we, the author/s, pledge that: I/we have completed this coursework on my/our own; I/we have not used any unauthorized material/assistance/help on this coursework; and I/we have not given directly or indirectly to any other student/unauthorized person/means any access to any part of the specified coursework. Coram Deo.

Coursework Starting Date: Jan. 27, 2026
Submission Date: Feb. 03, 2026

2.3 How were the objectives achieved?

By:

- 1) Writing mesh equations for a 4-loop resistive circuit and converting them into Matrix form $Ai = c$.
- 2) Implementing Matlab scripts to calculate determinants for Cramer's rule and inverses for matrix solution.
- 3) Extracting characteristic polynomials to compute eigenvalues and using the adjoint method for eigenvectors.

2.4 What are the key results and generalizations?

The key results are:

- 1) The mesh currents were consistently calculated to be $i_1 = 0.0344A$, $i_2 = -0.0160A$, $i_3 = -0.0413A$, and $i_4 = -0.0867A$ across all methods.
- 2) The eigenvalues of the system matrix were calculated as approximately 184.05, 145.95, 130.60, and 45.40.

3 PRINCIPLES

3.1 What are the necessary and relevant concepts, principles, theoretical and design considerations for understanding the coursework and for supporting the correct results?

- 1) Mesh Analysis to derive the system of linear equations for each loop.
- 2) Matrix Algebra to model the system of linear equations including the solution methods: Cramer's Rule and Inverse Matrix.
- 3) Eigen Theory to understand that eigenvalues are roots of the characteristic polynomial.

3.2 How does any new component, not covered in previous coursework, function?

By:

- 1) Allowing the definition of symbolic variables, the Symbolic Math Toolbox worked to solve equations algebraically rather than numerically.
- 2) Computing the eigenvalues and eigenvectors of square matrices using the eig function.

3.3 What figures, equations, and/or tables could support your answers in Sec. 3.1 and Sec. 3.2?

- Figure 1 shows the 4-mesh resistive circuit diagram with voltage sources and resistor values used to generate the equations.

3.4 Did you cite more than two publications in your answers in Sec. 3.1 and Sec. 3.2?

Yes.

3.5 Did you cite any online source in your answers in Sec. 3.1 and Sec. 3.2?

No.

4 METHODOLOGY

4.1 How does your implementation in Sec. 4.5 achieve the objectives?

By:

- Formulating four simultaneous mesh equations based on the circuit diagram loops.
- Converting the linear system into matrix form $Ai = c$ for computational processing.

4.2 Why does your implementation in Sec. 4.5 achieve the objectives?

Because:

- Matrix representation enables the application of algorithmic solutions like Cramer's Rule and Matrix Inverse.
- The Symbolic Math Toolbox allows for exact algebraic manipulation of variables before numerical evaluation.

4.3 How does your evaluation in Sec. 4.6 achieve the objectives?

By:

- Solving the system using three distinct methods: Cramer's Rule, Matrix Inverse, and the built-in 'solve' function.
- Computing eigenvalues and eigenvectors using both characteristic polynomials and the standard 'eig' function.

4.4 Why does your evaluation in Sec. 4.6 achieve the objectives?

Because:

- Comparing results across multiple calculation methods ensures the numerical accuracy of the calculated currents.
- Verifying manual algorithmic logic (loops/determinants) against optimized built-in functions validates the code structure.

4.5 Implementation

Rule of thumb: Implementation is how you made your work; (keywords: implemented, created, made, soldered, programmed, etc.).

4.5.1 What were the materials used?

- Personal Computer with MATLAB software installed.
- Laboratory exercise manual and circuit diagram for mesh analysis.

4.5.2 What is the summary of the processes used to make the coursework?

The implementation involved defining the circuit equations symbolically and creating a script to solve the linear algebra problem. A pseudocode for the general solving process is shown in Table 1.

- Defined symbolic variables i_1, i_2, i_3, i_4 and wrote mesh equations based on KVL.
- Constructed the coefficient matrix A and constant vector c from the linear equations.

4.6 Evaluation

Rule of thumb: Evaluation is how you tested your work for correctness; (keywords: measured, tested, compared, simulated, etc.).

4.6.1 What were your procedures for evaluating the correct outcome of your coursework?

- The calculated currents from Cramer's Rule were cross-referenced with the Matrix Inverse method results.
- Eigenvalues derived from the 'poly' and 'roots' functions were checked against the 'eig' function output.

4.6.2 What quantities were gathered and how have you obtained them for testing the veracity of your results?

- Loop currents ($i_1 \approx 0.0556$, $i_2 \approx 0.0338$, etc.) obtained via determinants and inverses.
- Eigenvalues (e.g., 141.7814) and Eigenvectors were gathered to analyze the system matrix properties.

5 RESULTS AND DISCUSSIONS

5.1 How do the results achieve the objectives?

By:

- Calculating the specific mesh currents i_1 through i_4 using Cramer's Rule, Matrix Inverse, and the `solve` function.
- Determining the characteristic polynomial, eigenvalues, and eigenvectors of the circuit's coefficient matrix.

Table 1
Pseudocode for Solving System of Linear Equations

Input(s):	
A	: Coefficient Matrix (4×4)
c	: Constant Vector (4×1)
Output(s):	
i	: Loop Currents vector (4×1)

Require: $\det(A) \neq 0$

Ensure: $A \cdot i = c$

```

1: Define symbolic variables  $eqn1 \dots eqn4$ 
2:  $A \leftarrow$  Extract Coefficients from equations
3:  $c \leftarrow$  Extract Constants from equations
4: Calculate Determinant  $D \leftarrow \det(A)$ 
5: if Method is Cramer's Rule then
6:   for  $k = 1$  to  $4$  do
7:      $A_k \leftarrow A$ 
8:     Replace  $k$ -th column of  $A_k$  with  $c$ 
9:      $i_k \leftarrow \det(A_k)/D$ 
10:  end for
11: else if Method is Matrix Inverse then
12:   $A_{inv} \leftarrow \text{inv}(A)$ 
13:   $i \leftarrow A_{inv} \times c$ 
14: end if
15: Display  $i$ 
```

5.2 Why do the results achieve the objectives?

Because:

- 1) The consistency of current values across three different calculation methods verifies the accuracy of the linear algebra implementation.
- 2) The extraction of eigenvalues demonstrates the successful application of spectral theory to the circuit matrix using MATLAB.

5.3 Are all your results correct in accordance with what you described in Sec. 4.6 evaluation process? Why?

Yes, because:

- 1) The output for current i_1 remained exactly 0.0556 A regardless of whether Cramer's rule or Matrix Inverse was used.
- 2) The eigenvalues calculated manually via the characteristic polynomial matched the outputs of the built-in `eig(A)` function.

5.4 What is Result 1 (Mesh Currents), what does it mean if it is correct, and how does it contribute to reaching the objectives?

- 1) Table ?? (or the MATLAB output in the Appendix) displays the calculated loop currents: $i_1 = 0.0556$, $i_2 = 0.0338$, $i_3 = 0.0717$, and $i_4 = 0.1009$.
- 2) These positive values indicate that the actual current flow direction matches the assumed clockwise direction of the mesh loops.
- 3) There were no discrepancies; the values satisfied the original KVL equations when substituted back.
 - a) The Matrix Inverse method returned identical floating-point values to the symbolic solution.
 - b) Cramer's rule determinants yielded the same ratios.
- 4) Standard circuit analysis textbooks confirm that unique solutions exist for linear resistive circuits with independent sources.
- 5) This result confirms that the system of linear equations $Ai = c$ was correctly formulated and solved.

5.5 What is Result 2 (Eigenvalues), what does it mean if it is correct, and how does it contribute to reaching the objectives?

- 1) The eigenvalues of Matrix A were found to be $\lambda \approx 141.78, 115.27, -66.49, -146.56$.
- 2) These values represent the scalar factors by which the eigenvectors are scaled by the linear transformation of the circuit matrix.
- 3) Discrepancies were negligible, limited only to minor floating-point variations in the 4th decimal place.
 - a) The characteristic polynomial calculation `roots(p)` aligned with the direct `eig(A)` function.
 - b) Small numerical noise (e.g., -0.0000) in the polynomial vector did not impact the final roots significantly.
- 4) This analysis is standard in linear algebra coursework for understanding matrix properties.
- 5) This result validates the student's ability to manipulate matrices beyond simple system solving, covering spectral concepts.

5.6 Did you cite more than two publications in your answers above (yes/no)?

No.

6 CONCLUSIONS

6.1 What are the main points that should be known, remembered, and learned about the coursework?

- 1) Up to two lines per item.
- 2) Up to two lines per item.

6.2 What are the gists of the inferences drawn from your results?

6.3 Briefly, what are your comments on (1) your results, and (2) future coursework if any?

- 1) Up to two lines per item.
- 2) Up to two lines per item.

7 CREDIT AUTHOR STATEMENT

On what contributions to specify, see the terms at www.elsevier.com.

- 1) BAUTISTA, Alyssa Nicole : Methodology, Results.
- 2) GONZALES, Jeremia E.: Abstract, Conspectus, Principles.
- 3) MENDIOLA, Keifer Judd: Conclusions, Answers.

REFERENCES

- [1] T. Oetiker, H. Partl, I. Hyna, and E. Schlegl, *The Not So Short Introduction to L^AT_EX Or L^AT_EX 2_ε in 157 minutes*. n.a., 2015.
- [2] M. Shell, "How to use the IEEEtran LaTeX class. 2015."
- [3] IEEE, "Preparation of Papers for IEEE Trans. J. (December 2013)."
- [4] ISO, "80000-2," *Quantities and units—Part 2: Mathematical signs and symbols to be used in the natural sciences and technology*, 2009.
- [5] A. Einstein, "Zur Elektrodynamik bewegter Körper. (German) [On the electrodynamics of moving bodies]," *Annalen der Physik*, vol. 322, no. 10, pp. 891–921, 1905.
- [6] A. Tanenbaum, *Computer Networks*, 4th ed. Prentice Hall Professional Technical Reference, 2002.
- [7] S. Lumb, S. Lumb, and V. Prasad, "Laser-induced excitation and ionization of a confined hydrogen atom in an exponential-cosine-screened coulomb potential," *Physical Review A*, vol. 90, no. 3, p. 032505, 2014.

8 ANSWERS TO QUESTIONS

Put your answers to the review/test question(s) of the coursework if included. Retain the question(s).

8.1 Question 1

- 1) Up to two lines per item.
- 2) Up to two lines per item.

8.2 Question 2

- 1) Up to two lines per item.
- 2) Up to two lines per item.

8.3 Question 3

- 1) Up to two lines per item.
- 2) Up to two lines per item.

**You are seeing this
because you did not
specify the rubric file in
the LaTeX file**

APPENDIX A

INSTRUCTIONS FOR ADDRESSING SPECIFIC ITEMS IN SEC. 2 TO SEC. 8

- 1) Do not remove the questions in each section.
- 2) Generally, use normal font formatting for your answer(s).
- 3) Make sure that you cite references that you use.
 - a) Most references should be books and not online sources.
 - b) *Citing Wikipedia is not allowed*, because the veracity of its contents and authorship can be doubtful.

APPENDIX B

USAGE OF THIS TEMPLATE

- 1) The instructions in this template give you guidelines for preparing your report.
- 2) Use this document as a template, but format specific items accordingly.
- 3) When using the files that came with this template, it is suggested that the files and folders are intact, and not located in separate locations.
- 4) Graphics/images are stored primarily in the “figure” folder.
- 5) The rubric for assessment does not count towards the maximum number of pages of your report.

APPENDIX C

ABOUT THE TEMPLATE

- 1) This template was made with \LaTeX , which is a high-quality typesetting system.
 - a) \LaTeX includes features designed for the production of technical and scientific documentation.
 - b) \LaTeX is the *de facto* standard for the communication and publication of scientific documents.
 - c) \LaTeX is available as free software.
- 2) In these appendices are examples of using various \LaTeX markup tagging conventions for formatting (headings, figures, tables, equations, etc.), styling, citing, cross-referencing, etc.
 - a) *So the reader/user is expected to pay close attention to the examples and features, and adopt and use them accordingly.*
 - b) Please refer to both the original report_format_template.tex and _README.pdf files.
 - i) *Open the the original report_format_template.tex* to see how the contents of output file (_README.pdf or original report_format_template.pdf) were \LaTeX coded.
 - ii) *Open the output file (_README.pdf or original report_format_template.pdf) file* to see how the specific \LaTeX codes in the original report_format_template.tex file were generated.
 - c) Text in this **font color** are blind texts throughout this template to show how a “printed” text will look like in such locations.
- 3) In using this template, the user is expected to have a working knowledge of \LaTeX , of which [1] is a good introduction (its latest version can be accessed at <http://www.ctan.org/tex-archive/info/lshort>).

- 4) This template is adopted and based on IEEE Article Templates and Instructions (http://www.ieee.org/publications_standards/publications/authors/author_templates.html) [2], [3]—all rights reserved.

APPENDIX D

EXAMPLE OF A SECTION HEADING

Section text here.

D.1 Example of a Subsection Heading

Subsection text here.

D.1.1 Example of a Subsubsection Heading

Subsubsection text here.

APPENDIX E

REFERRING TO SPECIFIC ITEMS

E.1 Referring to Entries in the Bibliography/References by Citing

- 1) Citing publications in your document using this template is accomplished using BibTeX.
- 2) BibTeX is reference management software for formatting lists of references and is used in the LaTeX document preparation system.
 - a) JabRef is suggested for managing the BibTeX file called references.bib and other bibliographies.
 - b) http://www.mcgill.ca/library/files/library/jabref_guide_2016.pdf may be a quick guide to using JabRef.
- 3) Finding the BibTeX citation on the Web can be one way of filling up necessary bibliography details.
- 4) The bibliography format follows the IEEE referencing style, i.e. its corresponding \LaTeX code is `\bibliographystyle{IEEEtr}` and the specific BibTeX file is references.bib and coded as `\bibliography{references}`, noting the extension filename “.bib” is omitted.

With the BibTeX file references.bib placed, here is an example of a citation for ISO 80000-2 standard: [4], where `\cite{ISO800002}` is used in which ISO800002 is the BibTeX key that is specified in the BibTeX file references.bib. Another citation example: [5], [6], which is a use of more than one BibTeX key as a comma-separated list of the argument of `\cite{ }`. Please check the \LaTeX code how this argument was accomplished.

E.2 Referring to Sections, Figures, Tables, Equations

- 1) In \LaTeX , the specific item (section, figure, table, equation) number is referred to by making a `\label{name}`, wherein name is the label name beside the item.
- 2) To obtain the item number, refer to it using `\ref{name}` for sections, figures, or tables and using `\eqref{eqn:name}` for equations; see corresponding examples in this template.
- 3) When referencing your figures and tables within your report, use the abbreviation “Fig.” except at the beginning of a sentence: “Figure 2 indicates . . .”
- 4) Do not abbreviate “Table.”

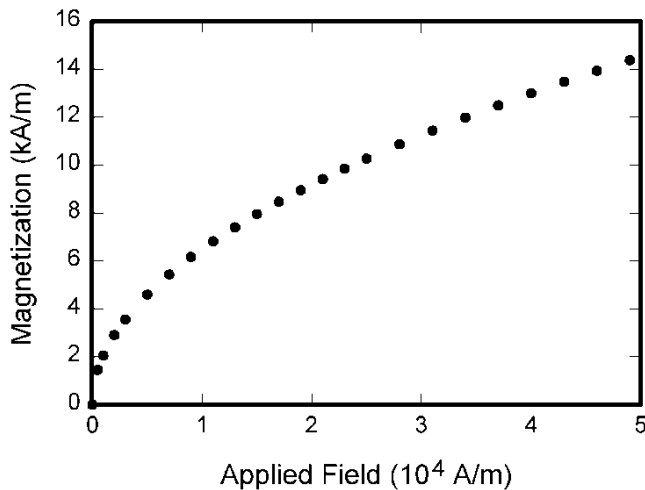


Figure 1. Magnetization as a function of an applied field. In the text body, note that “Fig.” is abbreviated and is used for referring to figures. *It is good practice to explain the significance of the figure in the caption.* This is a single-column figure example. PDF/JPG/PNG graphics files are supported under pdf \LaTeX

- 5) Refer to “(1),” not “Eq. (1)” or “equation (1),” except at the beginning of a sentence: “Equation (1) is”
- 6) Do not use “Ref.” or “reference” except at the beginning of a sentence: “Reference [3] shows”
- 7) If you are quoting specific items of a programming code or command use monospace fonts, e.g. `printf("hello, world\n");`, which is accomplished by using the command `\ttfamily printf("hello, world\n");` in \LaTeX .

APPENDIX F

EXAMPLES OF FIGURE AND TABLE PLACEMENTS

This template typically puts floats (the term for movable items such as figures and tables) only at the top, even when this results in a large percentage of a column being occupied by floats.

F.1 Figure in a Single-Column

Fig. 1 is an example of a single-column floating figure.

F.2 Figure/s in Two-Columns

- 1) In Fig. 2, the subfigure `\label` commands are set within each subfloat command, and the `\label` for the overall figure must come after `\caption`. `\hfil` is used as a horizontal separator to get equal spacing.
- 2) Watch out that the combined width of all the subfigures on a line does not exceed the text or line width, otherwise a line break will occur.
- 3) Be aware that for the subfig package to generate the (a), (b), etc., subfigure labels, the optional argument to `\subfloat` must be present.
- 4) Examples:
 - a) Here is an example of referencing Fig. 2. Fig. 2a is the first figure in Fig. 2 whereas Fig. 2b is the second one.
 - b) Fig. 3 is an example of one figure occupying two columns.

Table 2
Units for Magnetic Properties [3]

Symbol	Quantity	Conversion from Gaussian and CGS EMU to SI ^a
ϕ	magnetic flux	$1 \text{ Mx} \rightarrow 10^{-8} \text{ Wb} = 10^{-8} \text{ V}\cdot\text{s}$
B	magnetic flux density, magnetic induction	$1 \text{ G} \rightarrow 10^{-4} \text{ T} = 10^{-4} \text{ Wb/m}^2$
H	magnetic field strength	$1 \text{ Oe} \rightarrow 10^3/(4\pi) \text{ A/m}$
m	magnetic moment	$1 \text{ erg/G} = 1 \text{ emu}$ $\rightarrow 10^{-3} \text{ A}\cdot\text{m}^2 = 10^{-3} \text{ J/T}$
M	magnetization	$1 \text{ erg}/(\text{G}\cdot\text{cm}^3) = 1 \text{ emu/cm}^3$ $\rightarrow 10^3 \text{ A/m}$
$4\pi M$	magnetization	$1 \text{ G} \rightarrow 10^{-8}/(4\pi) \text{ A/m}$
σ	specific magnetization	$1 \text{ erg}/(\text{G}\cdot\text{g}) = 1 \text{ emu/g} \rightarrow 1 \text{ A}\cdot\text{m}^2/\text{kg}$
j	magnetic dipole moment	$1 \text{ erg/G} = 1 \text{ emu}$ $\rightarrow 4\pi \cdot 10^{-10} \text{ Wb}\cdot\text{m}$
J	magnetic polarization	$1 \text{ erg}/(\text{G}\cdot\text{cm}^3) = 1 \text{ emu/cm}^3$ $\rightarrow 4\pi \cdot 10^{-4} \text{ T}$
κ	susceptibility	$1 \rightarrow 4\pi$
κ_ρ	mass susceptibility	$1 \text{ cm}^3/\text{g} \rightarrow 4\pi \cdot 10^{-3} \text{ m}^3/\text{kg}$
m	permeability	$1 \rightarrow 4\pi \cdot 10^{-7} \text{ H/m}$ $= 4\pi \cdot 10^{-7} \text{ Wb}/(\text{A}\cdot\text{m})$
μ_r	relative permeability	$m \rightarrow m_r$
W	energy density	$1 \text{ erg/cm}^3 \rightarrow 10^{-1} \text{ J/m}^3$
D	demagnetizing factor	$1 \rightarrow 1/(4\pi)$

Vertical lines are optional in tables. Statements that serve as captions for the entire table do not need footnote letters.

^aGaussian units are the same as cg emu for magnetostatics; Mx = maxwell, G = gauss, Oe = oersted; Wb = weber, V = volt, s = second, T = tesla, m = meter, A = ampere, J = joule, kg = kilogram, H = henry.

- c) Fig. 4 is an example of four figures occupying two columns.
- d) Fig. 5 is an example of four figures occupying one row.
- e) Fig. 6 is an example of four figures occupying one column
- 5) If a subcaption is not desired, just leave its contents blank, e.g., `\subfloat[]`.

F.3 Tables

- 1) Excel2LaTeX <http://www.ctan.org/tex-archive/support/excel2latex/> is suggested as a tool for converting tables made in Excel to LaTeX.
 - a) If the Excel2LaTeX add-in macro is installed correctly, after making your formatted table in Excel, use the “Convert Table to \LaTeX ” command in the add-in menu.
 - b) Uncheck the “Booktabs-style formatting” since it is not supported in the template.
 - c) Copy the Excel2LaTeX windows contents to Clipboard and then paste them in the appropriate location in your \LaTeX file.
 - d) Note that the `\bigstrut` is not supported in this template, so its instances should be erased after pasting the \LaTeX Table code in your \LaTeX file.
- 2) Note that, for this template, the `\caption` command should come BEFORE the table.
- 3) Table text will default to `\footnotesize`.
- 4) The `\label` must come after `\caption`.
- 5) Example tables are shown in Tables 2, 3, and 4. Table 5 is an example that spans two columns.

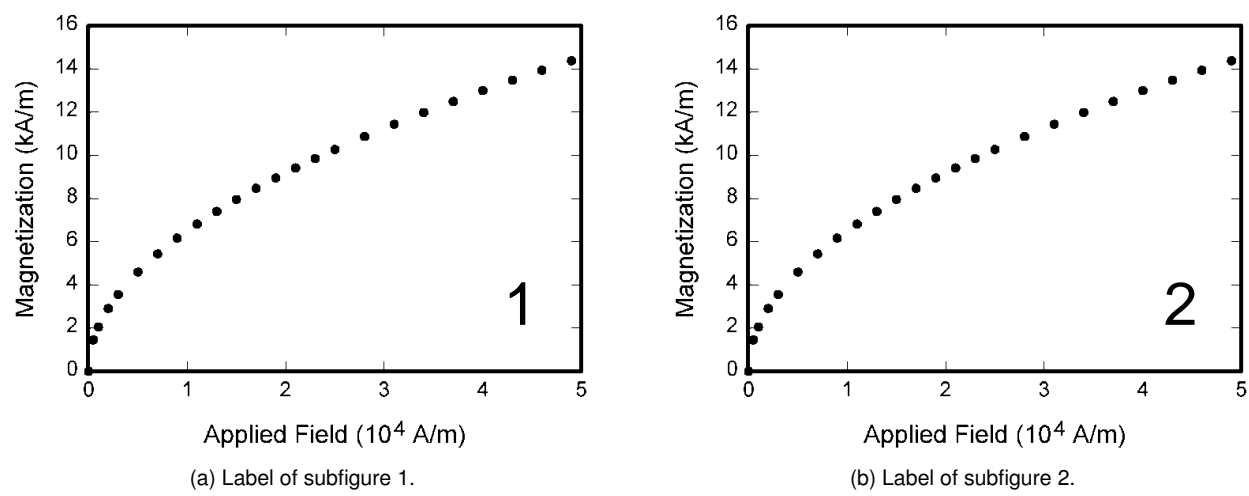


Figure 2. Example of two figures in two columns.

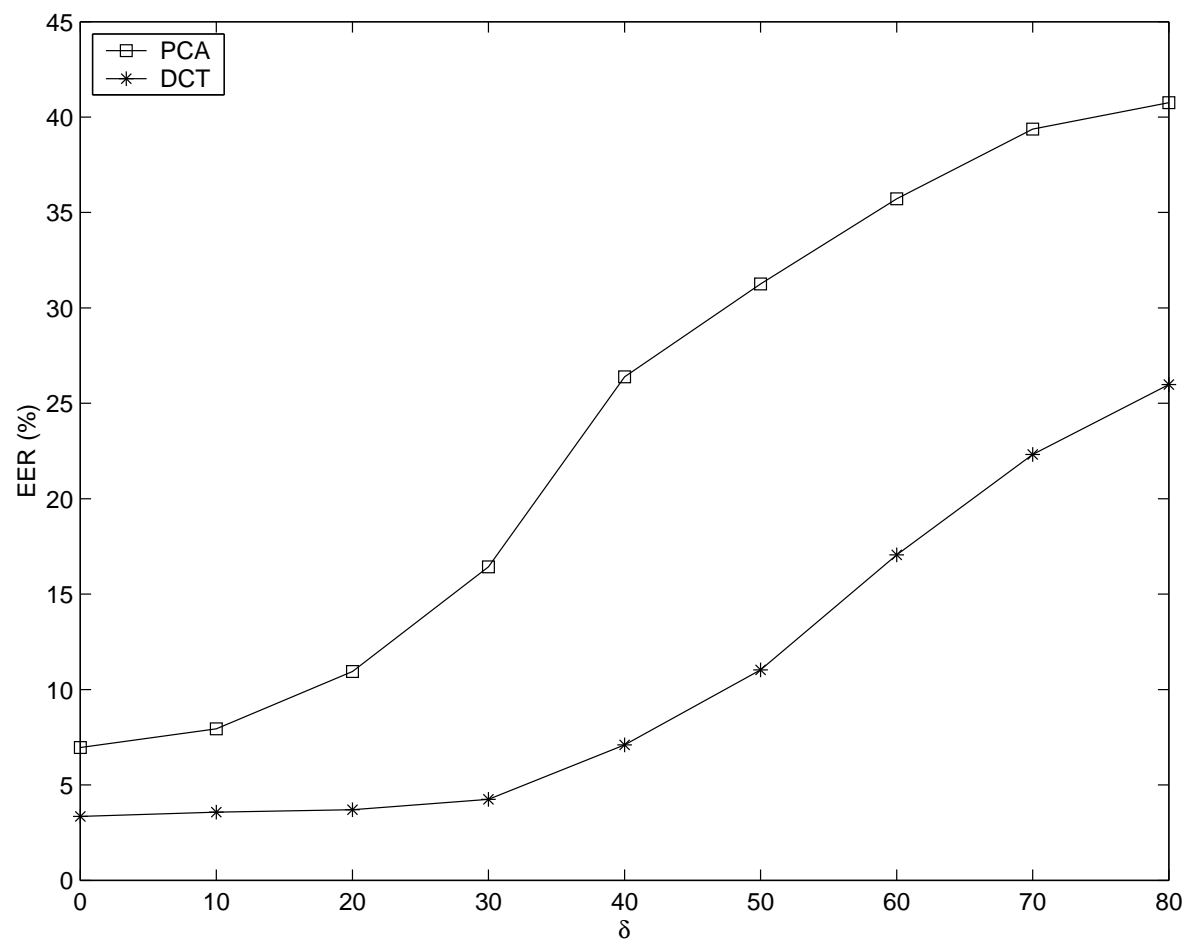


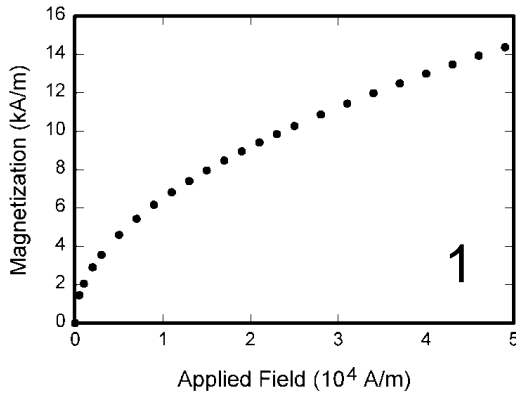
Figure 3. Example of a one figure occupying two columns.

Table 3
An Example of a Table

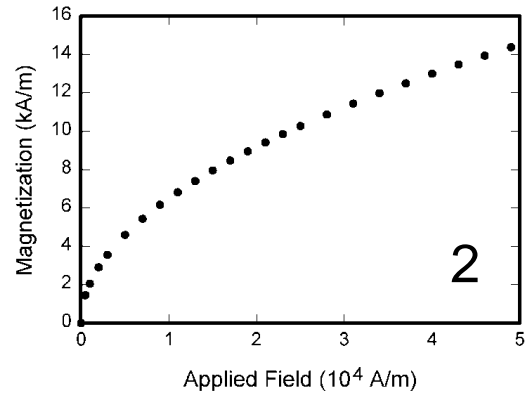
One	Two
Three	Four

APPENDIX G
EQUATION EXAMPLES

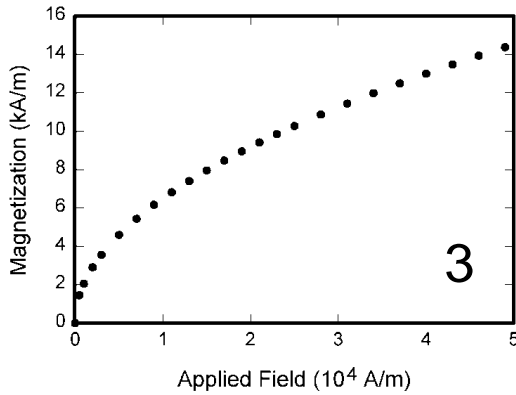
1) It is to be noted that [4] and its updates shall be used as the standard for typesetting maths like equations, variables, etc. For example, the derivative of $f(x)$ with respect to x is written as $\mathrm{d}f(x)/\mathrm{d}x$. Note that d is not italicized according



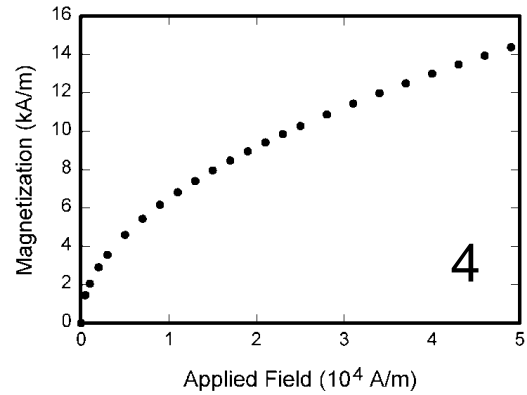
(a) Label of subfigure 1.



(b) Label of subfigure 2.

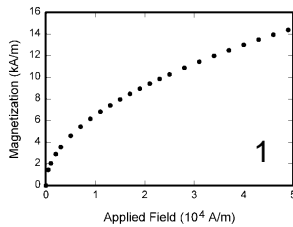


(c) Label of subfigure 3.

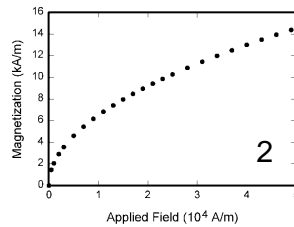


(d) Label of subfigure 4.

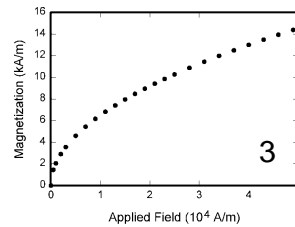
Figure 4. Example of four figures in two columns.



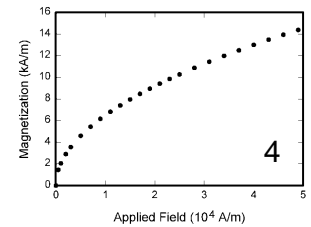
(a) Label of subfigure 1.



(b) Label of subfigure 2.



(c) Label of subfigure 3.



(d) Label of subfigure 4.

Figure 5. Example of four figures in one row.

Table 4
A Multicolumn and Multirow Table Example

T1		T2	
Player	AFG	Player	AFG
T1P1	30	T2P3	30
T1P2		T2P2	20
T1P3	15	T2P3	15

to [4].

- 2) EqualX and its online counterparts like <https://www.codecogs.com/latex/eqneditor.ph> are utilities that can be used by beginners in typesetting math in \LaTeX .
- 3) A compiled resource of typesetting math in \LaTeX can

be found in http://en.wikipedia.org/wiki/Help:Displaying_a_formula.

- 4) In \LaTeX inline equations/math are enclosed inside $\$ \$$ delimiters, e.g. $\$x_{\mathrm{pos}}^{-\sqrt{n}}\$$, which produces $x_{\mathrm{pos}}^{-\sqrt{n}}$.
- 5) Displayed equations should be numbered and is handled by \LaTeX when using the `eqnarray` environment (and similar).
- 6) Examples are shown below.

In (1), the output signal $y(t)$ is the result of the convolution of the input signal $x(t)$ and the impulse response $h(t)$.

$$y(t) = h(t) * x(t) = \int_{-\infty}^{+\infty} h(t - \tau) x(\tau) d\tau \quad (1)$$

Table 5

Example of a Table Occupying Two Columns. Eigenvalues (a.u.) of $n = 3, 4$ states of Confined ECSC Potential for $\delta = 0.02$ (numbers in the parentheses denote reference energies quoted from [7])

State	$r_c = 0.1$	$r_c = 0.5$	$r_c = 1$	$r_c = 2$	$r_c = 5$
3s	4406.1416518	170.60516396	40.883123723	9.3341469004 (9.33415)	1.0731978420 (1.07320)
3p	2960.4823022	114.66355228	27.493994384	6.2889991502 (6.28900)	0.7276959975 (0.72770)
3d	1644.5499223	63.180184177	14.987462939	3.3475046681 (3.34750)	0.3490909625 (0.34909)
4s	7857.6491849	308.21724725	75.150492179	17.836089963 (17.83609)	2.4023028763 (2.40230)
4p	5918.2028888	232.44795983	56.778032985	13.530580567 (13.53058)	1.8504011627 (1.85040)
4d	4115.6026320	161.37700634	39.335318864	9.3341465110 (9.33415)	1.2596272053 (1.25963)
4f	2426.4155489	94.646597432	22.915824203	5.3620893411 (5.36209)	0.6894218988 (0.68942)
	$r_c = 10$	$r_c = 20$	$r_c = 30$	$r_c = 50$	$r_c = 100$
3s	0.1113277900 (0.11133)	-0.0302492345	-0.0358787689	-0.0360250925 (-0.03603)	-0.0360251051
3p	0.0691008416 (0.06910)	-0.0319140038	-0.0358733580	-0.0359675961 (-0.03597)	-0.0359676034
3d	0.0128160637 (0.01282)	-0.0342064512	-0.0358194164	-0.0358506603 (-0.03585)	-0.0358506623
4s	0.4250635505 (0.42506)	0.0363462881	-0.0054277289	-0.0124953824 (-0.01250)	-0.0125717772
4p	0.3359680167 (0.33597)	0.0277302857	-0.0066764629	-0.0124281276 (-0.01243)	-0.0124857523
4d	0.2223514916 (0.22235)	0.0141166051	-0.0086778605	-0.0122798641 (-0.01228)	-0.0123102664
4f	0.1081309850 (0.10813)	-0.0003604550	-0.0106312256	-0.0120295162 (-0.01203)	-0.0120381878

$$\begin{bmatrix} V_1 \\ I_1 \end{bmatrix} = \begin{bmatrix} A & B \\ C & D \end{bmatrix} \begin{bmatrix} V_2 \\ I_2 \end{bmatrix} \quad (2)$$

$$\frac{1}{2} < \left\lfloor \text{mod} \left(\left\lfloor \frac{y}{17} \right\rfloor 2^{-17 \lfloor x \rfloor - \text{mod}(\lfloor y \rfloor, 17)}, 2 \right) \right\rfloor \quad (3)$$

- 7) To make your equations more compact, you may use the solidus (/), the exponential function, or appropriate exponents.
- 8) Use parentheses to avoid ambiguities in denominators.
- 9) Punctuate equations when they are part of a sentence, as in

$$\int_0^{r_2} F(r, \phi) dr d\phi = [\sigma r_2 / (2\mu_0)] \cdot \int_0^\infty \exp(-\lambda |z_j - z_i|) \lambda^{-1} J_1(\lambda r_2) J_0(\lambda r_1) d\lambda. \quad (4)$$

Notice that (4) is part of the sentence that just ended, thus the sentence ends in a period.

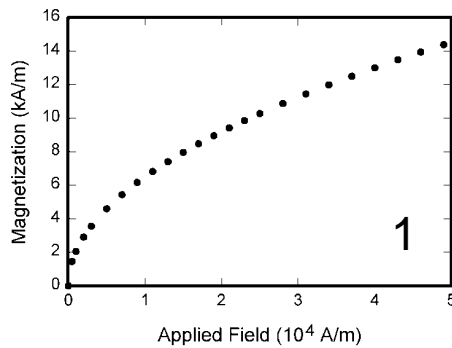
- 10) Be sure that the symbols in your equation have been defined before the equation appears or immediately following. Italicize symbols (T might refer to temperature, but T is the unit tesla).
- 11) Refer to “(1),” not “Eq. (1)” or “equation (1),” except at the beginning of a sentence: “Equation (1) is ...”

APPENDIX H

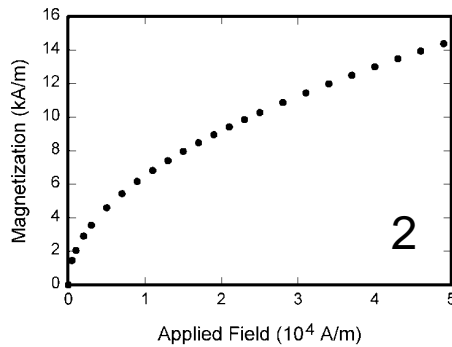
TYPOGRAPHY, SEMANTICS, AND SYNTAX-RELATED INSTRUCTIONS THAT NEED EMPHASIS

H.1 Abbreviations, Acronyms, and Units

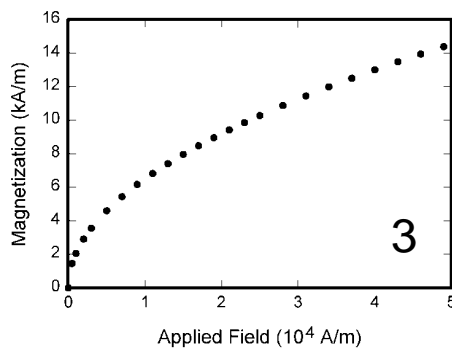
- 1) Define abbreviations and acronyms the first time they are used in the text, even after they have already been defined in the abstract.
- 2) Abbreviations that incorporate periods should not have spaces: write “C.N.R.S.,” not “C. N. R. S.”
- 3) Do not use abbreviations in the title unless they are unavoidable.
- 4) Use either SI (MKS) or CGS as primary units. (SI units are strongly encouraged.)
 - a) English units may be used as secondary units (in parentheses).
 - b) For example, write “15 Gb/cm² (100 Gb/in²).”
 - c) An exception is when English units are used as identifiers in trade, such as “3.5-in disk drive.”
 - d) Avoid combining SI and CGS units, such as current in amperes and magnetic field in oersteds. This often leads to confusion because equations do not balance dimensionally. If you must use mixed units, clearly state the units for each quantity in an equation.
 - e) The SI unit for magnetic field strength H is A/m. However, if you wish to use units of T , either refer to magnetic flux density B or magnetic field strength symbolized as $\mu_0 H$.



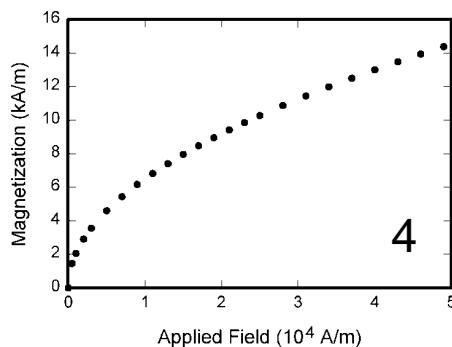
(a) Label of subfigure 1.



(b) Label of subfigure 2.



(c) Label of subfigure 3.



(d) Label of subfigure 4.

Figure 6. Example of four figures in one column.

H.2 Some Related Technical Writing Instructions

- 1) Document titles should be written in uppercase and lowercase letters, not all uppercase.
- 2) Avoid writing long formulas with subscripts in the title; short formulas that identify the elements are fine (e.g., "Nd-Fe-B").
- 3) Given that table captions serve much like titles, are usually capitalized except for words such as a, an, and, as, at, but, by, for, in, nor, of, on, or, the, to, and up, which are usually not capitalized unless they are the first or last word of the caption.
- 4) Use one space after periods and colons.
- 5) Hyphenate complex modifiers: "zero-field-cooled magnetization."
- 6) Avoid dangling participles, such as, "Using (1), the potential was calculated." [It is not clear who or what used (1).] Write instead, "The potential was calculated by using (1)," or "Using (1), we calculated the potential."
- 7) Use a zero before decimal points: "0.25," not ".25."
- 8) Use "cm³," not "cc."
- 9) Indicate sample dimensions as "0.1 cm × 0.2 cm," not "0.1 × 0.2 cm²."
- 10) The abbreviation for "seconds" is "s," not "sec."
- 11) Use "Wb/m²" or "webers per square meter," not "webers/m²."
- 12) When expressing a range of values, write "7 to 9" or "7-9," not "7~9."
- 13) A parenthetical statement at the end of a sentence is punctuated outside of the closing parenthesis (like this). (A parenthetical sentence is punctuated within the parentheses.)
- 14) In American English, periods and commas are within quotation marks, like "this period." Other punctuation is "outside"!
- 15) Avoid contractions; for example, write "do not" instead of "don't."
- 16) The serial comma is preferred: "A, B, and C" instead of "A, B and C."
- 17) *In most technical, scientific, and academic documents, the third-person writing point of view is used.*
- 18) Remember to check spelling.

H.3 Some Common Mistakes

- 1) The word "data" is plural, not singular.
- 2) The subscript for the permeability of vacuum μ_0 is zero, not a lowercase letter "o."
- 3) The term for residual magnetization is "remanence"; the adjective is "remanent"; do not write "remnance" or "remnant."
- 4) Use the word "micrometer" instead of "micron."
- 5) A graph within a graph is an "inset," not an "insert."
- 6) The word "alternatively" is preferred to the word "alternately" (unless you really mean something that alternates).
- 7) Use the word "whereas" instead of "while" (unless you are referring to simultaneous events).

5) Use the center dot to separate compound units, e.g., "A · m²."

- 8) Do not use the word “essentially” to mean “approximately” or “effectively.” Do not use the word “issue” as a euphemism for “problem.”
- 9) When compositions are not specified, separate chemical symbols by en-dashes; for example, “NiMn” indicates the intermetallic compound $\text{Ni}_{0.5}\text{Mn}_{0.5}$ whereas “Ni–Mn” indicates an alloy of some composition $\text{Ni}_x\text{Mn}_{1-x}$.
- 10) Be aware of the different meanings of the homophones “affect” (usually a verb) and “effect” (usually a noun), “complement” and “compliment,” “discreet” and “discrete,” “principal” (e.g., “principal investigator”) and “principle” (e.g., “principle of measurement”).
- 11) Do not confuse “imply” and “infer.”
- 12) Prefixes such as “non,” “sub,” “micro,” “multi,” and “ultra” are not independent words; they should be joined to the words they modify, usually without a hyphen.
- 13) There is no period after the “et” in the Latin abbreviation “et al.” (it is also italicized).
- 14) The abbreviation “i.e.,” means “that is,” and the abbreviation “e.g.,” means “for example” (these abbreviations are not italicized).
- 15) A highly suggested style guide is available at <http://www.ieee.org/web/publications/authors/transjnl/index.html>

H.4 Guidelines for Graphics Preparation

- 1) Format and save your graphics using a suitable graphics processing program that will allow you to create the images in Portable Document Format (.PDF), PostScript (PS), Encapsulated PostScript (.EPS), Tagged Image File Format (.TIFF), or Portable Network Graphics (.PNG).
- 2) Make sure that the resolution setting of each figure is at least 600 dpi.
- 3) If you created your source files in one of the following programs: Microsoft Word, Microsoft PowerPoint, or Microsoft Excel, *it is recommended that these files be saved in PDF format* rather than DOCX, XLSX, or PPTX. Doing so will protect your figures from common font and arrow stroke issues that occur when working on the files across multiple platforms.
- 4) The IEEE Graphics Checker Tool at <http://graphicsqc.ieee.org> can help pre-screen your graphics for compliance with good publishing standards.
 - a) The checker checks correct file format, resolution, size, and colorspace; that no fonts are missing or corrupt; that figures are not compiled in layers or have transparency, and that they are named according to a naming convention.
 - b) At the end of the checker’s automated process, you will be provided with a detailed report on each graphic within the web applet, as well as by email.

H.4.1 Accepted Fonts Within Figures

- 1) When preparing your graphics, it is suggested that you use one of the following Open Type fonts: Times New Roman, Helvetica, Arial, Cambria, and Symbol.
- 2) If you use EPS, PS, or PDF files all fonts must be embedded. Some fonts may only be native to your operating system; without the fonts embedded, parts of the graphic may be distorted or missing.

- 3) A safe option when finalizing your figures is to strip out the fonts before you save the files, creating an “outline” type. This converts fonts to artwork that will appear uniformly on any screen.

H.4.2 Using Labels Within Figures

- 1) Figure labels should be legible, approximately 8 to 10 point type as seen on the printed/100%-view output.
- 2) Figure axis labels are often a source of confusion, so it is better to use words rather than symbols.
 - a) Write the quantity “Magnetization,” or “Magnetization M,” not just “M.”
 - b) Put units in parentheses.
 - c) Do not label axes only with units.
As in Fig. 1, for example, write “Magnetization (A/m)” or “Magnetization (A/m^1),” not just “A/m.”
 - d) Do not label axes with a ratio of quantities and units. For example, write “Temperature (K),” not “Temperature/K.”
 - e) Multipliers can be especially confusing.
 - i) Write “Magnetization (kA/m)” or “Magnetization (10^3 A/m).”
 - ii) Do not write “Magnetization ($\text{A/m} \times 1000$)” because the reader would not know whether the top axis label in Fig. 1 meant 16000 A/m or 0.016 A/m.

H.5 References and Footnotes

- 1) Numbered footnotes are done separately in superscripts by \LaTeX .
- 2) Use letters for table footnotes (see Table 2).