Einführung in die Wahrscheinlichkeitstheorie Übungsserie 1

Aufgabe 2:

(a)
$$A \setminus (B \cup C) = A \cap (B \cup C)^C = A \cap B^C \cap C^C = (A \cap B^C) \cap (A \cap C^C) = (A \setminus B) \cap (A \setminus C)$$

(b)
$$A \cup \bigcap_{i=1}^{k} B_i = \left(A^C \cap \left(\bigcap_{i=1}^{k} B_i\right)^C\right)^C = \left(A^C \cap \left(\bigcup_{i=1}^{k} B_i^C\right)\right)^C = \left(\bigcup_{i=1}^{k} A^C \cap B_i^C\right)^C = \bigcap_{i=1}^{k} \left(A^C \cap B_i^C\right$$

Aufgabe 6:

$$B_{1} = \bigcap_{j=1}^{n} A_{j}, |B_{1}| = 1$$

$$B_{2} = \bigcup_{j=1}^{n} A_{j}, |B_{2}| = 2^{n} - 1$$

$$B_{3} = \bigcup_{j=1}^{n} \left(A_{j} \cap \bigcap_{i=1}^{n} A_{i}^{C} \mid i \neq j \right), |B_{3}| = n$$

$$B_{4} = \bigcap_{j=1}^{n} A_{j} \cup \bigcap_{j=1}^{n} A_{j}^{C}, |B_{4}| = 2$$