

# **Modelling three multilevel models with lme4 package in R**

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## Introduction

Lets fit some models with

1. Outcome: Clinical decision-making
2. Level 1 (Individual-level factors): Age, Gender, Education, Experience, post basic (PB), continous professional development (CPD), knowledge (NKS) and critical thinking (CTS)
3. Level 2 (Hospital-level factors): Unit, Department size, hospital settings and hospital size
4. Level 3 (Regional-level factors): State, state size

## Install packages

```
install.packages("lme4")  
install.packages("lmerTest")  
install.packages("performance")  
install.packages("reghelper")
```

## Load the library

```
library(lme4) #multilevel analysis
```

Loading required package: Matrix

```
library(lmerTest) # to get p-value estimations
```

Attaching package: 'lmerTest'

The following object is masked from 'package:lme4':

```
lmer
```

The following object is masked from 'package:stats':

step

```
library(performance) # to get ICC  
library(reghelper) # to plot the interaction
```

Attaching package: 'reghelper'

The following object is masked from 'package:base':

beta

## Import the data

```
library(readxl)  
CTCDMR <- read_excel("CTCDMR.xlsx", sheet = "sheet1")
```

Combine hospital and department ID within each region to create a unique identifier for hosp.dep

```
CTCDMR$hosp.dep <- paste(CTCDMR$Hospital, CTCDMR$DepartmentID, sep = "_")
```

## Select Data

```
library(dplyr)
```

Attaching package: 'dplyr'

The following objects are masked from 'package:stats':

filter, lag

The following objects are masked from 'package:base':

intersect, setdiff, setequal, union

```
CTCDMR <- select(CTCDMR, NurseID, hosp.dep, DepartmentID, Hospital, Age, Gender, Education, 1
head(CTCDMR, n=50)
```

```
# A tibble: 50 x 20
  NurseID hosp.dep DepartmentID Hospital Age Gender Education Experience
  <dbl> <chr>      <dbl> <chr>    <dbl> <chr> <chr>      <dbl>
1      1 1 Hosp Segamat~      1 Hosp Se~    31 Female Diploma      10
2      2 2 Hosp Segamat~      1 Hosp Se~    31 Female Diploma       8
3      3 3 Hosp Segamat~      1 Hosp Se~    33 Female Diploma       8
4      4 4 Hosp Segamat~      1 Hosp Se~    32 Female Diploma       9
5      5 5 Hosp Segamat~      1 Hosp Se~    35 Female Diploma      13
6      6 6 Hosp Segamat~      1 Hosp Se~    36 Female Diploma      13
7      7 7 Hosp Segamat~      1 Hosp Se~    25 Female Diploma       4
8      8 8 Hosp Segamat~      1 Hosp Se~    30 Female Diploma       9
9      9 9 Hosp Segamat~      1 Hosp Se~    31 Female Diploma      10
10     10 10 Hosp Segamat~      1 Hosp Se~    37 Female Diploma      14
# i 40 more rows
# i 12 more variables: PB <chr>, CPD <dbl>, HospitalSet <chr>,
# HospitalSize <dbl>, DepSize <dbl>, Unit <chr>, State <chr>, Region <chr>,
# StateSize <dbl>, CDMS <dbl>, CTS <dbl>, NKS <dbl>
```

## Two-level Multilevel analysis

### Null model

What is the average score of the CDM for the entire group as well as for each individual?

```
library(lme4)
m0 <- lmer(CDMS ~ 1 + (1 | hosp.dep), data = CTCDMR, REML = FALSE)
summary(m0)
```

```
Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
method [lmerModLmerTest]
Formula: CDMS ~ 1 + (1 | hosp.dep)
Data: CTCDMR
```

```

      AIC      BIC   logLik deviance df.resid
4752.1    4765.9  -2373.1   4746.1     716

Scaled residuals:
    Min       1Q   Median       3Q      Max
-2.6003 -0.7153  0.0565  0.7715  2.8980

Random effects:
 Groups   Name      Variance Std.Dev.
hosp.dep (Intercept) 14.52     3.811
Residual              38.71     6.221
Number of obs: 719, groups: hosp.dep, 36

Fixed effects:
              Estimate Std. Error    df t value Pr(>|t|)
(Intercept)  36.2638     0.6762 35.9611   53.63  <2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

The intra-class correlation (ICC):

```

library(performance)
performance::icc(m0)

```

# Intraclass Correlation Coefficient

```

Adjusted ICC: 0.273
Unadjusted ICC: 0.273

```

## Random intercept model

Add level 1 and 2 variables:

Do the CDMS is predicted by the nurse's individual-level and hospital-level variables?

```

ri <- lmer(CDMS ~ NKS + Age + Gender + Education + Experience + PB + CPD + CTS + Unit + DepS:
summary(ri)

```

```

Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
method [lmerModLmerTest]
Formula: CDMS ~ NKS + Age + Gender + Education + Experience + PB + CPD +

```

```

      CTS + Unit + DepSize + HospitalSet + HospitalSize + (1 | hosp.dep)
Data: CTCDMR

      AIC      BIC   logLik deviance df.resid
3905.3   3978.5  -1936.6   3873.3     703

Scaled residuals:
      Min       1Q   Median       3Q      Max
-3.523 -0.550  0.053  0.643  2.922

Random effects:
 Groups   Name                Variance Std.Dev.
hosp.dep (Intercept)  0.1986  0.4456
Residual                12.6223  3.5528
Number of obs: 719, groups: hosp.dep, 36

Fixed effects:
              Estimate Std. Error      df t value Pr(>|t|)
(Intercept)   2.257e+00  2.221e+00  7.121e+02   1.016  0.3099
NKS            1.117e-01  9.831e-03  7.161e+02  11.364 <2e-16 ***
Age           -2.902e-02  7.965e-02  7.159e+02  -0.364  0.7157
GenderMale     2.337e-02  7.909e-01  7.179e+02   0.030  0.9764
EducationDiploma -1.578e-01  6.274e-01  7.188e+02  -0.252  0.8015
EducationMaster  3.576e+00  2.626e+00  7.118e+02   1.362  0.1738
Experience      6.053e-02  8.160e-02  7.162e+02   0.742  0.4585
PBYES          4.119e-01  3.111e-01  7.102e+02   1.324  0.1859
CPD            1.690e-02  2.416e-02  4.105e+02   0.699  0.4848
CTS            5.660e-01  3.215e-02  7.161e+02  17.606 <2e-16 ***
UnitMedical    -4.530e-01  3.188e-01  3.781e+01  -1.421  0.1635
DepSize        1.348e-02  1.652e-02  4.749e+01   0.816  0.4184
HospitalSetGeneral -1.589e+00  7.179e-01  3.669e+01  -2.214  0.0332 *
HospitalSize    -4.175e-04  5.965e-04  4.060e+01  -0.700  0.4880
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Correlation matrix not shown by default, as  $p = 14 > 12$ .

Use `print(x, correlation=TRUE)` or  
`vcov(x)` if you need it

## Random Slopes model

Do the CDMS is predicted by the variables at both individual-level and hospital level?

- Do the combined effect of nurse's knowledge and experience vary across different hospital department?
  - Outcome: Clinical decision-making
  - Fixed: **Knowledge, experience** and hospital settings
  - Random: **Knowledge and experience**
- Different scale?
  - So we gonna use grand mean centering: NKS -> NKS.GM

```
CTCDMR$NKS.GM <- scale(CTCDMR$NKS, scale = F)
CTCDMR$CTS.GM <- scale(CTCDMR$CTS, scale = F)
```

```
rs <- lmer(CDMS ~ NKS.GM + Experience + factor(HospitalSet) +
(1 + NKS.GM + Experience | hosp.dep),
data = CTCDMR, REML = FALSE, lmerControl(optimizer = 'bobyqa'))
summary(rs)
```

Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's method [lmerModLmerTest]

Formula: CDMS ~ NKS.GM + Experience + factor(HospitalSet) + (1 + NKS.GM + Experience | hosp.dep)

Data: CTCDMR

Control: lmerControl(optimizer = "bobyqa")

	AIC	BIC	logLik	deviance	df.resid
	4106.9	4157.2	-2042.4	4084.9	708

Scaled residuals:

	Min	1Q	Median	3Q	Max
	-3.1879	-0.6149	0.0070	0.6467	3.0585

Random effects:

Groups	Name	Variance	Std.Dev.	Corr
hosp.dep	(Intercept)	1.093e+01	3.30591	
	NKS.GM	3.031e-04	0.01741	0.57
	Experience	6.959e-02	0.26380	-0.99 -0.55
Residual		1.565e+01	3.95652	

Number of obs: 719, groups: hosp.dep, 36

Fixed effects:

	Estimate	Std. Error	df	t value	Pr(> t )
(Intercept)	34.364635	0.730043	29.216304	47.072	< 2e-16 ***
NKS.GM	0.197242	0.008952	31.100975	22.034	< 2e-16 ***
Experience	0.194085	0.051109	28.750185	3.797	0.000699 ***
factor(HospitalSet)General	-1.266490	0.454201	38.192612	-2.788	0.008213 **

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Correlation of Fixed Effects:

	(Intr)	NKS.GM	Exprnc
NKS.GM	0.528		
Experience	-0.919	-0.378	
fctr(HspS)G	-0.429	-0.602	0.136

## Three-level Multilevel analysis

(1 | Region/hosp.dep)

or

(1 | Region) + (1 | Region:DepartmentID)

Both will give the **same** results, but there are some analysis that need to use the longer code

## Null model

Short version

```
L3.M0a <- lmer(CDMS ~ 1
+ (1 | Region/hosp.dep), data = CTCDMR)
summary(L3.M0a)
```

Linear mixed model fit by REML. t-tests use Satterthwaite's method [

lmerModLmerTest]

Formula: CDMS ~ 1 + (1 | Region/hosp.dep)

Data: CTCDMR

REML criterion at convergence: 4744.4



Scaled residuals:

Min	1Q	Median	3Q	Max
-2.5720	-0.7162	0.0362	0.7438	2.9257

Random effects:

Groups	Name	Variance	Std.Dev.
hosp.dep:Region	(Intercept)	12.436	3.527
Region	(Intercept)	3.814	1.953
Residual		38.718	6.222

Number of obs: 719, groups: hosp.dep:Region, 37; Region, 6

Fixed effects:

	Estimate	Std. Error	df	t value	Pr(> t )
(Intercept)	36.076	1.031	4.200	35.01	2.43e-06 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Longer version

```
L3.M0b <- lmer(CDMS ~ 1
+ (1|Region)
+ (1|Region: DepartmentID), data = CTCDMR)
summary(L3.M0b)
```

Linear mixed model fit by REML. t-tests use Satterthwaite's method [  
lmerModLmerTest]

Formula: CDMS ~ 1 + (1 | Region) + (1 | Region:DepartmentID)

Data: CTCDMR

REML criterion at convergence: 4744.4

Scaled residuals:

Min	1Q	Median	3Q	Max
-2.5720	-0.7162	0.0362	0.7438	2.9257

Random effects:

Groups	Name	Variance	Std.Dev.
Region:DepartmentID	(Intercept)	12.436	3.527
Region	(Intercept)	3.814	1.953
Residual		38.718	6.222

Number of obs: 719, groups: Region:DepartmentID, 37; Region, 6

Fixed effects:

	Estimate	Std. Error	df	t value	Pr(> t )
(Intercept)	36.076	1.031	4.200	35.01	2.43e-06 ***

---  
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

## Random intercept model

Do the CDMS is predicted by the nurse's individual and hospital department variables?

```
L3.ri <- lmer(CDMS ~ CTS + NKS + HospitalSize + (1|Region)
+ (1|Region: DepartmentID), data = CTCDMR, REML = FALSE)
summary(L3.ri)
```

Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's method [lmerModLmerTest]

Formula:

CDMS ~ CTS + NKS + HospitalSize + (1 | Region) + (1 | Region:DepartmentID)

Data: CTCDMR

AIC	BIC	logLik	deviance	df.resid
3906.6	3938.6	-1946.3	3892.6	712

Scaled residuals:

Min	1Q	Median	3Q	Max
-3.5960	-0.5589	0.0381	0.6226	2.6628

Random effects:

Groups	Name	Variance	Std.Dev.
Region:DepartmentID	(Intercept)	0.27588	0.5252
Region	(Intercept)	0.06633	0.2575
Residual		12.87336	3.5879

Number of obs: 719, groups: Region:DepartmentID, 37; Region, 6

Fixed effects:

	Estimate	Std. Error	df	t value	Pr(> t )
(Intercept)	1.847e+00	8.332e-01	3.356e+02	2.217	0.0273 *
CTS	5.957e-01	3.131e-02	7.092e+02	19.024	<2e-16 ***
NKS	1.075e-01	8.622e-03	4.433e+02	12.469	<2e-16 ***
HospitalSize	-9.103e-04	3.323e-04	4.838e+01	-2.739	0.0086 **

```
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Correlation of Fixed Effects:

	(Intr) CTS	NKS
CTS	-0.640	
NKS	-0.031	-0.712
HospitalSiz	0.044	0.111
		-0.404

## Random Slope model

Do the CDMS is predicted by the variables at both individual-level, hospital level, and regional level? - Do the **CTS effect vary across different region?**

```
L3.RS <-lmer(CDMS ~ CTS.GM + Experience + Unit + HospitalSet
+ (1+ CTS.GM|Region)
+ (1|Region: DepartmentID),
data=CTCDMR, REML=FALSE,lmerControl(optimizer = 'bobyqa'))
summary(L3.RS)
```

Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's method [lmerModLmerTest]

Formula: CDMS ~ CTS.GM + Experience + Unit + HospitalSet + (1 + CTS.GM | Region) + (1 | Region:DepartmentID)

Data: CTCDMR

Control: lmerControl(optimizer = "bobyqa")

AIC	BIC	logLik	deviance	df.resid
4018.9	4064.6	-1999.4	3998.9	709

Scaled residuals:

Min	1Q	Median	3Q	Max
-3.3170	-0.6134	-0.0153	0.6388	2.8700

Random effects:

Groups	Name	Variance	Std.Dev.	Corr
Region:DepartmentID	(Intercept)	0.161755	0.40219	
Region	(Intercept)	0.716231	0.84630	
	CTS.GM	0.006558	0.08098	-0.01
Residual		14.734358	3.83854	

Number of obs: 719, groups: Region:DepartmentID, 37; Region, 6

Fixed effects:

	Estimate	Std. Error	df	t value	Pr(> t )
(Intercept)	34.07860	0.56786	25.76862	60.012	< 2e-16 ***
CTS.GM	0.82348	0.04292	7.81381	19.188	7.46e-08 ***
Experience	0.10075	0.02371	487.04291	4.250	2.56e-05 ***
UnitMedical	-0.04234	0.32014	27.42463	-0.132	0.895744
HospitalSetGeneral	1.35417	0.34664	36.16166	3.907	0.000394 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Correlation of Fixed Effects:

	(Intr)	CTS.GM	Exprnc	UntMdc
CTS.GM	0.212			
Experience	-0.611	-0.268		
UnitMedical	-0.361	-0.014	0.143	
HspstlStGnrl	-0.356	-0.226	0.100	-0.004

## Interactions and Cross-Level Interactions

**Cross-level** interaction: Experience (level 1) and hospitalSet (level 2)

Interactions: NKS and experience, CTS and NKS, CTS and Experience

```
L3.int <- lmer (CDMS ~ NKS.GM * Experience + CTS.GM * NKS.GM + CTS.GM * Experience + Experience * HospitalSet + (1|Region: DepartmentID), data = CTCDMR, REML = FALSE)
summary(L3.int)
```

Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's method [lmerModLmerTest]

Formula: CDMS ~ NKS.GM \* Experience + CTS.GM \* NKS.GM + CTS.GM \* Experience + Experience \* HospitalSet + (1 | Region) + (1 | Region:DepartmentID)  
Data: CTCDMR

AIC	BIC	logLik	deviance	df.resid
3858.7	3913.7	-1917.4	3834.7	707

Scaled residuals:

Min	1Q	Median	3Q	Max
-3.7588	-0.5765	0.0370	0.6624	2.7531

Random effects:

```

Groups              Name          Variance Std.Dev.
Region:DepartmentID (Intercept)  0.34686 0.5889
Region              (Intercept)  0.05199 0.2280
Residual                                11.82346 3.4385
Number of obs: 719, groups:  Region:DepartmentID, 37; Region, 6

Fixed effects:
              Estimate Std. Error      df t value Pr(>|t|)
(Intercept)   3.371e+01  5.668e-01  1.407e+02  59.464 < 2e-16
NKS.GM         8.787e-02  1.792e-02  6.863e+02   4.903 1.18e-06
Experience     2.408e-01  3.557e-02  4.891e+02   6.771 3.69e-11
CTS.GM        7.858e-01  6.637e-02  7.146e+02  11.839 < 2e-16
HospitalSetGeneral 1.939e+00  7.337e-01  2.421e+02   2.643 0.00876
NKS.GM:Experience 1.701e-03  1.246e-03  7.141e+02   1.365 0.17257
NKS.GM:CTS.GM   2.589e-03  9.005e-04  6.880e+02   2.875 0.00416
Experience:CTS.GM -1.942e-02  4.393e-03  7.142e+02  -4.420 1.14e-05
Experience:HospitalSetGeneral -2.473e-01  4.937e-02  6.301e+02  -5.010 7.08e-07

(Intercept)          ***
NKS.GM                ***
Experience             ***
CTS.GM                ***
HospitalSetGeneral    **
NKS.GM:Experience
NKS.GM:CTS.GM         **
Experience:CTS.GM     ***
Experience:HospitalSetGeneral ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Correlation of Fixed Effects:
              (Intr) NKS.GM Exprnc CTS.GM HsptSG NKS.GM:E NKS.GM:C E:CTS.
NKS.GM          0.227
Experience    -0.865 -0.244
CTS.GM        -0.137 -0.618  0.181
HsptlStGnrl  -0.717 -0.446  0.657  0.104
NKS.GM:Expr   -0.144 -0.851  0.251  0.464  0.404
NKS.GM:CTS.   -0.310  0.319  0.251  0.278 -0.081 -0.340
Expr:CTS.GM   0.242  0.515 -0.351 -0.870 -0.169 -0.500  -0.269
Exprnc:HsSG   0.576  0.418 -0.714 -0.135 -0.832 -0.555   0.047   0.236

```

## Plot interaction

```
graph_model(  
  model = L3.int,  
  y = CDMS,  
  x = Experience,  
  lines = HospitalSet,  
  errorbars = "none")
```

