The micrOMEGAs user's manual, version 6.2

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Abstract

We give an up-to-date description of the micrOMEGAs functions. Only the routines which are available for the users are described. Examples on how to use these functions can be found in the sample main programs distributed with the code.

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1 Introduction

micromegas is a code to calculate the properties of cold dark matter (CDM) in a generic model of particle physics. First developed to compute the relic density of dark matter, the code also computes the rates for dark matter direct and indirect detection. micromegas computes CDM properties in the framework of a model of particle interactions presented in CalcHEP format [1]. It is assumed that the model is invariant under a discrete symmetry like R-parity (even for all standard particles and odd for some new particles including the dark matter candidate) which ensures the stability of the lightest odd particle. Similarly in multi-component dark matter models, a discrete symmetry that guarantees the stability of the lightest particle in each of the dark matter sectors is assumed. The CalcHEP package is included in micromegas and used for matrix elements calculations. All annihilation and coannihilation channels are included in the computation of the relic density. This manual gives an up-to-date description of all micromegas functions. The methods used to compute the different dark matter properties are described in references [2–10]. These references also contain a more complete description of the code. In the following the cold dark matter candidate also called weakly-interactive massive particle (WIMP) will be denoted by χ . Starting with version 5.0, micromegas also allows to compute the abundance of feebly interacting dark matter candidates (FIMP) through the freeze-in mechanism [10]

micrOMEGAs is written in C and uses some Fortran routines mostly in external packages. The complete format for all functions can be found in include/.h (for C). Examples on how to use these functions are provided in the MSSM/main.c file.

2 Discrete symmetry in micrOMEGAs

micromegas exploits the fact that models of dark matter exhibit a discrete symmetry and that the fields of the model transform as $\phi \to e^{i2\pi X_{\phi}}\phi$ where the charge $|X_{\phi}| < 1$. The particles of the Standard Model are assumed to transform trivially under the discrete symmetry, $X_{\phi} = 0$. In the following all particles with charge $X_{\phi} \neq 0$ will be called odd and the lightest odd particle will be stable. If neutral, it can be considered as a DM candidate. Typical examples of discrete symmetries used for constructing single DM models are Z_2 and Z_3 . Multi-component DM can arise in models with larger discrete groups. A simple example is a model with $Z_2 \times Z_2$ symmetry, the particles charged under $Z_2(Z_2)$ will belong to the first (second) dark sector. The lightest particle of each sector will be stable and therefore a potential DM candidate. Another example is a model with a Z_4 symmetry. The two dark sectors contain particles with $X_{\phi} = \pm 1/4$ and $X_{\phi} = 1/2$ respectively. The lightest particle with charge 1/4 is always stable while the lightest particle of charge 1/2 is stable only if its decay into two particles of charge 1/4 is kinematically forbidden. micromegas assumes that all odd particles have names starting with '~', for example, ~o1 for the lightest neutralino. To distinguish the particles with different transformation properties with respect to the discrete group, that is particles belonging to different 'dark' sectors, we use the number of '~' at the beginning of the name of the particles. The maximal number of sectors is limited by the maximal length of the particle names (11 in the current version). For the relic density calculation we also assume that all particles in a given sector are in thermal equilibrium with each other. This last assumption is not necessarily valid, therefore the user has the possibility to split default sectors in subsectors where thermal equilibrium is maintained. See Section 6.5 for details.

Note that microMEGAs does not check the symmetry of the Lagrangian, it assumes that the name convention correctly identifies all particles with the same discrete symmetry quantum numbers. For models with FIMPs, new particles are considered to be in thermal equilibrium with the SM bath (\mathcal{B}) at high temperatures unless explicitly defined as being feeble, ie belonging to \mathcal{F} . Both \mathcal{B} and \mathcal{F} can contain odd or even particles, see section 6.7.

3 Downloading and compilation of micrOMEGAs

```
To download micrOMEGAs, go to
```

http://lapth.cnrs.fr/micromegas

and unpack the file received, micromegas_6.2.tgz, with the command

tar -xvzf micromegas_6.2.tgz

This should create the directory micromegas_6.2/ which occupies about 116Mb of disk space. You will need more disk space after compilation of specific models and generation of matrix elements. In case of problems and questions

3.1 File structure of micrOMEGAs

calculator calc specify the fonts for graphics in CalCHEP calchep.ini to compile the kernel of the package Makefile generator of matrix elements for micrOMEGAs CalcHEP_src/ external codes Packages/ to remove compiled files clean fileMap.txt contains the list of all files in the code contains a list of changes in recent versions history contains the manual: description of micrOMEGAs routines man/ to create a new model directory structure newProject micrOMEGAs code sources/ include/ include files for micrOMEGAs routines or external codes contains library micromegas.a when micromegas is compiled lib/ MSSM model directory MSSM/ to compile the code and executable for this model Makefile files with sample main programs main.c[pp] README Brief description on how to use the code mssmX.par Sample input files lib/ directory for routines specific to this model Makefile to compile the auxiliary code library lib/aLib.a source codes of auxiliary functions *.c *.f *.h CalcHEP working directory for the generation of work/ matrix elements to compile the library work/work_aux.a Makefile calchep Executable for CalcHEP lanhep/ directory containing lanhep source model files models/ directory for files which specifies the model files *1.mdl are used in micrOMEGAs sessions. Other *.mdl files are intended for CalcHEP interactive sessions free variables vars1.mdl func1.mdl constrained variables prtcls1.mdl particles lgrng1.mdl Feynman rules results/ so_generated/ storage of matrix elements generated by CalcHEP Directories of other models which have the same structure as MSSM/ Next-to-Minimal Supersymmetric Model [11, 12] NMSSM/ CPVMSSM/ MSSM with complex parameters [13, 14] IDM/ Inert Doublet Model [15] Simplified model with singlet charged lepton and real scalar DM LLL_scalar/ Little Higgs Model [16]

LHM/

RDM/	Scalar Leptoquark and two singlet fermions [17]
SingletDM/	Singlet scalar DM model with Z_2 symmetry [18]
STFM/	Singlet-triplet fermionic model [19]
Z3IDM/	Inert doublet model with Z_3 discrete symmetry [20, 21]
Z4IDSM/	Inert doublet and singlet model with Z_4 symmetry [20, 21]
Z5M/	Two scalar singlets model with Z_5 symmetry [22]
ZpPortal/	Simplified model with a Z' portal and fermion DM
mdlIndep/	For model independent computation of DM signals

Other models can be downloaded on the web, http://lapth.cnrs.fr/micromegas, for example: RHNM, a right-handed Neutrino Model [23], SM4, a toy model with a 4th generation of leptons and neutrino DM, UMSSM, an U(1) extension of the MSSM [24,25].

3.2 Compilation of CalcHEP and micrOMEGAs routines

The graphical interface of CalcHEP and micrOMEGAs uses X11 routines. Therefore X11 header files

```
/use/include/X11/*.h
```

are needed to compile these codes. If you do not have these files on your computer, you have to install the X11-devel package. Its name depends on the operating system, namely,

```
libX11-devel for Fedora/Scientific, old Darwin(Mac)
Xquartz (https://www.xquartz.org) new Mac
libX11-dev for Ubuntu/Debian [old Ubuntu]
libx11-dev for Ubuntu/Debian [new Ubuntu]
xorg-x11-devel for SUSE
```

Calchep and micromegas are compiled by gmake. Go to the micromegas directory and launch

gmake

If gmake is not available, then make should work like gmake. In principle micrOMEGAs defines automatically the names of C and Fortran compilers and the flags for compilation. If you meet a problem, open the file which contains the compiler specifications, CalcHEP_src/FlagsForSh, improve it, and launch [g]make again. The file is written in sh script format and looks like

```
# C compiler
CC="gcc"
# Flags for C compiler
CFLAGS="-g -fsigned-char"
# Disposition of header files for X11
HX11=
# Disposition of lX11
LX11="-1X11"
# Fortran compiler
FC="gfortran"
```

```
FFLAGS="-fno-automatic"
```

After a successful definition of compilers and their flags, micromegas rewrites the file FlagsForSh into FlagsForMake and substitutes its contents in all Makefiles of the package.

[g]make clean deletes all generated files, but asks permission to delete FlagsForSh. [g]make flags only generates FlagsForSh. It allows to check and change flags before compiling the codes.

3.3 External packages

micrOMEGAs is interfaced with a number of external packages, some of which are directly included in the micrOMEGAs distributions, those are stored in the directory /Packages, while others are downloaded automatically upon request.

The codes included in the micromegas distribution are:

Suspect2.41 [26]	spectrum calculator for MSSM		
NMSSMTools5.6.0 [27, 28]	spectrum calculator for NMSSM		
CPsuperH2.3 [13,29]	spectrum calculator for the MSSM and CPVMSSM		
LoopTools [30]	for computing some loop-induced processes		
lf2c	auxilliary library for Fortran-C converter		
LanHEP [31]	for generating model files		
maxGap [32]	for recasting experimental limits using		
	the Optimal Intervals method		
Lilith-2.1 [33-35]	for checking Higgs signal strengths		
FermiDwarfs [36-38]	To determine the limit from the FermiLAT experiment		
	on photons from Dwarf Spheroidal galaxies		

The packages that are downloaded automatically during runtime are:

SOFTSUSY [39]	SUSY spectrum generator
SPheno [40]	SUSY spectrum generator
SModelS [41-45]	for simplified-model constraints from LHC searches
superIso [46]	for flavor constraints
HiggsBounds $[47,48]$	for checking Higgs-sector constraints
HiggsSignals $[49,50]$	

The versions of the codes to be downloaded can be defined by the user via the parameter VERSION in the corresponding files:

```
MSSM/lib/ssusy_call.c include/SMODELS.inc include/hBandS.inc MSSM/lib/spheno_call.c sources/superIso.c
```

The URL for the source code and compilation instructions are presented in makefiles

```
SSUSY.makef SMODELS.makef HBOUNDS.makef
SPHENO.makef SUPERISO.makef HSIGNALS.makef
```

Note however, that care must be taken that new versions remain compatible with the existing interface structure. We also point out that Lilith SModelS and FermiDwarfs are python packages; for the latest versions of these codes, a python3 installation is required in addition to the compilers mentioned above.

3.4 Module structure of main programs

Each model included in micromegas is accompanied with sample files for C programs which call micromegas routines, the main.c files. These files consist of several modules enclosed between the instructions

#ifdef XXXXX #endif Each of these blocks contains some code for a specific problem

```
#define MASSES_INFO
                           //Displays information about mass spectrum
#define CONSTRAINTS
                           //Displays B_>sgamma, Bs->mumu, etc
#define HIGGSBOUNDS
                           //Calls HiggsBounds to constrain the Higgs sector
#define HIGGSSIGNALS
                           //Calls HiggsSignal to constrain the Higgs boson
#define SUPERISO
                           //calls SuperISO to compute flavour observables
#define LILITH
                           //Calls LiLith to constrain the Higgs sector
#define SMODELS
                           //Calls SModelS to constrain the new physics sector
                           //Constrain the new physics sector using the LHC monojet limit
#define MONOJET
#define OMEGA
                           //Calculates the relic density
#define FREEZEIN
                           //Calculates the relic density in the freeze-in mechanism
#define INDIRECT_DETECTION //Signals of DM annihilation in galactic halo
#define LoopGAMMA
                           //Gamma-Ray lines - available only in some models
#define RESET_FORMFACTORS
                           //Redefinition of Form Factors and other
                           //parameters
#define CDM_NUCLEON
                           //Calculates amplitudes and cross-sections
                           //for DM-nucleon collisions
#define CDM_NUCLEUS
                           //Calculates number of events for 1kg*day,
                           //recoil energy distribution for various nuclei
                           //and compares with experimental data.
#define NEUTRINO
                           //Calculates flux of solar neutrinos and
                           //the corresponding muon flux
#define DECAYS
                           //Calculates decay widths and branching ratios
#define CROSS_SECTIONS
                           //Calculates cross sections
#define CLEAN
                           //Removes intermediate files.
   The flag
```

```
#define SHOWPLOTS //switches on graphic facilities of micrOMEGAs.
```

All these modules are completely independent. The user can comment or uncomment any set of define instructions to suit his/her need.

3.5 Compilation of codes for specific models

After the compilation of micrOMEGAs one has to compile the executable to compute DM related observables in a specific model. To do this, go to the model directory, say MSSM, and launch

```
[g]make
```

This should generate the executable main using the main.c source file. In general

```
gmake main=filename.ext
```

generates the executable filename based on the source file *filename.ext*. For *ext* we support 2 options: 'c', 'cpp' which correspond to C and C++ sources. [g]make called in the model directory automatically launches [g]make in the subdirectories lib and work to compile

```
lib/aLib.a – the library of auxiliary model functions, and work/work_aux.a – the library of model particles, free and dependent parameters.
```

3.6 Command line parameters of main programs

The default versions of main.c programs need some arguments which have to be specified in command lines. If launched without arguments main explains which parameter are needed. As a rule main needs the name of a file containing the numerical values of the free parameters of the model. The structure of a file record should be

```
Name Value # comment (optional)
```

For instance, an Inert Doublet model (IDM) input file contains

```
Mh
      125
            # mass of SM Higgs
MHC
      200
            # mass of charged Higgs ~H+
MH3
            # mass of odd Higgs ~H3
      200
      63.2 # mass of ~X particle
MHX
1a2
     0.01
            # \lambda_2 coupling
            \# 0.5*(\lambda_3+\lambda_4+\lambda_5)
laL
     0.01
```

In other cases, different inputs can be required. For example, in the MSSM with input parameters defined at the GUT scale, the parameters have to be provided in a command line. Launching ./main will return

```
This program needs 4 parameters:

m0 common scalar mass at GUT scale

mhf common gaugino mass at GUT scale

a0 trilinear soft breaking parameter at GUT scale

tb tan(beta)

Auxiliary parameters are:

sgn +/-1, sign of Higgsino mass term (default 1)

Mtp top quark pole mass

MbMb Mb(Mb) scale independent b-quark mass

alfSMZ strong coupling at MZ

Example: ./main 120 500 -350 10 1 173.1
```

4 Global Parameters and constants

The list of the global parameters and their default values are given in Tables 1 and 2. The numerical value for any of these parameters can be simply reset anywhere in the code. The numerical values of the scalar quark form factors can also be reset by the calcScalarQuarkFF routine presented below. Some physical values evaluated by micrOMEGAs also are presented as global variables, see Table 3.

Table 1: Global input parameters of micrOMEGAs

Name	default value	units	comments
deltaY	0		Difference between DM/anti-DM abundances
K_dif	0.0112	$\rm kpc^2/Myr$	The normalized diffusion coefficient
$L_{-}dif$	4	kpc	Vertical size of the Galaxy diffusive halo
Delta_dif	0.7		Slope of the diffusion coefficient
Tau_dif	10^{16}	s	Electron energy loss time
Vc_dif	0	$\rm km/s$	Convective Galactic wind
Fermi_a	0.52	$_{ m fm}$	nuclei surface thickness
Fermi_b	-0.6	fm	parameters to set the nuclei radius with
Fermi_c	1.23	fm	$R_A = cA^{1/3} + b$
Rsun	8.5	kpc	Distance from the Sun to the center of the Galaxy
Rdisk	20	kpc	Radius of the galactic diffusion disk
rhoDM	0.3	GeV/cm^3	Dark Matter density at Rsun
vEarth	232	$\rm km/s$	Galaxy velocity of the Earth
vRot	220	$\rm km/s$	Galaxy rotation velocity at Rsun
vEsc	544	$\rm km/s$	Escape velocity at Rsun
etaSHMpp	0.2		η parameter of SHM++
betaSHMpp	0.9		β parameter of SHM++

Table 2: Global parameters of micrOMEGAs: nucleon quark form factors

Proton		Neutron			
Name	value	Name	value	comments	
ScalarFFPd	0.0191	ScalarFFNd	0.0273		
ScalarFFPu	0.0153	.0153 ScalarFFNu		Scalar form factor	
ScalarFFPs	0.0447	0.0447 ScalarFFNs 0			
pVectorFFPd	-0.427	pVectorFFNd	0.842		
pVectorFFPu	pVectorFFPu 0.842 pVectorFFNu		-0.427	Axial-vector form factor	
pVectorFFPs	-0.085	pVectorFFNs	-0.085		
SigmaFFPd	-0.23	SigmaFFNd	0.84		
SigmaFFPu	0.84	SigmaFFNu	-0.23	Tensor form factor	
SigmaFFPs	-0.046	SigmaFFNs	-0.046		

All physical constants used in relic density calculations are defined in the file include/micromegas_aux.h, they are listed in Table 4.

Table 3: Evaluated global variables

Name	units	comments	Evaluated by
Ncdm	integer	number of thermal sectors for DM particles.	sortOddParticles
CDM[k]	character	name of the lightest particles in each sector	sortOddParticles
		k=1Ncdm	
McdmN[k]	${ m GeV}$	Mass of CDM[k]	sortOddParticles
Mcdm	${ m GeV}$	minimal mass of odd particles	sortOddParticles
fracCDM[k]		fraction of CDM[k] in relic density.	darkOmega*
dmAsymm		Asymmetry between relic density of DM - \overline{DM}	darkOmega[FO]
Tstart, Tend	${ m GeV}$	Temperature interval	
		for solving the differential equation	darkOmega[2]

Table 4: Some useful constants included in micrOMEGAs

Name	Value	Units	Description
MPlank	1.22091×10^{19}	GeV	Planck mass
EntropyNow	2.8912×10^9	m^{-3}	Present day entropy, s_0
RhoCrit100	10.537	${\rm GeVm^{-3}}$	ρ_c/h^2 or ρ for $H=100 \mathrm{km/s/Mpc}$

5 Setting of model parameters, spectrum calculation, parameter display

The independent parameters of a given model are specified in work/models/vars1.mdl. Three functions can be used to set the values of these parameters:

- assignVal(name, val)
- assignValW(name, val)

assign value *val* to parameter *name*. The function assignVal returns a non-zero value if it cannot recognize a parameter name while assignValW writes an error message.

• readVar(fileName)

reads parameters from a file. The file should contain two columns with the following format (see also Section 3.6)

name value

readVar returns zero when the file has been read successfully, a negative value when the file cannot be opened for reading and a positive value corresponding to the line where a wrong file record was found.

The constrained parameters of the model are stored in work/models/func1.mdl. Some of these parameters are treated as *public* parameters. The *public* parameters include by default all particle masses and all parameters whose calculation requires external functions (except simple mathematical functions like sin, cos, ...). The parameters needed for the calculation of any *public* parameters in work/models/func1.mdl are also treated as *public*. It is possible to enlarge the list of *public* parameters. There are two ways to do

this. One can type * before a parameter name to make it *public* or one can add a special record in work/models/func1.mdl

%Local! |

Then all parameters listed above this record become *public*.

The calculation of the particle spectrum and of all *public* model constraints is done with:

• sortOddParticles(txt)

This routine has to be called after a reassignment of any input model parameter, after changing the sets of particles in thermal equilibrium (section 6.5), and after defining the set of feeble particles (section 6.7). The routine calculates the constrained parameters of the model. This routine returns a non zero error code for a wrong set of parameters, for example parameters for which some constraint cannot be calculated. The name of the corresponding constraint is written in txt. This routine also defines the number of dark sectors containing particles in chemical equilibrium, Ncdm, and finds the name of the lightest particle in each sector CDM[k] (k=1...Ncdm) as well as the minimal mass in each sector, McdmN[k]. It also defines the mass of the lightest dark particle Mcdm, this particle can either be a WIMP or a FIMP. 1

• qNumbers(pName, &spin2,&charge3,&cdim)

returns the quantum numbers for the particle pName. Here spin2 is twice the spin of the particle; charge3 is three times the electric charge; cdim is the dimension of the representation of $SU(3)_c$, it can be 1,3,-3,6,-6 or 8. The parameters spin2, charge3, cdim are variables of type int. The value returned is the PDG code. If pName does not correspond to any particle of the model then qNumbers returns zero.

• pdg2name(nPDG)

returns the name of the particle which PDG code is nPDG. If this particle does not exist in the model the return value is NULL.

• antiParticle(pName)

returns the name of the anti-particle for the particle pName.

pMass(pName)

returns the numerical value of the particle mass.

• nextOdd(n, &pMass)

returns the name and mass of the n^{th} odd particle assuming that particles are sorted according to increasing masses. For n=0 the output specifies the name and the mass of the CDM candidate.

• findVal(name, &val)

finds the value of variable name and assigns it to parameter val. It returns a non-zero value if it cannot recognize a parameter name.

• findValW(name)

returns the value of variable *name* and writes an error message if it cannot recognize a parameter name.

¹Note that Mcdm1 and Mcdm2 that were defined for two DM models are not defined anymore and have been replaced by McdmN[1] and McdmN[2].

The variables accessible by these last two commands are all free parameters and the constrained parameters of the model (in file model/func1.mdl) treated as public.

The following routines are used to display the value of the independent and the constrained public parameters:

• printVar(FD)

prints the numerical values of all independent and public constrained parameters into FD

• printMasses(FD, sort)

prints the masses of 'odd' particles (those whose names started with $\tilde{\ }$). If $sort \neq 0$ the masses are sorted so the mass of the CDM is given first.

• printHiggs(FD, sort)

prints the masses and widths of 'even' colorless scalars.

6 Relic density calculation

6.1 Switches and auxiliary routines

• VWdecay, VZdecay

Switches to turn on/off processes with off-shell gauge bosons in the final state for DM annihilation and particle decays. If VW/VZdecay=1, the 3-body final states will be computed for annihilation processes only while if VW/VZdecay=2 they will be included in coannihilation processes as well. By default the switches are set to (VW/VZdecay=1).² Note that micrOMEGAs calculates the width of each particle only once and stores the result in Decay Table. A second call to the function pWidth (whether an explicit call or within the computation of a cross section) will return the same result even if the user has changed the VW/VZdecay switch. We recommend to call

• cleanDecayTable()

after changing the switches to force micrOMEGAs to recalculate the widths taking into account the new value of VW/VZdecay. The sortOddParticles command which must be used to recompute the particle spectrum after changing the model parameters also clears the decay table.

• useSLHAwidth

Switch to determine how the particle widths are computed. If =1 the particle widths stored in a SLHA file (SUSY Les Houches Accord [51]) are downloaded by micrOMEGAs. These widths then do not depend on the VW/VZdecay switches. If =0 micrOMEGAs will calculate the widths, it will also do so if the switch is set to 1 and the widths are not provided in the SLHA file. By default this swith is set to 0.

The thermodynamics of the Universe is determined by the effective numbers of degrees of freedom $h_{eff}(T)$ and $g_{eff}(T)$,

$$\rho_R(T) = \frac{\pi^2}{30} g_{eff}(T) T^4$$
 and $s(T) = \frac{2\pi^2}{45} h_{eff}(T) T^3$. (1)

²Including the 3-body final states can significantly increase the execution time for the relic density computation.

Note that h_{eff} and g_{eff} are related by the equation ³

$$\frac{d\rho}{dT} = T\frac{ds}{dT} \tag{2}$$

These functions can be called with

• gEff(T)

which returns the effective number of degrees of freedom for the energy density of radiation at a bath temperature T, only SM particles are included.

• hEff(T)

which returns the effective number of degrees of freedom for the entropy density of radiation at a bath temperature T.

By default the tables for h_{eff} , g_{eff} correspond to the ones in Ref. [52] and can be found in the file sources/hgEff/DHS.thg. These default tables can be changed using

• loadHeffGeff(char*fname)

that reads the file *fname* located in the directory sources/hgEff. This file should contain 3 columns for T, $h_{eff}(T)$ and $g_{eff}(T)$. A positive return value corresponds to the number of lines in the table. A negative return value indicates the line which creates a problem (e.g. wrong format), the routine returns zero when the file fname cannot be opened.

The directory sources/hgEff also contains solutions described in Ref. [53], LM.thg, and in Ref. [54], HP_B.thg, HP_C.thg, as well as the tables used in DarkSUSY, GG.thg. The latter was used as default in previous versions of micrOMEGAs and does not include the contribution of the Higgs boson.

• hEffLnDiff(T)

returns the derivative of h_{eff} with respect to the log of the bath temperature, $\frac{d \log(h_{eff}(T))}{d \log(T)}$.

• Hubble(T)

returns the Hubble expansion rate in GeV units at a bath temperature T[GeV]. Hubble is defined via the density of the Universe and includes the contribution of radiation, dark matter, baryonic matter and dark energy,

$$H = \sqrt{\frac{8\pi\rho(T)}{3M_P^2}} \tag{3}$$

$$\rho(T) = \frac{\pi^2}{30} g_{eff}(T) T^4 + \mu_M \frac{2\pi^2}{45} h_{eff}(T) T^3 + \mu_{DE}^4$$
(4)

where M_P is the Planck mass, $\mu_M = 0.519$ eV, $\mu_{DE} = 2.24 \ 10^{-3}$ eV.

Entropy conservation

$$\frac{ds(T)}{dt} = -3Hs(T) \tag{5}$$

allows to write a relation between time and temperature:

$$\frac{dt}{dT} = -\left(1 + \frac{1}{3} \frac{d\log(h_{eff}(T))}{d\log(T)}\right) \frac{1}{H(T)T}$$
(6)

In particular micrOMEGAs has a function

• HubbleTime(T1,T2)

³This equation is not valid for $T \leq 1$ MeV, where photons and neutrinos have different temperatures.

which calculates the time interval in seconds during which the temperature of the Universe decreases from T1[GeV] to T2[GeV].

$$t = \int_{T_2}^{T_1} \left(-\frac{dt}{dT} \right) dT \tag{7}$$

The constant T2_73K gives the current temperature T= 2.725K. The age of the Universe calculated as Hubble(10,T2_73K) is 13.806 Gyr in agreement with the value quoted in the Particle Data Group [55] of 13.797(23) Gyr.

• freeStreaming(p/m, T1,T2)

calculates the length of the trajectory in Mpc units for a freely propagating particle between T1[GeV] and T2. The parameter p/m characterizes the initial velocity of the particle $v = \frac{p/m}{\sqrt{1+(p/m)^2}}$. Usually the free streaming length, λ_{FS} , is obtained by the integral over time

$$\lambda_{FS} = \int_{t_0}^{t_1} \frac{v(t)}{a(t)} dt \tag{8}$$

where a(t) is the scale factor, in particular $a = (s(T2_{-}73K)/s(T))^{\frac{1}{3}}$. In the code we compute the free-streaming length as integral over T.

$$\lambda_{FS} = \int_{T_2}^{T_1} \left(1 + \left(\frac{a(T)m}{a(T_1)p} \right)^2 \right)^{-\frac{1}{2}} \frac{1}{a(t)} \left(-\frac{dt}{dT} \right) dT \tag{9}$$

• improveCrossSection(n1,n2,n3,n4, Pcm, &cs)

allows to substitute a new cross-section for a given process instead of the one calculated by micrOMEGAs at tree level. Here $\tt n1,n2$ are the PDG codes for particles in the initial state and $\tt n3,n4$ for those in the final state. Pcm is the center of mass momentum and cs is the cross-section in $[GeV^{-2}]$. This function is called just after the calculation of the annihilation cross section in routines that calculates the relic density and indirect detection. $\tt micrOMEGAs$ calls this routine substituting for the last parameter the address of the memory where the calculated tree level cross section cs is stored. This function is useful if, for example, the user wants to include their loop improved cross-section calculation and/or the Sommerfeld effect. $\tt micrOMEGAs$ contains a dummy version of this routine disposed in $\tt sources/improveCS.c$ which does not modify the default cross section. This file also contains some commented out example of the code for the IDM model. To activate this facility the user has to write their own version of the $\tt improveCrossSection$ routine and place it in the directory MODEL/lib, then the $\tt dummy$ version will be ignored.

• SYukawa(a,b) and SHulthen(a,b)

These functions can be used to calculate Sommerfeld enhancement in the improveCrossSection routine for Yukawa and Hulthen potentials for s-channel scattering. The arguments are

$$a = \alpha/v \tag{10}$$

$$b = m_{med}/(m_r v) \tag{11}$$

where v is the relative velocity of colliding particles, m_{med} is the mass of the mediator, $m_r = \frac{m_1 m_2}{m_1 + m_2}$ - the reduced mass of colliding particles and $\alpha = \frac{e^2}{4\pi}$ where the coupling e is

defined from the Lagrangian that describes interactions of a Dirac particle (f_D) or of a charged scalar field (ϕ) with a scalar (h) or a vector (V_μ) mediator,

$$\mathcal{L} = eh\bar{f}_D f_D, \quad \mathcal{L} = ev_\mu \bar{f}_D \gamma^\mu f_D$$

$$\mathcal{L} = 2eM_\phi h\phi\phi^*, \quad \mathcal{L} = ieV_\mu (\partial^\mu \phi h\phi^* - \phi\partial^\mu \phi^*)$$
(12)

For Majorana particles \mathcal{L} contains an extra factor $\frac{1}{2}$. The Sommerfeld factor for pseudoscalar and axial-vector interactions is not available in micrOMEGAs, since it has been shown to be negligible [56]. The calculation of SYukawa is based on Eq.5.1-5.4 of [57]. Here we solve numerically the differential equation for DM elastic scattering in spherical coordinates and compute the wave function at zero to get the enhancement factor. For the Hulthen potential we use an analytical solution described in Eq. 5.6 of [58] . A demonstration of the Sommerfeld enhancement for both SYukawa and SHulthen can be found in the file mdlIndep/Sommerfeld.c.

6.2 Temperature interval and Error codes for routines calculating relic density

micrOMEGAs provides three routines, darkOmega, darkOmega2, darkOmegaN for calculating the relic density of one-component, two-component and N-component DM respectively by solving differential equations for the abundances

$$Y_i = n_i/\mathfrak{s} \tag{13}$$

where n_i is the number density of the i^{th} -component DM and $\mathfrak s$ is the entropy density. The equations contain the thermal equilibrium abundance $\overline{Y_i} = \frac{\overline{n_i}}{\mathfrak s}$ as well as $\chi\chi \to SM, SM$ annihilation cross sections $v\sigma(T)$. Decays of dark sector particles and processes such as $\chi, SM \to \chi', SM$ are taken into account only in darkOmegaN. Abundances are calculated at a temperature Tend that can be defined by the user. The default value is Tend= 10^{-3} GeV since in general the evolution of the relic abundance stops at higher temperatures. The initial temperature for integration, Tstart, is set by the condition

$$Y(Tstart) - \bar{Y}(Tstart) \approx 0.1\bar{Y}(Tstart).$$

These functions are described in the following subsections.

micrOMEGAs provides as well the routines darkOmegaTR, darkOmegaTR, darkOmegaNTR which also calculate the DM relic density. However the input parameters for these routines specify the initial temperature and abundances. The initial temperature is assigned to the variable Tstart.

All the darkOmega* routines have an &err parameter which returns the following error code:

- 32 no WIMP
- 64 Tstart is not found. It means that one of the DM component was never in thermal equilibrium with SM particles.
- 128 problem in solution of differential equation. It can appear if the equation is stiff because Tstart is very large.

The darkOmega* routines return NAN if one of these error appears.

For calculating $v\sigma(T)$ we use the program simpson to evaluate the integrals over scattering angle and energy of collisions. This program can return the following error codes

- 1 NAN in integrand;
- 2 too deep recursion;
- 4 loss of precision.

which are passed to &err. In general, these codes can be treated as warnings, although it can be useful to check the calculation of the problematic integrals using e.g. the gdb debugging tools. More information on this tool can be found in section 17.1. The error code err is a binary code which can signal several problems simultaneously.

6.3 Calculation of relic density for one-component Dark Matter models

All routines to calculate the relic density in version 3 are available in further versions. For these routines, the difference between dark sectors is ignored and the dark matter if the lightest particle among all those whose names starts with a $\tilde{}$. These routines are intended for models with either a Z_2 or Z_3 discrete symmetry.

• vSigmaA(T,fast,Beps), vSigmaS(T,fast,Beps) calculates the thermally averaged cross section for DM annihilation times velocity at a temperature T [GeV], $\sigma_v = \langle v\sigma \rangle$ for DM annihilation (A) and semi-annihilation. (S),

$$\langle v\sigma^A \rangle_T = \frac{T}{8\pi^4 \overline{n}(T)^2} \int ds \sqrt{s} K_1 \left(\frac{\sqrt{s}}{T}\right) \sum_{\tilde{\alpha},\tilde{\beta}} p_{\tilde{\alpha}\tilde{\beta}}^2(s) g_{\tilde{\alpha}} g_{\tilde{\beta}} \sum_{x \geq y} \sigma_{\tilde{\alpha}\tilde{\beta} \to xy}(s)$$
 (14)

$$\langle v\sigma^{S} \rangle_{T} = \frac{T}{8\pi^{4}\overline{n}(T)^{2}} \int ds \sqrt{s} K_{1} \left(\frac{\sqrt{s}}{T}\right) \sum_{\tilde{\alpha},\tilde{\beta}} p_{\tilde{\alpha}\tilde{\beta}}^{2}(s) g_{\tilde{\alpha}}g_{\tilde{\beta}} \sum_{x\tilde{\gamma}} \sigma_{\tilde{\alpha}\tilde{\beta}\to x\tilde{\gamma}}(s)$$
 (15)

where

$$\overline{n}(T) = \frac{T}{2\pi^2} \sum_{\tilde{\alpha}} g_{\tilde{\alpha}} m_{\tilde{\alpha}}^2 K_2(\frac{m_{\tilde{\alpha}}}{T}), \tag{16}$$

is the equilibrium number density of DM particles. Here $\tilde{\alpha}$, $\tilde{\beta}$, $\tilde{\gamma}$ is used for Odd particles and x,y for Even particles. Here only $2\to 2$ processes are included and $\sigma_{\tilde{\alpha}\tilde{\beta}\to x[\tilde{\gamma}/y]}$ is the cross section for the corresponding process averaged over the spins of incoming particles and summed over the spins of outgoing particles. K_1, K_2 are modified Bessel functions of the second kind, and $m_{\tilde{\alpha}}$ and $g_{\tilde{\alpha}}$ stand for the mass and the number of degrees of freedom of particle $\tilde{\alpha}$. Note, that if $\tilde{\alpha}\neq\tilde{\beta}$ then each $\sigma_{\tilde{\alpha}\tilde{\beta}}$ term will be presented twice. The value for $v\sigma$ is expressed in $[pb\cdot c]$. The parameter Beps defines the criteria for including coannihilation channels as for darkOmega described below. The fast=1/0 option switches between the fast/accurate calculations.

Note, that if $\tilde{\alpha} \neq \tilde{\beta}$, both $\sigma_{\tilde{\alpha}\tilde{\beta}}$ and $\sigma_{\tilde{\beta}\tilde{\alpha}} = \sigma_{\tilde{\alpha}\tilde{\beta}}$ will contribute to the sum. Moreover, the sum over α in Eq.14,15,16 runs over each particle and anti-particle separately.

In the low temperature limit

$$\langle v\sigma^A \rangle_T = \frac{1}{\overline{n}(T)^2} \sum_{\tilde{\alpha},\tilde{\beta}} \sum_{x \geq y} \bar{n}_{\tilde{\alpha}}(T) \bar{n}_{\tilde{\beta}}(T) \lim_{v \to 0} v\sigma_{\tilde{\alpha}\tilde{\beta} \to xy}(v)$$
 (17)

where v is the relative velocity. When only one particle and its anti-particle contribute to DM annihilation, Eq. 17 reads

$$\langle v\sigma^A \rangle_T = \frac{1}{2} \lim_{v \to 0} (v\sigma_{\tilde{\alpha},\tilde{\tilde{\alpha}}\to SM,SM}(v) + v\sigma_{\tilde{\alpha},\tilde{\alpha}\to SM,SM}(v))$$
 (18)

In many models, for example when DM is a Dirac fermion, there are no process $\tilde{\alpha}, \tilde{\alpha} \to SM, SM$ and our definition of $\langle v\sigma \rangle_T$ looks unnatural. However this definition has the advantage that it leads to a universal formula for the number of annihilation events in unit of space-time volume, regardless of the nature of DM,

$$\frac{dN}{dtd^3x} = \frac{1}{2} \langle v\sigma \rangle_T n^2 \tag{19}$$

where n is the number density of DM particles⁴.

After a call to vSigmaA or vSigmaS, the global array vSigmaTCh contains the contribution of different channels to vSigma. vSigmaTCh[i].weight specifies the relative weight of the i^{th} channel,

vSigmaTCh[i].prtcl[j] (j=0, 4) defines the particles names for the i^{th} channel. The last record in vSigmaTCh array has zero weight and NULL particle names.

In terms of $v\sigma^A$ and $v\sigma^S$ the abundance equation reads

$$\frac{dY}{dt} = -\langle v\sigma^A \rangle_T (Y^2 - \bar{Y}^2) - \frac{\langle v\sigma^S \rangle_T}{2} (Y^2 - Y\bar{Y})$$
 (20)

• vSigmaCC(T,cc,mode)

calculates the thermally averaged $cross\ section \times velocity$ for $2 \to 2,\ 2 \to 3$, and $2 \to 4$ processes. T is the temperature in [GeV], cc is the address of the code for each process. This address can be obtained by the function newProcess presented in Section 12. The returned value is given in $[c \cdot pb]$.

If $mode \neq 0$, vSigmaCC calculates the contribution of a given process to the total annihilation cross section, see Eq.14,15. The incoming particles should belong to the odd sector. For $2 \to 2$ processes the result after summation over all subprocesses should be identical to the one obtained via vSigma above. For this mode, vSigmaCC includes combinatorial factors: 2 if $\tilde{\alpha} \neq \tilde{\beta}$, an additional factor 2 if the incoming state is not self-conjugated, and a factor $\frac{1}{2}$ for semi-annihilation.

If mode = 0, vSigmaCC is defined by the integral

$$< v \sigma^{\tilde{\alpha} \tilde{\beta} \to X}>_T = \frac{1}{2T m_{\tilde{\alpha}}^2 m_{\tilde{\beta}}^2 K_2(\frac{m_{\tilde{\alpha}}}{T}) K_2(\frac{m_{\tilde{\beta}}}{T})} \int ds \sqrt{s} K_1(\frac{\sqrt{s}}{T}) p_{cm}^2(s) \sigma^{\tilde{\alpha} \tilde{\beta} \to X}(p_{cm}(s))$$

 $^{^4}$ {Eq.19 is valid if we assume a Maxwell-Boltzmann distribution, as is done for all routines that compute the relic density of WIMPs, the treatment of quantum statistics in the case of FIMPs is discussed in section $^{6.7}$.

where p_{cm} is the center of mass momentum of incoming particles. Note that

$$\lim_{T\to 0} vSigmaCC(T, cc, 0) = \lim_{p_{cm}\to 0} \sigma(p_{cm})v_{rel}(p_{cm})$$

where $v_{rel}(p_{cm})$ is the relative velocity of incoming particles. The result of vSigmaCC can be different from that of vSigma described above when there is an important contribution from NLSP's to the total number density of DM particles.

• darkOmega(&Xf,fast,Beps,&err)

calculates the dark matter relic density Ωh^2 . This routine solves the differential evolution equation using the Runge-Kutta method. $X_f = Mcdm/T_f$ characterizes the freeze-out temperature which is defined by the condition $Y(T_f) = 2.5\overline{Y}(T_f)$. For asymmetric DM this condition reads $2\sqrt{Y^+(T_f)Y^-(T_f)} = 2.5\overline{Y}(T_f)$. The value of X_f is given for information and is also used as an input for the routine that gives the relative contribution of each channel to Ωh^2 , see printChannels below. The fast = 1 flag forces the fast calculation (for more details see Ref. [3]). This is the recommended option and gives an accuracy around 1%. The parameter Beps defines the criteria for including a given coannihilation channel in the computation of the thermally averaged cross-section, [3]. The recommended value is $Beps = 10^{-4} - 10^{-6}$ whereas if Beps = 1 only annihilation of the lightest odd particle is computed. Non-zero error code means that the temperature where thermal equilibrium between the DM and SM sectors is too large Mcdm/T < 2 or $T > 10^5 \text{GeV}$.

darkOmega solves the differential equation for the abundance Y(T) in two temperature intervals [Tstart,Tf] and [Tf,Tend] [2]. The temperatures are defined by the conditions $Y(T_{start}) \approx 1.1\overline{Y}(T_{start}), Y(T_f) \approx 10\overline{Y}(T_f)$ while Tend is defined by the user. In the second interval, [Tf,Tend], the contribution of \overline{Y} is neglected and the differential equation is integrated explicitly. The solution in the interval [Tstart,Tf] is tabulated and can be displayed via the function YF(T). The equilibrium abundance can be accessed with the function Yeq(T).

• darkOmegaFO(&Xf, fast, Beps) calculates the dark matter relic density Ωh^2 using the freeze-out approximation.

• printChannels(Xf,cut,Beps,prcnt,FD)

name, e.g "*" in place of p1.

writes into FD the contributions of different channels to $(\Omega h^2)^{-1}$. Here Xf is an input parameter which should be evaluated first in darkOmega[FO]. Only the channels whose relative contribution is larger than cut will be displayed. Beps plays the same role as in the darkOmega[FO] routine. If $prcnt \neq 0$ the contributions are given in percent. Note that for this specific purpose we use the freeze-out approximation.

• oneChannel (Xf,Beps,p1,p2,p3,p4) calculates the relative contribution of the channel p1,p2 \rightarrow p3,p4 to $(\Omega h^2)^{-1}$. p1,...,p4 are particle names. To sum over several channels one can write "*" instead of a particle

• omegaCh is an array that contains the relative contribution and particle names for each annihilation channel. These array and function are similar to vSigmaTCh described above.

The array omegaCh if filled after calling either darkOmegaFO or printChannels.

• darkOmegaTR(Tstart, Ystart, fast, Besp)

This function is similar to darkOmega except that the initial temperature (Tstart) and abundance (Ystart) that are needed for solving the evolution equation have to be provided by the user as arguments to the function.

There is an option to calculate the relic density in models with $\overline{\rm DM}$ - $\overline{\rm DM}$ asymmetry. In this case, we assume that the number difference of $\overline{\rm DM}$ - $\overline{\rm DM}$ is conserved in all reactions. Thus a small difference in initial abundances can lead to a large $\overline{\rm DM}$ asymmetry after freeze-out as is the case for the baryon asymmetry.

• deltaY

describes the difference between the DM and anti-DM abundances for the models where the number of DM particles minus the number of anti-DM is conserved in decays and collisions. In such models deltaY is a constant during the thermal evolution of the Universe, see Ref. [7].

• dmAsymm

is defined by the equation

$$\Omega_{\pm} = \Omega \frac{1 \pm dm Asymm}{2}$$

and evaluated by micrOMEGAs while calculating the relic density with an initial asymmetry deltaY, see [7]. This parameter can also be reset after the relic density computation and will then be taken into account for direct and indirect detection rates.

darkOmegaExt(&Xf, vs_a, vs_sa)

calculates the dark matter relic density Ωh^2 using annihilation cross sections provided by external functions. Here vs_a is the annihilation cross section in $[c \cdot pb]$ as a function of the temperature in [GeV] units, Eq.14, while vs_sa is the semi-annihilation cross section, Eq.15. vs_a is required for all models, while vs_sa is relevant only for models where semi-annihilation occurs. The user can substitute NULL for vs_sa when semi-annihilation is not possible.

darkOmegaExt can also be used if processes other than $2 \to 2$ processes contribute to DM annihilation. In this case the appropriate annihilation or semi-annihilation cross sections can be calculated by vSigmaCC and the tabulated results stored in vs_a and vs_sa.

darkOmegaExt solves the Runge-Kutta equation in the interval [Tstart, Tend] where Tstart is defined automatically while Tend has a fixed value 10^{-3} GeV. darkOmegaExt is sensitive to effect of DM asymmetry.

One important application of darkOmegaExt is that it can be used to take into account off shell resonances in the calculation of the relic density. For this one has to first compute the corresponding $2 \to 3$ and/or $2 \to 4$ processes, this can be done with the functions:

• vSigmaPlus24(proc22, T, &err)

which calculates the contribution to $v\sigma$ for a $2 \to 4$ process associated with the $2 \to 2$ process for which outgoing particles are off-shell. Here proc22 is the name of the $2 \to 2$ process and T is the temperature. For each virtual particle, the decay channel with the largest branching fraction is chosen, the result is then divided by the corresponding branching fractions.

• vSigmaPlus23(proc22, T, &err)

calculates the contribution to $v\sigma$ for a $2\to 3$ process associated with the $2\to 2$ process (proc22) for which one of the outgoing particles can be off-shell. The contribution of the on-shell $2\to 2$ process (for example $\chi\chi\to BB'$) is subtracted. First, the 3-body cross-section for the process corresponding to one real and one virtual final state (corresponding to the main decay channel of the virtual particle) is computed. To ensure the proper behaviour near threshold one would need to compute the 4-body final state, rather we use a trick to approximate the 4-body result from the 3-body result after applying a K-factor. To obtain the K factor we assume that the 4-body matrix element is proportional to

$$|\mathcal{M}_4^2| \propto \left[m_{B'}^2 m_B^2 + \frac{1}{8} (s - m_{B'}^2 - m_B^2)^2 \right] \times$$
 (21)

$$\frac{\Gamma_B}{((m_B^2 - m_B'^2)^2 - \Gamma_B^2 m_B'^2)} \frac{\Gamma_B'}{((m_{B'}^2 - m_{B'}'^2)^2 - \Gamma_{B'}^2 m_{B'}'^2)}$$
(22)

where $m_B, m_{B'}$ and $m_B', m_{B'}'$ are respectively the virtual and pole masses of B and B', $\Gamma_B, \Gamma_{B'}$ the widths of the virtual particles, and s is taken in the range $2m_\chi < \sqrt{s} < m_B + m_{B'} + 10(\Gamma_B + \Gamma_{B'})$. We integrate this matrix element with $\Gamma_B = 0$ in order to simulate the 3-body result, then we integrate the same matrix element with the correct value for Γ_B . The ratio of these integrals gives the K factor. The same trick is applied automatically for calculating matrix elements with virtual W and Z if the flags VWdecay and VZdecay are activated. see Section 6.1 [7].

When first called, both vSigmaPlus23 and vSigmaPlus24 tabulate the cross sections of $2 \to 3$ and $2 \to 4$ processes respectively and keep results in memory for subsequent calls to calculate integrals over s. A call to sortOddParticles() cleans the tabulated cross sections.

To take into account the off-shell contribution in the computation of the relic density one has to create a new function which sums the contributions of vSigmaA and vSigmaPlus23 and vSigmaPlus24 and pass this function to darkOmegaExt. We have checked that both vSigmaPlus23 and vSigmaPlus24 give similar results.

The functions presented in this section are used to calculate the relic density of a single WIMP particle. If they are used for a model with multiple dark sectors, it will assume that all particles of the dark sectors are in chemical equilibrium with each other and will solve only for the relic density of the lightest particle of the dark sectors. The fractional contribution of heavier DM particles to the total relic density will be set to zero. A proper calculation of multi-component DM must rather rely on the routines described in sections 6.4 and 6.5. If the DM is feeble (FIMP), special routines have to be used to compute the relic density, see Section 6.7. The particles that are marked as feeble are just ignored by the routines described in this section.

6.4 Calculation of relic density for two-component Dark Matter models

• darkOmega2(fast, Beps)

Calculates Ωh^2 for either one- or two-components DM models. In the former case it should give the same result as darkOmega. The parameters fast and Beps have the same

meaning as for the darkOmega routine. The returned value corresponds to the sum of the contribution of the two DM components to Ωh^2 .

The two-component DM are referred to as CDM[1] and CDM[2] and correspond to the lightest particle in each sector. darkOmega2 also fills the elements of the array fracCDM[1], fracCDM[2] which contains the mass fraction of CDM[1] and CDM[2] in the total relic density, namely,

$$fracCDM[i] = \frac{\Omega_i}{\Omega_1 + \Omega_2} \tag{23}$$

These fractions are then used in routines which calculate the total signal from both DM components in direct and indirect detection experiments, nucleusRecoil, calcSpectrum, and neutrinoFlux. The user can change the global fracCDM[i] parameter before the calculation of these observables to take into account the fact that the value of the DM fraction in the Milky Way could be different than in the early Universe.

The routines that were described in section 6.3 are not available for two-component DM models. In particular the individual channel contribution to the relic density cannot be computed and DM asymmetry is ignored. After calling darkOmega2 the user can check the cross sections for each class of reactions (but not for individual processes) which were tabulated during the calculation of the relic density. The functions

• vsabcd F(T)

computes the sum of the cross sections for each class of reactions (a,b,c,d=0,1,2) tabulated during the calculation of the relic density. Here T is the temperature in [GeV] and the return value is $v\sigma$ in [c·pb]. These functions are defined in the interval [Tstart, Tend], where Tstart is a global parameter defined by darkOmega2, Tend= 10^{-3} GeV. Specifically the functions available are

The temperature dependence of the abundances can also be called by the user, the functions are named Y1F(T) and Y2F(T) and are defined only in the interval $T \in [Tend, Tstart]$. The equilibrium abundances are accessible via the Yeq1(T), Yeq2(T) functions and the deviation from equilibrium by the functions dY1F(T) = Y1F(T) - Y1eq(T) and dY2F(T) = Y2F(T) - Y2eq(T).

• darkOmega2TR(Tstart, Y1start, Y2start, fast, Beps)

This function is similar to darkOmega2 described above, however the initial temperature (Tstart) and abundances (Y1start, Y2start) that are needed for solving the evolution equations should be passed by the user as arguments to the function.

As was the case for routines for one component DM, darkOmega2 ignores particles declared as feeble. However one can use darkOmega2TR for a model which contains both a FIMP and a WIMP by specifying e.g. Y1start= Yeq for the WIMP in sector 1 and Y2start= 0 for the FIMP in sector 2. Note that the decay processes between particles of different sectors are not taken into account, for models, where these can be important we recommend rather to use darkOmegaN described in the next section.

6.5 Calculation of relic density for N-component DM taking into account coscattering processes.

In this section we present routines for the calculation of the relic density of N-component DM. The dark particles need to be divided into *sectors*, within each of which chemical equilibrium is observed. By default, this separation is defined by the number of "symbols in the beginning of the particle names. Thus, "x1 and "x2 denote dark particles of two different sectors. Usually, the sector assignment corresponds to the charge of the discrete symmetry responsible for DM stability, cf. section 2. However, in the absence of chemical equilibrium, the splitting into sectors needs to be done differently.

There are two types of processes which are responsible for chemical equilibrium: decays and coscattering (or DM conversion) processes. The latter corresponds to processes of the type

$$\chi_i, SM \to \chi_i', SM'$$
 (24)

In general the decay processes are responsible for chemical equilibrium at low temperatures, while coscattering processes maintain chemical equilibrium at high temperatures. The darkOmegaN routine calculates DM abundances taking into account both coscattering and decay processes which relate different sectors.

In the absence of chemical equilibrium, the splitting into sectors is done using the function

• defThermalSet(n, particles_list) which moves all particles mentioned in particles_list to sector n. All particles that were assigned to sector n before this command are returned to their default sectors specified by the number of $\tilde{\ }$ in the beginning of their names. Particles in the particles_list have to be separated by commas, and particle and anti-particle automatically belong to the same sector. By definition, sector 0 is the SM bath while sector -1 is used to define feeble particles which do not take part in freeze out. Such particles will be ignored when solving for the relic density. Sectors n > 0, are used for all other cases.

In general, defThermalSet can define a set which includes particles with different charges of the discrete symmetry group (different number of symbols) — in particular the set could include Z_2 odd particles as well as SM particles. In this case the user must keep in mind that the abundance equations are solved for sectors n i, 0 only. This entails that a Z_2 odd particle assigned to sector 0 will not be considered as potential DM candidate. The function returns an error code if $particles_list$ contains a particle name which is not defined in the model.

• printThermalSets() prints the contents of all particle sets specified by defChEset on the screen.

To verify whether chemical equilibrium is reached in one sector, one can use

- checkTE(n, T, mode, Beps) which checks the condition for chemical equilibrium in the n^{th} sector at temperature T. If mode=0, then both decay and co-scattering are taken into account. If mode=1 (2), then only decay (co-scattering) processes are taken into account. checkTE returns the minimal value of $\Gamma/H(T)$ obtained after testing all possible subsets of particles in sector n. The particle assignment corresponding to the minimal value of $\Gamma/H(T)$ is printed on the screen. This value has to be $\gg X_f$ to have chemical equilibrium, when this condition is satisfied the correction to the abundance calculated assuming chemical equilibrium is approximately $\Delta Y/Y \approx X_f H/\Gamma$.
- YdmNEq(T, α) calculates the thermal equilibrium abundance for particles of sector α ,

where α has to be presented by a text label. For instance, YdmNeq(T,"1").

- vSigmaN(T, channel) calculates the thermally averaged cross section $\langle v\sigma \rangle$ in [pb·c] units. Here *channel* is a text code specifying the reaction, e.g. vSigmaN(T,"1100") for $1,1 \leftrightarrow 0,0$ processes. If *channel* starts with an exclamation mark, then *vSigmaN* returns the results of the previous call of darkOmegaN. Otherwise vSigmaN recalculates all needed cross sections using the parameters *fast*, *Beps* defined in previous call of darkOmegaN or the parameters defined by a call to
- setFastBeps(fast,Beps)

To find the contribution of different processes to vSigmaN, one can call

• vSigmaNCh(T, channel, fast, Beps, &vsPb) which returns an array of annihilation processes together with their relative contributions to the total annihilation cross section. The cross section is given by the return parameter vsPb in [pb c] units. The elements of the array are sorted according to weights and the last element has weight=0. The structure of this array is identical to vSigmaTCh which was defined for one-DM models, see 6.3. The input parameter channel is written in text format. The memory allocated by outCh can be cleaned after usage with the command free(outCh). The following lines of code give an example on how to use this function

```
aChannel*outCh=vSigmaNCh(T, "1100", Beps, &vsPb);
for(int n=0;;n++)
{    if(outCh[n].weight==0) break;
    printf(" %.2E %s %s -> %s %s\n", outCh[n].weight,
    outCh[n].prtcl[0], outCh[n].prtcl[1], outCh[n].prtcl[2], outCh[n].prtcl[3]);
}
free(outCh);
```

- darkOmegaNTR(TR, Y, fast, Beps, &err) solves the equation of the thermal evolution of abundances starting from the initial temperature TR and returns the total Ωh^2 as described in [19]. The array Y has to contain the initial abundances at the temperature TR. After completion, Y[k] contains the abundances of sector k-1 at the temperature Tend defined by the user 5 . The parameter TR is assigned to the global variable Tstart.
- darkOmegaN(fast, Beps, &err) calls darkOmegaNTR to solve the equations of the thermal evolution of abundances in the temperature interval [Tend,Tstart]. In each sector, the function looks for the temperature T_i where $Y_i(T_i) \approx Y_{eq}(T_i)$. The minimum value of T_i is assigned to Tstart. i If Tstart is not found, then the error code 64 is generated and darkOmegaN returns NaN.
- YdmN(T, α) presents the evolution of abundances for particles of sector α calculated by darkOmegaN or darkOmegaNTR for $T \in [\texttt{Tend}, \texttt{Tstart}]$.

For the above functions, micrOMEGAs provides the possibility to selectively exclude part of the terms in the evolution equation. This is realized via the string ExcludedForNDM,

 $^{^5\}mathrm{By}$ default Tend= $10^{-3}\mathrm{GeV}$, however when the decay contribution is important it is preferable to choose a smaller value such as Tend= $10^{-8}\mathrm{GeV}$.

which can be assigned specific keywords. The keyword "DMdecay" excludes decay processes which contribute to the DM evolution, while the keyword "1100" excludes $1, 1 \leftrightarrow$ 0,0 processes. to exclude coscattering $(2,0\leftrightarrow 1,0 \text{ or } 1,0\leftrightarrow 2,0)$ processes, set

ExcludedForNDM="2010";

To reset and include all channels one must use ExcludedForNDM=NULL;.

Note that, for the computation of coscattering, the user defines which particles belong to sector 1 and sector 2. If all particles are in thermal equilibrium but one of them is nevertheless assigned to sector 2 which contains no other particle, the two abundance equations will be solved and should give the same result as the single abundance equation, that is Y(heavier particles) = 0 and Y(lightest particle) = Y of the single equation.

Finally, in the coscattering phase kinetic equilibrium may be lost; it is the responsibility of the user to verify that this is not the case for the parameters considered, so that the momentum-integrated Boltzmann equations remain a good approximation.

6.6 Scenario with slow Inflaton decay

During cosmic reheating, the inflaton ϕ is assumed to decay into SM radiation with a total decay width Γ . The dynamics of the background is driven by the set of Boltzmann equations for the inflaton energy density ρ_{ϕ} and the SM entropy density, [59]

$$\frac{d\rho_{\phi}}{dt} = -\Gamma \rho_{\phi} - 3H \rho_{\phi}$$

$$\frac{ds}{dt} = \Gamma \frac{\rho_{\phi}}{T} - 3Hs$$
(25)

$$\frac{ds}{dt} = \Gamma \frac{\rho_{\phi}}{T} - 3Hs \tag{26}$$

where $s = \frac{2\pi^2}{45} h_{eff}(T) T^3$. The Hubble expansion rate is given by

$$H = \sqrt{\frac{8\pi}{3} \frac{\rho_{\phi} + \rho_R}{M_P^2}} \tag{27}$$

and the SM energy density, ρ_R , by

$$\rho_R = \frac{\pi^2}{30} g_{eff}(T) T^4. \tag{28}$$

The function

•getInflDecay(HI, Gamma, &Trh, &Tmax, &aEnd)

solves Eqs. (25) and (26). The solution is stored in the tabulated functions Ta(a) and Ha(a), which respectively return the temperature and the Hubble parameter as a function of the scale parameter $a \in [1, aEnd]$. These functions are available to the user. Here, HI is the Hubble rate at the end of inflation when HI is generated by the inflaton only. Gamma is Γ_{ϕ} , the decay width of the inflaton. Trh, Tmax and aEnd are return parameters. They represent respectively the temperature when the energy density of inflation becomes equal to the energy density of SM particles, the maximal temperature reached, and the expansion factor at the temperature Tend. This temperature is defined by the user as a global parameter. The function getInflDecay returns 0 when it can find a solution to the differential equations or 128 otherwise.

The function

•darkOmegaInfl(Beps, &isWimp, &err) solves the DM evolution equation,

$$\frac{dz_{DM}}{da} = -\frac{1}{Ha^4} \left(\langle v\sigma_A \rangle \left(z_{DM}^2 - \bar{z}_{DM}^2 \right) + \langle v\sigma_S \rangle \left(z_{DM}^2 - z_{DM} \bar{z}_{DM} \right) \right) \tag{29}$$

where $z_{DM}=n_{DM}a^3$ and $\bar{z}_{DM}=\bar{n}_{DM}a^3$ with n_{DM} the DM number density and \bar{n}_{DM} the equilibrium DM number density. It uses Ta and Ha constructed by getInflDecay. The main return value of this routine is the DM relic density $\Omega_{\chi}h^2$. The auxiliary output parameters are integer isWIMP, and integer err. The parameter isWIMP indicates whether the DM candidate behaves as a WIMP, that is, if the final relic density decreases when the cross section increases, then isWIMP=1, otherwise isWIMP=0. The error code err indicates whether there is a problem with the solution of the differential equations (26) and (25), in which case the 8th bit of the error code err is 1, or with the solution of Eq. (29), then the 9th bit is 1. The lowest bits contain information about problems with numerical integration and should be treated as warnings. The parameter Beps has the same meaning as in other darkOmega routines; it determines the condition to include Boltzmann suppressed channels [2].

The evolution of the DM abundance is stored in an array and is available via the functions Za(a), ZaEq(a), Ya(a), while the equilibrium abundance is stored in YaEq(a).

There is a similar function for N-component DM:

•darkOmegaNInfl(Beps, &err)

Here the argument isWimp is omitted because some of the components can be WIMPs while others are FIMP. The evolution of the DM abundances are stored in an array and are available via the functions Za(a), ZaEq(a), Ya(a), while the equilibrium abundance is stored in YaEq(a). As above the evolution of the abundances is available via the functions ZaN, ZaNEq, YaN, YaNEq while vSigmaN gives the thermally averaged cross-section as described in section 6.5.

6.7 Calculation of relic density for freeze-in

Several routines are provided in micromegas to compute the DM abundance in freeze-in scenarios. These can be found in the file sources/freezein.c. The first line of this file contains the statement

//#define NOSTATISTICS

This statement can be uncommented for micromegas to compute the relic density assuming a Maxwell-Boltzman distribution. This option is faster.

The auxiliary functions that are needed for the computation of the factors from statistical quantum mechanics are

• Stat2($P/T, x_Y, x_1, x_2, \eta_1, \eta_2$),

returns the S function defined in Eq. (30), that takes into account particle statistical distributions for the decay of a mediator $Y \to a, b$ of fixed momentum P.

$$S(P/T, x_Y, x_a, x_b, \eta_a, \eta_b) = \frac{1}{2} \int_{-1}^{1} dc_\theta \frac{e^{E_Y/T}}{(e^{E_a(c_\theta)/T} - \eta_a)(e^{E_b(c_\theta)/T} - \eta_b)} .$$
 (30)

where $x_i \equiv m_i/T$, E_a, E_b are the energies of the outgoing particles and $\eta_i \equiv \pm e^{\mu_i/T}$ and μ_i is the chemical potential.

• K1to2($x_1, x_2, x_3, \eta_1, \eta_2, \eta_3$), returns the \tilde{K}_1 function defined in Eq. (31), that takes into account particle statistical distributions.

$$\tilde{K}_{1}(x_{1}, x_{2}, x_{3}, \eta_{1}, \eta_{2}, \eta_{3}) \equiv \frac{1}{(4\pi)^{2} p_{\text{CM}} T} \int \prod_{i=1}^{3} \left(\frac{d^{3} p_{i}}{E_{i}} \frac{1}{e^{E_{i}/T} - \eta_{i}} \right) e^{E_{1}/T} \delta^{4} \left(P_{1} - P_{2} - P_{3} \right)$$
(31)

The code does *not* check whether or not a particle is in thermal equilibrium with the SM thermal bath and that it is the responsability of the user to specify which particles belong to the bath, \mathcal{B} , or are out of equilibrium, \mathcal{F} . This can be done through the function

• toFeebleList(particle_name)

which assigns the particle_name to the list of feebly interacting ones (i.e. those which belong to \mathcal{F}). Feebly interacting particles can be odd or even. This function can be called several times to include more than one particle. All odd or even particles that are not in this list are assumed to be in thermal equilibrium with the SM and belong to \mathcal{B} . The treatment of the particles that belong to \mathcal{F} for the computation of Ωh^2 within the freeze-in routines is described below. Calling toFeebleList(NULL) will reassign all particles to \mathcal{B} .

The actual computation of the freeze-in DM abundance can be performed with the help of three functions:

• darkOmegaFiDecay(TR, bathParticle, feebleParticle) calculates the abundance of feebleParticle resulting from the decay of bathParticle The equations used for the three different cases are described in [10].

For the freeze-in routines that compute $2 \to 2$ processes described below (darkOmegaFi and darkOmegaFi22, the effect of the thermal masses of particles in the t/u - channel can be simulated by introducing a cut on the Mandelstam variables t or u. The thermal masses, M_T , are defined by the user in the array Tkappa,

$$M_T = T \cdot Tkappa[k] \tag{32}$$

where k in the internal particle number. This number can be obtained by

k=abs(pTabPos(pName))-1

The cut is applied on $t > t_{max} - M_T^2$ for a t-channel propagator and on $u > u_{max} - M_T^2$ for a u-channel propagator. By default Tkappa[k]=0 for all particles.

• darkOmegaFi22(TR, Process, feebleParticle, &err) calculates the DM abundance of feebleParticle taking into account only $2 \to 2$ Process. For example "b,B ->~x1,~x1" for the production of DM (here ~x1) via $b\bar{b}$ scattering. This routine allows the user to extract the contribution of individual processes. TR is the reheating temperature. err is the returned error code, it has the following meaning 1: the requested processes does not exist

- 2: $2 \rightarrow 2$ process is expected
- 3: can not calculate local parameters // some constrain parameters can not be calculated.
- 4: $T_{end} >= T_R$, or $T_{end} = 0$
- 5: one of the incoming particles belong to \mathcal{F} .
- 6: None of the outgoing particles are odd and feeble.
- 7: Lost of precision in temperature integrand
- 8: Pole in temperature integrand
- 9: NAN in temperature integrand
- 10: Lost of precision in sqrt(s) integrand
- 11: Pole in sqrt(s) integrand
- 12: NAN in sqrt(s) integrand
- 13: Lost of precision in angle integrand
- 14: Pole in angle integrand
- 15: NAN in angle integrand
- 16: lost of precision caused by diagram cancellation

• darkOmegaFi(TR,feebleParticle &err)

calculates the DM abundance after summing over all $2 \to 2$ processes involving particles in the bath $\mathcal B$ in the initial state and at least one particle in $\mathcal F$ in the final state. The routine checks the decay modes of all bath particles and if one of them has no decay modes into two other bath particles, the $2 \to 2$ processes involving this particle are removed from the summation and instead the contribution to the DM abundance computed from the routine darkOmegaFiDecay is included in the sum. This is done to avoid appearance of poles in the corresponding $2 \to 2$ cross-section. We recommend for such models to compute individual $2 \to 2$ processes with darkOmegaFi22 described above. As before, we assume that all odd FIMPs will decay into the lightest one which is the DM. T_R has the same meaning as above. err is the returned error code, err=1 if feeble particles have not been defined.

• printChannelsFi(cut,prcnt,filename)

writes into the file filename the contribution of different channels to Ωh^2 . The cut parameter specifies the lowest relative contribution to be printed. If $\mathtt{prcnt} \neq 0$, the contributions are given in percent. The routine $\mathtt{darkOmegaFi}$ fills the array $\mathtt{omegaFiCh}$ which contains the contribution of different channels ($2 \to 2$ or $1 \to 2$) to Ωh^2 . $\mathtt{omegaFiCh[i]}.\mathtt{weight}$ specifies the relative weight of the ith channel, $\mathtt{omegaFiCh[i]}.\mathtt{prtcl[j]}$ ($\mathtt{j=0}$, 4) defines the particles names for the ith channel. The last record in the array $\mathtt{omegaFiCh}$ has zero weight and NULL particle names.

The temperature evolution of the abundances generated by these three routines can be obtained by calling the function YFi(T) in the interval $T \in [\texttt{Tend}, \texttt{Tstart}]$ where Tstart is set internally by the three routines and is assigned to the variable TR.

Note that if no particle has been declared as being feebly interacting, the freeze-out routines darkOmega, darkOmegaFO, and darkOmega2 [8] will work exactly like in previous versions of micrOMEGAs. A non-empty feeblelist, however, will affect these routines since micrOMEGAs will exclude all the particles in this list from the computation of the relic density via freeze-out. To compute the relic density of particles in feeblelist one has to use the darkOmegaFi function (or the other routines describe in this section) for each of

these particles. Alternatively the relic density of feeble particles can be computed using the darkOmega*TR routines described in section 6.4,6.5 by setting the initial abundance of these particles to zero. Note that the result can differ from the one obtained by the darkOmegaFi routines since these take into account the Maxwell-Boltzmann statistics. ⁶

7 Direct detection

7.1 Amplitudes for elastic scattering

• nucleonAmplitudes(CDM,pAsi,pAsd,nAsi,nAsd)

calculates the amplitudes for CDM-nucleon elastic scattering at zero momentum. pAsi(nAsi) are spin independent amplitudes for protons(neutrons) whereas pAsd(nAsd) are the corresponding spin dependent amplitudes. Each of these four parameters is an array of dimension 2. The zeroth (first) element of these arrays gives the χ -nucleon amplitudes whereas the second element gives $\overline{\chi}$ -nucleon amplitudes. Amplitudes (in GeV⁻²) are normalized such that the total cross section for either χ or $\overline{\chi}$ cross sections is

$$\sigma_{tot} = \frac{4M_{\chi}^2 M_N^2}{\pi (M_{\chi} + M_N)^2} (|A^{SI}|^2 + 3|A^{SD}|^2)$$
(33)

nucleonAmplitudes depends implicitly on form factors which describe the quark contents in the nucleon. These form factors are global parameters (see Table 1 for default values)

where Type is either "Scalar", "pVector", or "Sigma", FFP and FFN denote proton and neutron and q specifies the quark, d, u or s. Heavy quark coefficients are calculated automatically.

micrOMEGAs automatically takes into account loop contributions from box diagrams as calculated in [60] (DM spin 1/2 case) and [61] (DM spin 0 and 1 cases).

nucleon Amplitudes does not take into account an operator involving DM-DM-gluon-gluon interactions. It is by default assumed that such interactions are generated at one-loop from DM interactions with heavy colored particles and this loop-induced contribution of heavy coloured particles to DM-DM-gluon-gluon interactions ⁷ is taken into account automatically. Thus a direct contribution might lead to double counting. Note that to avoid double counting an Hgg vertex in the model file will also be ignored. To include the contribution of an additional operator that involves DM interactions with gluons, it is rather recommended to introduce a new auxiliary heavy color (dim=3) fermion in the model file, the direct detection amplitude that results from the effective operator $\alpha_s G_{\mu\nu} G^{\mu\nu} \bar{\chi} \chi$ can be represented by a term $-12\pi M_F \bar{F} F \bar{\chi} \chi$, where M_F is the fermion mass which should be chosen large enough to ensure that F does not contribute to other processes.

• calcScalarQuarkFF $(m_u/m_d, m_s/m_d, \sigma_{\pi N}, \sigma_s)$ computes the scalar coefficients for the quark content in the nucleon from the quark mass

⁶Note that in previous versions of micrOMEGAs the relic density of darkOmegaFi was rescaled when it was not the lightest particle in the dark sector to take into account the fact that the FIMP will eventually decay into the DM. In this version this rescaling has to be done by the user.

⁷Heavy quarks include c,b,t quarks

ratios m_u/m_d , m_s/m_d as well as from $\sigma_{\pi N}$ and σ_s . The default values given in Table 2 are obtained for $\sigma_s = 42 \text{MeV}$, $\sigma_{\pi N} = 34 \text{MeV}$, $m_u/m_d = 0.56$, $m_s/m_d = 20.2$ [62]. The function calcScalarQuarkFF(0.553,18.9,55.,243.5) will reproduce the default values of the scalar quark form factors used in micrOMEGAs2.4 and earlier versions.

7.2 Scattering on nuclei

• nucleusRecoil(f,A,Z,J,Sxx,dNdE)

This is the main routine of the direct detection module. The input parameters are:

 $\diamond\,$ f - the DM velocity distribution normalised such that

$$\int_0^\infty f(v)dv = 1 \tag{34}$$

The units are km/s for v and s/km for f(v).

- ♦ A atomic number of nucleus;
- ♦ Z number of protons in the nucleus;
- ♦ J nucleus spin;
- \diamond void Sxx(double p, double*S00,double*S01,double*S11) is a routine which calculates nucleus form factors for spin-dependent interactions (S00,S01,S11), it depends on the momentum transfer p in fm^{-1} . For nucleus with zero spin one has to substitute NULL for this parameter;
- ♦ The distribution over recoil energy is stored in the array dNdE

$$dNdE[n] = \frac{dN}{dE_n}$$

in units of (1/keV/kg/day) where

The include/micromegas.h file contains predefined values for charges and spins of atomic nucleus. They are called with Z_{Name} and J_{Name} and J_{Name} where Name is the name of an atom. For example, for ^{73}Ge , a call to this routine will be:

```
nucleusRecoil(Maxwell,73,Z_Ge,J_Ge73,SxxGe73,dNdE);
```

The returned value of the function nucleusRecoil gives the number of events per day and per kilogram of detector material. The result depends implicitly on the global parameter rhoDM, the density of DM near the Earth. This routine is based on the spin-dependent and spin-independent cross sections, but also takes into account the modification of the

recoil energy distribution caused by a light t- channel propagator. For a light mediator, the nucleus recoil energy distribution reads

$$\frac{dN_A}{dE} = \frac{M_{\text{med}}^4}{(M_{\text{med}}^2 + 2M_A E)^2} \frac{dN_A^{std}(M_{DM}, \sigma_0)}{dE}$$
(35)

where N_A^{std} is the standard expression for the number of recoil events for a point-like interaction with a DM- nucleon elastic scattering cross-section σ_0 , M_{med} is the mass of the t-channel mediator. The factor to correct the recoil energy distribution as in Eq.35 is introduced automatically in the code after an internal check for the existence of a light mediator. For a complex WIMP and if DM has only one component, nucleusRecoil averages over χ and $\overline{\chi}$ taking into account the asymmetry between χ and $\overline{\chi}$. For models with 2 DM particles the result takes into account the relative contribution of each DM particle through the parameter fracCDM2.

• dNdERecoil (E, dNdE) interpolates the dNdE table.

Nucleus form factors 7.2.1

The form factors for the spin independent (SI) cross section are defined by the Fermi distribution

$$F_A(q) = \int e^{-qx} \rho_A(|x|) d^3x$$

$$\rho_A(r) = \frac{c_{\text{norm}}}{1 + exp((r - R_A)/a}$$
(36)

$$\rho_A(r) = \frac{c_{\text{norm}}}{1 + exp((r - R_A)/a} \tag{37}$$

$$R_A = cA^{\frac{1}{3}} + b (38)$$

where a, b, c are defined with the global parameters Fermi_a, Fermi_b, Fermi_c. The spin dependent form factors collected in [63] are implemented in micrOMEGAs [5]:

SxxF19 SxxNa23 SxxNa23A SxxA127 SxxSi29 SxxSi29A SxxK39 SxxGe73 SxxGe73A SxxNb92 SxxTe125 SxxTe125A SxxI127 SxxI127A SxxXe129 SxxXe129A SxxXe129M SxxXe131 SxxXe131A SxxXe131B SxxXe131Me

Here the characters after the atomic number are used to distinguish different implementations of the form factor for the same isotope. Recently we have added some form factors used in XENON1T and PICO-60 experiments. See Table 5.

The minimal and maximal values for the SD form factors, $S_{00}(q), S_{01}(q), S_{11}(q)$, are computed in Ref. [65] within the shell model. The ID SHELL corresponds to the average

$$S_{ab} = (S_{ab}^{min} + S_{ab}^{max})/2 (39)$$

which are obtained from the minimum and maximum fitted values in Table VI in [65].

The ID SHELLm corresponds to the form factors which lead to the most robust exclusion. Since S_{ab}^{min} often leads to a negative value for the subdominant component of the form factor, and this has no physical meaning, we use rather the minimum value of the protononly, S_p^{min} , and neutron-only, S_n^{min} , form factors also given in [65]. These correspond to

Name	reference	ID
SxxF19EF		
SxxXe131EFT	[64]	EFT
SxxXe129EFT		
SxxF19SHELL		
SxxXe129SHELL	[65]	SHELL
SxxXe131SHELL		
SxxF19SHELLm		
SxxXe129SHELLm	[65]	SHELLm
SxxXe131SHELLm		

Table 5: Implemented form factors

the minimal form factor for the case when only one type of interaction (with proton or neutron) is included. With this we construct the nucleus form factors

$$S_{00} = \frac{1}{4} \left(S_p^{min} + S_n^{min} \pm 2\sqrt{S_p^{min} S_n^{min}} \right)$$

$$S_{11} = \frac{1}{4} \left(S_p^{min} + S_n^{min} \mp 2\sqrt{S_p^{min} S_n^{min}} \right)$$

$$S_{01} = \frac{1}{2} (S_p^{min} - S_n^{min})$$
(40)

The sign in Eq.40 is chosen to reproduce the ratio $S_{00}(0)/S_{11}(0)$ for the central value of the form factors in Ref. [65].

For nuclei whose form factors are not known one can use the routine

• nucleusRecoilO(f,A,Z,J,Sp,Sn,dNdE)

which is similar to the function nucleusRecoil except that the spin dependent nuclei form factors are described by Gauss functions [5] whose values at zero momentum transfer are defined by the coefficients Sp,Sn. Predefined values for the coefficients Sp,Sn in the format

$$Sp_{Nucleus\ Name} \{Atomic\ Number\} \}$$

 $Sn_{Nucleus\ Name} \{Atomic\ Number\} \}$

are presented in the file include/micromegas.h. For example,

#define Sn_He3 0.552 #define Sn_017 0.5

7.2.2 Velocity distribution

Ignoring the direction of motion of DM particles and the small effect of DM acceleration by the gravitational field of the Sun, the DM velocity distribution in the vicinity of the direct detection experiment is given by

$$f(\mathbf{v}) = \int_{|\vec{v}| < \mathbf{v} Esc} d^3 \vec{v} F_G(\vec{v} - \vec{v}_{Earth}) \delta(\mathbf{v} - |\vec{v}|)$$
(41)

where F_G is the DM velocity distribution in the frame of the galaxy, \vec{v}_{Earth} is the velocity of the Earth in the Galaxy and vEsc is the maximal DM velocity in the Sun's orbit due to the finite gravitational potential of our Galaxy. vEsc and vEarth= $|\vec{v}_{Earth}|$ are global parameters of micrOMEGAs.

The velocity distributions that are available in micromegas are the following

• Maxwell(v)

returns

$$F_G^M(\mathbf{v}) = c_{\text{norm}} \frac{1}{(2\pi \mathbf{v} \text{Rot}^2)^{3/2}} \exp\left(-\frac{(\vec{v})^2}{\mathbf{v} \text{Rot}^2}\right) \theta(\mathbf{v} \text{Esc} - |\vec{v}|)$$
(42)

which corresponds to the isothermal model. Here vRot is the orbital velocity of stars in the Milky Way, it is also a global parameter of micrOMEGAs. $c_{\mathtt{norm}}$ is the normalization factor,

$$c_{\text{norm}}^{-1} = \operatorname{erf}\left(\frac{\text{vEsc}}{\text{vRot}}\right) - \frac{2}{\sqrt{\pi}} \frac{\text{vEsc}}{\text{vRot}} \exp\left(-\frac{\text{vEsc}^2}{\text{vRot}^2}\right)$$
(43)

• SHMpp(v)

returns the velocity distribution SHM++ proposed in [66].

$$F_G(\vec{v}) = (1 - \eta)F_G^M(v) + \eta F_G^S(v)$$
(44)

This distribution consists of two components. The first, $F_G^M(\vec{v})$, is the standard Maxwell velocity distribution described above. The second component is the velocity distribution from the *Gaia* sausage [67,68], it is not spherically symmetric and is defined by the anisotropy parameter β with

$$F_G^S(\vec{v}) = \frac{c_{\text{norm}}}{(2\pi)^{3/2} \Delta v_r \Delta v_\theta \Delta v_\phi} \exp\left(-\left(\frac{v_r}{\Delta v_r}\right)^2 - \left(\frac{v_\theta}{\Delta v_\theta}\right)^2 - \left(\frac{v_\phi}{\Delta v_\phi}\right)^2\right) \theta(\text{vEsc} - |\vec{v}|)$$
(45)

where

$$\Delta v_r = \frac{\text{vRot}}{\sqrt{1 - \frac{2}{3}\beta}}, \quad \Delta v_\phi = \Delta v_\theta = \frac{\text{vRot}\sqrt{1 - \beta}}{\sqrt{1 - \frac{2}{3}\beta}}$$
(46)

and

$$c_{\text{norm}}^{-1} = \operatorname{erf}\left(\frac{\operatorname{vEsc}}{\operatorname{vRot}}\right) - \left(\frac{1-\beta}{\beta}\right)^{1/2} \exp\left(-\frac{\operatorname{vEsc}^2}{\operatorname{vRot}^2}\right) \operatorname{erfi}\left(\frac{\operatorname{vEsc}}{\operatorname{vRot}}\frac{\beta^{1/2}}{(1-\beta)^{1/2}}\right)$$
(47)

where erfi is the imaginary error function.

The central values and uncertainties of the SHM++ parameters are

$$\begin{array}{rcl} \mathsf{rhoDM} &=& 0.55 \pm 0.17 \; \mathrm{GeV/cm^3} \\ \\ \mathsf{vRot} &=& 233 \pm 3 \; \mathrm{km/s} \\ \\ \mathsf{vEsc} &=& 580 \pm 63 \; \mathrm{km/s} \\ \\ \beta &= \mathsf{betaSHMpp} &=& 0.9 \pm 0.05 \\ \\ \eta &= \mathsf{etaSHMpp} &=& 0.2 \pm 0.1 \end{array} \tag{48}$$

Note that these central values for the global parameters, vRot, vEsc and rhoDM are different from the ones in Table 1, thus the user has to change these parameters before using SHMpp.

7.3 Comparison with Direct Detection experiments

Examples on how to use the routines described below to impose constraints from direct detection experiments can be found in mdlIndep/dd_exp.c of micrOMEGAs.

7.3.1 Experimental data

The SI 90% DD limits tabulated from the results presented by LZ5T [69], LZ₂024 [70], XENON1T [71], DarkSide-50 [72], PICO-60 [73] and CRESST-III [74] are accessible through the following functions

```
\begin{array}{lll} \bullet \text{ LZ}\_2024\,(\text{Mdm}) & \text{for } 9 < M_{DM} < 10000 \text{ GeV}, \ [70] \\ \bullet \text{ LZ5T}\,(\text{Mdm}) & \text{for } 9 < M_{DM} < 10000 \text{ GeV}, \ [69] \\ \bullet \text{ PandaX4T}\,(\text{Mdm}) & \text{for } 5 < M_{DM} < 10000 \text{ GeV}, \ [75] \\ \bullet \text{ XENON1T}\_90\,(\text{Mdm}) & \text{for } 6 < M_{DM} < 1000 \text{ GeV}, \ [71] \\ \bullet \text{ DS50}\_90\,(\text{Mdm}) & \text{for } 0.7 < M_{DM} < 15 \text{ GeV}, \ [72] \\ \bullet \text{ PIC060}\_90\,(\text{Mdm}) & \text{for } 3 < M_{DM} < 10000 \text{ GeV}, \ [73] \\ \bullet \text{ CRESST}\_III}\_90\,(\text{Mdm}) & \text{for } 0.35 < M_{DM} < 12 \text{ GeV}. \ [74] \\ \end{array}
```

The corresponding SD 90% exclusion limits are contained in the functions

These functions give the excluded cross sections in $\rm cm^2$. For a DM mass outside the range specified the function returns NAN.

7.3.2 Recasting the experimental limits with micrOMEGAs

• DD_pvalCS(expCode, f_v , σ_{SI_P} , σ_{SI_N} , σ_{SD_P} , σ_{SD_N} , &expName) calculates the value $\alpha = 1 - C.L$. for a model with DM-nucleon cross sections σ_{SI_P} , σ_{SI_N} , σ_{SD_P} , σ_{SD_N} . Cross sections are specified in [pb] units. The return value 0.1 corresponds to a 90% exclusion. The expCode parameter can be any of the codes LZ5Tmedian, XENON1T_2018, DarkSide_2018, CRESST_2019, PICO_2019 or their combination concatenated with the symbol |. There is also a predefined parameter that currently combines these experiments

```
AllDDexp=LZ5Tmedian|XENON1T_2018|DarkSide_2018|PICO_2019|CRESST_2019;
```

The parameter char* expName is used to indicate the experiment that provides the best exclusion among those specified in expCode. The function DD_pvalCS calculates the exclusion for each experiment independently, returns the smallest α , and assigns the name of the corresponding experiment to expName if it is not NULL.

The f_v parameter specifies the DM velocity distribution in the detector frame. For example, one can use Maxwell or SHMpp which are included in micrOMEGAs, otherwise the user can define another distribution. The DM velocity distribution has to be normalized as in Eq.34. The units are km/s for v and s/km for $f_v(v)$. DD_pvalCS implicitly depends

on the global parameters Mcdm and rhoDM which specify the DM mass and DM local density respectively.

For Xenon1T one can chose between three recasting, p_{eff}^q with q=0,1,2, see Ref. [77]. The flag Xe1TnEvents=q allows to choose the corresponding recasting, otherwise and by default the code uses p_{eff}^1 . The three approaches agree within 5%. For PICO-60, the user can choose between the recasting based on Feldman-Cousins statistics, PICO60Flag=0 which is the default value, or the one based on Neyman one side belt exclusion, PICO60Flag=1.

• DD_factorCS(expCode, α , f_v , σ_{SI_P} , σ_{SI_N} , σ_{SD_P} , σ_{SD_N} , &expName) returns the overall factor which should be applied to the cross sections, σ_{SI_P} , σ_{SI_N} , σ_{SD_P} , σ_{SD_N} to reach the exclusion level α . All parameters are the same as in DD_pvalCS above.

• *dNdEFact(Enr_kev, A)

is the address of the function which modifies the nucleus recoil distribution for DD_pvalCS and DD_factorCS to take into account a t-channel propagator with small or zero mass. By default dNdEfact=NULL and this function does not contribute to the calculation of the direct detection cross sections. Otherwise it is taken as an additional factor in the nucleus recoil distribution, see Eq.35. The parameter Enr_kev is the recoil energy in [keV] units, A is the atomic number of the nucleus. This function should be defined by the user, an example is given in mdlIndep/dd_exp.c.

- DD_pval(expCode, f_v ,&expName)
- DD_factor(expCode, α , f_v ,&expName)

These functions are similar to DD_pvalCS and DD_factorCS described above but use the cross section calculated from the DM model under consideration in micrOMEGAs. The necessary corrections for a light mediator are implemented automatically, these functions do not use dNdEFact.

7.3.3 Setting spin-dependent form factors

The spin dependent form factors for XENON1T and PICO60 are defined via the parameters

The default values for these parameters correspond to the ones used by the experiments, namely

SxxXe129SHELL SxxXe131SHELL SxxF19EFT

They can be replaced by any form factor listed in Section 7.2.1 through direct assignment. Form factors can also be changed using the routine

setSpinDepFF(ExperimentID, setID)

where the choice for ExperimentID is given in Section 7.3.2 and setID can be

EFT - corresponding to the form factors in [64]

SHELL - corresponding to the average form factors in [65], Eq. 39

SHELLm - corresponding to the minimal form factor of [65], Eq. 40. See section 7.2.1.

8 Indirect detection

8.1 Interpolation and display of spectra

Various spectra and fluxes of particles relevant for indirect detection are stored in arrays with NZ elements. The first (zeroth) element of the array contains the maximum energy E_{max} . As a rule E_{max} is the mass of the DM particle. The i^{th} element $(1 \le i \le NZ - 1)$ of the spectrum array contains the value of $E_i \frac{dN}{dE_i}$ where $E_i = E_{max} e^{Zi(i)}$, Zi(i)= $-7\log(10)\left(\frac{i-1}{250}\right)^{1.5}$. Here E is the kinetic energy $E = \sqrt{p^2 + m^2} - m$. By default **NZ=250**, thus the array covers the energy interval $E_{max} \ge E > 1.101 \times 10^{-7} E_{max}$. The user can change the value of NZ defined in the file include/micromegas.h in order to treat smaller energies as described in section 8.2. To decode and interpolate the spectrum array one can use the following functions:

• SpectdNdE(E,spectTab)

interpolates the tabulated spectra and returns the particle distribution dN/dE where E is the energy in GeV. For a particle number distribution the returned value is given in GeV^{-1} while a particle flux is expressed in (sec cm² sr GeV)⁻¹.

- eSpectdNdE(E,spectTab) returns $E \times \text{SpectdNdE}(E, \text{spectTab})$.
- addSpectrum(SpectTab, toAdd)

sums the spectra toAdd and SpectTab and writes the result in SpectTab. For example, this routine can be useful for summing spectra with different maximal energy.

• spectrMult(SpectTab, func)

allows to multiply the spectrum SpecTab by any energy dependent function func

• spectrInt(Emin, Emax, SpectTab)

integrates a spectrum/flux, SpecTab from Emin to Emax.

• spectrInfo(Emin, Spec, &Etot)

provides information on the spectra. The returned value and Etot corresponds respectively to

$$N_{tot} = \int_{E_{min}}^{E_{max}} SpectdNdE(E, Spec)dE = spectrInt(E_{min}, E_{max}, Spec)$$

$$E_{tot} = \int_{E_{min}}^{E_{max}} E SpectdNdE(E, Spec)dE$$

$$(50)$$

$$E_{tot} = \int_{E_{min}}^{E_{max}} E \ SpectdNdE(E, Spec)dE \tag{50}$$

where the first element of the table Spec contains the value of E_{max} . Alternatively the user can directly integrate the spectra using standard simpson routines, for example

$$N_{tot} = simpson_arg(SpectdNdE, Spec, E_{min}, Spec[0], 0.01, NULL)$$
 (51)
 $E_{tot} = simpson_arg(eSpectdNdE, Spec, E_{min}, Spec[0], 0.01, NULL)$

The spectrum can be displayed on the screen with displayPlot("Spectrum", "E", E_min, Spec[0], 0, 1, "dNdE", 0, SpectdNdE, Spec)

To boost a spectrum one can use the command

boost(γ,Emax,m,SpectTab)

where γ is the boost parameter, SpectTab is an array of NZ lines which contains the initial spectrum for the particle of mass m. After calling the boost command the array SpectTab will be overwritten with the new spectrum. The first element of the resulting array is SpectTab[0]=Emax unless the maximal energy of the particle after boost, E, exceeds Emax, then SpectTab[0]=E.

•fillSpect(dNdE, Emax, SpectArray)

This routine converts the spectrum dNdE which is a function of energy E into an array SpectArray which contains NZ elements. The Emax parameter is assigned to SpectArray[0].

• FSRdNdE(E, p, m, q, spin2, med) computes the Final State Radiation spectrum, $\frac{dN}{dE_{\gamma}}$, for DM annihilation in charged particles with momentum p and mass m. The spin2 parameter is 0 for bosons and 1 for fermions. The parameter med=0 if the particle and antiparticle are produced via a scalar mediator and 1 for a vector mediator. E is the energy of the photon. Here we use formulas 4.8-4.11 of [78]. Note that FSRdNdE contains the photon spectrum generated by both particle and anti-particle.

8.2 Annihilation spectra

DM pair annihilation into SM particles will lead to stable particles

$$\gamma, e^+, p^-, \nu_e, \nu_\mu, \nu_\tau, D^-$$
 (52)

The resulting spectra which take into account final state radiation, hadronisation and decays were calculated by Pythia and tabulated.

• basicSpectra(Mass,pdg,outN,Spectr)

computes the spectra of outgoing particles and writes the result in an array of dimension NZ, Spectr, pdg is the PDG code of the particles produced in the annihilation of a pair of WIMPs. outN specifies the outgoing particle,

outN =
$$\{0, 1, 2, 3, 4, 5, 6\}$$
 for $\{\gamma, e^+, p^-, \nu_e, \nu_\mu, \nu_\tau, D^-\}$

The Mass parameter defines the mass of the DM particle.

basicSpectra returns an error code if the parameter outN (err=1) or pdg (err=2) is out or range. The spectrum depends on SpectraFlag which specifies the external package used to calculated the spectra, see below. In particular, the antideuterons spectra is provided only within PPPC. The Mass parameter has to be larger than 2 GeV if SpectraFlag=0 and larger than 5 GeV otherwise. When basicSpectra is called for lower masses, micrOMEGAs extrapolates the spectra assuming that the xdN/dx distribution, where x = E/Mass, depends only weakly on the DM mass.

• decaySpectrum(pName,outN,spectTab) calculates the spectrum of the outgoing particle outN from the decay of particle pName .

The result is written in an array of dimension NZ, spectTab, outN specifies the outgoing particle. decaySpectrum returns the error code 1 if pName is stable and 2 if $1 \to 2$ and $1 \to 3$ decay channels are not kinematically closed.

• SpectraFlag

is a switch to choose the tables that contain the spectra for $\gamma, e^+, \bar{p}, \nu$ from DM pair annihilation into two particle final states. This Flag has to be set before calling the functions calcSpectrum and basicSpectra.

SpectraFlag=0 corresponds to the tables obtained with Pythia-6 [6] for DM mass in the range 2GeV - 5TeV for e^+, \bar{p}, ν . For the photon channel the tables have been extended to cover the range 110MeV - 5TeV. These tables include also the spectra for polarized W's and Z's. To get the spectra generated by transverse and longitudinal W's substitute pdgN= 24 + T' and 24 + T' correspondingly. In the same manner pdgN= 23 + T' and 23 + T' and 23 + T' provides the spectra produced by a polarized Z boson.

SpectraFlag=1 corresponds to the spectra generated by Pythia-8 [79,80] for DM mass in the range 5GeV - 5TeV, here polarization is not taken into account.

SpectraFlag=2 corresponds to the spectra generated with PPPC [81, 82] for DM mass larger than 5GeV. The spectra take into account polarized W and Z, as well as polarized leptons, pgd=11+R or pgd=11+L, the latter are however not supported in the current version of micrOMEGAs.

Finally SpectraFlag=3 corresponds to the spectra provided in CosmiXs for DM in the range $5 \, \text{GeV} - 100 \, \text{TeV}$ [83]. These spectra are generated with PYTHIA and include electroweak corrections. These spectra also included longitudinal/transverse W and Z as well as left/right polarized charged leptons.

The *Pythia-8*, *PPPC*, and *CosmiXs* tables contain spectra that start at $x \gtrsim 10^{-9}$, while the default spectra SpectraFlag=0 start at $x \gtrsim 10^{-7}$. To download the spectra including smaller energies one has to recompile micrOMEGAs after setting the parameter **NZ=295** in the file include/micromegas.h.

The maximal values of the x parameter in Pythia-8 and CosmiXs tables are 0.94 and 0.9 respectively. For this reason, the spectral line for $DM, DM \to \gamma, \gamma$ which corresponds to a contribution $2\delta(1-x)$ in the photon spectra is not included, only the sub-dominant part of the photon spectra from photon radiation is included. In micrOMEGAs the δ -like contribution to photon spectra in the γ, γ channel are added to the Pythia-8 and CosmiXs tables. In the same manner we add a $\delta(1-x)$ contribution to the neutrino spectra forthe $\nu, \bar{\nu}$ channel. In PPPC the corresponding δ -like contributions are simulated by a linear function in the interval $x \in [0.89, 1]$.

The QCD uncertainties that can impact the annihilation spectra were evaluated in [80]. For each DM mass, annihilation channel and choice of final state, Ref. [80] have estimated three types of QCD uncertainties and provide tabulated spectra including these uncertainties. These tables are now incorporated in the code. We have defined three parameters that determines which uncertainties are taken into account,

- DHad: uncertainties on the flux from the variations of the hadronisation model parameters.
- DScale: shower uncertainties on the flux from the variation of the shower evolution variable by a factor of 2.
- DcNS: uncertainties from the variations of the non-singular terms of the DGLAP

splitting kernels.

By default these parameters are set to 1 and all types of uncertainties are taken into account, however any one can be switched off by setting the corresponding parameter to zero. The total uncertainties $\Delta^2(E)_{min,max}$ are obtained by taking the sum of the square of the individual uncertainties. The global parameter, spectUncert determines whether or not uncertainties are included in the spectra. When spectUncert=0, the default spectra without uncertainties, $(dN/dE)_{wo}$, are used, spectUncert=1 means that basicSpectra returns the maximal spectra corresponding to $(dN/dE)_{wo} + \Delta(E)_{max}$ while spectUncert=-1 the minimal spectra corresponding to $(dN/dE)_{wo} - \Delta(E)_{min}$ are used. Note that although these uncertainties were calculated for the Pythia-8 spectra, micrOMEGAs uses the same uncertainties for other spectra as well. One can access the spectra corresponding to the specified value of spectUncert by calling

• spectraUncertainty(Mass,pdgN,outN,Spectr) which has the same parameters as basicSpectra.

The test code mdlIndep/basicSpectra.c contains an example of a call to basicSpectra and compares the four different spectra that are included in micrOMEGAs, checks energy conservation and shows uncertainties.

• calcSpectrum(key,Sg,Se,Sp,Sne,Snm,Snl,&err) calculates the spectra of DM annihilation at rest and returns σv in cm^3/s . For multicomponent DM the number of annihilation events in one cm^3 during one second at a distance R from the galactic center is given by

$$N(R) = \frac{1}{2}\sigma v \left(\frac{\rho(R)}{M_{cdm}^{eff}}\right)^2 \tag{53}$$

where

$$M_{cdm}^{eff} = \left(\sum_{i=1}^{Ncdm} \frac{fracCDM[i]}{McdmN[i]}\right)^{-1}$$
(54)

and $\rho(R)[GeV/cm^3]$ is the DM density. In the special case of one-component DM, $M_{cdm}^{eff} =$ Mcdm is the mass of DM.

The calculated spectra for γ , e^+ , \bar{p} , ν_e , ν_μ , ν_τ are stored in arrays of dimension NZ as described above: Sg, Se, Sp, Sne, Snm, Snl. To remove the calculation of a given spectra, substitute NULL for the corresponding argument. key is a switch to include the polarisation of the W, Z bosons (key=1) or photon radiation (key=2). Note that final state photon radiation (FSR) is always included. When key=2 the 3-body process $\chi\chi' \to XX + \gamma$ is computed for those subprocesses which either contain a light particle in the t-channel (of mass less than 1.2 Mcdm) or an outgoing W when Mcdm>500GeV. The FSR is then subtracted to avoid double counting. Only the electron/positron spectrum is modified with this switch. When key=4 the contributions for each channel to the total annihilation rate are written on the screen. More than one option can be switched on simultaneously by adding the corresponding values for key. For example both the W polarization and photon radiation effects are included if key=3. A problem in the spectrum calculation will produce a non zero error code, $err \neq 0$. calcSpectrum uses basicSpectra to interpolate and sum spectra obtained by Pythia, thus it depends on the switch SpectraFlag.

• vSigmaCh

is an array that contains the relative contribution and particle names for each annihilation channel. It is similar to vSigmaTCh described in Section 6.2. Note that the list of particles contains five elements to allow to include gamma radiation. For 2->2 processes vSigmaCh[n].prtcl[4]=NULL. The array vSigmaCh is filled by calcSpectrum.

• calcSpectrumPlus(proc22, outP, Spect, &err)

calculates DM annihilation into 3-body and 4-body final states via the exchange of virtual particles. These processes are not taken into account by calcSpectrum. Here proc22 specifies the $2 \to 2$ process such as " $\chi, \chi' \to X, Y$ " which is kinematically forbidden at small relative velocity. calcSpectrumPlus includes all reactions with virtual X and Y particles. The parameter outP specifies the spectrum: 0 - photons, 1- positrons, 2-anti-protons, 3,4,5 - neutrinos. Spect is an array of size NZ which stores the calculated spectrum. The routine returns the value of $v\sigma$ in $[cm^3/s]$ units. If DM particles are not selfconjugated, the corresponding conjugated channel is added automatically.

8.3 Distribution of Dark Matter in Galaxy

The indirect DM detection signals depend on the DM density in our Galaxy. The DM density is given as the product of the local density at the Sun with the halo profile function

$$\rho(r) = \rho_{\odot} F_{halo}(r) \tag{55}$$

where we assume that

$$F_{halo}(R_{\odot}) = 1 \tag{56}$$

In micrOMEGAs ρ_{\odot} is a global parameter rhoDM and R_{\odot} is a global parameter Rsun. The default profile is the Zhao profile [84].

$$F_{halo}(r) = \left(\frac{R_{\odot}}{r}\right)^{\gamma} \left(\frac{r_c^{\alpha} + R_{\odot}^{\alpha}}{r_c^{\alpha} + r^{\alpha}}\right)^{\frac{\beta - \gamma}{\alpha}}$$
(57)

By default we use $\alpha = 1, \beta = 3, \gamma = 1$ which corresponds to the NFW profile and we set $r_c = 8.1[kpc]$ [85]. Note that we have modified the default value, it was $r_c = 20[kpc]$ in previous versions. The parameters of the Zhao profile can be reset by

• setProfileZhao($\alpha, \beta, \gamma, r_c$)

The function to set another density profile is

• setHaloProfile(F_{halo})

where $F_{halo}(r)$ is any function which depends on the distance from the galactic center, r, defined in [kpc] units. For instance, setHaloProfile(hProfileEinasto) sets the Einasto profile

$$F_{halo}(r) = exp\left[-\frac{2}{\alpha}\left(\left(\frac{r}{r_2}\right)^{\alpha} - \left(\frac{R_{\odot}}{r_2}\right)^{\alpha}\right)\right]$$
 (58)

where by default $\alpha = 2.33$, $r_2 = 10.7$ [86], note that the default values in previous versions were $\alpha = 0.17$, $r_2 = \text{Rsun}$. The values can be changed by

• setProfileEinasto(α, r_2).

The command setHaloProfile(hProfileZhao) sets back the Zhao profile.

Dark matter annihilation in the Galaxy depends on the average of the square of the DM density, $\langle \rho^2 \rangle$. This quantity can be significantly larger than $\langle \rho \rangle^2$ when clumps of DM are present [87]. In micromegas, we use a simple model where f_{cl} is a constant that characterizes the fraction of the total density due to clumps and where all clumps occupy the same volume V_{cl} and have a constant density ρ_{cl} . Assuming clumps do not overlap, we get

$$\langle \rho^2 \rangle = \rho^2 + f_{cl} \rho_{cl} \rho. \tag{59}$$

This simple description allows to demonstrate the main effect of clumps: far from the Galactic center the rate of DM annihilation falls as $\rho(r)$ rather than as $\rho(r)^2$. The parameters ρ_{cl} and f_{cl} have zero default values. The routine to change these values is

• setClumpConst (f_{cl}, ρ_{cl})

To be more general, one could assume that ρ_{cl} and f_{cl} depend on the distance from the galactic center. The effect of clumping is then described by the equation

$$<\rho^2>(r)=\rho(r)(\rho(r)+\rho_{clump}^{eff}(r)),$$
 (60)

and the function

ullet setRhoClumps $(
ho_{clump}^{eff})$

allows to implement a more sophisticated clump structure. To return to the default treatment of clumps call setRhoClumps(rhoClumpsConst) or setClumpConst.

8.4 Photon signal

The photon flux does not depend on the diffusion model parameters but on the angle ϕ between the line of sight and the center of the galaxy as well as on the annihilation spectrum into photons

• gammaFluxTab(fi,dfi,sigmav,Sg,Sobs)

multiplies the annihilation photon spectrum with the integral over the line of sight and over the opening angle to give the photon flux. fi is the angle between the line of sight and the center of the galaxy, dfi is half the cone angle which characterizes the detector resolution (the solid angle is $2\pi(1-\cos(dfi))$, sigmav is the annihilation cross section, Sg is the DM annihilation spectra. Sobs is the spectra observed in 1/(GeV cm^2 s) units.

The function gammaFluxTab can be used for the neutrino spectra as well.

• gammaFluxTabGC(1,b,d1,db,sigmav,Sg,Sobs)

is similar to gammaFluxTab but uses standard galactic coordinates. Here l is the galactic longitude (measured along the galactic equator from the galactic center, and b is the latitude (the angle above the galactic plane). Both l and b are given in radians. The relation between the angle fi used above and the galactic coordinates is $\mathtt{fi} = \cos^{-1}(\cos(l)\cos(b))$. gammaFluxTabGC integrates the flux over a rectangle [(l,b)-(l+dl,b+db)].

• loopGamma(&vcs_gz,&vcs_gg)

calculates σv for loop induced processes of DM pair annihilation into γZ and into $\gamma \gamma$. The result is given in $\frac{cm^3}{s}$. The function returns a non-zero value to signal a problem. This function is available only for MSSM [88], NMSSM [89], CPVMSSM and IDM. Note that this function does not include non-perturbative effects that are in particular important when the mass of DM is much above the weak scale [90, 91].

• gammaFlux(fi,dfi,dSigmavdE)

computes the photon flux for a given energy E and a differential cross section for photon

production, dSigmavdE. For example, one can substitute dSigmavdE= σv SpectdNdE(E,SpA) where σv and SpA are obtained by calcSpectrum. This function can also be used to compute the flux from a monochromatic gamma-ray line by substituting the cross section at fixed energy (in cm^3/s) instead of dSigmavdE, for example the cross sections obtained with the loopGamma function in the MSSM, NMSSM, CPVMSSM models (vcsAA and vcsAZ). In this case the flux of photons can be calculated with gammaFlux(fi,dfi,2*vcsAA+vcsAZ).

• gammaFluxGC(1,b,d1,db,vcs)

is the analog of gammaFlux when using standard galactic coordinates.

8.5 Propagation of charged particles

The observed spectrum of charged particles strongly depends on their propagation in the Galactic Halo. The propagation depends on the global parameters

as well as

Tau_dif (positrons), Vc_dif (antiprotons)

• posiFluxTab(Emin, sigmav, Se, Sobs)

computes the positron flux at the Earth. Here sigmav and Se are values obtained by calcSpectrum. Sobs is the positron spectrum after propagation. Emin is the energy cut to be defined by the user. Note that a low value for Emin increases the computation time. The format is the same as for the initial spectrum. The function SpectrdNdE(E,Sobs) described above can also be used for the interpolation, in this case the flux is returned in (GeV s cm²sr)⁻¹.

• pbarFlux(E,dSigmavdE)

computes the antiproton flux for a given energy \mathtt{E} and a differential cross section for antiproton production, $\mathtt{dSigmavdE}$. For example, one can substitute

 $dSigmavdE = \sigma vSpectdNdE(E,SpP)$

where σv and SpP are obtained by calcSpectrum. This function does not depend on the details of the particle physics model and allows to analyse the dependence on the parameters of the propagation model.

- pbarFluxTab(Emin, sigmav, Sp, Sobs) computes the antiproton flux, this function works like posiFluxTab,
- solarModulation(Phi, mass, stellarTab, earthTab)

takes into account modification of the interstellar positron/antiproton flux caused by the electro-magnetic fields in the solar system. Here Phi is the effective Fisk potential in MeV, mass is the particle mass, stellarTab describes the interstellar flux, earthTab is the calculated particle flux in the Earth orbit.

Note that for solarModulation and for all *FluxTab routines one can use the same array for the spectrum before and after propagation.

9 Planck CMB constraint

The function

PlanckCMB(vSigma, SpA, SpE)

determines whether the DM model under consideration is consistent with Planck measurements of the CMB anisotropies caused by the injection of electrons and photons coming from DM annihilation [92]. The spectra of DM annihilation into photons and positrons are provided in the arrays SpA and SpE. Here it is assumed that the DM relic density $\Omega h^2 = 0.12$, for multi-component DM the fraction of each DM component described by the fracCDM array is taken into account. We also assume that the input parameter vSigma represents the s-wave cross section in [cm³/s] units, this limit does not apply if the DM annihilation cross-section depends on velocity at small velocities. A return value more than 1 indicates that the model is excluded at 95% C.L. Note that if the DM model gives $\Omega h^2 < 0.12$ and one assumes that DM forms only a fraction ξ of the total DM in the Universe, then the value returned by PlanckCDM should be scaled by ξ^2 .

By default we assume that the annihilation is s-wave and that vSigma is the cross-section computed from calcSpectrum, the number of events will be computed using M_{cdm}^{eff} , as given in Eq.54. If a model of elementary particles is not loaded, and the user just defined the spectra assuming some specific annihilation channels, then the number of events is computed using the Mcdm parameter instead. This allows for a model independent test of the function PlanckCMB.

In the file mdlIndep/CMB.c we reproduce the top panels of Fig.3 and Fig.4 of Ref. [92], here we use the PPPC spectra.

10 Photons from Dwarf Spheroidal galaxies

DwarfSignal(vSigma, SpA)

determines whether the photon spectra SpA is compatible with the 95% limits obtained from observations of Dwarf Spheroidal galaxies [36–38]. Here vSigma is the DM annihilation cross section at low velocities ($< v\sigma > \inf [cm^3/s]$ units) as obtained by calcSpectrum. The return value is the ratio of $< v\sigma > \inf$ the given model to the limit extracted from observations, a value more than 1 indicates that the model is excluded. Conversely dividing $< v\sigma > \inf$ the given model by the value returned by the routine gives the excluded cross-section.

To compute the signal vSigma is divided by the squared mass M_{cdm}^{eff} , Eq.54. For a model independent test of this function the Mcdm parameter is used instead. For an example, see the file mdlIndep/Dwarf.c which reproduces the *combined* curve in [38], Fig.5 (Right).

11 Neutrino signal from the Sun and the Earth

This module only works for single component dark matter

After being captured, DM particles concentrate in the center of the Sun/Earth and then annihilate into Standard Model particles. These SM particles further decay producing neutrinos that can be observed at the Earth. The neutrino spectra originating from different annihilation channels into SM particles and taking into account oscillations and Sun medium effects were computed both in WimpSim [93] and in PPPC4DM ν [94]. We use the set of tables provided by these two groups as well as those from DM ν [95] which were included in previous versions of micrOMEGAs. The new global parameter

WIMPSIM allows to choose the neutrino spectra. The default value WIMPSIM=0 8 corresponds to the PPPC4DM ν spectra while WIMPSIM=1 corresponds to the WimpSim spectra and WIMPSIM=-1 to the DM ν spectra.

• neutrinoFlux(f,forSun,nu, nu_bar)

calculates the muon neutrino/anti-neutrino fluxes near the surface of the Earth. Here f is the DM velocity distribution normalized such that $\int_0^\infty v f(v) dv = 1$. The units are km/s for v and s^2/km^2 for f(v). For example, one can use the same Maxwell function introduced for direct detection. This routine implicitly depends on the WIMPSIM switch.

If forSun==0 then the flux of neutrinos from the Earth is calculated, otherwise this function computes the flux of neutrinos from the Sun. The calculated fluxes are stored in nu and nu_bar arrays of dimension NZ=250. The neutrino fluxes are expressed in [1/Year/km²].

• muonUpward(nu,Nu,muon)

calculates the muon flux which results from interactions of neutrinos with rocks below the detector. Here nu and Nu are input arrays containing the neutrino/anti-neutrino fluxes calculated by neutrinoFlux. muon is an array which stores the resulting sum of μ^+ , μ^- fluxes. SpectdNdE(E,muon) gives the differential muon flux in [1/Year/km²/GeV] units. The muon flux weakly depends on the propagation medium, e.g. rock or ice. The energy lost during propagation is described by the equation [96]

$$\frac{dE}{dx} = -(\alpha + \beta E)\rho \tag{61}$$

For propagation in ice (the switch forRocks=0), micrOMEGAs substitutes $\rho=1.0\,\mathrm{g/cm^3}$, $\alpha=0.00262\,\mathrm{GeVcm^2/g},~\beta=3.5\times10^{-6}\,\mathrm{cm^2/g}$ [97], while for propagation in rocks, $\rho=2.6\,\mathrm{g/cm^3},~\alpha=0.002\,\mathrm{GeVcm^2/g},~\beta=3.0\times10^{-6}\,\mathrm{cm^2/g}$ [96]. The result depends on the ratio α/β .

• muonContained(nu,Nu,rho, muon) calculates the flux of muons produced in a given detector volume. This function has the same parameters as muonUpward except that the outgoing array gives the differential muon flux resulting from neutrinos converted to muons in a km^3 volume given in [1/Year/km³/GeV] units. rho is the density of the detector in g/cm^3 .

atmNuFlux(nu,cs,E)

returns the atmospheric muon neutrinos (nu > 0) and anti-neutrinos spectrum (nu < 0) in [1/Year/km^2] units for a given cosine of the zenith angle, cs. This function is based on [98].

Two functions allow to estimate the background from atmospheric neutrinos creating muons after interaction with rocks below the detector or with water inside the detector.

- ATMmuonUpward(cosFi,E) calculates the sum of muon and anti-muon fluxes resulting from the interaction of atmospheric neutrinos with rocks in units of [1/Year/km²/GeV/Sr]. cosFi is the energy between the direction of observation and the direction to the center of Earth. E is the muon energy in GeV. The result depends on the forRock switch.
- ATMmuonContained(cosFi, E, rho) calculates the muon flux caused by atmospheric neutrinos produced in a given (detector) volume. The returned value for the flux is given

⁸Since PPPC4DM ν does not provide neutrino spectra produced at the center of the Earth, in this case and for WIMPSIM=0 micrOMEGAs uses the DM ν spectra.

in 1/Year/km³/GeV/Sr. rho is the density of the detector in g/cm³ units. cosFi and E are the same as above.

11.1 Comparison with IceCube results

These functions are described in [99] and allow to compare the predictions for the neutrino flux from DM captured in the Sun with results of IceCube22.

• IC22nuAr(E)

effective area in $[km^2]$ as a function of the neutrino energy, $A_{\nu_n}(E)$

• IC22nuBarAr(E)

effective area in $[km^2]$ as a function of the anti-neutrino energy, $A_{\bar{\nu}_{\mu}}(E)$).

• IC22BGdCos(cs)

angular distribution of the number of background events as a function of $\cos \phi$, $\frac{dN_{bg}}{d\cos \varphi}$.

• IC22sigma(E)

neutrino angular resolution in radians as a function of energy.

• exLevIC22(nu_flux, nuB_flux,&B)

calculates the exclusion confidence level for number of signal events generated by given ν_{μ} and $\bar{\nu}_{\mu}$ fluxes, [99]. The fluxes are assumed to be in [GeV km² Year]⁻¹. This function uses the IC22BGdCos(cs) and IC22sigma(E) angular distribution for background and signal as well as the event files distributed by IceCube22 with $\phi < \phi_{cut} = 8^{\circ}$. The returned parameter B is a Bayesian factor representing the ratio of likelihood functions for the model with given fluxes and the model with null signal. See details in [99].

• fluxFactorIC22(exLev, nu,nuBar)

For given neutrino, nu, and anti-neutrino fluxes, nuBar, this function returns the factor that should be applied to the fluxes (neutralino-proton cross sections) to obtain a given exclusion level exLev in exLevIC22. This is used to obtain limits on the SD cross section for a given annihilation channel.

12 Cross sections and decays

The calculation of particle widths, decay channels and branching fractions can be done by the following functions

• pWidth(pName,&address)

returns directly the width for particle pName and the returned parameter address gives an address where information about the branchings is stored. See below description of routines which use this parameters. We first describe default work of pWidth which can be modified specially for each particle by the pWidthPref command. For models which read a SLHA parameter file, the values of the widths and branchings are taken from the SLHA file when useSLHAwidth=1.

If useSLHAwidth=0 or decay of given particle is not presented in SLHA file, then micrOMEGAs applies its own calculation of width. If the 1->2 decay channels are kinematically accessible then by default⁹ only these channels are included in the width. If not, pWidth compiles all open 1->3 channels and use these for computing the width. If all 1->3 channels are kinematically forbidden, micrOMEGAs compiles 1->4 channels. If VWdecay(VZdecay) \neq 0,

⁹See pWidthPref below.

then micrOMEGAs also computes the 1->3 processes with virtual W(Z) and adds these to the list of 1->2 decay channels. Note that 1->3 decay channels with a virtual W will be computed even if the mass of the decaying particle exceeds the threshold for 1->2 decays by several GeV's. This is done to ensure a proper matching of 1->2 and 1->3 processes.

The routine

•pWidthPref(pName, pref) changes the mode of the pWidth calculation individually for the particle pName. Here pref=4 restores the default pWidth mode. Otherwize the useSLHAwidth flag is ignored and for pref=0,1,2,3 we have

- 0 widths are calculated using processes with minimal number of outgoing particles.
- 1 widths are calculated using processes with minimal and next to minimal number of outgoing particles excluding processes with s-channel resonances to avoid double counting.
- 2- widths are read from the SLHA file if the SLHA file does not contain widths, they are calculated as in pref=0 case.
- 3- widths are read from the SLHA file if the SLHA file does not contain widths, they are calculated as in pref=1 case.

printTxtList(address,FD)

lists the decays and their branching fractions and writes them in a file. address is the address returned by pWidth.

• findBr(address, pattern)

finds the branching fraction for a specific decay channel specified in pattern, a string containing the particle names in the CalcHEP notation. The names are separated by commas or spaces and can be specified in any order. If the pattern contains "*", then findBr sums all branching fractions which contain particles included in the pattern.

• printPartialWidth(width,address,FD)

prints the branching fractions and partial widths for each decay channel of a particle in the file FD. Here width and address are the result of the function pWidth described above.

slhaDecayPrint(pname, delVirt, FD)

uses pWidth described above to calculate the width and branching ratios of particle pname and writes down the result in SLHA format. The return value is the PDG particles code. In case of problem, for instance wrong particle names, this function returns zero. This function first computes $1 \to 2$ decays. If such decays are kinematically forbidden then $1 \to 3$ decay channels are computed. Decays via virtual W/Z bosons will be listed via their decay products when delVirt $\neq 0$.

• newProcess(procName)

compiles the codes for any $2 \to 2$ or $1 \to 2$ reaction. The result of the compilation is stored in the shared library in the directory work/so-generated/. The name of the library is generated automatically.

The newProcess routine returns the *address* of the compiled code for further usage. If the process can not be compiled, then a NULL address is returned.

Note that it is also possible to compute processes with polarized massless beams, for example for a polarized electron beam use e% to designate the initial electron.

• procInfo1(address,&ntot,&nin,&nout)

provides information about the total number of subprocesses (ntot) stored in the library specified by address as well as the number of incoming (nin) and outgoing (nout) particles for these subprocesses. Typically, for collisions (decays), nin=2(1) and nout=2,3. NULL can be substitute if this information is not needed.

• procInfo2(address, nsub, N, M)

fills an array of particle names N and an array of particle masses M for the subprocess nsub $(1 \le nsub \le ntot)$. These arrays have size nin + nout and the elements are listed in the same order as in CalcHEP starting with the initial state, see the example in MSSM/main.c.

• cs22(address,nsub,P,c1,c2,&err)

calculates the cross-section for a given $2 \to 2$ process, nsub, with center of mass momentum P(GeV). All model parameters except the strong coupling GG can be specified with the functions findVal[W]/assignVal[W] described in Section 5. The strong coupling GG is defined via the scale parameter GGscale. The differential cross-section is integrated within the range $c1 < \cos\theta < c2$. θ is the angle between \vec{p}_1 and \vec{p}_3 in the center-of-mass frame. Here \vec{p}_1 (\vec{p}_3) denote respectively the momentum of the first initial(final) particle. err contains a non zero error code if nsub exceeds the maximum value for the number of subprocesses (given by the argument ntot in the routine procInfo1). To set the polarization of the initial massless beam, define Helicity[i] where i=0,1 for the 1^{st} and 2^{nd} particles respectively. The helicity is defined as the projection of the particle spin on the direction of motion. It ranges from [-1,1] for spin 1 particles and from [-0.5,0.5] for spin 1/2 particles. By definition a left handed particle has a positive helicity.

• hCollider(Pcm,pp,nf, Qren,Qfac, pName1,pName2,Tmin,wrt) calculates the cross section for particle production at hadron colliders. Here Pcm is the beam energy in the center-of-mass frame. pp is 1(-1) for $pp(p\bar{p})$ collisions, $nf \leq 5$ defines the number of quark flavors taken into account. The parameters Qren and Qfac define the renormalisation and factorization scales respectively. pName1 and pName2 are the names of outgoing particles. If $T_{\min} \leq 0$ then hCollider calculates the total cross section for the 2-body final state process. Otherwise it calculates the cross section for

proton, [a]proton -> pName1, pName2, jet

where $T_{\min} > 0$ defines the cut on the jet transversee momentum. The jet content is defined by the parameter \mathbf{nf} . If $Q_{\text{fac}} \leq 0$, then running \hat{s} is used for the factorization scale. If $Q_{\text{ren}} \leq 0$, \hat{s} is used for the renormalization scale for a $2 \to 2$ process and p_T of the jet is used for the renormalization scale for a process with a jet in the final state. The last argument in the hCollider routine allows to switch on/off (wrt=1/0) the printing of the contribution of individual channels to the total cross section. The value returned is the total cross section in [pb].

One of the arguments pName1, pName2 can be NULL. Then the cross section for $2 \to 1$ or $2 \to 1 + \text{jet}$ process will be calculated.

By default hCollider uses the cteq66 [100] structure function built-in the micrOMEGAs code. One can set any other parton distribution stored in micrOMEGAs/CalcHEP_src/pdTables (PDT-distributions) or by linking the LHAPDF library [101]. The list of PDT structure functions can be obtained with the command • PDTList()

and one of these can be activated by

• setPDT(name)

To work with other PDF's available in LHAPDF one should recompile micrOMEGAs with a parameter which defines the path to the LHAPDF library:

make LHAPDF= Path_to_LHAPDF_library. 10

microMEGAs assumes the existence of a file \$LHAPDF/lib/libLHAPDF.so
The list of available LHAPDF distributions can be obtained with the command

- LHAPDFList()
- and one of these can be activated by
- setLHAPDF(name, nset)

where nset specifies the subset number. Note, that if a wrong input is provided, setLHAPDF terminates the execution.

Alternatively, one can convert a PDF distribution to the PDT format with the command lhapdf2pdt disposed in CalcHEP_src/bin.

 ${\tt lhapdf2pdt} \quad directory_with_PDF_disctribution$

the generated .pdt file has to be placed in the folder /CalcHEP_src/pdTables.

The parton densities are defined by the function

• parton_distr(pdg,x,q)

where pdg is the PDG code of a particle. Note that parton_distr defines the parton number density and contains a factor 1/x with respect to the definition used in LHAPDF.

13 Tools for model independent analysis

A model independent calculation of the DM observables is also available. After specifying the DM mass, the cross sections for DM spin dependent and spin independent scattering on proton and neutron, the DM annihilation cross section times velocity at rest and the relative contribution of each annihilation channel to the total DM annihilation cross section, one can compute the direct detection rate on various nuclei, the fluxes for photons, neutrinos and antimatter resulting from DM annihilation in the galaxy and the neutrino/muon fluxes in neutrino telescopes. All the routines presented here depend implicitly on the global parameter Mcdm except for basicSpectra and basicNuSpectra. They also explicitly depend on spin-independent and spin-dependent cross sections of DM scattering on proton and neutron: csIp,csIn,csDp, csDn. These cross sections have to be specified in [pb]units. A negative value for one of these cross sections is interpreted as a destructive interference between the proton and neutron amplitudes.

These routines do not take into account the multi-component structure of DM and, in particular, possible differences between DM and anti-DM. For multi-component DM the user has to perform a summation over the different DM components.

The routines available include:

- nucleusRecoilCS(f_v ,A,Z,J,Sxx,csIp,csIn,csDp,csDn,dNdE) is similar to nucleusRecoil, see Section 7.2.
- nucleusRecoilOCS(f_v , A, Z, J, Sp, Sn, csIp, csIn, csDp, csDn, dNdE) is the correspond-

¹⁰The path will be stored in FlagsForSh and FlagsForMake files and subsequent call of make without parameters in the micrOMEGAs directory will not clean the corresponding records.

ing modification of nucleusRecoil0.

- DD_pvalCS(Exp, \$f_v\$, Sxx,csIp,csIn,csDp,csDn,\&expName) and
- DD_factorCS(Exp, pval, \$f_v\$,Sxx,csIp,csIn,csDp,csDn,\&expName) are similar to DD_pval, DD_factor described in Section 7.3.

DD_pvalCS, DD_factorCS have an option to handle a low mass mediator which modifies the recoil energy distribution, see Eq.35.

• (*dNdEfact)(Enr,MA)

is the address of the function which modifies the nucleus recoil distribution to take into account a t-channel propagator with small or zero mass as described in Section 7.3.

For indirect detection, we also provide a tool for model independent studies

• basicSpectra(Mass,pdgN,outN,Spectr)

computes the spectra of outgoing particles and writes the result in an array of dimension NZ, Spectr. pdgN is the PDG code of the particles produced in the annihilation of a pair of WIMPs. To get the spectra generated by transverse and longitudinal W's substitute pdgN= 24+'T' and 24+'L' correspondingly. In the same manner pdgN= 23+'T' and 23+'L' provides the spectra produced by a polarized Z boson. outN specifies the outgoing particle,

outN =
$$\{0, 1, 2, 3, 4, 5\}$$
 for $\{\gamma, e^+, p^-, \nu_e, \nu_\mu, \nu_\tau\}$

The Mass parameter defines the mass of the DM particle. Note that the propagation routines for e^+, p^-, γ can be used after this routine as usual. Note that the result of basicSpectra are not valid for Mcdm < 2GeV as explained in the description of calcSpectrum.

To get indirect detection signals one can substitute the obtained spectra in the [photon/posi/pbar]FluxTab routines.

- captureCS(f,forSun,Mass,csIp,csIn,csDp,csDn)
- calculates the number of DM particles captured per second assuming the cross sections for spin-independent and spin-dependent interactions with protons and neutrons csIp, csIn, csDp, csDn are given as input parameters (in [pb]). A negative value for one of the cross sections is interpreted as a destructive interference between the proton and neutron amplitudes. The first two parameters have the same meaning as in the neutrinoFlux routine Section 11. The result depends implicitly on the global parameters rhoDM and Mcdm in Table 1.
- basicNuSpectra(forSun,Mass,pdg, pol, nu_tab, nuB_tab) calculates the ν_{μ} and $\bar{\nu}_{\mu}$ spectra corresponding to the pair annihilation of DM in the center of the Sun/Earth into a particle-antiparticle pair with PDG code pdg. Mass is the DM mass. Note that this routine depends implicitly on the global parameter WIMPSIM (1,0,-1) which selects the neutrino spectra computed by WimpSim [93], PPPC4DM ν [94] and DM ν [95]. The parameter pol selects the spectra for polarized particles available in PPPC4DM ν . pol=-1(1) corresponds to longitudinal (transverse) polarisation of vector bosons or to left-handed (right-handed) polarisation of fermions, pol=0 is used for unpolarized spectra. When polarized spectra are not available, the unpolarized ones are generated irrespective of the value of pol. The parameter outN is 1 for muon neutrino and -1 for anti-neutrino. The resulting spectrum is stored in the arrays nu_tab and nuB_tab with NZ=250 elements.

The files main.c/F in the directory mdlIndep contain an example of the calculation of the direct detection, indirect detection and neutrino telescope signals using the routines described in this section. The numerical input data in this sample file corresponds to 'MSSM/mssmh.dat'.

14 Constraints from colliders

14.1 The Higgs sector

To obtain the limits on the Higgs sector for models with one or several Higgs bosons, the predictions for the signal strengths of the 125 GeV Higgs can be compared to the latest results of the LHC, for this an interface to the public code HiggsSignals [49] or Lilith [33–35] is provided. Moreover the exclusion limits obtained from Higgs searches in different channels at LEP, Tevatron and the LHC can be applied to other Higgses in the model using HiggsBounds [47].

14.1.1 Lilith

Lilith [33–35] is a Python library that is used to construct a global likelihood function \mathcal{L} from the latest ATLAS and CMS results on the 125 GeV Higgs. The Lilith inputs are the set of reduced couplings of the 125 GeV state, *i.e.*, couplings normalized by the SM ones, as well as the branching ratios of Higgs decays to invisible, BR_{inv}, or to undetected non-SM final states, BR_{undetected} = $1 - \mathrm{BR_{inv}} - \sum \mathrm{BR}(H \to \mathrm{SM\,SM})$. By default, the automatic generation of the input file assumes that only DM contributes to the invisible width. Note that the reduced couplings of the 125 GeV Higgs are defined for all the models provided with micromegas with the exception of the $Z\gamma$ coupling. The latter is computed within Lilith assuming that only SM particles run in the loop. The file include/Lilith.inc (or Lilith.inc_f) contains the instructions to launch Lilith using a system call. The input file Lilith_in.xml for Lilith can be created by two commands

```
LilithMDL("Lilith_in.xml")
LilithMO("Lilith_in.xml")
```

both also return the number of neutral Higgs particles. LilithMDL requires that the reduced couplings be defined in lib/lilith.c of the model. These files are defined for all models provided with micrOMEGAs and should be written by the user for new models. On the other hand LilithMO generates automatically the input file required by Lilith. The functionality of LilithMO is described in Section 14.1.3. As input parameters, Lilith also requires the number of free parameters, n_par, and a reference likelihood point, m2logL_reference. Those are defined in the main.c file of each model and set to 0 by default.

¹¹Lilith can test Higgs bosons with masses within the [123, 128] GeV interval, a warning will be issued if no such state can be found. In the case where two or more states have masses within this interval, their signal strengths will be summed incoherently and an effective Higgs state will be tested against the LHC measurements.

The SLHA output file, Lilith_out.slha, consists of six entries which are respectively the log-likelihood evaluated at a parameter space point \mathcal{P} , $-2\log\mathcal{L}(\mathcal{P})$, the number of experimental degrees of freedom, n^{exp} , the reference likelihood point, the number of degrees of freedom, ndf, the p-value, p and the database version. For a detailed description of the various outputs and their interpretation see [33,34]. For example, one could flag or exclude points with too low p-value. In this context, a point with a p-value smaller than 0.3173, 0.0455, 0.0027 could be excluded at more than the 1σ , 2σ , 3σ levels, respectively.

14.1.2 HiggsBounds and HiggsSignals

Constraints on the properties of the 125 GeV Higgs boson can also be obtained with HiggsSignals. Moreover exclusion limits provided by the experimental LHC and Tevatron collaborations on additional Higgs bosons are obtained through an interface to HiggsBounds [102]. Theses codes are no longer distributed with micrOMEGAs but are downloaded and compiled when required 12. The file include/hBandS.inc contains the instructions to call both HiggsBounds and HiggsSignals, in particular the options for running HiggsSignals are set in this file by fixing the Dataset, Method and PDF parameters. Moreover the interface uses the effective coupling option for specifying the input see [47] for more details. Two functions can be used to generate the input SLHA file, HB.in

```
hbBlocksMDL("HB.in",&NchHiggs)
hbBlocksMO("HB.in",&NchHiggs)
```

Both return the number of neutral Higgses and NchHiggs gives the number of charged Higgs particles. The function hbBlocksMDL is located in lib/hbBlocks.c for each MSSM-like model and contains the appropriate definition of the reduced couplings. The function hbBlocksMO generates automatically the required input file for any model and is thus very convenient to use for new models. The content of this function is described in Section 14.1.3. Note that the PDG numbers which will be considered by HiggsBounds for Higgs-like particles are only 25, 35, 36, 37, 45, and 46. Moreover HiggsBounds will check the contribution to the Higgs invisible width only for particles with PDG codes 1000022, 1000012, 1000014, 1000016, 1000017, 1000018 or 1000019. Also note that the theoretical uncertainty on the mass of the Higgs boson should be specified in the SLHA BLOCK DMASS, see the example given in main.[c/F] to set the uncertainty at 2 GeV.

The complete outputs of HiggsBounds and HiggsSignals are stored in the files HB.out and HS.out respectively and can be accessed and read by the user using the slhaval function [103]. The screen output of micrOMEGAs contains the following information

```
HiggsBounds(version number)
id result obsratio channel
```

where three channels are listed, result = 0, 1, -1 denotes respectively whether a parameter point is excluded at 95% CL, not excluded, or invalid; obsratio gives the ratio of the theoretical expectation relative to the observed value for the channel specified in channel. The first channel in this list is the one with the highest expected sensitivity and is the

 $^{^{12}}$ For compilation one needs Fortran f90 compiler, for instance gfortran, and cmake

one that determines the overall exclusion, see [47], other channels are to be interpreted by the user.

The HiggsSignals output displayed on the screen is simply

```
HiggsSignals(version number)
Nobservables chi^2 pval
```

where Nobservables gives the number of observables used in the fit, chi² the associated χ^2 and pval the p-value. The interpretation of these values is left to the user, see [49] for a detailed description.

14.1.3 Automatic generation of interface files

The functions LiLithMO and hbBlocksMO contain two routines that allow to extract the couplings contained in the model file, lgrng1.mdl. The first routine returns a description of a given vertex. The format used is

```
1Vert* vv=getLagrVertex(name1,name2,name3,name4);
```

where name1,...,name4 are the names of the particles included in the vertex; for vertices with three particles, name4 should be replaced by NULL. The return parameter vv is the memory address of a structure which contains information about the vertex:

- vv->GGpower power of strong coupling included in vertex
- vv->nTerms number of different Lorentz structures in vertex
- vv->SymbVert[i] text form of Lorentz structures $i \in [0, nTerms]$

The second routine allows to obtain the numerical coefficients corresponding to each Lorentz structure. The command is

```
getNumCoeff(vv,coeff)
```

with <code>coeff[i]</code> the numerical coefficient for <code>SymbVert[i]</code>. Note that the strong coupling is factored out of the coefficients.

All the QCD-neutral scalars belonging to the even sector (not designated with $\tilde{\ }$) are considered as Higgs particles. For each of these, microMEGAs calculates the couplings to SM fermions and massive bosons and writes down into the interface file the ratio of these couplings to the corresponding SM Higgs coupling. Note that the couplings of the Higgs to SM fermions can significantly depend on the QCD scale; microMEGAs assumes that the quark masses entering the vertices are obtained at the same scale in both the SM and the new model, thus the scale dependence in the reduced couplings to fermions disappears. The loop-induced couplings of the Higgs to gluons and photons are calculated by the LiLithMO/hbBlocksMO routines whether or not the Hgg and $H\gamma\gamma$ vertices are already implemented in the Lagrangian. This includes NLO-QCD corrections and is performed as described in [7,104].

The various branching ratios and widths of the Higgs required by HiggsBounds, HiggsSignals or Lilith are also written automatically in the interface file. When these values are provided in an SLHA file, they will be used. Otherwise LiLithMO/hbBlocksMO check the existence of $H \to gg$ and $H \to \gamma\gamma$ in the table of decays generated from the model Lagrangian. If found, the branching ratios and total widths are written in the interface file without comparing with the internal calculations. If not found, then LiLithMO/hbBlocksMO add these channels and recompute the total widths and all branching ratios.

14.2 Searches for New particles

14.2.1 SModelS

LHC limits on new (odd) particles can be obtained using SMode1S [41–45], a code which tests Beyond the Standard Model (BSM) predictions against Simplified Model Spectra (SMS) results from ATLAS and CMS searches for new physics. The basic working principle of SMode1S is to decompose a full input model (consisting of particle content, masses, production cross sections and decay widths) of a given BSM scenario into SMS components with their corresponding signal weights. These are then used to evaluate the constraints from a large database of experimental results. The outcome is presented as the ratio of predicted over excluded cross section, so-called r-values, for each experimental analysis in the database that provides a constraint. For efficiency-map type experimental results, the output also reports likelihoods. The (user-defined) combination of likelihoods from uncorrelated analyses is also possible [45, 105].

The SModelS approach provides a fast way to cast BSM predictions for the LHC in a model-independent framework, which can be directly confronted with the relevant experimental constraints. The underlying assumption is that differences in the event kinematics (e.g. from different production mechanisms or from the spin of the BSM particle) do not significantly affect the signal selection efficiencies. The majority of experimental results in the SModelS database are from searches for promptly decaying SUSY particles, but there are also a number of 'exotics' results and a growing number of results from searches for long-lived particles.

micrOMEGAs is now interfaced to version 3.0.0 of SModelS, which, among other novelties, features an improved treatment of width-dependent constraints. Most importantly, this new version can handle arbitrary simplified model topologies, without the need of an imposed \mathcal{Z}_2 -like symmetry. It is thus capable of treating also resonant production of new particles, RPV signatures, etc., in addition to the pair-production of new particles followed by linear cascade decays, which is typical for models with a \mathcal{Z}_2 -like symmetry.

For running SModelS, micrOMEGAs automatically generates an SLHA-type input file smodels.slha which contains

- QNUMBER blocks for the BSM particles as specification of the model;
- MASS block for masses of BSM particles;
- DECAY blocks for decay widths and branchings for BSM and Higgs particles;
- XSECTION blocks which contains cross sections of LHC processes with production of BSM particles.¹³

 $^{^{13}\}mathrm{At}$ present, cross sections are computed automatically for $pp\to \mathrm{BSM}\,\mathrm{BSM}$ production. Resonant (s-

This input file, per default called smodels.slha, is located in the same directory as main.c and is written by micrOMEGAs by calling the function

```
smodels(Pcm, nf, csMinFb, fileName, version, wrt)
```

where Pcm is the proton beam energy in GeV and nf is the number of parton flavors used to compute the production cross sections of the odd-sector particles. (Note that u, d, \bar{u} , \bar{d} and gluons are always included while s, c, and b quarks are included for nf = 3, 4, 5 respectively.) By default, micrOMEGAs uses the cteq66 [100] structure functions (set in the hCollider() function, see section 12). csMinFb defines the minimum production cross section in pb for odd particles; processes with lower cross sections are not added to the SLHA file passed to SModelS, here denoted by fileName. Finally, wrt is a steering flag for the screen output; if wrt $\neq 0$ the computed cross sections will be also written on the screen. The call of smodels() is per default done in the file micromegas_6.1.X/include/SMODELS.inc

For this functionality, the user first needs to specify which LHC energies should be considered. This is done by setting in main.c the switch

```
LHCrun = LHC8 and/or LHC13
```

for Run 1 (8 TeV), Run 2 (13 TeV) or both. This determines whether 8 TeV or 13 TeV cross sections or both will be appended to the SLHA file, which in turn determines which simplified model results will be considered from the SModelS database.

The run parameters for SModelS can be set in the file

```
micromegas_6.1.X/include/smodels_parameters.ini.
```

This concerns for example the parameter sigmacut, which is the cutoff cross section for topologies to be considered in the decomposition. Also the database version to be used is set in this parameters file; the default is path = official, which means that the official database pickle file corresponding to the SModelS code version will be downloaded and used. An interesting alternative may be to set path = latest, in which case always the latest available database will be used.

The SModelS parameters combineSRs and combineAnas can now be defined in main.c.

- combineSRs != 0 turns on the combination of signal regions on when a covariance matrix or full JSON likelihood is available, see [43, 106]. 14
- combineAnas = [list of analysis IDs] is a text parameter, which lists the analyses to be combined in a global likelihood. This switch works only for analyses with efficiency-map results. All the analyses are assumed to be fully uncorrelated, so use with caution!

channel) or associated production of one new particle, i.e. $pp \to BSM$ or $pp \to BSM$ SM, which is relevant for models without a \mathcal{Z}_2 -like symmetry, will be added in a future release of the micrOMEGAs-SModelS interface.

¹⁴Signal region combination can significantly increase the sensitivity of an analysis. However, since it can require much more CPU time, considerably increasing the run time, it is turned off by default.

By default, char*combineAnas=NULL;. For example, the following can be set by the user char*combineAnas= "ATLAS-SUSY-2018-41, ATLAS-SUSY-2019-08, CMS-SUS-21-002"; For detailed information on the different options and parameters available, see the online SModelS manual.

The output is written in SLHA-type format to smodels.slha.smodelsslha (or an alternative name selected by the user in SMODELS.inc). This output consists of the following blocks:

- SModelS_Settings, which lists the SModelS code and database versions as well as input parameters for the decomposition;
- SModelS Exclusion, which contains as the first line the status information if a point is excluded (1), not excluded (0), or not tested (-1), the latter being reported when no matching SMS results are found. This is followed by the list of experimental results. If expandedOutput = True (default), all results are printed. Otherwise, if the model is excluded, all results with r-value greater than one are shown and if the point is not excluded, only the result with the highest r-value is displayed;
- SModelS_CombinedAnas containing information about the combination of results, if combineAnas is defined (see above);
- SModelS_Coverage, which, if testCoverage is set to True (default: False) in the parameters file, lists the cross sections of missing topologies with prompt and/or displaced decays, and of topologies outside the grids of the experimental results

If a point is excluded (status 1), this is followed by a list of all results with r > 1, starting from the highest r-value. We remind the user that the SModelS r-values are defined as the ratio of the predicted theory cross section and the corresponding experimental upper limit at 95% confidence level. For each of these results, the SMS topology identifier as entry 0 (so-called Tx-name, see the online SMS dictionary for an explanation of the terminology), the r-value as entry 1, a measure of condition violation as entry 2, and the analysis identifier as entry 3 are listed. If the point is not excluded (status 0), the result with the highest r-value is given instead to show whether a point is close to the exclusion limit or not.

Last but not least, in order to exploit decay channels involving a SM-like Higgs for which the experimental collaborations assumed SM branching ratios for the h with the mass fixed to $m_h = 125$ GeV, microMEGAs checks whether neutral scalar particles with a mass in the range 123–128 GeV have branching ratios to WW^* , ZZ^* , $\tau\tau$, $b\bar{b}$ within 15% of those of a SM Higgs of the same mass. The corresponding particle will be identified as a SM Higgs through PDG code 25 in the smodels.slha file. Note that, for SModelS, PDG code 25 is reserved for a SM-like Higgs and should not be assigned generically.

14.2.2 Other limits

Limits from searches for a new massive Abelian gauge boson at the LHC, from LEP on an invisible Z as well as limits on light neutralinos from LEP are provided through the functions:

• Zinvisible()

returns 1 and prints a WARNING if the invisible width of the Z boson of the Standard

Model is larger than 0.5 MeV ([107]) and returns 0 if this constraint is fulfilled. This routine can be used in any model with one DM where the Z boson is uniquely defined by its PDG=23 and whether the neutral LSP is its own antiparticle or not.

• Zprimelimits()

returns 0 if the scenario considered is not excluded by Z' constraints, 1 if the point is excluded and 2 if both subroutines dealing with Z' constraints cannot test the given scenario. The routine can be used for any Z' uniquely defined by the PDG code 32. Currently two types of searches defined in different subroutines of Zprimelimits() are implemented. The 3.2/fb Z' search in the dilepton final state at $\sqrt{s} = 13$ TeV from ATLAS [108] is considered in the first subroutine Zprime_dilepton. If the scenario considered is allowed or not tested by Zprime_dilepton, a second subroutine called Zprime_dijet analyses the point using constraints from LHC dijet searches at $\sqrt{s} = 8$ TeV [109–111] and at $\sqrt{s} = 13$ TeV [112,113]. This subroutine uses the recasting performed in [114] for a combination of ATLAS and CMS searches. Zprimelimits() returns 1 if $M_{Z'} < 0.5$ TeV and 2 for points for which the narrow-width approximation is not valid, i.e. $\Gamma/M_{Z'} > 0.3$.

• LspNlsp_LEP(&ncs)

checks the compatibility with the upper limit obtained at LEP [115] on the cross section for the production of neutralinos $\sigma(e^+e^- \to \tilde{\chi}_1^0 \tilde{\chi}_i^0)$, $i \neq 1$, when the heavier neutralino decays into quark pairs and the LSP, $\tilde{\chi}_i^0 \to \tilde{\chi}_1^0 q \bar{q}$. The function calculates ncs= $\sigma \times BR = \sum_i \sigma(e^+e^- \to \tilde{\chi}_1^0 \tilde{\chi}_i^0) \times \text{BR}(\tilde{\chi}_i^0 \to \tilde{\chi}_1^0 q \bar{q})/cs_{Lim}$ where $cs_{Lim} = 0.1 \text{pb}$ if $m_{\text{NLSP}} > 100 \text{GeV}$ and 0.5pb otherwise. The function returns 1 if ncs >= 1 and 0 otherwise. This function can also be applied for non-SUSY models which feature the same signature, in this case the function will compute the cross section for production of the LSP and any other neutral particle from the odd sector which can decay into the LSP and a Z boson.

monoJet(pName1,pName2)

computes the cross section for $p, p \to pName1, pName2+jet$ at $\sqrt{s}=8$ TeV where pName1, pName2 are the names of neutral outgoing particles and jet includes light quarks (u,d,s) and gluons. The function returns the resulting confidence level obtained with the CLs technique [116,117] for each signal region of the 8 TeV CMS mono-jet analysis [118] and chooses the most constraining one.

15 Additional routines for specific models

The models included in micrOMEGAs contain some specific routines which we describe here for the sake of completeness. The current distribution includes the following models: MSSM, NMSSM, CPVMSSM, IDM (inert doublet model), LHM(little Higgs model), Z3IDM (Inert doublet model with Z_3 symmetry), Z4IDSM (Inert doublet and singlet model with Z_4 symmetry, Z5M (Two scalar singlets model with Z_4 symmetry), RDM (scalar leptoquark and two singlet fermions), STFM (singlet-triplet fermionic model) as well as three models which serve as examples for freeze-in and for which there are currently no additional routines (SingletDM, ZpPortal, LLL_scalar).

Some of these models contain a special routine for reading the input parameters:

• readVarMSSM, readVarNMSSM, readVarCPVMSSM, readVarlHiggs, readVarRHNM.

These routines are similar to the general readVar routine described in Section 5 but they

write a warning when a parameter is not found in the input file and display the default values for these parameters.

The supersymmetric models contain several additional routines to calculate the spectrum and compute various constraints on the parameter space of the models. Some functions are common to the MSSM, NMSSM, CPVMSSM, UMSSM models:

• o1Contents(FD)

prints the neutralino LSP components as the $\tilde{B}, \tilde{W}, \tilde{h_1}, \tilde{h_2}$ fractions. For the NMSSM the fifth component is the singlino fraction \tilde{S} and for the UMSSM the sixth component is the bino' fraction \tilde{B}' . The sum of the squares of the LSP components should add up to 1.

15.1 The MSSM

The MSSM has a long list of low scale independent model parameters, those are specified in the SLHA file [51,119]. They are directly implemented as parameters of the model. micrOMEGAs can either read an SLHA file computed externally or generate this file in the framework of popular SUSY scenarios, these are specified by one of the instructions

#define SUGRA
#define SUGRANUH
#define AMSB
#define EWSB

If none of these instructions are given then micrOMEGAs reads the external SLHA file which should be passed as an argument when executing the *main* routine. To generate an SLHA file, micrOMEGAs uses either SuSpect, SPHENO, or SoftSusy. These codes, if need be, solve the RGE equations and calculate the masses of Higgs and SUSY particles including one-loop corrections. Note that SuSpect is included within the micrOMEGAs distribution while SPHENO or SOFTSUSY will be downloaded automatically when needed (see section 3.4). To specify the spectrum calculator the user has to define the parameter RGE in *main.c/main.cpp*. For instance

#define RGE suspect

Other possibilities for RGE are softSusy, spheno and tree. The option tree will generate the needed SLHA file for the spectrum using EWSB input parameters and tree-level formulas. One-loop corrections to the Higgs masses and to the effective Higgs potential are based on [120]. In this case, the realization of the MSSM is completely gauge invariant. This option can be useful to check the effect of loop corrections.

For **EWSB** scenarios the input parameters are the soft parameters, the names of these parameters are given in the MSSM/mssm[1/2].par files. The user can assign new values to these parameters by means of assignVal or readVarMSSM.

• spectEwsbMSSM()

calculates the masses of Higgs and supersymmetric particles in the MSSM including one-loop corrections starting from weak scale input parameters.

In these functions *spect* is defined by RGE.

For other MSSM scenarios, the parameters at the electroweak symmetry breaking scale are derived from an input at high scale. The same codes suspect, spheno, or softSusy are used for this. The corresponding routines are:

• spectSUGRA(tb,MG1,MG2,MG3,A1,At,Ab,signMu,MHu,MHd,Ml1,Ml3,Mr1,Mr3,Mq1,Mq3,Mu1,Mu3,Md1,Md3)

assumes that all input parameters except tb and signMu are defined at the GUT scale. The SUGRA/CMSSM scenario is a special case of this general routine.

• spectSUGRAnuh(tb,MG1,MG2,MG3,A1,At,Ab,Ml1,Ml3,Mr1,Mr3,Mq1,Mq3,Mu1,Mu3,Md1,Md3,mu,MA)

realizes a SUGRA scenario with non universal Higgs parameters. Here the Mhu, MHd parameters in the Higgs potential are replaced with the mu parameter defined at the EWSB scale and MA, the pole mass of the CP-odd Higgs. The signMu parameter is omitted because mu is defined explicitly.

• spectAMSB(am0, m32, tb, sng).

does the same as above within the AMSB model.

We have an option to directly read a SLHA input file, this uses the function

• lesHinput(file_name)

which returns a non-zero number in case of problem.

The routines for computing constraints are (see details in [3]).

• deltarho()

calculates the $\Delta \rho$ parameter in the MSSM. It contains for example the stop/sbottom contributions, as well as the two-loop QCD corrections due to gluon exchange and the correction due to gluino exchange in the heavy gluino limit.

• bsgnlo(&SMbsg)

returns the value of the branching ratio for $b \to s\gamma$, see Appendix A. We have included some new contributions beyond the leading order that are especially important for high $\tan \beta$. SMbsg gives the SM contribution.

• bsmumu()

returns the value of the branching ratio $B_s \to \mu^+\mu^-$ in the MSSM. It includes the loop contributions due to chargino, sneutrino, stop and Higgs exchange. The Δm_b effect relevant for high tan β is taken into account. Code is bases on [121].

• btaunu()

computes the ratio between the MSSM and SM branching fractions for $\bar{B}^+ \to \tau^+ \nu_{\tau}$.

• gmuon()

returns the value of the supersymmetric contribution to the anomalous magnetic moment of the muon.

• R123()

computes the ratio of the MSSM to SM value for R_{l23} in $K^+ \to \mu\nu$ due to a charged higgs contribution, see Eq.70 in [7].

• dtaunu(&dmunu)

computes the branching ratio for $D_s^+ \to \tau^+ \nu_{\tau}$. dmunu gives the branching ratio for $D_s^+ \to \mu^+ \nu_{\mu}$

• masslimits()

returns a positive value and prints a WARNING when the choice of parameters conflicts with a direct accelerator limits on sparticle masses from LEP. The constraint on the light Higgs mass from the LHC is included.

• treeMSSM()

This function transforms a loop improved model defined in an SLHA file into a tree level one. The masses and mixing angles are stored in the file tree.slha. This option can be

useful to check the effect of loop induced masses and mixings. This option guarantees gauge invariance for all processes.

15.2 The NMSSM

As in the MSSM there are specific routines to compute the parameters of the model as specified in SLHA. The spectrum calculator is NMSPEC [11] in the NMSSMTools_5.0.1 package [27].

• nmssmEWSB()

calculates the masses of Higgs and supersymmetric particles in the NMSSM starting from the weak scale input parameters [28]. These can be downloaded by the readVarNMSSM routine.

• nmssmSUGRA(m0,mhf,a0,tb,sgn,Lambda,aLambda,aKappa) calculates the parameters of the NMSSM starting from the input parameters of the CNMSSM.

The routines for computing constraints are taken from NMSSMTools (see details in [4]).

- bsgnlo(&M,&P), bsmumu(&M,&P), btaunu(&M,&P), gmuon(&M,&P) are the same as in the MSSM case. Here the output parameters M and P give information on the lower/upper experimental limits [122]
- deltaMd(&M,&P), deltaMs(&M,&P) compute the supersymmetric contribution to the $B_{d,s}^0 \overline{B^0}_{d,s}$ mass differences, ΔM_d and ΔM_s .
- NMHwarn(FD)

is similar to masslimits_ except that it also checks the constraints on the Higgs masses, returns the number of warnings and writes down warnings in the file FD.

15.3 The CPVMSSM

The independent parameters of the model include, in addition to some standard model parameters, only the weak scale soft SUSY parameters. The independent parameters are listed in CPVMSSM/work/models/vars1.mdl. Masses, mixing matrices and parameters of the effective Higgs potential are read directly from CPsuperH [13, 123], together with the masses and the mixing matrices of the neutralinos, charginos and third generation sfermions. Masses of the first two generations of sfermions are evaluated (at tree-level) within micrOMEGAs in terms of the independent parameters of the model.

The routines for computing constraints are taken from CPsuperH, [29]

- bsgnlo(), bsmumu(), btaunu(), gmuon() are the same as in the MSSM case.
- deltaMd(), deltaMs() are the same as in the NMSSM case.
- Bdll()

computes the supersymmetric contribution to the branching fractions for $B_d \to \tau^+ \tau^-$ in the CPVMSSM.

• ABsg()

computes the supersymmetric contribution to the asymmetry for $B \to X_s \gamma$.

• EDMel(), EDMmu(), EDMTl()
return the value of the electric dipole moment of the electron d

return the value of the electric dipole moment of the electron, d_e , the muon, d_{μ} , and of Thallium, d_{Tl} in units of ecm.

15.4 The UMSSM

The independent parameters of the UMSSM are the standard model parameters and weak scale soft SUSY parameters listed in UMSSM/work/models/vars1.mdl. All masses, mixing matrices and parameters of the different sectors of the model are computed by micrOMEGAs [24, 25].

Some routines for computing constraints were taken from the MSSM and were adapted to the UMSSM. For example

- masslimits() which is essentially the same as in the MSSM except that the constraint on the light Higgs mass from the LHC was removed as other routines in the UMSSM include this constrain, or
- deltarho()

calculates the $\Delta \rho$ parameter in the UMSSM where in addition to MSSM contributions a pure UMSSM tree-level contribution from the extended Abelian gauge boson sector is included. Two other routines in C are included, Zinvisible() and Zprimelimits() that were defined above.

The remaining routines for computing B-physics, K-physics and Higgs observables as well as the anomalous magnetic moment of the muon were taken from NMSSMTools_5.0.1 and adapted to the UMSSM [24,124]. To call these routines use umssmtools(PDG_LSP) where PDG_LSP is the PDG code of the LSP. The result is contained in four files (UMSSM_inp.dat, UMSSM_spectr.dat, UMSSM_decay.dat and SM_decay.dat) and the WARNING messages from these routines can be displayed with slhaWarnings(stdout).

As in the NMSSM the following routines are available:

• bsg(&M,&P), bsmumu(&M,&P), btaunu(&M,&P), gmuon(&M,&P), deltamd(&M,&P), deltams(&M,&P).

as well as the routines

• bdg(&M,&P), bdmumu(&M,&P), bxislllow(&M,&P), bxisllhigh(&M,&P), bxisnunu(&M,&P), bksnunu(&M,&P), rdtaul(&M,&P), rdstaul(&M,&P)

to compute respectively $b \to d\gamma$, $B_d \to \mu^+\mu^-$, the $b \to sl^+l^-$ transition in the low ([1,6] GeV²) and high ($\geq 14.4 \text{ GeV}^2$) $m_{l+l^-}^2$ ranges, $B \to X_s \nu \bar{\nu}$, $B^+ \to K^+ \nu \bar{\nu}$, $B \to K^* \nu \bar{\nu}$, $R_D \equiv \frac{\text{BR}(B^+ \to D\tau^+\nu_{\tau})}{\text{BR}(B^+ \to Dl^+\nu_{l})}$ and $R_{D^*} \equiv \frac{\text{BR}(B^+ \to D^*\tau^+\nu_{\tau})}{\text{BR}(B^+ \to D^*l^+\nu_{l})}$.

The K-physics observables $K^+ \to \pi^+ \nu \bar{\nu}$, $K_L \to \pi^0 \nu \bar{\nu}$, ΔM_K and ϵ_K can be computed respectively with

• kppipnunu(&M,&P), klpiOnunu(&M,&P), deltamk(&M,&P), epsk(&M,&P).

See the README of the UMSSM for further details.

16 Tools for new model implementation

It is possible to implement a new particle physics model in micrOMEGAs. For this the model must be specified in the Calchep format. micrOMEGAs then relies on Calchep to generate the libraries for all matrix elements entering DM calculations. Below we describe the main steps and tools for implementing a new model.

16.1 Main steps

- The command ./newProject MODEL
 MODEL launched from the root micrOMEGAs directory creates the directory MODEL.
 This directory and the subdirectories contain all files needed to run micrOMEGAs with the exception of the new model files.
- The new model files in the CalcHEP format should then be included in the subdirectory MODEL/work/models. The files needed are vars1.mdl, func1.mdl, prtcls1.mdl, lgrng1.mdl, extlib1.mdl. For more details on the format and content of model files see [1].
- For odd particles and for the Higgs sector it is recommended to use the widths that are (automatically) calculated internally by CalcHEP/micrOMEGAs. For this one has to add the '!' symbol before the definition of the particle's width in the file prtcls1.mdl, for example

• Some models contain external functions, if this is the case they have to be compiled and stored in the MODEL/lib/aLib.a library. These functions should be written in C and both functions and their arguments have to be of type double. The library aLib.a can also contain some functions which are called directly from the main program. The MODEL/Makefile automatically launches make in the lib directory and compiles the external functions provided the prototypes of these external functions are specified in MODEL/lib/pmodel.h. The user can of course rewrite his own—lib/Makefile if need be.

If the new aLib.a library needs some other libraries, their names should be added to the SSS variable defined in MODEL/Makefile.

The MODEL directory contains samples of *main* routines. In these sample main programs it is assumed that input parameters are provided in a separate file. In this case the program can be launched with the command:

```
./main data1.par
```

Note that for the direct detection module all quarks must be massive. However the cross sections do not depend significantly on the exact numerical values for the masses of light quarks.

16.2 Automatic width calculation

Automatic width calculation can be implemented by inserting the '!' symbol before the name of the particle width in the CalcHEP particle table (file prtcls1.mdl). In this case the width parameter should not be defined as a free or constrained parameter. Actually the pWidth function described in section 12 is used for width calculation in this case. We recommend to use the automatic width calculation for all particles from the 'odd' sector and for Higgs particles. For models which use SLHA parameter transfer (Section 16.6), the automatic width option will use the widths computed internally unless the user chooses to use those contained in the SLHA file by setting useSLHAwidth=1.

16.3 One-loop scalar vertices

The loop-induced couplings of scalars and pseudoscalars to gluons and photons can be calculated internally by micrOMEGAs with the use of the functions described below. First, effective vertices mush be defined in the model file. These vertices correspond to the Lagrangian

$$\mathcal{L} = \lambda h F_{\mu\nu} F^{\mu\nu} + \lambda_5 h F_{\mu\nu} \tilde{F}^{\mu\nu} \tag{62}$$

where the first term is the effective operator for the CP-even part while the second term is for the CP-odd part. Similar operators can be defined for the couplings to gluons with $F^{\mu\nu}$ replaced by $G^{\mu\nu}$. In the CalcHEP notation, the vertices will appear in the file lgrng1.mdl as

where LAAh, LAA5h correspond respectively to λ , λ_5 in Eq. 62. These coefficients are computed internally by micrOMEGAs with the functions

•lAAhiggs(Mass, Name)

which calculates the coefficient of the loop-induced Scalar - photon - photon vertex based on the generic contributions of scalars/fermions/vector bosons given in Ref. [125]. Here Name specifies the scalar and Mass its mass. To do this, micrOMEGAs searches the model file to find the couplings of the scalar to all possible coloured scalars/fermions or vector bosons that can enter the one-loop process.

•lAA5higgs(Mass,Name)

which calculates the coefficient of the loop-induced Pseudoscalar - photon - photon vertex based on the results in Ref. [125] where Name specifies the pseudoscalar and Mass its mass.

As explained in [7, 126], an overall QCD correction factor is included for coloured particles in the loop. HDECAY [104] is used to generate this factor and is therefore tuned for the SM Higgs.

Similar effective operators can be defined for hgg vertices. The vertex describing the couplings of the Higgs to gluon pairs is defined

where RQCDh is the NLO QCD correction corresponding to the radiation of gluons for the SM Higgs. Other NLO QCD vertex corrections for heavy quarks, light quarks and coloured scalars are included in the coefficient of the vertex as described in [7, 126]. As for the photon, the coefficients including NLO QCD vertex corrections are computed internally by micrOMEGAs with the functions

•lGGhiggs(Mass,Name)

which calculates the coefficient of the loop-induced Scalar - gluon - gluon vertex based on the formulae in Ref. [125] where Name specifies the scalar and Mass its mass.

•lGG5higgs(Mass,Name)

which calculates the coefficient of the loop-induced Pseudoscalar - gluon - gluon vertex based on the formulae in Ref. [125] where Name specifies which scalar and Mass its mass.

The coefficient of the vertices should be defined in func1.mdl, for example for the scalar vertices

```
LAAh |-cabs(lAAhiggs(Mh, "h"))

LGGh |-cabs(lGGhiggs(Mh, "h"))

and the overall QCD corrections are defined with

aQCDh |alphaQCD(Mh)/acos(-1)

RQCDh |sqrt(1+149/12*aQCDh+68.6482*aQCDh^2-212.447*aQCDh^3)|
```

where alphaQCD(Mh) is the strong coupling, $\alpha_s(m_h)$ evaluated at the Higgs mass. Note that this construction is tuned for Higgs decays. In particular the RQCDh factor is caused by hadronization of gluons. For $g,g\to H$ production, other NLO factors need to be introduced by the user. The difference between NLO production and decays is ignored in micrOMEGAs. The scale entering the definition of α_s can be adapted to the process under consideration.

The four functions for loop-induced vertices were not available in micrOMEGAs' versions before v5.1, hence most of the models implemented use the functions introduced in [7] where the user had to give by hand the names of all particles that could contribute to the triangle diagrams. The IDM model is an example where this newer and simpler implementation of the loop-induced vertices can be found.

Note that in the interface to Lilith and HiggsBounds, the loop induced couplings to the Higgs are calculated by the LiLithMO/hbBlocksMO routines whether or not the Hgg and $H\gamma\gamma$ vertices are already implemented in the Lagrangian, as mentioned in section 14.1.

16.4 Using LanHEP for model file generation

For models with a large number of parameters and various types of fields/particles such as the MSSM, it is more convenient to use an automatic tool to implement the model. LanHEP is a tool for Feynman rules generation. A few minor modifications to the default format of LanHEP have to be taken into account to get the model files into the micromegas format.

• The **lhep** command has to be launched with the -ca flag

```
lhep -ca source_file
```

• The default format for the file prtcls1.mdl which specifies the particle content has to be modified to include a column containing the PDG code of particles. For this, first add the following command in the LanHEP source code, before specifying the particles

```
prtcformat fullname:
'Full Name', name:' P', aname:' aP', pdg:' number ',
spin2,mass,width, color, aux, texname: '> LaTeX(A) <',
atexname:'> LateX(A+) <' .

Then for each particle define the PDG code. For instance:
vector 'W+'/'W-': ('W boson', pdg 24, mass MW, width wW).</pre>
```

• LanHEP does not generate the file extlib1.mdl. micrOMEGAs works without this file but it is required for a CalcHEP interactive session. The role of this file is to provide the linker with the paths to all user's libraries needed at compilation. For example for the lib/aLib.a library define

```
$CALCHEP/../MODEL/lib/aLib.a
```

For examples see the extlib1.mdl files in the directory of the models provided.

16.5 QCD functions

Here we describe some QCD functions which can be useful for the implementation of a new model.

• initQCD(alfsMZ,McMc,MbMb,Mtp)

This function initializes the parameters needed for the functions listed below. It has to be called before any of these functions. The input parameters are the QCD coupling at the Z scale, $\alpha_s(M_Z)$, the quark masses, $m_c(m_c)$, $m_b(m_b)$ and $m_t(pole)$.

- alphaQCD(Q)
- calculates the running α_s at the scale Q in the \overline{MS} scheme. The calculation is done using the NNLO formula in [127]. Thresholds for the b-quark and t-quark are included in n_f at the scales $m_b(m_b)$ and $m_t(m_t)$ respectively.
- MtRun(Q), MbRun(Q), McRun(Q) calculates top, bottom and charm quarks running masses evaluated at NNLO.
- MtEff(Q), MbEff(Q), McEff(Q), calculates effective top, bottom and charm quark masses using [127]

$$M_{eff}^{2}(Q) = M(Q)^{2} \left[1 + 5.67a + (35.94 - 1.36n_{f})a^{2} + (164.14 - n_{f}(25.77 - 0.259n_{f}))a^{3} \right]$$
(63)

where $a = \alpha_s(Q)/\pi$, M(Q) and $\alpha_s(Q)$ are the quark masses and running strong coupling in the \overline{MS} -scheme. In micromegas, we use the effective quark masses calculated at the scale Q = 2Mcdm. In some special cases one needs a precise treatment of the light quarks masses. The function

- MqRun(M2GeV, Q)
- returns the running quark mass defined at a scale of 2 GeV. The corresponding effective mass needed for the Higgs decay width is given by
- Mqeff(M2GeV, Q)

16.6 SLHA reader

Very often the calculation of the particle spectra for specific models is done by some external program which writes down the particle masses, mixing angles and other model parameters in a file with the so-called **SLHA** format [51,119]. The microMEGAs program contains routines for reading files in the SLHA format. Such routines can be very useful for the implementation of new models.

In general a SLHA file contains several pieces of information which are called blocks. A block is characterized by its name and, sometimes, by its energy scale. Each block contains the values of several physical parameters characterized by a *key*. The key consists in a sequence of integer numbers. For example:

```
BLOCK MASS
             # Mass spectrum
                                 particle
# PDG Code
                mass
        25
               1.15137179E+02
                                # lightest neutral scalar
        37
               1.48428409E+03
                                # charged Higgs
BLOCK NMIX # Neutralino Mixing Matrix
           9.98499129E-01
                            # Zn11
    1
  1
    2
          -1.54392008E-02
                            # Zn12
BLOCK Au Q= 4.42653237E+02 # The trilinear couplings
          -8.22783075E+02
                            # A_u(Q) DRbar
    1
    2
          -8.22783075E+02
                            # A_c(Q) DRbar
```

• slhaRead(filename, mode)

downloads all or part of the data from the file filename. mode is an integer which determines which part of the data should be read form the file, mode= 1*m1+2*m2+4*m4 where

```
m1 = 0/1 -  overwrites all/keeps old data

m2 = 0/1 -  reads DECAY /does not read DECAY

m4 = 0/1 -  reads BLOCK/does not read BLOCK
```

For example mode=2 (m1=0,m2=1) is an instruction to overwrite all previous data and read only the information stored in the BLOCK sections of filename. In the same manner mode=3 is an instruction to add information from DECAY to the data obtained previously. slhaRead returns the values:

```
0 - successful reading
-1 - can not open the file
-2 - error in spectrum calculator
-3 - no data
n>0 - wrong file format at line n
```

• slhaValExists(BlockName, keylength, key1, key2,...)

checks the existence of specific data in a given block. BlockName can be substituted with any case spelling. The keylength parameter defines the length of the key set {key1,key2,...}. For example slhaValExists("Nmix",2,1,2) will return 1 if the neutralino mass mixing element Zn12 is given in the file and 0 otherwise.

• slhaVal(BlockName,Q, keylength, key1, key2,....)

is the main routine which allows to extract the numerical values of parameters. BlockName and keylength are defined above. The parameter $\mathbb Q$ defines the scale dependence. This parameter is relevant only for the blocks that contain scale dependent parameters, it will be ignored for other blocks, for example those that give the particle pole masses. In general a SLHA file can contain several blocks with the same name but different scales (the scale is specified after the name of the block). slhaVal uses the following algorithm to read the scale dependent parameters. If $\mathbb Q$ is less(greater) than all the scales used in the different blocks for a given parameter slhaVal returns the value corresponding to the minimum(maximum) scale contained in the file. Otherwise slhaVal reads the values corresponding to the two scales Q_1 and Q_2 just below and above $\mathbb Q$ and performs a linear interpolation with respect to $\log(\mathbb Q)$ to evaluate the returned values.

Recently it was proposed to use an extension of the SLHA interface to transfer Flavour Physics data [128]. Unfortunately the structure of the new blocks is such that they cannot be read with the slhaVal routine. We have added two new routines for reading such data

• slhaValFormat(BlockName, Q, format)

where the *format* string allows to specify data which one would like to extract from the given block BlockName. For instance, to get the $b \to s\gamma$ branching ratio from the block

Block FOBS # Flavour observables

```
# ParentPDG type value
                                  NDA ID1 ID2 ID3 ... comment
    5
             2.95061156e-04
                                    2
                                        3
                                            22
                                                    # BR(b->s gamma)
  521
             8.35442304e-02
                              0
                                    2 313
                                            22
                                                    # Delta0(B->K* gamma)
             3.24270419e-09
                                      13 -13
                                                    \# BR(B_s->mu+mu-)
  531
```

one has to use the command slhaValFormat("FOBS", 0., "5 1 %E 0 2 3 22"). In this command the *format* string is specified in C-style. The same routine can be used to read HiggsBound SLHA output.

A block can also contain a textual information. For example, in HIGGSBOUNDS a block contains the following records,

${\tt Block\ HiggsBoundsResults}$

In particular, the last record contains the name of the channel which gives the strongest constraint on the Higgs. To extract the name of this channel one can use the new function

- slhaSTRFormat("HiggsBoundsResults","1 5 || %[^|]||",channel); which will write the channel name in the text parameter *channel*.
- slhaWarnings(fileName)

writes into the file the warnings or error message stored in the SPINFO block and returns the number of warnings. If FD=NULL the warnings are not written in a file.

• slhaWrite(fileName)

writes down the information stored by readSLHA into the file. This function can be used for testing purposes.

SLHA also describes the format of the information about particle decay widths. Even though micrOMEGAs also performs the width calculation, one might choose to read the information from the SLHA file.

slhaDecayExists(pNum)

checks whether information about the decay of particle pNum exists in the SLHA file. pNum is the particle PDG code. This function returns the number of decay channels. In particular zero means that the SLHA file contains information only about the total width, not on branching ratios while -1 means that even the total width is not given.

- slhaWidth(pNum)
- returns the value of particle width.
- slhaBranch(pNum,N, nCh)

returns the branching ratio of particle pNum into the N-th decay channel. Here O<N<=slhaDecayExists(pNum). The array nCh is an output which specifies the PDG numbers of the decay products, the list is terminated by zero.

The functions slhaValExists, slhaVal, slhaDecayExists, slhaWidth can be used directly in CalcHEP model files, see an example in

MSSM/work/models/func3.mdl. Note that in this example the call to slhaRead is done within the function suspectSUGRAc.

16.6.1 Writing an SLHA input file

We have included in the micrOMEGAs package some routines which allow to write an SLHA input file and launch the spectrum generator via the CalcHEP constraints menu. This way a new model can be implemented without the use of external libraries. The routines are called from func1.mdl, see example below.

• openAppend(fileName)

deletes the input file fileName and stores its name. This file will then be filled with the function aPrintF.

- aPrintF(format,...)
- opens the file fileName and writes at the end of the file the input parameters needed in the SLHA format or in any other format understood by the spectrum calculator. The arguments of aPrintF are similar to the arguments of the standard printf function.
- System(command, ...) generates a command line which is launched by the standard system C-function. The parameter *command* works here like a format string and can contain %s, %d elements. These are replaced by the next parameters of the System call.

For example to write directly the SLHA model file needed by SuSpect to compute the spectrum in a CMSSM(SUGRA) model, one needs to add the following sequence in the func1.mdl model file.

```
open |openAppend("suspect2_lha.in")
input1|aPrintF("Block MODSEL # Select model\n 1 1 # SUGRA\n")
input2|aPrintF("Block SMINPUTS\n 5 %E#mb(mb)\n 6 %E#mt(pole)\n",MbMb,Mtp)
input3|aPrintF("BLOCK MINPAR\n 1 %E #m0\n 2 %E #m1/2\n ",Mzero,Mhalf)
input4|aPrintF("3 %E #tb\n 4 %E #sign(mu)\n 5 %E #A0\n",tb,sgn,A0)
sys |System("./suspect2.exe")
rd |slhaRead("suspect2_lha.out",0)
```

It is possible to cancel the execution of a program launched with System if it runs for too long. For this we have introduced two global parameters sysTimeLim and sysTimeQuant. sysTimeLim sets a time limit in milliseconds for System execution, if sysTimeLim==0 (the default value) the execution time is not checked. The time interval between checks of the status of the program launched with System is specified by the parameter sysTimeQuant, the default value is set to 10. Note that it is preferable not too use too large a value for sysTimeQuant as it defines the lower time limit for a system call.

The function prototypes are available in CalcHEP_src/c_source/SLHAplus/include/SLHAplus.h

16.7 Routines for diagonalisation

Very often in a new model one has to diagonalize mass matrices. Here we present some numerical routines for diagonalizing matrices. Our code is based on the jacobi routine provided in [129]. To use the same routine for a matrix of arbitrary size, we use a C option that allows to write routines with an arbitrary number of arguments.

- initDiagonal() should be called once before any other rDiagonal(A) routine described below. initDiagonal() assigns zero value to the internal counter of eigenvalues and rotation matrices. Returns zero.
- ullet rDiagonal(d,M11,M12,..M1d,M22,M23...Mdd) diagonalizes a symmetric matrix of dimension d. The d(d+1)/2 matrix elements, Mij $(i \leq j)$, are given as arguments. The function returns an integer number id which serves as an identifier of eigenvalues vector and rotation matrix.
- MassArray(id, i) returns the eigenvalues m_i ordered according to their absolute values.
- MixMatrix(id,i,j) returns the rotation matrix R_{ij} where

$$M_{ij} = \sum_{k} R_{ki} m_k R_{kj}$$

A non-symmetric matrix, for example the chargino mass matrix in the MSSM, is diagonalized by two rotation matrices,

$$M_{ij} = \sum_{k} U_{ki} m_k V_{kj}.$$

• rDiagonalA(d,M11,M12..M1d,M21,M22...Mdd)
diagonalizes a non-symmetric matrix, the d² matrix

diagonalizes a non-symmetric matrix, the d^2 matrix elements, Mij, are given as arguments. The eigenvalues and the V rotation matrix are calculated as above with MassArray and MixMatrix.

• MixMatrixU(id,i,j) returns the rotation matrix U_{ij} .

One can find example of work of diagonalozation routines in mdlIndep/diagonal.c. The function prototypes can be found in

CalcHEP_src/c_source/SLHAplus/include/SLHAplus.h

17 Mathematical tools

Some mathematical tools used by micromegas are available only in C format. Prototypes of these functions can be found in

include/micromegas_aux.h

17.1 Integration

• simpson(F, x1, x2, eps,&err)

performs numerical integration of the function F(x) in the interval [x1,x2]. simpson tries to reach relative precision eps or absolute precision $\frac{eps}{10} \int_{x1}^{x2} |F(x)| dx$. For one interval simpson compares the results of 3, 5 and 9 points formulas. If they do not agree within the required precision, simpson splits the interval in two and applies the same procedure recursively. The smallest interval is $|x_2 - x_1|/2^{25 - log(eps)}$.

A non-zero error code *err* means

- 1: NAN in integrand: simpson replaces NAN by zero and continues integration
- 2: Too deep recursion: one needs the smallest minimal interval to reach the required precision. For instance, these two error codes will show up in the integration of $\int dx/|x|^{0.8}$ with a precision $eps = 10^{-3}$.
- 4: Lost of precision: If in a small interval $\approx |x1-x2|/2^{10}$ the derivative of the function changes sign more than twice, it is treated as a lost of precision in the integrand and simpson decreases precision to eps=0.01 and treats uncertainties of each interval as a random numbers.

In case of several error messages, err contains their sum. If the last argument of simpson is NULL, the error messages are displayed on the screen. If the integrand has a discontinuity or a pole, the requirement of reaching a fixed relative precision can not be satisfied. Thus we also stop the recursion if the integration uncertainty on the interval is small as compared to the current estimation of $\frac{eps}{10} \int_{x1}^{x2} |F(x)| dx$. Since the current estimation of this integral can be significantly smaller than the final one, we keep the sum of errors obtained at the end of the recursion chains and compare it with the final estimation of the total integral. It the sum of errors is small, then the error 2 is not generated.

We have implemented a debugging tool for the simpson code based on gdb. To initiate it the user has to launch the ./main code under gdb and set a breakpoint

```
gdb ./main
break verifySimpson
r inputParameters  // to launch code
```

The execution of the program will stop when simpson generates an error code. With the bt command one can see the sequence of calls leading to the problematic call of simpson. After

```
n // next
```

command one reaches the cycle which is executed until the variable $show \neq 0$. The user should see on the screen

```
293 while(show) {drawP(f, par, x1, x2,ans,nErr);
```

By default show=0 and the cycle is not executed, but it can be changed by the set command

```
set show=1
```

and the user will see a plot of the function F(x) on the screen. When the user closes the window with the plot, he/she will reach the next line of code

```
294 continue; }
```

Here the user can leave the cycle using the commands

or verify a narrower range of the function F(x) by redefining the variables x1 and x2.

The file mdlIndep/simpson.c contains several examples which allow to test how this routine works.

- gauss (F,x1,x2,N) performs Gauss N-point integration for N < 8.
- peterson21(F, x1, x2,&aErr)

performs numerical integration of the function F(x) in the interval [x1, x2] using Gauss-Kronrod-Peterson formula with 21 points. aErr is a parameter which returns the accuracy of the calculation using 10 points subset.

17.2 Solution of differential equations.

- odeint(Y, Dim, x1, x2, eps,h1, deriv)
- solves a system of Dim differential equations in the interval [x1, x2]. The Dim component array Y contains the starting variables at x1 as an input and is replaced by the resulting values at x2 as an output. eps determines the precision of the calculation and h1 gives an estimation of step of integration. The function deriv calculates $Y'_i = dY_i/dx$ with the call deriv(x, Y, Y'). The Runge-Kutta method is used, see details in [129].
- stiff (first, x1, x2, Dim, Y, Yscal, eps, &htry,derivs)
- stifbs(first, x1, x2, Dim, Y, Yscal, eps, &htry,derivs)

these two functions solve stiff differential equations. Both routines are slightly adapted codes from [129]. Here the parameters x1, x2, Dim, Y have the same meaning as in the routine odeint above. The parameter first should be set to one for the first call to the routines with a given number of equations Dim and to zero for subsequent calls. The flag first is used for memory allocation. If Yscal=NULL the parameter eps defines the absolute precision of calculation ($\delta Y_i < eps$). Otherwise, the precision is defined by the condition $\delta Y_i < epsYscale_i$. The parameter htry defines the initial step of integration and contains the last step of integration used during calculations. The function derivs evaluates the differential equation F = dY/dx and its partial derivatives:

```
derivs(x, Y, F, h, dFdx,dFdY) where dFdY[i*Dim+j]=\frac{dF_i}{dY_i}
```

This routine can be called with parameters dFdx=NULL and dFdY=NULL. The parameter h presents current step of integration and can be used for numerical evaluation of dFdx.

17.3 Interpolation

- polint3(x,Dim,X,Y) performs cubic interpolation for *Dim*-dimension arrays X,Y. Similar functions, polint1 performs linear interpolations.
- spline(x, y, dim, y2)
- splint(x, y, y2, dim, double x0, &y0)

spline constructs cubic spline and splint calculates spline interpolation y0 for a given point x0. Here x and y are a grid of function arguments and function values $y_i = Y(x_i)$. The function spline fills an array of second derivatives y2 which is used by splint.

• buildInterpolation(F,x1,x2,eps,delt, &Dim,&X,&Y) constructs a cubic interpolation of the function F in the interval [x1,x2]. eps controls the precision of interpolation. If eps < 0 the absolute precision is fixed, otherwise a relative precision is required. The delt parameter limits the distance between interpolation points: $|x_i - x_{i+1}| < delt|x2 - x1|$. The function checks that after removing any grid point, the function at that point can be reproduced with a precision eps using only the other points. It means that the expected precision of interpolation is about eps/16. Dim gives the number of points in the constructed grid. X and Y are variables of the double* type. The function allocates memory for the Dim array for each of these parameters. X[i] contains the x-grid while Y[i] = F(X[i]).

17.4 Functions with additional parameters

We use routines that work with functions of type double F(double x,void*arg), where the structure of arg is open, here arg presents the memory address where these parameters are stored. This is useful for example for integrating a function f(x,y) over x, y is then passed as 'arg'. The functions available are simpson_arg, peterson21_arg, buildInterpolation_arg. The additional argument is the address arg which is specified just after the function name.

The recent versions of C-compiler may refuse the substitution of a function if the type of the argument does not correspond. For example, if there is a problem for the function double myF(double x, double *par)

to be used in simpson_arg, we recommend to use a type conversion: simpson_arg((funcArg) myF,)

17.5 Plots

• displayPlot(title,xName,xMin,xMax,lScale, N, ...) displays several curves/histograms on one plot. Here title contains some text, xName is the name of a variable, xMin,xMax are the lower and upper limits. If $lScale \neq 0$, a logarithmic scale is used for the x axis.

N is the number of curves/histograms to display. After the parameter N, displayPlot expects $N \times 4$ parameters, where each tetrad can contain

text label	dimension of array	array of data	array of error
text label	dimension of array	array of data	NULL
text label	0	double *f(double x)	NULL
text label	0	double *f(double x, void *arg)	arg

where the first line is used for an histogram with error bars, the second line for a tabulated function, the third for a function f(x) and the fourth for a function f(x,arg) which also depends on some arguments contained in the structure arg. For a linear scale 1Scale=0, the arrays of data and errors should correspond to a grid

$$x_i = xMin + (i + 0.5)(xMax - xMin)/Dim$$
,

where i = 0, ..., Dim - 1. For logarithmic scale

$$x_i = \text{xMin} \cdot \left(\frac{\text{xMax}}{\text{xMin}}\right)^{\frac{i+0.5}{\text{Dim}}}$$

displayPlot uses the X11 font presented in the file CalcHEP_src/calchep.ini. One can change the font by editing the file or via key signals: $Ctrl\pm$ increases/decreases font size, while $Ctrl_{<}^{>}$ - changes the font saving its size.

17.6 Bessel functions

- bessIO(x), bessI1(x), bessKO(x), bessK1(x), bessK2(x) Bessel functions I_0, I_1, K_1, K_2 .
- Klpol(x)= $K_1(\frac{1}{x})e^{\frac{1}{x}}\sqrt{\frac{2}{\pi x}}$
- K2pol(x)= $K_2(\frac{1}{x})e^{\frac{1}{x}}\sqrt{\frac{2}{\pi x}}$

micrOMEGAs uses these functions for calculating the relic density. For small values of $x = T/M_{cdm}$, where these functions can be presented as polynomials in x. K1pol(0)=K2pol(0)=1.

17.7 Statistics

• FeldmanCousins(n0, b,cl)

is the Feldman-Cousins [130] function for a Poisson distribution. Here n0 is the observed number of events, b - the expected background, cl< 1 - the requested confidence level. This function sets the upper limit on the number of signal events compatible with n0 and cl.

• ch2pval(ndf,chi2)

returns the p-value assuming a χ^2 distribution with ndf degrees of freedom (expected χ^2) and chi2 is the observed χ^2 .

$$\mathtt{ch2pval}(k,q) = \int_q^\infty \frac{1}{2^k \Gamma(\frac{k}{2})} Q^{\frac{k}{2}-1} e^{-\frac{Q}{2}} dQ$$

A An updated routine for $b \rightarrow s\gamma$ in the MSSM

The calculation of $b \to s\gamma$ was described in micromegas 1.3 [3]. The branching fraction reads

$$B(\bar{B} \to X_s \gamma) = B(\bar{B} \to X_c e \bar{\nu}) \left| \frac{V_{ts}^* V_{tb}}{V_{cb}} \right|^2 \frac{6\alpha_{em}}{\pi f(z_0)} K_{NLO}(\delta)$$
 (64)

where $\alpha_{em} = 1./137.036$, the factor K_{NLO} involves the photon energy cut-off parameter δ and $f(z_0) = 0.542 - 2.23(\sqrt{z_0} - 0.29)$ depends on $z_0 = (m_c/m_b)^2$ defined in terms of pole masses. In the code the standard model and Higgs contribution at NLO were included as well as the leading order SUSY contributions. However in the last few years the NNLO standard model contribution has been computed [131] and shown to lead to large corrections, shifting the standard model value by over 10%. It was also argued that the NNLO SM result could be reproduced from the NLO calculation by appropriately choosing the scale for the c-quark mass [132, 133].

In this improved version of the bsgnlo routine, we have changed the default value for the parameter $z_1 = (m_c/m_b)^2$ where m_c is the \overline{MS} running charm mass $m_c(m_b)$. Taking $z_1 = 0.29$ allows to reproduce the NNLO result. It is therefore no longer necessary to apply a shift to the microMEGAs output of $b \to s\gamma$ to reproduce the SM value.

We have also updated the default values for the experimentally determined quantities in Eq. 64, see Table 6, and we have replaced the factor $f(z_0)$ by C_{sl} where

$$C_{sl} = \left| \frac{V_{ub}}{V_{cb}} \right|^2 \frac{\Gamma(\bar{B} \to X_c e \bar{\nu})}{\Gamma(\bar{B} \to X_u e \bar{\nu})}$$
(65)

accounts for the m_c dependence in $\bar{B} \to X_c e \bar{\nu}$.

$B(\bar{B} \to X_c e \bar{\nu})$	0.1064 [55]
C_{sl}	0.546 [133]
$ V_{ts}^*V_{tb}/V_{cb} ^2$	0.9613 [55]
A	0.808
λ	0.2253
$ar{ ho}$	0.132
$ ar{\eta} $	0.341
m_b/m_s	50
$\lambda_2 \approx \frac{1}{4} (m_{B^*}^2 - m_B^2)$	$0.12 \text{GeV}^2 [134]$
$\alpha_s(M_Z)$	0.1189

Table 6: Default values in micrOMEGAs

The CKM matrix elements in the Wolfenstein parametrisation given in Table 6 are used to compute the central value of ckmf at order λ^4 ,

$$ckmf = \left| \frac{V_{ts}^* V_{tb}}{V_{cb}} \right|^2 = 1 + \lambda^2 (2\bar{\rho} - 1) + \lambda^4 (\bar{\rho}^2 + \bar{\eta}^2 - A^2)$$
 (66)

With these default values the NLO- improved SM contribution is $B(\bar{B} \to X_s \gamma)|_{\text{SM}} = 3.27 \times 10^{-4}$ which corresponds to the result of Gambino and Giordano [133] after correcting for the slightly different CKM parameter used (ckmf = 0.963).

We have performed a comparison with superIso which includes the NNLO SM calculation for 10^5 randomly generated MSSM scenarios. The results are presented in Fig. 1 after applying a correction factor in superISO to account for the different value for the overall factor $F = B(\bar{B} \to X_c e \bar{\nu}) \left| \frac{V_{ts}^* V_{tb}}{V_{cb}} \right|^2 / C_{sl}$. The ratio of $F_{micro}/F_{ISO} = 0.942$. The two codes agree within 5% most of the time.

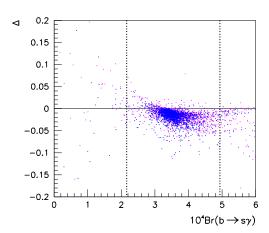


Figure 1: Relative difference for $B(\bar{B} \to s\gamma)$ between micromegas 2.4 and super Iso 3.1. the vertical lines show the 3σ experimentally measured value.

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