Making Siddon's method auto-differentiable







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Reformulate as an analytical function of the 3D pose

• From $\theta, \varphi, \gamma, b_x, b_y, b_z$, make X-ray source (s) and detector plane (P)

• Calculate intersections:
$$\mathbf{A} = \begin{pmatrix} b_x \\ b_y \\ b_z \end{pmatrix} + \begin{pmatrix} i \\ j \\ k \end{pmatrix} \otimes \begin{pmatrix} \Delta X \\ \Delta Y \\ \Delta Z \end{pmatrix} - \mathbf{s} \otimes (\mathbf{P} - \mathbf{s})$$

• Synthesize DRR:
$$I = \|\mathbf{P} - \mathbf{s}\|_2 \sum_{m=1}^{M-1} (\alpha_{m+1} - \alpha_m) \mathbf{V} \left[\mathbf{s} + \frac{\alpha_{m+1} + \alpha_m}{2} (\mathbf{P} - \mathbf{s}) \right]$$

Evaluation