

```

#include <bits/stdc++.h>
using namespace std;

void merge(int gArray[], int low, int mid1, int mid2, int high, int destArray[]){
    int i = low, j = mid1, k = mid2, l = low;
    //Choose smaller of the smallest in the three ranges
    while((i < mid1) && (j < mid2) && (k < high)){
        if(gArray[i] < gArray[j]){
            if(gArray[i] < gArray[k]){
                destArray[l++] = gArray[i++];
            }
            else{
                destArray[l++] = gArray[k++];
            }
        }
        else{
            if(gArray[j] < gArray[k]){
                destArray[l++] = gArray[j++];
            }
            else{
                destArray[l++] = gArray[k++];
            }
        }
    }
    while((i < mid1) && (j < mid2)){
        if(gArray[i] < gArray[j]){
            destArray[l++] = gArray[i++];
        }
        else{
            destArray[l++] = gArray[j++];
        }
    }
    while((j < mid2) && (k < high)){
        if(gArray[j] < gArray[k]){
            destArray[l++] = gArray[j++];
        }
        else{
            destArray[l++] = gArray[k++];
        }
    }
    while((i < mid1) && (k < high)){
        if(gArray[i] < gArray[k]){

```

```

        destArray[l++] = gArray[i++];
    }
    else{
        destArray[l++] = gArray[k++];
    }
}
while (i < mid1)
    destArray[l++] = gArray[i++];
while (j < mid2)
    destArray[l++] = gArray[j++];
while (k < high)
    destArray[l++] = gArray[k++];
}

```

```

void mergeSort3WayRec(int gArray[], int low, int high, int destArray[]){
    if (high - low < 2) return; //If array size is 1 then do nothing

    int mid1 = low + ((high - low) / 3);
    int mid2 = low + 2 * ((high - low) / 3) + 1;
    // Sorting 3 arrays recursively
    mergeSort3WayRec(destArray, low, mid1, gArray); //T(n/3)
    mergeSort3WayRec(destArray, mid1, mid2, gArray); //T(n/3)
    mergeSort3WayRec(destArray, mid2, high, gArray); //T(n/3)
    //Merge the sorted arrays
    merge(destArray, low, mid1, mid2, high, gArray); //n
}

```

```

void mergeSort3Way(int gArray[], int n){
    if (n == 0) return;

    int fArray[n];
    for (int i = 0; i < n; i++) //n
        fArray[i] = gArray[i];

    mergeSort3WayRec(fArray, 0, n, gArray);

    for (int i = 0; i < n; i++) //n
        gArray[i] = fArray[i];
}

```

```

int main(){
    int data[] = {45, -2, -45, 78, 30, -42, 10, 19, 73, 93};
}

```

```

mergeSort3Way(data,10);
cout << "Sorted: ";
for (int i = 0; i < 10; i++){ //n
    cout << data[i] << " ";
}

return 0;
}

```

**n is the size of the list**

## Space complexity

陣列 `data` 需要  $n$  個空間，陣列 `fArray` 需要  $n$  個空間，其他變數各 1 個空間，共  $c$  個空間。

$$O(n+n+c) = n$$

## Time complexity

Best case:

當 list 裡的資料只有一筆的時候，時間複雜度為  $O(1)$

Worst case

如果三個小陣列加起來有  $n$  個數字，總共就需要  $n$  個步驟。

每回合的 `merge` 需要花： $O(n)$ ，總共需要回合數： $O(\log_3^n)$ 。

`Divide` 的步驟數為  $n-1$ ，合併的步驟數為  $n * \log_3^n$ ，相加後可以得知總共的步驟數為  $n - 1 + n\log_3^n$ 。

$$O(n - 1 + n\log_3^n + C) = n\log_3^n$$