

# ANALYTICAL SOLUTION

$p_i$ : probability that a student in category  $i$  attends any given lecture

$N_i$ : true number of students in category  $i$

$O_i$ : observed number of students in category  $i$  who filled in the TEQ

Because students attend independently, the expected number of observed TEQ responses from category  $i$  is

$$E[O_i] = N_i p_i$$

Rearranging gives  $N_i = \frac{E[O_i]}{p_i}$

True distribution:  $N \approx \frac{O_i}{p_i}$  correction for attendance bias

Observed TEQ

Attendance	$p_i$	Observed $O_i$	$\bar{N}_i = O_i/p_i$
25%	0.25	7	28
50%	0.50	19	38
75%	0.75	42	56
100%	1.00	29	29

$$\sum \bar{N}_i = 151$$

$$150 \times \bar{N}_i$$

$$\sum \bar{N}_i$$

Total number in class is 150 so rescale

Attendance	Estimated True Number
25%	28
50%	38
75%	56
100%	28