

# Mid-Term Stochastic Modeling of Energy Markets and its Applications

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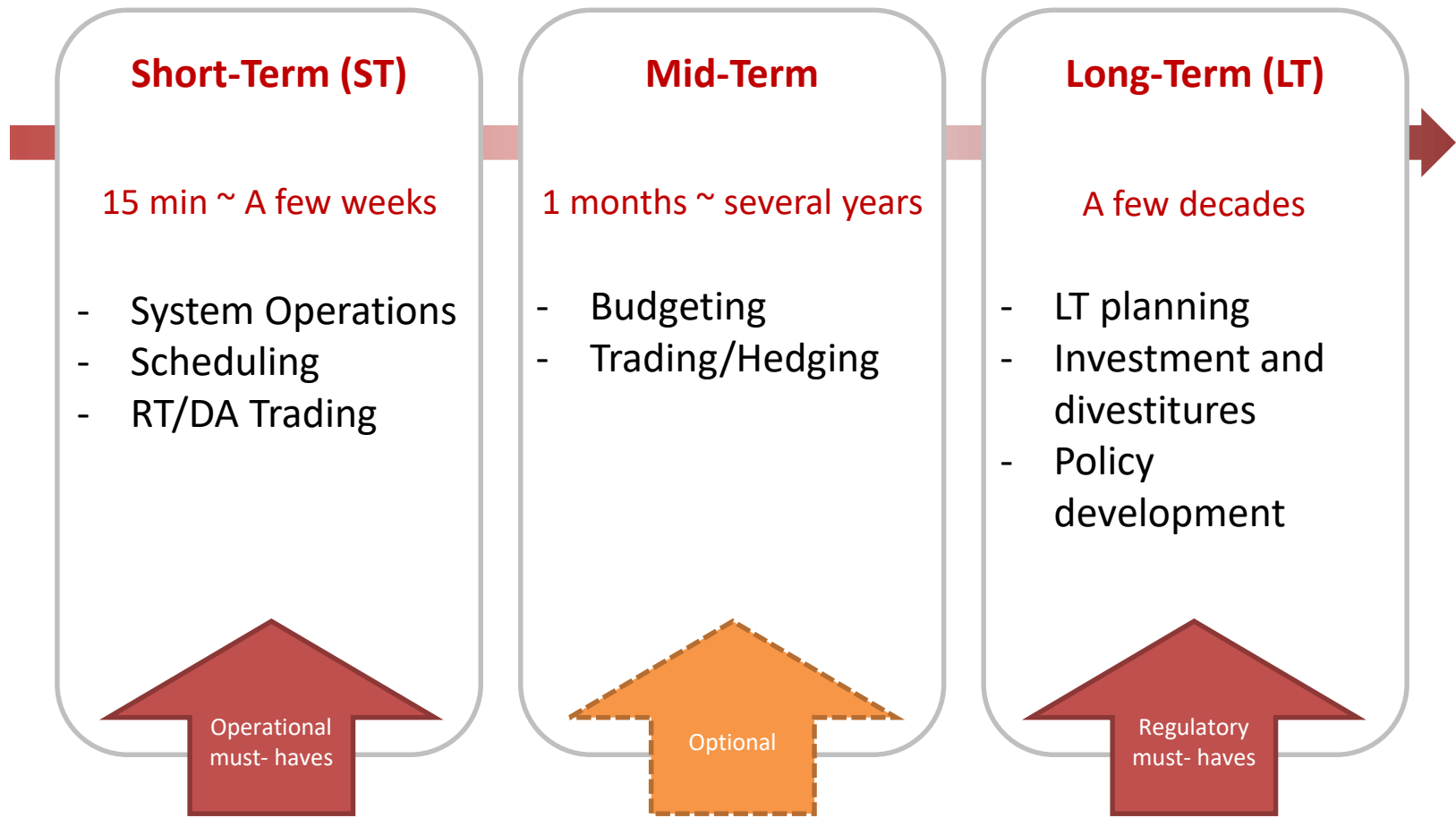


# Power Utility Industry




- **The Energy Authority** serves public utilities nationwide for trading and analytics.
- Mid-term (1 month – 5 years) portfolio management.
- Stochastic simulation models for energy and gas market.



# Types of Energy Market Models

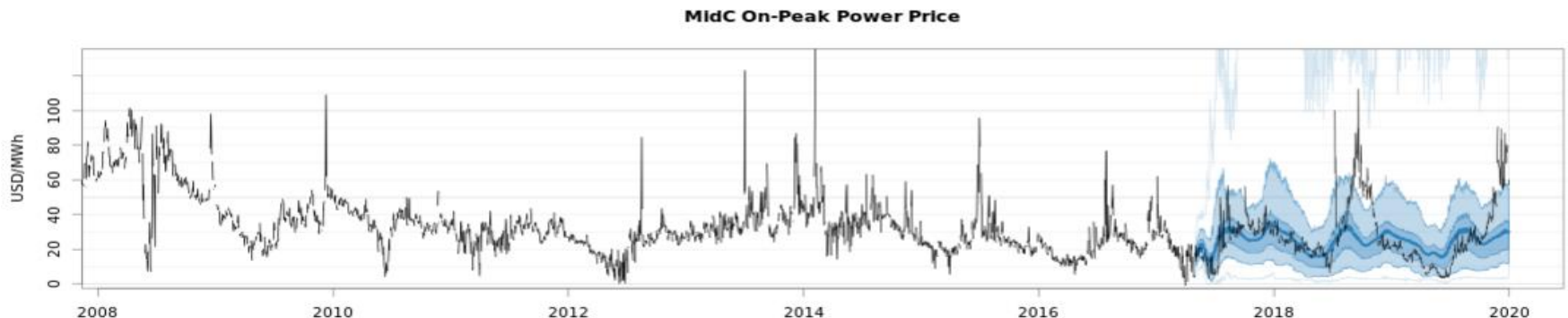


# Traditional Approach to Mid-Term Modeling

- Use commercially available **cost-production models**
  - Many utilities already have ST and TL models. Utilize those for mid-term modeling by simply adjusting the simulation time.
  - Some cost-production models
    - Focus only on particular resource dispatches. In these models, power prices are often generated by a simple random variable generator.
      -  Too simplistic and cannot capture the time series behaviors.
    - Are system optimization models that generate power prices as a result of system-wide grid simulation.
      -  Can be too sensitive to small changes and takes too long to run. For active trading purposes, it's too slow.
- Solution
  -  **Statistical simulation**
    - Right after wholesale energy market restructuring, cost-production model made sense. But we have gotten enough historical data for building robust statistical model now.

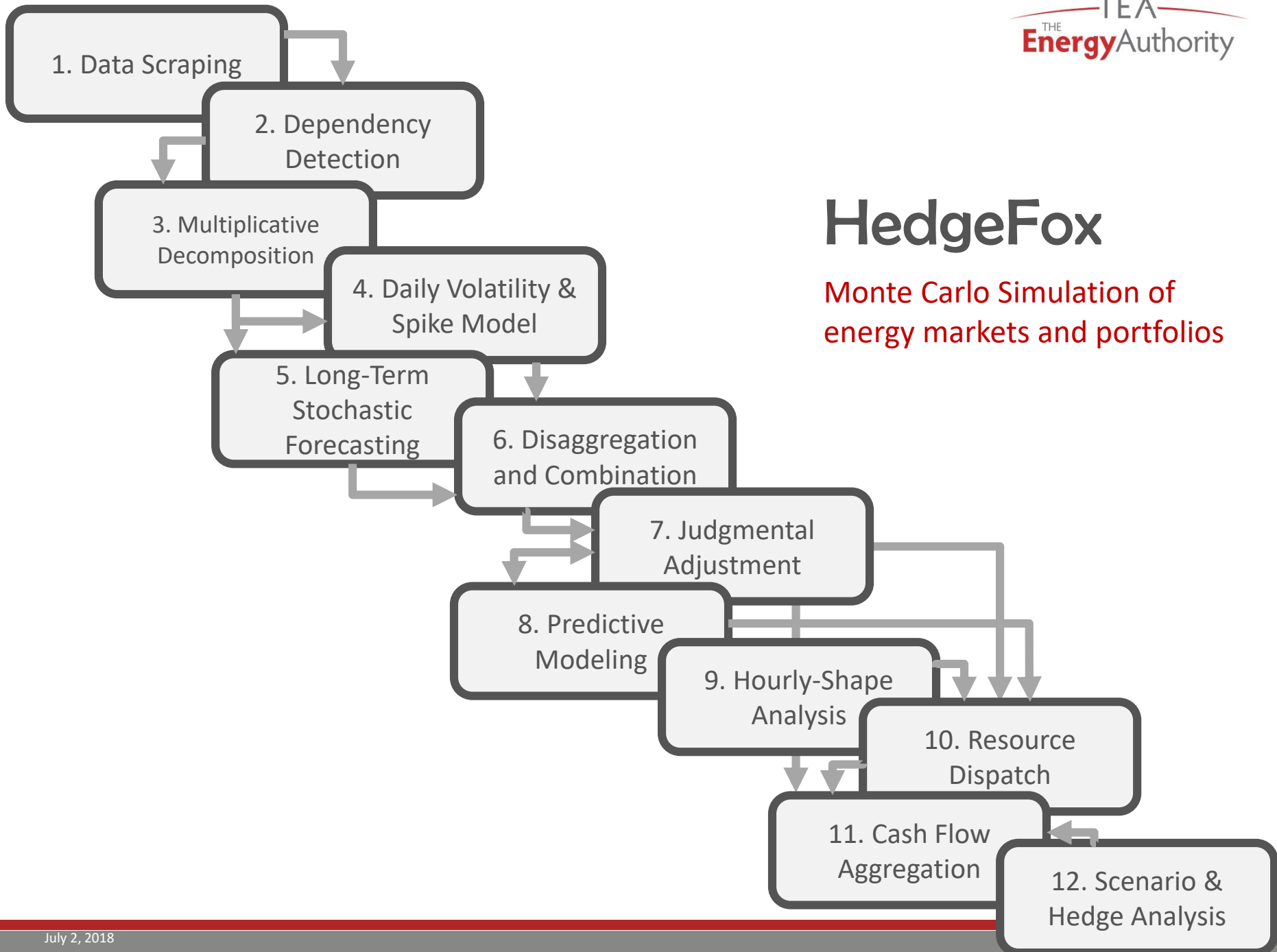
# Power Price TS Characteristics

- Autocorrelation
- Seasonal and weekly shapes
- Volatility & Heteroscedasticity
  - Seasonal and weekly variability
- Multivariate cross-correlation and non-linear dependency
  - NG, load, regional hydro and other variable generation
- Non-normal distributions
  - fat tails
  - Extreme peaks and drops
- Negative prices
- Consistency with market expectations
- Consistency among different time granularities.



# HedgeFox

Monte Carlo Simulation of  
energy markets and portfolios



## Daily Stochastic Data

are decomposed and simulated.

- Loads
- Hydro & variable generations
- Natural gas prices

# HedgeFox

## Monthly LT Forecasts

are simulated or imported and daily data are adjusted accordingly.

- Forward prices
- External load and hydro forecast

## Daily Power Price Simulation

are derived from simulated daily data

- Major Power Hub
- Other LMPs as price differentials

## Hourly Resource Simulation

Hourly adder shape classification

Monthly aggregation into portfolio cash flow

1. Data Scraping

2. Dependency Detection

3. Multiplicative Decomposition

4. Daily Volatility & Spike Model

5. Long-Term Stochastic Forecasting

6. Disaggregation and Combination

7. Judgmental Adjustment

8. Predictive Modeling

9. Hourly-Shape Analysis

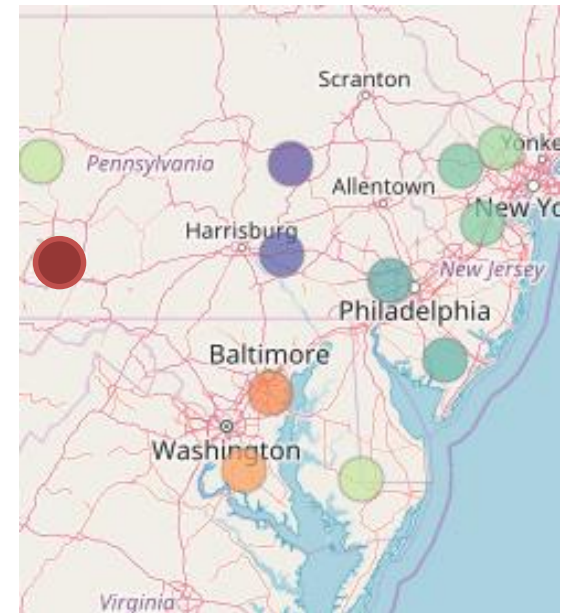
10. Resource Dispatch

11. Cash Flow Aggregation

12. Scenario & Hedge Analysis

# Power Price Simulation

- Simulate multiple prices as price differentials to one major hub price.
- Feature space
  - Autoregressive terms
  - Month and Day-of-Week
  - Already simulated fundamentals such as solar, wind & hydro generation, gas prices and multiple loads
  - Power price series at a major hub
  - All other LMP price differential simulated prior to the particular LMP
- Feature space may not include all price drivers.





# Common Approach for Stochastic Modeling

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- $Price = f(...) + Error(...)$

Where  $f$  is some sort of regression model

- Requirements for the residuals



Normal distribution



$f$ 's features need to include enough information

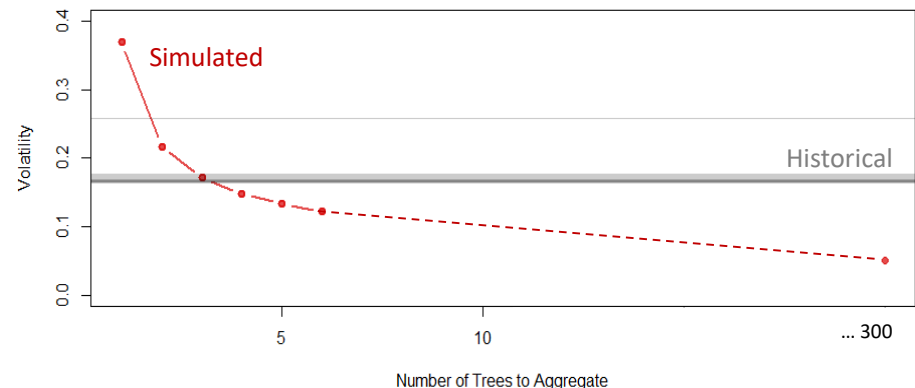


Need careful examinations of error terms for each variables.

- If requirements are met, the correct level of volatility should be captured automatically, but otherwise, volatility may not match.
- We need something robust for the error terms.

# Bunched Random Forest

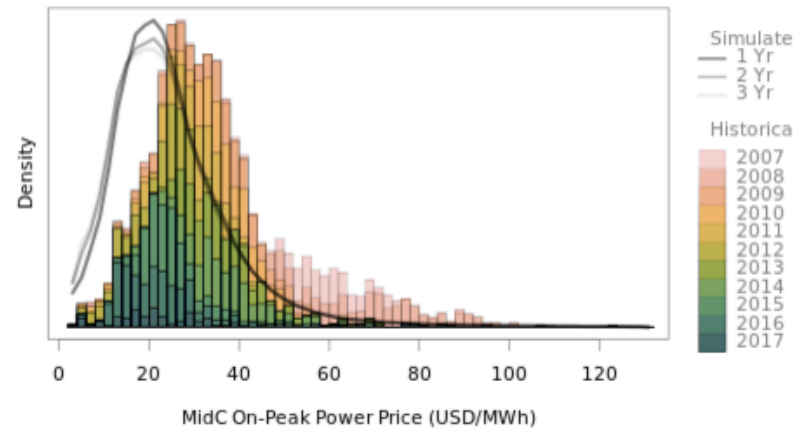
- Random Forest
  - Aggregation of a few hundred trees moderate values too much → **Low volatility**
  - a single tree encompasses too little predictability → **High volatility**
- Bunched RF in MC
  - Aggregating a selected number of trees for each Monte Carlo iteration
  - Achieve plausible volatility in each MC series, while maintaining the same predictability as RF in the whole MC simulation.
- Implementation
  - `randomForest::predict.randomForest()` includes individual tree outputs.
  - After figuring out the bunching number based on historical volatility, sample and aggregate suitable number of individual tree outputs.



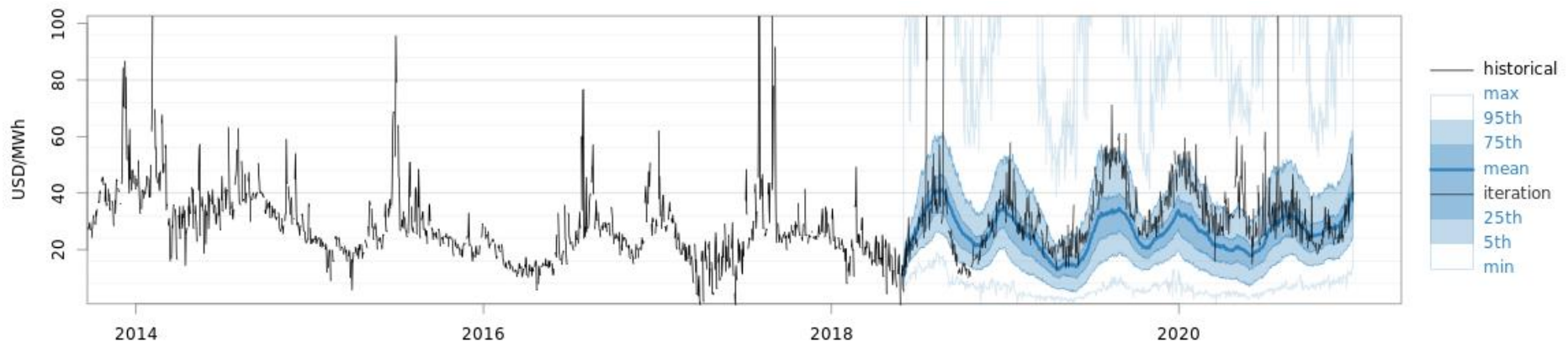
# Results

- ✓ Price distribution (overall and at monthly level).

Price Distribution

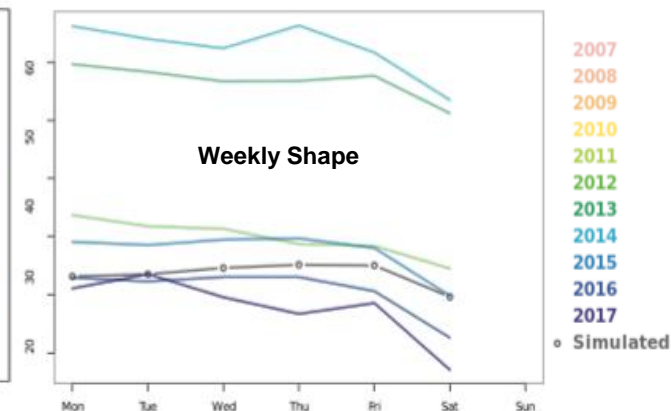
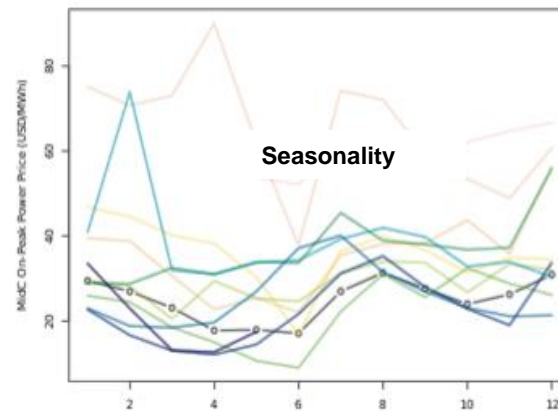
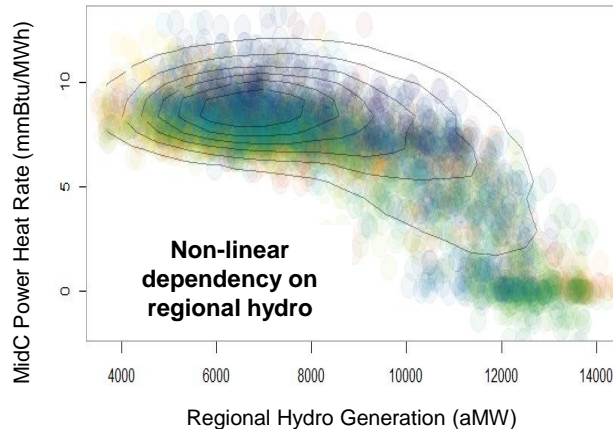
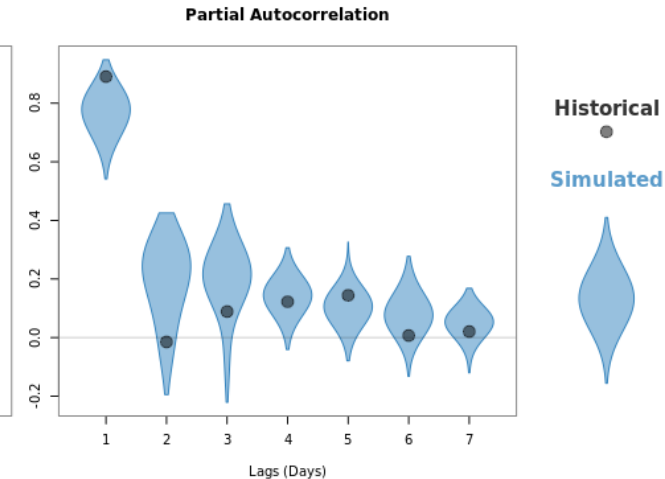
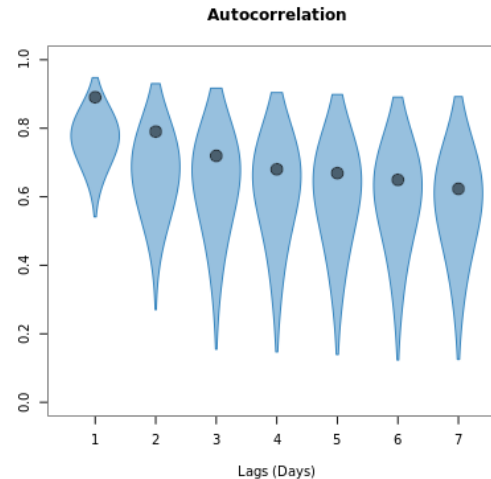


Mid-C Power Price (Historical + Simulated)



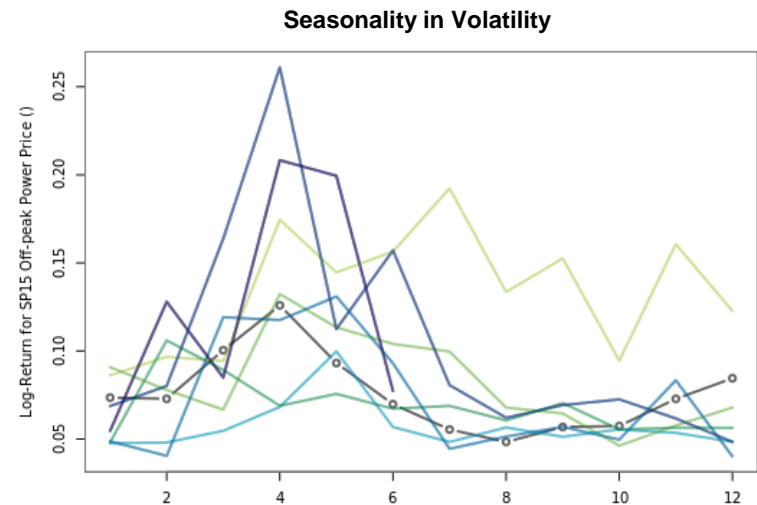
# Results

- ✓ Autocorrelation
- ✓ Seasonal Shapes
- ✓ Weekly shapes
- ✓ Non-linear dependencies

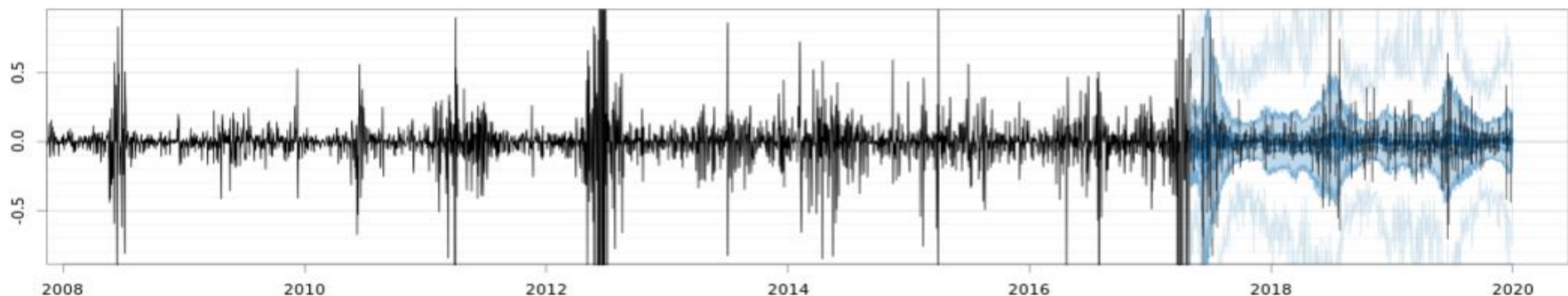


# Results

- ✓ Volatility
- ✓ Heteroscedasticity
- ✓ Seasonality

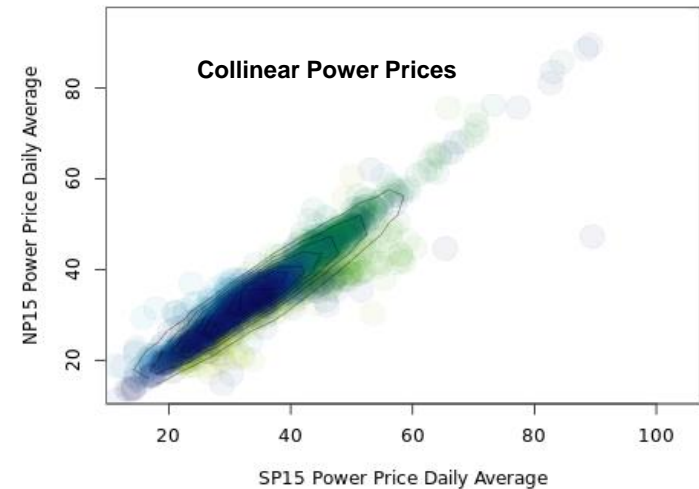


**Power Price Log-Returns (Historical + Simulated)**

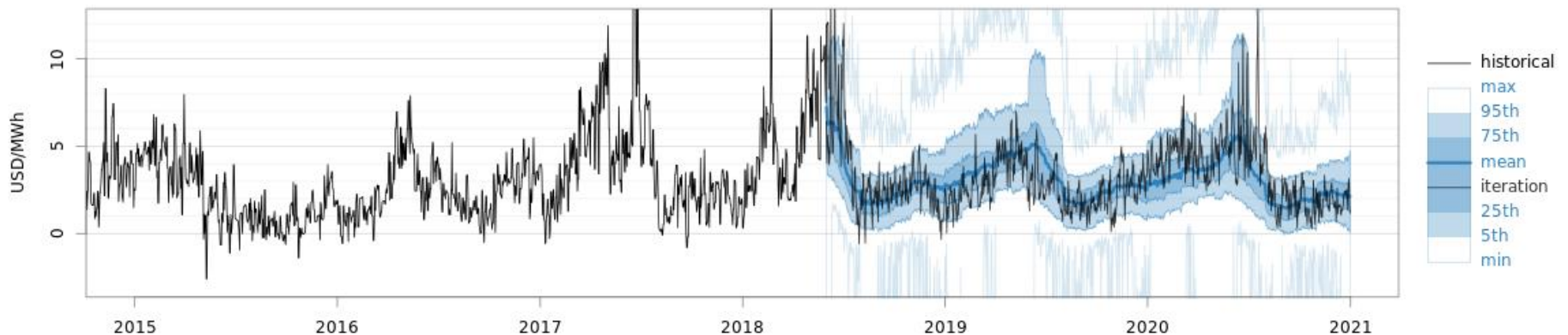


# Results

✓ Multivariate cross-correlations



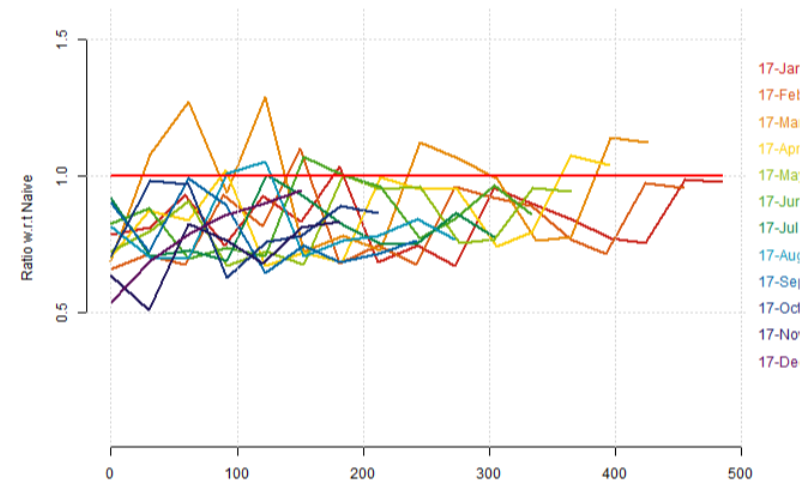
Price Differential between LMPs



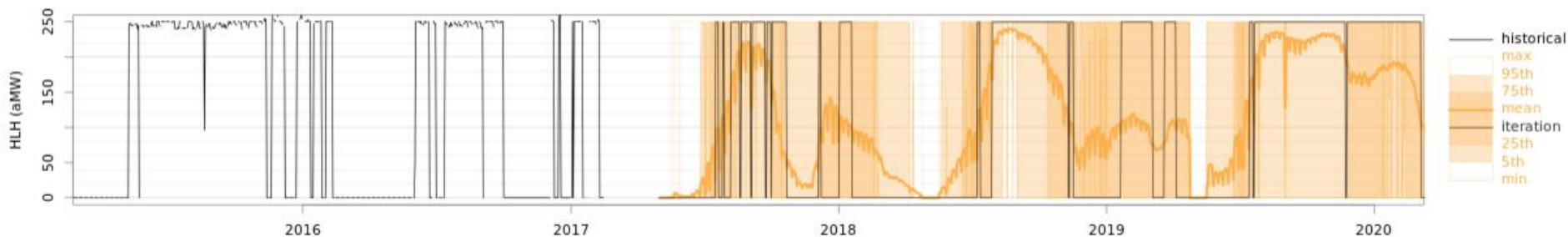
# Scoring Methods

In order to make sure that all needed behaviors are captured multiple scoring methods are used.

1. Volatility
  - ✓ Check is simulated volatility matches with historical.
2. CRPS against naïve model
  - ✓ Calculate ratio between CRPS of simulated and naïve models
3. Pinball Loss Score on Resource dispatch simulation outputs
  - ✓ Resource dispatch model transforms power price behavior to cash flow. This combines and checks many of the power price characteristics.



Natural Gas Resource Dispatch (Historical + Simulated)



# Summary of BRF

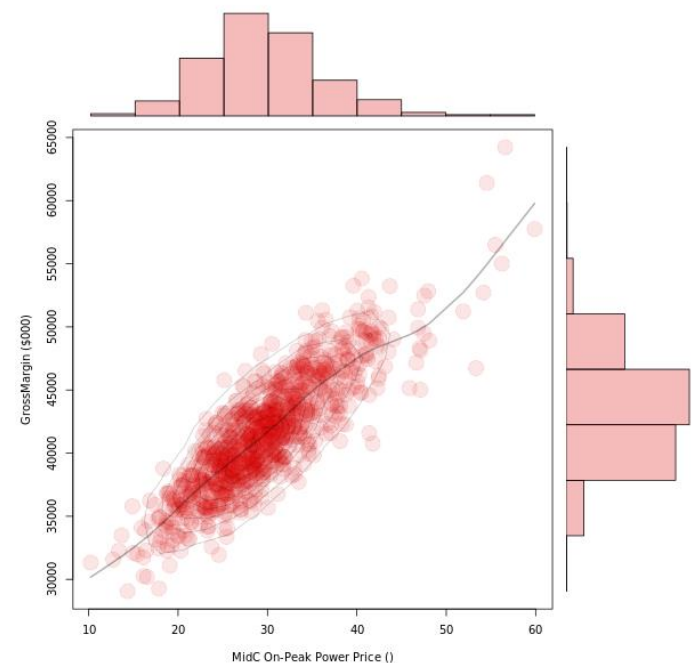
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- Benefits
  - No concern about residual behaviors.
  - Robust in feature space (many collinear variables or too little drivers)
  - Volatility is automatically adjusted in the process.
  - Heteroscedasticity is captured.
  - Variable importance can be insightful in learning the drivers of particular price nodes.
- Limitations
  - Difficult to tune bunching numbers, particularly when a large number of prices are derived sequentially.



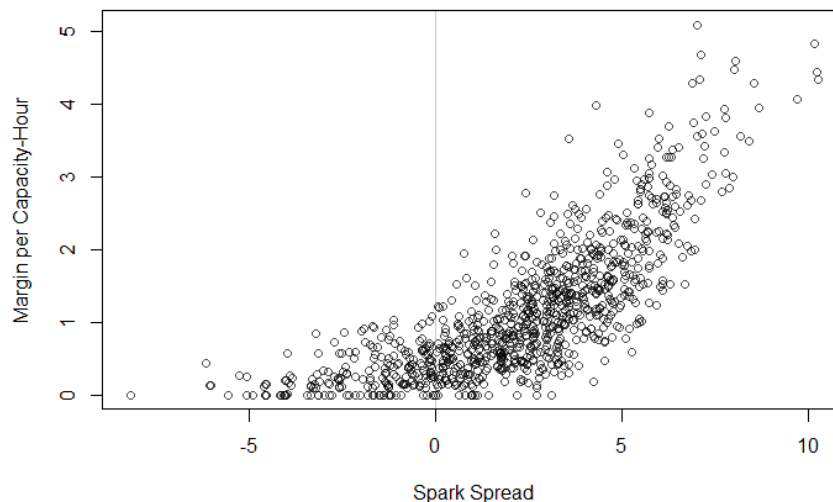
# Delta Hedging

- **Delta** is the change in portfolio value with respect to market prices.
- **Delta neutral** is a portfolio strategy where portfolio value remains unchanged when small changes occur in the market.
- Some of the risk averting utilities like to manage portfolios actively, and requires a swift market & portfolio model.




# Delta Hedging of a Thermal Unit

- Natural gas resources can be treated as a 'real option' with respect to spark spread.
  - $\text{Spark Spread} = \text{Power Price} - (\text{HeatRate} \times \text{Gas Price} + \text{VOM})$
- Through dynamic delta-hedging, realization of extrinsic value is possible.
  - Have a market and resource model be always up-to-date.
  - Watch spark spread and corresponding delta on daily basis.
  - When market moves, trade heat rate. Unwinding positions should lock in positive cash flow.

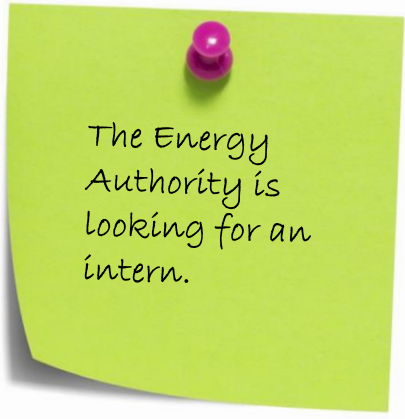


Thank you!

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