

Software Lab Computational Engineering Science

Group 12, Pusher Mechanism

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Informatik 12: Software and Tools for Computational Engineering (STCE) RWTH Aachen University

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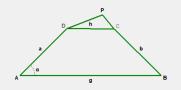
Summary and Conclusion

Preface

Four-bar linkage model









Analysis

User Requirements





- Implement 27 motion types of the four-bar linkage with one bar fixed:
 - Classification values:

►
$$T_1 = g + h - b - a$$

►
$$T_2 = b + g - h - a$$

$$T_3 = h + b - g - a$$

- Implement GUI with motion animation and the ability to choose geometrical parameters:
 - Length of the bars
 - Position of the coupler
 - Input angle
 - Angle relative to the horizon
 - Classification values as alternative input

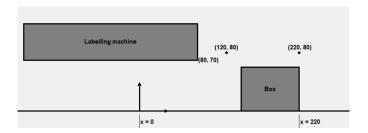
	m	m	m	mm	m m		
No.	$T_{_I}$	T_2	T_3	$T_{_{I}}T_{_{2}}$	$T_{_{I}}T_{_{3}}$	а	ь
1	+	+	+	+	+	crank	rocker
2	0	+	+	0	0	crank	π-rocker
3	-	+	+	-	-	$\pi\text{-rocker}$	πrocker
4	+	0	+	0	+	crank	0-rocker
5	0	0	+	0	0	crank	crank
6	-	0	+	0	-	crank	crank
7	+	-	+	-	+	π-rocker	0-rocker
8	0	-	+	0	0	crank	crank
9	-	-	+	+	-	crank	crank
10	+	+	0	+	0	crank	π-rocker
11	0	+	0	0	0	crank	π-rocker
12	-	+	0	-	0	π-rocker	π-rocker
13	+	0	0	0	0	crank	crank
14	0	0	0	0	0	crank	crank
15	-	0	0	0	0	crank	crank
16	+	-	0	-	0	π-rocker	crank
17	0	-	0	0	0	crank	crank
18	-	-	0	+	0	crank	crank
19	+	+	-	+	-	0-rocker	π-rocker
20	0	+	-	0	0	0-rocker	π-rocker
21	-	+	-	-	+	rocker	rocker
22	+	0	-	0	-	0-rocker	crank
23	0	0	-	0	0	0-rocker	crank
24	-	0	-	0	+	0-rocker	0-rocker
25	+	-	-	-	-	rocker	crank
26	0	-	-	0	0	0-rocker	crank
27	-	-	-	+	+	0-rocker	0-rocker
-201	8-26	1-26	6 by	Ivana	Cvet	kovic et	al.

Figure from "Classification, geometrical and kinematic analysis of four-bar linkages" 10.15308/Sinteza-2018-261-266

User Requirements







- ► Solve an optimization problem:
 - Push box with size 80×60 from x = 220 to x = 0
 - ▶ Do not cross the area of the labelling machine (Area with x < 80 and y > 70).
 - ▶ Pass above points (120, 80) and (220, 80)

System Requirements: Functional





► Four-bar linkage model:

- System simulates all the motion types of the four-bar linkage.
- System does not crash with any input of geometrical configuration.

Tests:

- Implement test cases for geometry.
- Implement test cases with bad input to test system stability.

Graphical User Interface:

- ► GUI provides the four-bar linkage visualization and motion animation.
- User can input geometrical data by moving a point on a slide bar.
- GUI is coupled with the four-bar linkage model to use implemented motion cases for animation.
- GUI provides tracing for trajectories of the points.
- GUI classifies of the linkage.

▶ Optimization problem:

- It should be possible to find a solution (manually) for the optimization problem using the four-bar linkage model.
- GUI visualizes the solution.

System Requirements: Non-Functional





Performance:

- The four-bar linkage model is fast enough to provide smooth GUI animations.
- ► GUI animations are not slower than 30 frames per second.

Usability:

- Every essential part of the four-bar linkage model is well documented.
- ▶ GUI is easy to operate and all functionalities are self-explanatory.
- GUI source code is well documented.

Theory Base: Grashof's Theorem





- s = length of shortest bar
- *l* = length of longest bar
- p, q = lengths of intermediate bar

Grashof's theorem states that a four-bar mechanism has at least one revolving link if

$$s + 1 \le p + q$$

(5-1)

and all three mobile links will rock if

$$s + 1 > p + q$$

(5-2)

The inequality 5-1 is Grashof's criterion.

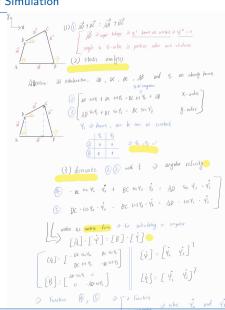
https://www.cs.cmu.edu/~rapidproto/mechanisms/chpt5.html

Software and Tools for Computational Engineering



Theory Base: Geometric or Dynamic Simulation

- ► The right figure is our kinematic analysis of the four-bar linkage.
- Ultimately, we chose the geometric simulation as it is more convenient to implement.



Development Infrastructure





▶ 1. Operating System:

Xubuntu/Windows

2. Developing Environment:

- Programming Language: Python.
- ► IDE: Spyder/Pycharm.
- Package Manager: Anaconda.

3. Libraries:

- Frontend: tkinter, math, numpy
- Backend: math, numpy

▶ 4. Version Control System:

GitHub: Remote code repositories for team collaboration, code reviews, and version control.

https://github.com/einsflash/Project_Pusher_Mechanism

► 5. Frameworks:

Pdoc: Used for generating project documentation, helping the team understand and maintain the code better.

Design

Class Model(s)













Introduction





a. Elements in Class

▶ 1. Input Parameters:

- AB, BC, CD, DA
- alpha, theta, alpha_rad, theta_rad
- coupler_position, coupler_offset
- t, alpha_velocity, C_mode

2. Animation-Related Attributes:

- switch_C2_C1_180, switch_C2_C1_360
- C2_C1_switched_last_time, direction

3. Geometry Validity & Type Check:

- Linkage_Type, geometric_Validity
- Input_Link_Type, Output_Link_Type

▶ 4. Angle Limits:

- alpha_lims, alpha_rad_lims, alpha_limited
- ▶ 5. Position of Points:
 - ► A, B, C, C1, C2, D, P

6. Classification Values:

► T1, T2, T3, L

Backend

Introduction





b. Two Modes for User Parameters

- calculate_Classification_Value(self)
- calculate_Edge_Value(self)

c. Display Linkage Motion Type

- find_Linkage_Type(self)
 - Use a Python dictionary to store the type data.

d. Check Parameter

- check_Parameter(self)
 - Check linkage type.
 - ▶ geometric_Validity

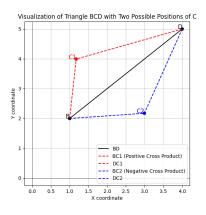
e. Update Parameters Every Run

- run(self)
 - self.calculate_Classification_Value()
 - self.check_Parameter()
 - If geometric_Validity is False, exit.
 - self.find_Linkage_Type()
 - self.calculate_alpha_lims()
 - self.calculate_Point_Position()





- A and B are fixed points.
- D can be determined using angle alpha and length AD.
- ▶ Given positions of B and D, and all side lengths of triangle BCD, point C has two possible locations C₁ and C₂.
- ightharpoonup Calculating point C_1 and C_2 .
- Choose C as C₂ per default and switch to C₁ if needed.



Picture from "test for calculating point C.py"





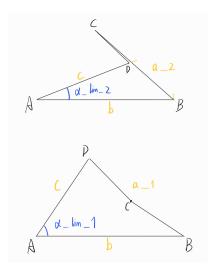
Cosine Law Formula:

$$\cos(\alpha_{\text{lims1}}) = \frac{b^2 + c^2 - a_1^2}{2bc}$$

$$\cos(\alpha_{\text{lims2}}) = \frac{b^2 + c^2 - a_2^2}{2bc}$$

$$\cos(\alpha_{\text{lims2}}) = \frac{b^2 + c^2 - c^2}{2bc}$$

- Determine whether to switch between C_1 and C_2 to ensure animation continuity:
 - Switch when α reaches its limits.
 - ightharpoonup Switch in special cases, when α limits are exactly 0°, 360° and/or 180°.



Backend

Animation





Basic Concept:

- Change alpha according to the defined limits.
- Reverse direction at boundaries.
- ▶ Switch between configurations (C_1 and C_2) to ensure continuity.

▶ Direction Control:

- direction = 0: Increasing alpha
- direction = 1: Decreasing alpha

Updating alpha:

- Update by alpha_velocity * t.
- Reverse direction when reaching limit values.

▶ Switching Between C_1 and C_2 :

- Switch at α limits.
- ▶ Switch at 0°, 360° and/or 180° if it corresponds to α limits.
- Handle floating-point precision issues (10⁻¹²).

Configuration Tracking:

Avoid redundant switching between C_1 and C_2 .





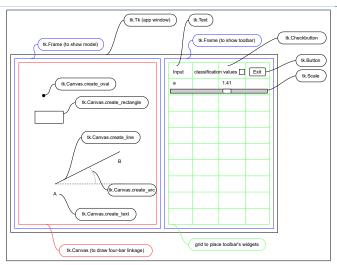
- ▶ Tests classify motion of four-bar linkage based on values T_1 , T_2 , and T_3
- Verifies correct behavior for Crank, Rocker, and intermediate states
- Covers all possible combinations of positive, negative, and zero values
- Ensures accurate classification of input and output links
- ▶ Test cases include Crank-Rocker, Double Crank, Double Rocker, and Rocker-Crank scenarios
- Each test checks specific link motion configurations
- Automated with unittest framework for reproducibility and consistency

Frontend

GUI, Tkinter Intro







► Initiate all tkinter objects inside GUI class and generate app window: GUI().tk.mainloop()

GUI, Show and hide objects





- ► To display different modes, some objects have to be hidden or shown.
- For objects in tk.Canvas use itemconfigure:
 - ▶ Hide:
 - self.model_animation.itemconfigure(self.model_animation.AB_line, state='hidden')

 Show:
 - self.model_animation.itemconfigure(self.model_animation.AB_line, state='normal')
- ► For widgets like tk.Scale or tk.Text:
 - Hide: self.slider_T1.grid_remove()
 - Show: self.slider_T1.grid()

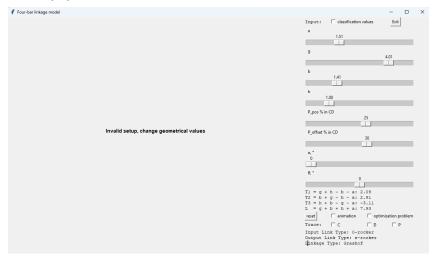
Frontend

GUI, Invalid Setup Handling





- ▶ In Backend check if parameters are valid: $V = I s p q \le 0$
- ► If *V* > 0:



Results

27 movement types















 $T_{1,2,3} = 1.0, 1.0, 1.0$



 $T_{1,2,3} = 0.0, 1.0, 1.0$ $T_{1,2,3} = -1.0, 1.0, 1.0$



 $T_{1,2,3} = 0.0, 0.0, 1.0$







 $T_{1,2,3} = 1.0, 1.0, 0.0$









 $T_{1,2,3} = 0.0, 1.0, 0.0$ $T_{1,2,3} = -1.0, 1.0, 0.0$ $T_{1,2,3} = 1.0, 0.0, 0.0$

 $T_{1,2,3} = 0.0, 0.0, 0.0$

 $T_{1,2,3} = -1.0, 0.0, 0.0$

Results

27 movement types

















 $T_{1,2,3} = -1.0, -1.0, 0.0$



 $T_{1,2,3} = 0.0, 1.0, -1.0$



 $T_{1,2,3} = -1.0, 1.0, -1.0$ $T_{1,2,3} = 1.0, 0.0, -1.0$



 $T_{1,2,3} = 0.0, 0.0, -1.0$





 $T_{1,2,3} = -1.0, -1.0, -1.0$

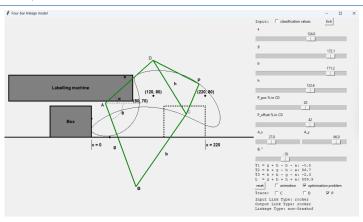
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Results

Optimization problem







- ▶ 9 degrees of freedom (all lengths in cm):
 - ▶ Length of four bars: a = 124.0, b = 171.2, g = 172.1, h = 122.6.
 - ► Coupler position: $P_{pos} = 20.0\%$, $P_{offset} = 42.0\%$ of h.
 - Position of point A: $A_x = 27.0$, $A_y = 66.0$.
 - ▶ Angle of ground bar relative to horizon: $\theta = -70.0^{\circ}$

Live Software Demo





- 1. Changing the input of slidebar.
- 2. Start the animation.
- 3. Test different motion types.
- 4. Enable points tracing.
- 5. Solve the optimization problem.

Documentation





Comprehensive Documentation of the FourBarLinkage Class in Python

October 15, 2024

Introduction

The FourBarLinkage class in Python models a four-bar linkage mechanism, commonly used in mechanical systems. A four-bar linkage consists of four rigid bars connected by rotary joints, and depending on the bar lengths and angles, it can exhibit different motion types like crank-rocker, double-rocker, or doublecrank. This class allows for the simulation of the mechanism and provides users the ability to input parameters such as link lengths, initial angles, and angular velocities,

User Inputs

Users can directly input the following parameters:

- . AB, BC, CD, DA: Lengths of the four bars in the linkage.
- · alpha, theta: Angles of the input and fixed links (in degrees).
- · alpha_velocity: Angular velocity of the input link (in degrees per second)

4 GUI Implementation

The FourBarLinkage class is integrated with a graphical user interface (GUI), allowing users to interact with the linkage system dynamically. Through the GUL users can adjust parameters like link lengths and angles in real-time and observe the system's behavior.

4.1 init_linkage_display() - Initialize Linkage Display

- · Location: In the GUI class
- . Description: Sets up the visual elements needed to display the linkage on the canyas, such as drawing the bars and marking the points A. B. C. D. and P.

4.2 refresh() - Refresh GUI

- · Location: In the GUI class
- Description: Undates the visual representation of the linkage every time a user changes the parameters, ensuring the display remains synchronized with the system's current state.

4.3 run_animation() - Run Animation

- · Location: In the GUI class
- Description: Runs the continuous animation of the four-bar linkage mechanism on the canvas. The points and bars update in real-time as the system moves, based on the input parameters.

Unit Test Documentation for Four-Bar Linkage

October 13, 2024

Overview of the Test Collection

The unit tests for the Four-Bar Linkage system are designed to verify the correct classification of linkage motion types. Each test checks whether the linkage is correctly identified as a specific combination of crank, rocker, and intermediate states based on the values of T_1 , T_2 , and T_3 . These tests ensure that for various configurations of the four-bar linkage, the input and output links are classified accurately The classifications are important for understanding the behavior of the system and ensuring correct functionality in different scenarios.

The test cases systematically cover all possible combinations of positive, negative, and zero values for the parameters T₁, T₂, and T₃, ensuring that every possible motion configuration is tested. The expected outcomes are predefined according to the known behavior of four-bar linkages.

Explanation of Test Collection

Each collection of test cases verifies a specific motion classification of the four-bar linkage system. The classifications generally fall into the categories of Crank, Rocker, and intermediate states like π -rocker or flyrocker

Crank-Rocker Classifications

The tests in this group verify the combinations where one of the links acts as a crank while the other

Project Management





Task

1.Discuss and Design:

- weekly discussion in discord.
- gathering information / generating ideas for program.

2.Frontend:

- Design of GUI
- Implementation
- Debug

► 3.Backend:

- Algorithm for calculating positions and angle extremum
- Interface for animation
- Two types of input
- Display information(Grashof condition, geometric validity)

4.Test the motion case:

5.Presentation:

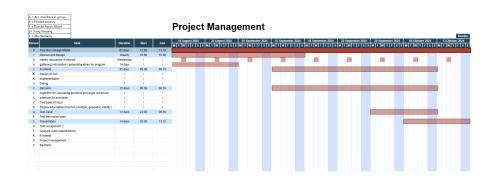
- Analysis (user requirements)
- Frontend
- Project management
- Backend
- ▶ *The following page outlines the responsibilities of each person.

Project Management

Gantt Chart







Project Management

Task Assignment





A = A	LL members in group
K = K	holod Arseniy
F = F	oerke Aaron Albert
S= Sc	ong Xinyang
Z = Z	hu Yanliang

Project Management

2110	Tarmang												_						
erson	Task	Duration	Start	End		8 Aug			6 1			ust 20					ber 2		
0	Four Bar Linkage Model	62 days	12.08	13.10	M T	W	. 1	ъI	2 1		w	171	اءاء	, IW	ш	W I	1.	2 2	T W
	Discuss and Design	Weekly	12.08	15.10		_	_	_	-	_	_	_	_	_	_	-		_	
	weekly discussion in discord	Wednesday	/	/				_	_				_					_	Н
	gathering information / generating ideas for program	14 days	1	1															
	Frontend	35 days	09.09	06.10			_	_	_				_	•					
	Design of GUI	/	/	1															٦
K	Implementation	1	1	1															
Α	Debug	1	1	1															
3	Backend	35 days	09.09	06.10															Г
Z	Algorithm for calculating positions and angle extremum	/	1	1															Г
K	Interface for animation	1	1	1															
Z	Two types of input	1	1	1															
S	Display information(Grashof condition, geometric validity)	1	1	1															
4	Test Case	14 days	23.09	06.10															
F	Test the motion case																		
5	Presentation	14 days	30.09	13.10															
Α	Task assignment ()																		
F	Analysis (user requirements)																		
K	Frontend																		
S	Project management																		
Z	Backend																		

Summary and Conclusion





- Analysis:
 - User requirements
 - System requirement
 - Theory base
- Design:
 - ▶ Development infrastructure: Python and Tkinter
 - Class models
- ► Implementation:
 - ► Backend: four bar linkage geometry
 - Frontend: GUI
 - Unittest
- Results:
 - 27 movement cases
 - Optimization problem solution
- Documentation
- Project management: Gantt Chart.

Literature





Cvetkovic, Ivana and Stojicevic, Misa and Popkonstantinović, Branislav and Cvetković, Dragan. (2018). Classification, geometrical and kinematic analysis of four-bar linkages. 261-266. 10.15308/Sinteza-2018-261-266.