

```

1 clear all
2 clc
3
4 % Parameters
5 syms m1 m2 L g real
6 % Force
7 u = sym('u',[3,1]);
8
9 % Position point mass 1
10 pm1 = sym('p1',[3,1]);
11 dp1 = sym('dp1',[3,1]);
12 ddp1 = sym('d2p1',[3,1]);
13 % Angles for point mass 2
14 a = sym('a',[2,1]);
15 da = sym('da',[2,1]);
16 dda = sym('d2a',[2,1]);
17 % Generalized coordinates
18 q = [pm1;a];
19 dq = [dp1;da];
20 ddq = [ddp1;dda];
21
22 % Position of point mass 2
23 pm2 = pm1 + [L*sin(a(1))*cos(a(2)); L*sin(a(1))*sin(a(2)); L*cos(a(1))];
24 % Velocity of point mass 2
25 dpm2 = jacobian(pm2,q)*dq;
26 % Generalized forces
27 Q = [u; 0; 0];
28 % Kinetic energy
29 T = 1/2 * m1 * (dpm1.') * dpm1 + 1/2 * m2 * (dpm2.') * dpm2;
30 T = simplify(T);
31 % Potential energy
32 V = m1 * g * pm1(3) + m2 * g * pm2(3);
33 V = simplify(V);
34 % Lagrangian
35 Lag = T - V;
36
37 % Derivatives of the Lagrangian
38 Lag_q = simplify(jacobian(Lag,q)).';
39 Lag_qdq = simplify(jacobian(Lag_q.',dq));
40 Lag_dq = simplify(jacobian(Lag,dq)).';
41 Lag_dqdq = simplify(jacobian(Lag_dq.',dq)); % W
42
43 % Matrices for problem 1
44 M = Lag_dqdq;
45 b = Q + simplify(Lag_q - Lag_qdq*dq);
46

```