

```

1 clear all
2 clc
3
4 % Parameters
5 syms m1 m2 L g real
6 % Force
7 u = sym('u',[3,1]);
8
9 % Positions of point masses
10 pm1 = sym('pm1',[3,1]);
11 pm2 = sym('pm2',[3,1]);
12 dpm1 = sym('dpm1',[3,1]);
13 dpm2 = sym('dpm2',[3,1]);
14 ddpm1 = sym('d2pm1',[3,1]);
15 ddpm2 = sym('d2pm2',[3,1]);
16 % Generalized coordinates
17 q = [pm1;pm2];
18 dq = [dpm1;dpm2];
19 ddq = [ddpm1;ddpm2];
20 % Algebraic variable
21 z = sym('z');
22
23 % Generalized forces
24 Q = [u; zeros(3,1)];
25 % Kinetic energy (function of q and dq)
26 T = 1/2 * m1 * (dpm1.') * dpm1 + 1/2 * m2 * (dpm2.') * dpm2;
27 % Potential energy
28 V = m1 * g * pm1(3) + m2 * g * pm2(3);
29 % Lagrangian (function of q and dq)
30 Lag = T - V;
31 % Constraint
32 dpm = pm1 - pm2; % difference of positions
33 C = 1/2 * ((dpm.') * dpm - L^2);
34
35 % Derivatives of constrained Lagrangian
36 Lag_q = simplify(jacobian(Lag,q)).';
37 Lag_qdq = simplify(jacobian(Lag_q.',dq));
38 Lag_dq = simplify(jacobian(Lag,dq)).';
39 Lag_dqdq = simplify(jacobian(Lag_dq.',dq)); % W
40 C_q = simplify(jacobian(C,q)).';
41
42 % Matrices for problem 1b
43 M = Lag_dqdq;
44 b = Q + simplify(Lag_q - Lag_qdq*dq - z*C_q);
45
46 % Matrices for problem 2
47 Himplicit = [M, C_q; C_q.', 0];
48 c = [Q + simplify(Lag_q - Lag_qdq*dq); -jacobian((C_q.')*dq,q)*dq];
49
50 Hexplicit = simplify(inv(Himplicit));
51 rhs = simplify(Hexplicit*c);
52

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