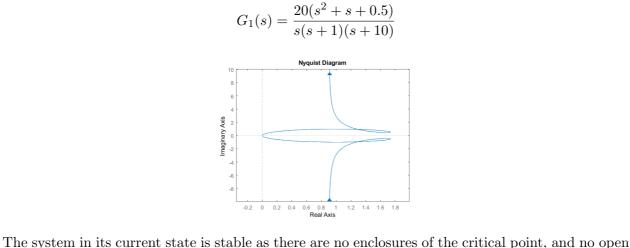
Daniel Eisen: 300447549

July 28, 2021

1. (a)

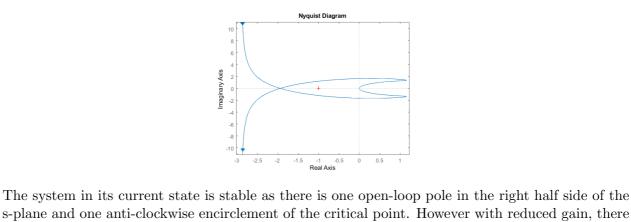
Section A - Formative Questions



enclosure, and thus the system cannot be made unstable with this method. $G_2(s) = \frac{20(s^2 + s + 0.5)}{s(s-1)(s+10)}$

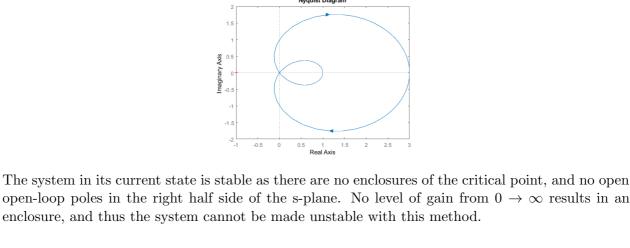
open-loop poles in the right half side of the s-plane. No level of gain from $0 \to \infty$ results in an

(b)



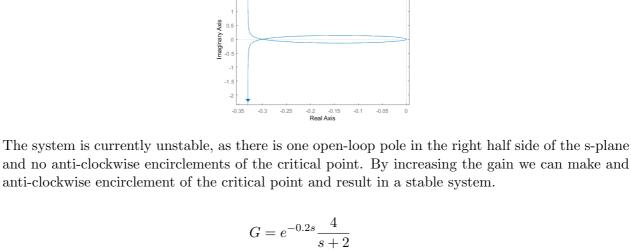
(c) $G_3(s) = \frac{s^2 + 3}{(s+1)^2}$

will be no enclosure of the critical point and the system can be driven unstable.



 $G_4(s) = \frac{3(s+1)}{s(s-10)}$

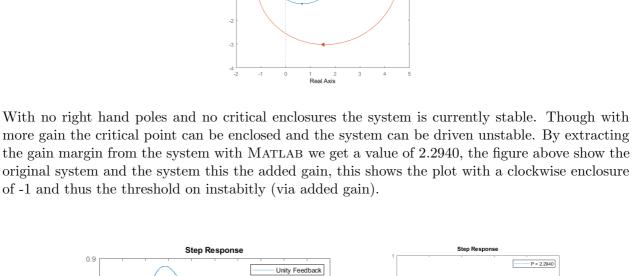
(d)



Eq: Delayed transfer function

2.

(a)



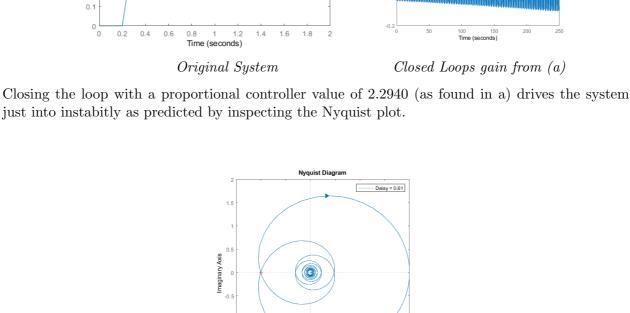
0.3 0.2

(b)

0.8

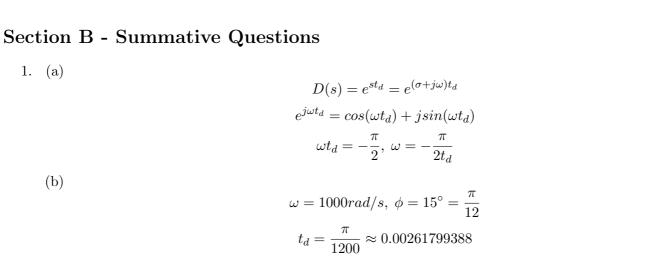
enclosure divergence angle.

phase of both impulse and matched.



The figure above shows that a delay time of 0.61 causes the Nyquist plot to enclose the critical point. Though note a differences from the increased gain plot, smaller overall plot and a tighter

3.



(c) Using Matlab to model the 1st and 2nd Pade approximations and modifying ts until $\phi = 15^{\circ}$.

Figure above show the resultant gain of the frequency response of these approximations. This results in a ts 0.00027 for the 1st and 0.000261 for the 2nd. Both already close to the model delay.

 $substitute \rightarrow sampler \approx \frac{2}{s + \frac{s}{t_a}}$

2nd Pade

The above figure show the different conversion methods time and frequency responses. All but the impulse invariance method perform accurately to a step, which has steady state error. All perform well

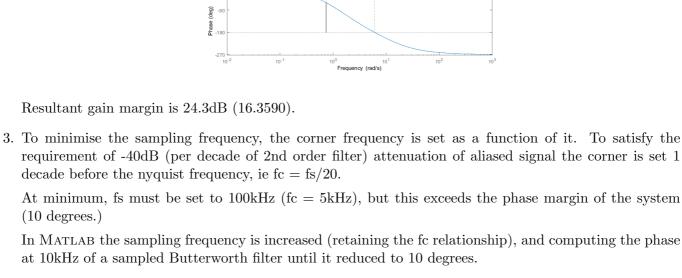
Frequency response reveal larger differences in these methods. The bilinear methods by far more closely match the model system in phase and do not violate the gain roll of at higher frequencies like impulse invariance and match pole-zero, in fact increasing roll off. Also note the huge divergence from the model

to an impulse but the impulse invariance is the only one to lack a delay delay at 0.

 $sampler = \frac{1 - e^{st_s}}{s}$ $pade: e^{st_s} \approx \frac{1 - s\frac{t_2}{2}}{1 + s\frac{t_s}{2}}$

1st Pade

Sampler inserts a left hand pole at 2/sampling time. Therefore as the sampling speed increases, the inserted pole becomes less and less dominant, the gain margin increases and the system more accurately represents the unsampled system. Figures above shows this progression with (left to right) low sampling speed, higher sampling speed and unsampled system. For 10x: Unity gain frequency is 3.55rad/s = 0.565Hz, new sampling: f = 5.56Hz, $t_s = 0.177$



(10 degrees.)

Though note the gain of the sampled system is heavily reduced so this would still need to the scaled.

fs = 1.81Mhz, fc = fs/20

Frequency Response (using 1st Pade delay)