

ECEN321 : Engineering Statistics

Assignment 8 Submission

Daniel Eisen : 300447549

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Confidence Intervals

1. (Navidi 5.2.2), $n = 100$ $x = 73$

(a) $\tilde{p} = \frac{x+2}{n+4} = 0.721153846154$

$z_{\alpha/2} = 1.96$

$\tilde{p} \pm z_{\alpha/2} \cdot \sqrt{\frac{\tilde{p}(1-\tilde{p})}{n+4}}$

$\tilde{p} \pm 0.086185795204 \Rightarrow (0.63496805095, 0.807339641358)$

(b) $\tilde{p} = \frac{x+2}{n+4} = 0.721153846154$

$z_{\alpha/2} = 2.575$

$\tilde{p} \pm z_{\alpha/2} \cdot \sqrt{\frac{\tilde{p}(1-\tilde{p})}{n+4}}$

$\tilde{p} \pm 0.113228787066 \Rightarrow (0.607925059087, 0.83438263322)$

(c) $n = \left(\frac{1.96 \sqrt{\tilde{p}(1-\tilde{p})}}{0.05} \right)^2 - 4 \approx 305$

note as \tilde{p} is relative to previous n, the actual required n is lower, but 305 will still bring the E below 0.05.

(d) $n = \left(\frac{2.575 \sqrt{\tilde{p}(1-\tilde{p})}}{0.05} \right)^2 - 4 \approx 530$

note as \tilde{p} is relative to previous n, the actual required n is lower, but 530 will still bring the E below 0.05.

(e) $p = 0.7, n = 100, \tilde{p} = 0.72115$

$z = \frac{p-\tilde{p}}{\sqrt{\frac{\tilde{p}(1-\tilde{p})}{n+4}}} = -0.48$

$P(Z > -0.48) = .6844 = 68.44\%$

Y is approximately normal with mean= $200 \cdot .95$ and variance= $\text{sqrt}(.95(1-0.95) \cdot 200)$

(f) $n = 200, p = 0.95, k = 193 \dots 200$

$P(X = k) = \frac{n!}{k!(n-k)!} \cdot p^k \cdot (1-p)^{n-k}$

$P(X > 192) = \sum_{k=193}^{200} \frac{n!}{k!(n-k)!} \cdot p^k \cdot (1-p)^{n-k} = 0.2133$

I used wolfram to compute the sum, due to the large factorial.

$(Y > 192) = (Y > 192 + 0.5)$ use the continuity correction
 $= 1 - (192.5 - (200 \times 0.95)) / \sqrt{200 \times 0.95(1-0.95)}$
 $= 1 - (0.81)$
 $= 0.19$
 $(Y > 192) = 0.2090$

2. (Navidi 5.3.8) $\bar{X} = 3410.14, s = 1.018, n = 8, df = 7, CI = \bar{X} \pm t_{\alpha/2} \cdot \frac{s}{\sqrt{n}}$

(a) $t_{\alpha/2} = 2.356$

$CI = 3410.14 \pm 2.356 \cdot \frac{1.018}{\sqrt{8}} \Rightarrow (3409.29, 3410.99)$

(b) $t_{\alpha/2} = 2.998$

$CI = 3410.14 \pm 2.998 \cdot \frac{1.018}{\sqrt{8}} \Rightarrow (3409.06, 3411.22)$

(c) No, because to be able to use the student t CI's and calculations the samples must come from a population that is approximately normal, as seen by the outlier (3412.66) this sample cannot be said to come from a normal population so the above CI's cannot be used.

3. (Navidi 5.6.13)

$X = (207.4, 233.1, 215.9, 235.1, 225.6, 244.4, 245.3)$

$\bar{X} = 229.54, s_X = 14.17, n_X = 7$

$Y = (84.3, 53.2, 127.3, 201.3, 174.2, 246.2, 149.4, 156.4, 103.3)$

$\bar{Y} = 143.96, s_Y = 59.76, n_Y = 9$

$CI = \bar{X} - \bar{Y} \pm z_{\alpha/2} \cdot \sqrt{\frac{s_X^2}{n_X} + \frac{s_Y^2}{n_Y}}, z_{\alpha/2} = 1.96$

$85.58 \pm 1.96 \cdot \sqrt{\frac{14.17^2}{7} + \frac{59.76^2}{9}} \approx 85.58 \pm 40.43$

$CI = (45.15, 126.01)$