

ECEN 321 Lab 5

Regression

Niels Clayton : 300437590

Introduction

Regression is a commonly used tool for assessing the relationship between variables. It is often used to compute the line of best fit of a dataset, and can even be used to help predict future values of a dataset. In this Lab we will be performing a regression on temperature anomaly data from a collection of locations around the globe. We will attempt to use this regression to come to a conclusion on if the average global temperature is increasing, decreasing, or remaining static.

Theory

For a simple linear regression, the first step is to calculate the correlations coefficient of the data sets, often denoted r . This is done with the following equation:

$$r = \frac{1}{n-1} \sum_{i=1}^n \left(\frac{x_i - \bar{x}}{s_x} \right) \left(\frac{y_i - \bar{y}}{s_y} \right)$$
$$= \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2 (y_i - \bar{y})^2}}$$

Using the above equation we are able to calculate the correlation coefficient between variable x and variable y . From the correlation coefficient, we are then able to calculate the slope of the line of best fit, and plot it against the data using the following equation:

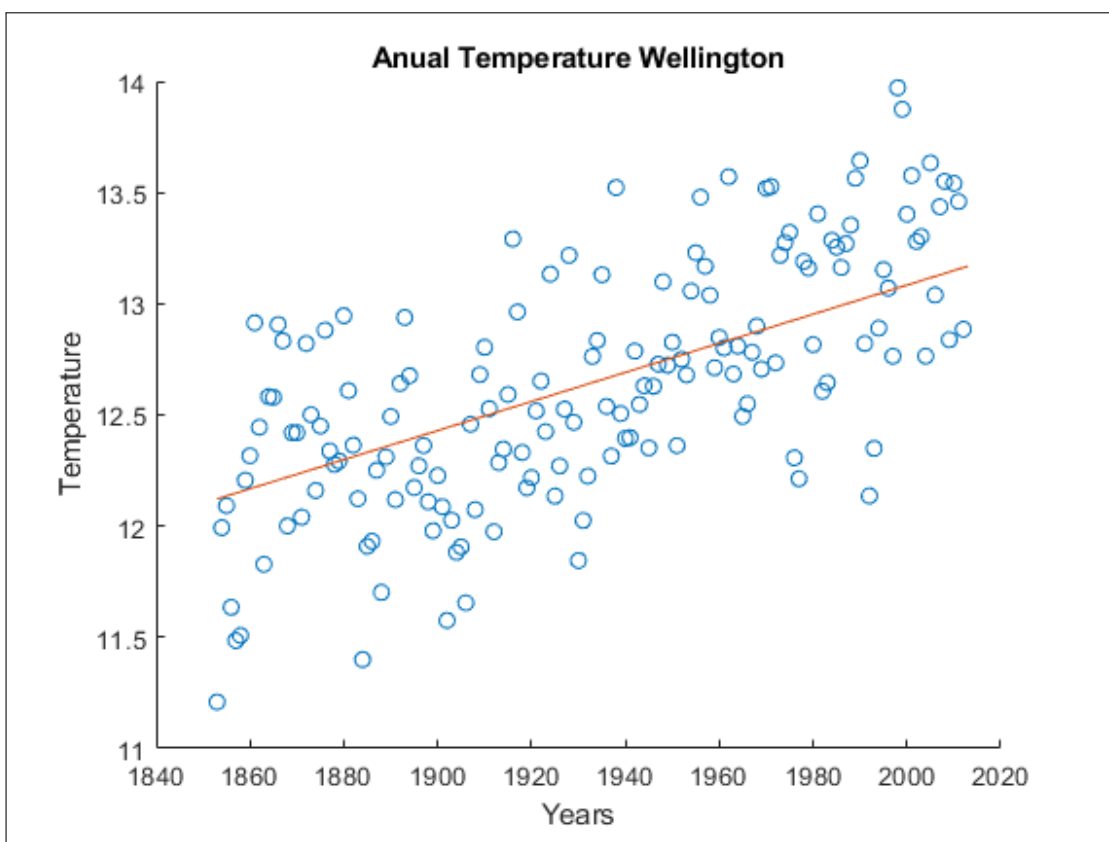
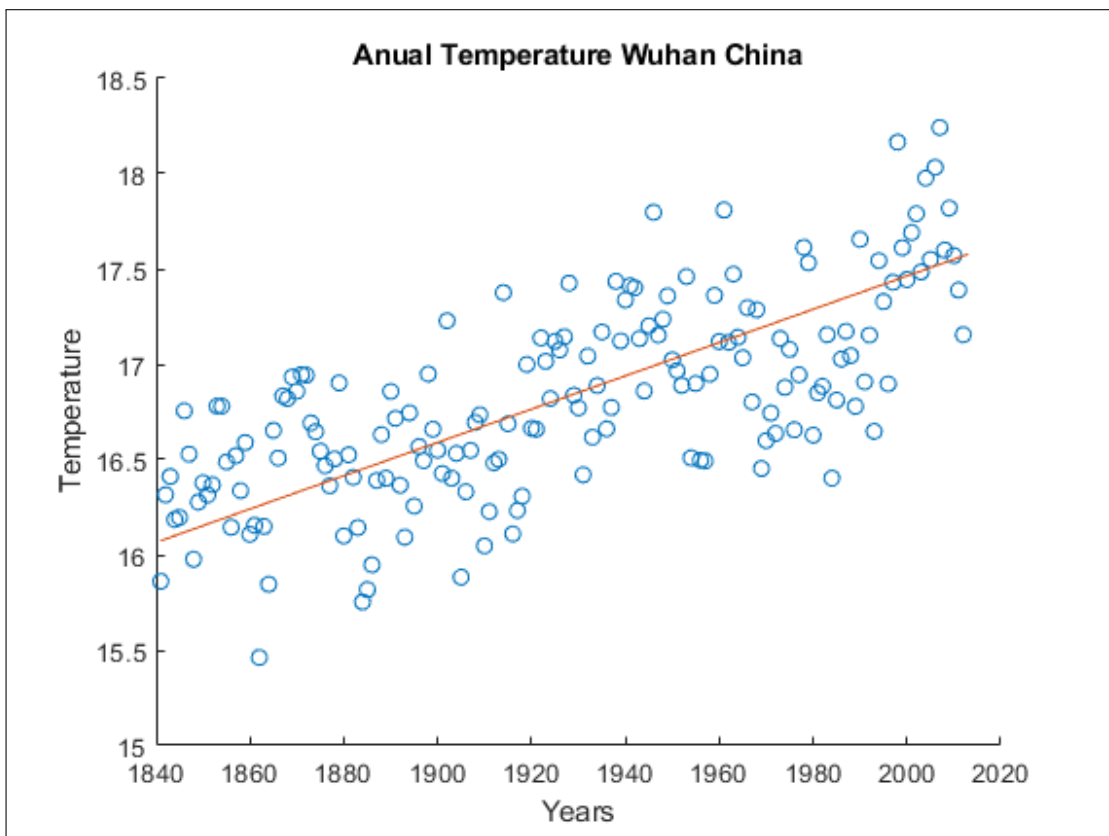
$$\beta_1 = r \frac{s_y}{s_x}$$

Once this correlation coefficient has been computed, we can compute the p-statistic of the correlation coefficient using the following equation:

$$U = \frac{r\sqrt{n-2}}{\sqrt{1-r^2}} \sim t(n-2)$$

Results

This regression was performed on data from Wuhan China, and Wellington New Zealand, the results can be seen below in figures 1, and 2



Using the null hypotheses that the correlation coefficient is zero the following was calculated:

$H_o : r = 0$

$H_1 : r > 0$

using the equation above, the p-static was calculated to be:

Wuhan China - $p = 0$

Wellington New Zealand - $p = 5.9 \times 10^{-15}$

Due to the the insignificance of the p statistic for both Wuhan China, and Wellington New Zealand, we can confidently disregard the null hypotheses that $H_o : r = 0$. This would suggest that there is an increase in the average temperature in these locations.