

- The equation for a line is  $y = mx + b$ . The  $m$  is the “slope” or “coefficient of  $x$ ” and the  $b$  is the intercept or bias.
- Let  $x_i$  and  $y_i$  for stand in for our feature values and target values respectively.
  - For example, if our feature values are  $[1, 2, 3, 4, 5]$  then  $x_0$  is 1, and  $x_1$  is 2, and so on.
- Let  $\hat{y}_i$  stand in for our line’s values at each  $x_i$ .
  - So if our line is  $y = 2x + 1$ , then

$$\hat{y}_0 = 2x_0 + 1 = 2 \times 1 + 1 = 3.$$

$$y_3$$

$$\hat{y}_3$$

$$\hat{y}_3 - y_3$$

- To find the line of best fit, we minimize the “residual sum of squares”.
  - A residual is the difference between the true value of a data point, and our model’s predicted value.
  - Residuals are usually defined as  $y_i - \hat{y}_i$ .
  - To save us from negative residuals, we square them, so each residual in our “sum of squares” is
- $$(y_i - \hat{y}_i)^2.$$
- And finally we sum them up for each  $i$  to get our “residual sum of squares”.

- Let  $n$  be the number of real data points that we have.
- Thus our “loss function” is as follows:

$$RSS = (y_0 - \hat{y}_0)^2 + (y_1 - \hat{y}_1)^2 + \dots + (y_n - \hat{y}_n)^2$$

- Some fancy calculus allows us to find out exactly what our model’s coefficient and intercept need to be.

- Let  $p$  equal our number of features.
- The equation for our linear regression in higher dimensional space:

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_p x_p$$

- $R^2$