

Home Assignment 5

Advanced Web Security

2017

B-assignments

Complete the four B-assignments below and solve them in groups of two students.

B-1 A problem with public key cryptography using a *Public Key Infrastructure*, PKI, is that the keys need to be distributed prior to encryption which may not always be feasible. Instead, one may use *Identity Based Encryption*, IBE. In an IBE system, the public key is generated from a known identity, e.g. an email address. A trusted third party, known as the *Private Key Generator*, PKG, generates the corresponding private key.

One implementation of an IBE system is known as Cocks's encryption scheme, which is based on the difficulty of finding quadratic residues¹. Given a and p , a is said to be a *quadratic residue modulo p* if there exists an integer b such that

$$a \equiv b^2 \pmod{p}$$

otherwise, a is a *non-residue*. It is customary to use the *Legendre symbol*:

$$\left(\frac{a}{p}\right) = \begin{cases} 0, & \text{if } a \equiv 0 \pmod{p} \\ 1, & \text{if } a \text{ is a quadratic residue modulo } p \\ -1, & \text{if } a \text{ is a quadratic non-residue modulo } p \end{cases}$$

where p is an odd prime number. For composite numbers, e.g. $M = p \cdot q$, the *Jacobi symbol* is used instead, which is just a product of the Legendre symbol of the prime factors of M . There are more properties for the Jacobi symbol². You are given the code for calculating the Jacobi symbol³.

Read the paper,

Cocks. “*An Identity Based Encryption Scheme Based on Quadratic Residues*” Proceedings of the 8th IMA International Conference on Cryptography and Coding, 2001

and implement both the PKG and the decryption function. Note that in the paper for encryption, (a/t) means $(a \cdot t^{-1})$, where t^{-1} is the multiplicative inverse modulo M . Encode “+1” as 1 and “-1” as 0.

Your program should take as input

- your public identity, e.g. `alice@crypto.sec`,
- the primes, p and q ,
- a list of the encrypted bits.

¹https://en.wikipedia.org/wiki/Quadratic_residuosity_problem

²https://en.wikipedia.org/wiki/Jacobi_symbol#Properties

³https://github.com/eit-1th/Advanced-Web-Security_EITN41/tree/master/5%20Data%20Representation%20and%20PKI/
code

To derive the public *identity value*, a , use SHA-1 repeatedly on the given *identity*, e.g.

$$a_{i+1} = H(a_i)$$
$$a_0 = \text{alice@crypto.sec}$$

Encode the identity, e.g. `alice@crypto.sec`, as a byte array.

Example:

You have received an encrypted message to your mail, which is your public identity. You are given the following values:

id: `walterwhite@crypto.sec`
p: `9240633d434a8b71a013b5b00513323f`
q: `f870cfcd47e6d5a0598fc1eb7e999d1b`

Encrypted bits:

`83c297bfb0028bd3901ac5aaa88e9f449af50f12c2f43a5f61d9765e7beb2469`
`519fac1f8ac05fd12f0cbd7aa46793210988a470d27385f6ae10518a0c6f2dd6`
`2bda0d9c8c78cb5ec2f8c038671ddffc1a96b5d42004104c551e8390fbf4c42e`

The identity value, a , is computed to be

`25a4d152bf555e0f61fb94ac4ee60962decbb99`

The PKG computed the private key, r , to be

`814a8c2282ca8f4d0f2b2b72df6e6e5e3d8f438c039bdb5d059550739fdcec`

Decrypting the above bits, we get $[1, 1, -1]$ which we decode to $110_2 = 6$.

Do not fear: The assignment is not as hard as it looks.

Assessment:

- Upload your code to Urkund, `paul.stankovski.lu@analys.orkund.se`. One upload per group is sufficient.
- There will be one Moodle question following the problem statement above. **Both students must finish the Moodle quiz.** There will be a test quiz on Moodle, where you can try your implementation as many times as you like. The test quiz will not be graded.

B-2 CMS can be used to nest encryptions, signatures MACs and message digests in any order. CMS is e.g., used by the S/MIME message format for sending signed and encrypted emails. Alice has sent an important message to Bob using the S/MIME format. Instead of signing it, she has first hashed the message, and then encrypted it using the Enveloped Data content type.

You will receive 3 emails, named `mail1.msg`, `mail2.msg` and `mail3.msg`. All are sent from Alice to Bob by first hashing them using

`openssl cms -digest_create ...`

and then enveloping the result using

`openssl cms -encrypt ...`

However, only one of the messages has a valid hash. Your task is to find the subject line of the message with a valid hash. The subject will be an integer. The problem is easiest solved by using the `openssl cms` tool.

In addition to the emails, you will be given Bob's private key (`keyreceiver.pem`), Bob's certificate (`certreceiver.pem`) and a CA certificate (`CACert.pem`) that has been used to sign Bob's certificate.

Assessment:

- There will be one Moodle question following the problem statement above. **Both students must finish the Moodle quiz.** There will be a test quiz on Moodle which you can use to test your OpenSSL commands. You can try the test quiz as many times as you like. The test quiz will not be graded.

B-3 While OCSP solves some problems present in the use of CRLs, it has its own disadvantages. Some of these have been addressed by a technique known as OCSP-stapling. Read about OCSP-stapling, how it works and how it solves some of the OCSP problems. You do not have to go into the technical details or the message formats. Just make sure you understand its purpose and its consequences.

Assessment:

- There will be one Moodle-question with statements regarding the different properties. Four of these statements are correct and your task is to identify these statements. You will receive 0.5p for each correct answer and -0.5p for each wrong answer. You can never get less than 0.0p. It can be a good idea to have the material you have used accessible when you answer the questions, but it is extremely recommended that you read and understand it in advance. **Both students must finish the quiz.**

B-4 The following excerpt from PKCS #1 v2.2 describes the ASN.1 format of an RSA private key with additional CRT information for decryption efficiency (the most common in practice).

```
RSAPrivateKey ::= SEQUENCE {
    version          Version,
    modulus           INTEGER,  -- n
    publicExponent    INTEGER,  -- e
    privateExponent   INTEGER,  -- d
    prime1            INTEGER,  -- p
    prime2            INTEGER,  -- q
    exponent1         INTEGER,  -- d mod (p-1)
    exponent2         INTEGER,  -- d mod (q-1)
    coefficient       INTEGER,  -- (inverse of q) mod p
    otherPrimeInfos   OtherPrimeInfos OPTIONAL
}
```

First learn how ASN.1 works. Then implement your own function for DER-encoding large (up to 2048-bit) integers.

Example 1: The (decimal) integer 2530368937 has TLV DER-encoding 02050096d25da9. Note that a zero byte 00 is appended to the hex representation of the integer value. This is because the value is represented in two's complement, which is a *signed* representation of integers where the highest bit is the sign bit. Without the zero padding, the number 96d25da9 would therefore represent a negative value.

While the encoding above uses the short definite form to represent the length part L in the TLV encoding, your implementation needs to support long definite form (using 81 and 82) as well.

Example 2: If, say, 129 bytes are needed to represent the integer (the value part V of the TLV), then the L part is represented as 8181. The first 81 denotes long definite length encoding with one length byte, and the length itself is encoded in the second byte (129 is 81 in hex). Note that here we do not pad with zero bytes as in Example 1 (lengths are never negative).

Your core function should output a byte vector, but prepare an alternative version that outputs a string representation of the byte vector, as the one shown in Example 1. The alternative implementation will be useful later when you take the Moodle quiz.

Using this core function as a subroutine, implement another function that takes the private RSA parameters p and q as input and outputs the entire Base64-encoded DER-encoding of that private key

according to the above format. This is usually what you will find if you look inside PEM-files containing private RSA keys.

Example 3: Given $p = 2530368937$, $q = 2612592767$ and $e = 65537$ (all decimal), you can compute the following values.

parameter	decimal value	DER-encoding
n	6610823582647678679	02085bbe5d05d47d76d7
e	65537	0203010001
d	3920879998437651233	02083669c395b9cf7321
p	2530368937	02050096d25da9
q	2612592767	0205009bb9007f
exponent1	2013885953	020478097601
exponent2	1498103913	0204594b4069
coefficient	1490876340	020458dcf7b4

Note that **Version** is an **INTEGER** with value 0 (zero). Furthermore, we will always use the value $e = 65537$. Also, for our purposes in this assignment, the optional parameter **otherPrimeInfos** will simply be omitted.

The DER-encoded RSA private key is then assembled as

303c02010002085bbe5d05d47d76d70203010001020836...<omitted bytes>...4069020458dcf7b4,

with the Base64-encoded RSA private key (your answer) being

MDwCAQACCFu+XQXUfXbXAgMBAECCDZpw5W5z3MhAgUA1tJdqQIFAJu5AH8CBHgJdGECBF1LQGkCBFjc97Q=

Hint: There are several online parsing tools that you may find useful during development, e.g., <https://lapo.it/asn1js/>.

Note: You may utilize third-party code for Base64-encoding.

Assessment:

- There will be two Moodle questions for this part. The first (0.5p) will ask you to DER-encode integers. That is, given an integer, you will answer with the DER-encoding of that integer in textual format, as detailed above.

The second question (1.5p) will ask you to convert given integers p and q according to the full CRT-enhanced format given above. Your answer should be the Base64-encoding of the DER-encoding as a single line of text.

Both students must finish the Moodle quiz. There will be a test quiz on Moodle that you can use to test your implementation. You can try the test quiz as many times as you like. The test quiz will not be graded.

- Upload your code to Urkund, paul.stankovski.lu@analys.urkund.se.

C-Assignments

For Home Assignment 5, there is only one C-assignment. Solve it in groups of two students.

C-1 The following is based on a true event. Joe User has created a private RSA key. Accidentally, it ended up on some public Internet location, i.e., some sort of cloud service. Joe tried to save the situation by “censoring” part of the published private key.

```
$ cat key.pem
-----BEGIN RSA PRIVATE KEY-----
MIICXQIBAAKBgQDGlensoredensoredensoredensored1TUxhnjkCbowxZc
7PIpI1E2Po6aIgCBd9+6i0NUIfYm8vR6kqiqlZ8k8o4LYoBkq/9Jx7pgV2Jqhr4u
wvlaQQUzi9c4qPKXp+QGoUu9f1zp80RIMpeJmF7uA20DC93uba07qdC6twIDAQAB
AoGBAIovDuYnGiiQS6K27L4EY8e/5sbqAwdlT0VlWsfz+ai3DLNiFPSbbT1Wx9G4
4b06X60258SD1suZ/g/ICnmnxxe5ua3a5+iiDIwGYmBDcNfq5gMq/d+1/UJF/Bb4
A1nuH2iUg6gRTPEpbg2+RYwquyWenFbqfHMgXqbHVGmOXj7hAkEA8rChKjs5zVmd
j9Gk53psry4CtuxRc39NrHuLqat9Iu0MA51Sgv4c+8dgo75DVAnT5PoLBhHJJAVa
e+rUMC4kfwJBANF7jcKzJ2UuPmL6JpbWcyirybjMIm2eCxR5U1bY1NYT+A49oOFS
Eg5woswgCyH9gDPk2Zwpq3qud9HD7Rn0bckCQQDHgwdRxc2ZybN1eZAWffBaAzZ
PpuTXK0JWaOuX4mnTcLjsdDkWW2QWw8Kbd7B1rZ49kpbuGfmeHQzjRDVbwmXAkBm
T3nFBcrP1+4QWSxPrx0/V+eFoe2OrAmtTjQtzkmi5M3Z5q+UXIkFFG3uVBgb2bur
nLHLW26s1FkgOhgS/RZBAkAFnE+7QvRCW4+v30sIkN63f+GIjHfCuv8L15RpBLlf
XXQyOmmu8YekTu5vbFhtSAiLywW1yCeSsNmKYkX6Ew99
-----END RSA PRIVATE KEY-----
```

Flo Friend has sent Joe User an encrypted message, which you have intercepted:

```
Qe7+h90PQ7PN9CmF0Z0mD32fwpJotrUL67zxdRvhBn2U3fDtoz4iUGRXN0xwUXdJ2Cmz7zjSODE8
ST5dozBysByz/u1H//iAN+QeG1FVaS1Ee5a/TZilrTCbGPWxfNY4vRXHP6CB82QxhMjQ7/x90/+J
LrhdA099lvmdNetGZjY=
```

- Recover the private key in PEM format.
- Decrypt the message.

There are several ways to solve this, so make sure that you clearly explain each step in your solution. Hint: OpenSSL can be very helpful, in particular in the decryption phase.

Assessment:

- Upload your report to Urkund, paul.stankovski.lu@analys.urkund.se.
- Upload your report to Moodle (it will be manually graded).