Instacart Basket Prediction

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1 Introduction

1.1 Problem: Predict the Items Instacart Costumers Purchase

Instacart is a grocery-on-demand start-up which, in 2017, released a dataset containing 3 million orders from 200,000 (anonymized) users. A now-completed Kaggle competition asked entrants to predict which previously purchased products would be in a consumer's next order. In addition, Instacart would like to develop recommender systems that could predict which products a user would buy for the first time and which products would be added to a user's cart in future orders.

Section 6.3 makes predictions according to the Kaggle competition, that is, from a given user's set of previously purchased products, predict which of those products the user will ultimately order. The model includes different product application variants, for instance

- more precise predictions to, for example, autopopulate a user's cart
- top-N most-likely products a particular user will purchase to, for example, display on a web page of fixed results

1.2 Data: The Instacart Online Grocery Shopping Dataset

The Instacart public dataset release is a sample of 3 million orders from 200,000 anonymized users released in 2017. For each user, Instacart has provided between 4 and 100 of their orders, including the intraorder sequence in which products were purchased, the week and hour of the day the order was placed, the relative time between orders, and the grocery store department to which each product belongs. A blog post by Instacart provides some information about the dataset and a Kaggle competition provides additional details.

All data was obtained from the Kaggle competition website. The dataset is a relational set of .csv files which describe customer orders over relative times. Each entity (customer, order, department, etc.) has a unique id.

1.3 Overview: The Data Map Composition

The structure of the subsequent sections corresponds to the maps of the composition

$$RawData \stackrel{\mathsf{P}}{\longmapsto} D \stackrel{\mathsf{F}}{\longmapsto} X \stackrel{\mathsf{RFC}_{\mathbf{n_0}}}{\longmapsto} \hat{y}^{\star} \stackrel{\mathsf{TopN}}{\longmapsto} \hat{y}. \tag{1.1}$$

as well as the domain and image. In section 2 we perform exploratory data analysis on RawData, the dataset described in section 1.2. Section 3 describes the train/test partition P. The feature design map F of section 4 assembles the partitioned raw data D into a design matrix X which has user-product pairs as its rows. The random forest classifier RFC $_{n_0}$ of section 5 makes a probabilistic prediction \hat{y}^* of user-product pairs appearing in the user's ultimate order. In particular, section 5.4 locates optimal hyperparameters n_0 for the random forest classifier. We devise various TopN schemes in section 6.3 to assign binary predictions \hat{y} . Finally, we exhibit a data visualization utility in section 7 to compare the predictions \hat{y} against the true values y_{test} .

In addition, section 8 describes a wishlist of potential improvements to the project. The list of features is in Appendix I – section 9.1 and the Jupyter notebooks containing code for this project are in Appendix II – section 9.2.

2 Exploration

Section 9.2.1 references the code described in this section.

Kaggle posts Simple Exploration Notebook - Instacart and Exploratory Analysis - Instacart, both of which the author viewed while deciding on the dataset and project, were very instructive. First, we display the *.csv files forming the RawData. Displayed in this section are number of plots and tables showing the most (and sometimes least) popular products, aisles, departments, and times for (re)orders:

- order_products*.csv
- orders.csv
- Dictionaries between *_id and *_name
- Merged DataFrame of RawData
- Reorder rates for products and aisles
- The most popular products, aisles, and departments

- Heatmap of order times
- Histogram of order frequency
- Histogram of order counts by user
- Histogram of basket sizes

Table 1: order_products*.csv

order_id	product_id	add_to_cart_order	reordered
1	49302	1	1
1	11109	2	1
1	10246	3	0
1	49683	4	0
1	43633	5	1

While only order_products__train.csv is displayed, order_products__prior.csv has the same structure.

Table 2: orders.csv

order_id	user_id	eval_set	order_number	order_dow	order_hour	days_since
2539329	1	prior	1	2	8	NaN
2398795	1	prior	2	3	7	15.0
473747	1	prior	3	3	12	21.0
2254736	1	prior	4	4	7	29.0
431534	1	prior	5	4	15	28.0

The abbreviated column headers are order_hour_of_day and days_since_prior_order.

Table 3: Dictionaries between *_id and *_name

(a) products.csv

product_id	product_name	aisle_id	department_id
1	Chocolate Sandwich Cookies	61	19
2	All-Seasons Salt	104	13
3	Robust Golden Unsweetened Oolong Tea	94	7
4	Smart Ones Classic Favorites Mini Rigatoni Wit	38	1
5	Green Chile Anytime Sauce	5	13

aisle_id	aisle	department_id	department
1	prepared soups salads	1	frozen
2	specialty cheeses	2	other
3	energy granola bars	3	bakery
4	instant foods	4	produce
5	marinades meat preparation	5	alcohol
-	(b) aisles.csv	(c) department	ents.csv

Table 4: Merged DataFrame of RawData

			dow	hr	days	re	product_name	aisle	department
1	1	1	2	8	NaN	0	Soda	soft drinks	beverages
		2	2	8	NaN	0	Organic Unsweetened	soy lactosefree	dairy eggs
		3	2	8	NaN	0	Original Beef Jerky	popcorn jerky	snacks
		4	2	8	NaN	0	Aged White Cheddar Popcorn	popcorn jerky	snacks
		5	2	8	NaN	0	XL Pick-A-Size Paper Towel	paper goods	household
	2	1	3	7	15.0	1	Soda	soft drinks	beverages
		2	3	7	15.0	0	Pistachios	nuts seeds	snacks
		3	3	7	15.0	1	Original Beef Jerky	popcorn jerky	snacks
		4	3	7	15.0	0	Bag of Organic Bananas	fresh fruits	produce
		5	3	7	15.0	1	Aged White Cheddar Popcorn	popcorn jerky	snacks

Merge of order_products*.csv with orders.csv on order_id upon a reindexing (and deletion of column order_id). The MultiIndex is (user_id, order_number, add_to_cart_order) while order_dow, order_hour_of_day, days_since_prior_order, and reordered are abbreviated dow, hr, days, and re, respectively. The total number of rows – that is, the total number of items ordered – is 33,819,106.

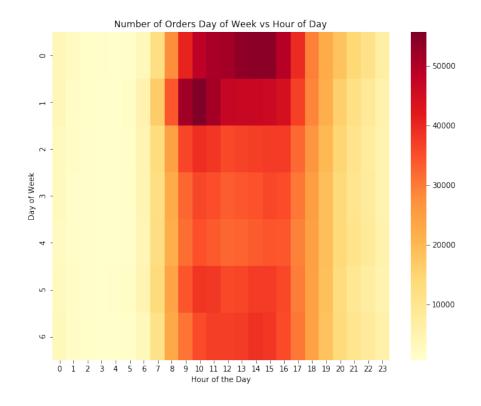


Figure 1: Saturday afternoon and Sunday morning are the most popular time to make orders.

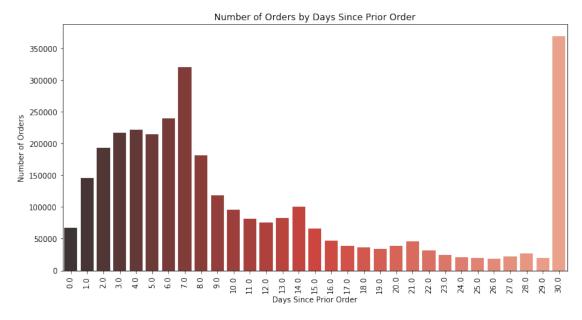


Figure 2: The most popular relative time between orders is monthly (30 days), but there are "local maxima" at weekly (7 days), biweekly (14 days), triweekly (21 days), and quadriweekly (28 days).

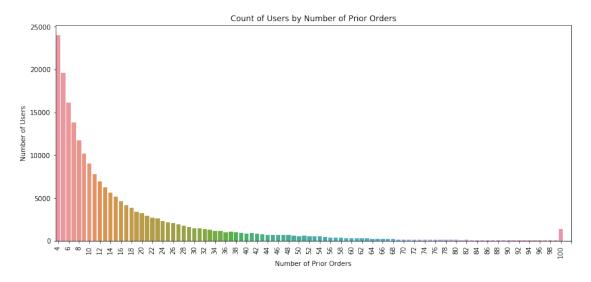


Figure 3: Users have between 4 - 100 orders. Those users in the dataset with 100 orders seem to have at least 100 orders and we have only their most recent 100 orders.

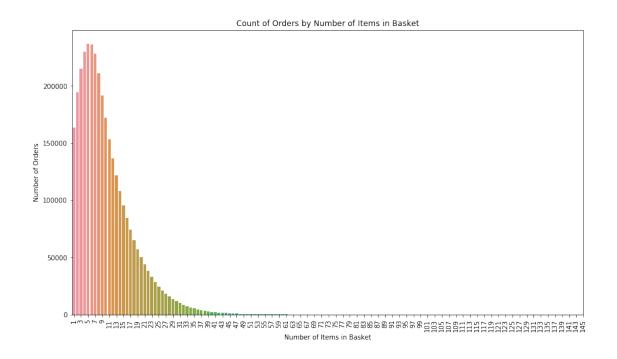


Figure 4: As one should expect, this distribution is right-skew. The mode basket size is 5.

Table 5: Reorder rates for products and aisles. 59.01% of purchases were reorders.

product_name	reorder
Raw Veggie Wrappers	0.9420
Serenity Ultimate Extrema	0.9333
Chocolate Love Bar	0.9215
Bars Peanut Butter	0.8985
Soy Crisps Lightly Salted	0.8955
Maca Buttercups	0.8942
Benchbreak Chardonnay	0.8918
Organic Blueberry B Mega	0.8888
Sparking Water	0.8870
Fragrance Free Clay	0.8702

⁽a) The most reordered products.

aisle	department	reorder
milk	dairy eggs	0.7818
water seltzer	beverages	0.7299
fresh fruits	produce	0.7188
eggs	dairy eggs	0.7063
soy lactosefree	dairy eggs	0.6923
		• • •
beauty	personal care	0.2128
first aid	personal care	0.1958
kitchen supplies	household	0.1948
baking supplies	pantry	0.1675
spices seasonings	pantry	0.1529

⁽b) The most and least reordered from aisles.

nnodust nome	
product_name	count
Banana	491291
Bag of Organic Bananas	394930
Organic Strawberries	275577
Organic Baby Spinach	251705
Organic Hass Avocado	220877
Organic Avocado	184224
Large Lemon	160792
Strawberries	149445
Limes	146660
Organic Whole Milk	142813
Organic Raspberries	142603
Organic Yellow Onion	117716
Organic Garlic	113936
Organic Zucchini	109412
Organic Blueberries	105026
Cucumber Kirby	99728
Organic Fuji Apple	92889
Organic Lemon	91251
Organic Grape Tomatoes	88078
Apple Honeycrisp Organic	87272
Seedless Red Grapes	86748
Organic Cucumber	85005
Honeycrisp Apple	83320
Organic Baby Carrots	80493
Sparkling Water Grapefruit	79245

⁽a) The majority of the 25 most popular products are organic fruits or vegetables.

aisle_name	count
fresh fruits	3792661
fresh vegetables	3568630
packaged vegetables fruits	1843806
yogurt	1507583
packaged cheese	1021462
milk	923659
water seltzer sparkling water	878150
chips pretzels	753739
soy lactosefree	664493
bread	608469

(b) The most popular aisles.

department_name	total_pct
produce	0.2923
dairy eggs	0.1665
snacks	0.0888
beverages	0.0829
frozen	0.0690
pantry	0.0578
bakery	0.0362
canned goods	0.0329
deli	0.0323
dry goods pasta	0.0267
household	0.0229

⁽c) The share of the most popular departments.

0.0218

meat seafood

Table 6: The most popular products, aisles, and departments

3 Train-Test Split

Section 9.2.2 references the code described in this section.

It is worth taking a moment to discuss the dataset partition process. Typically, training a model, tuning its hyperparameters, and evaluating its performance are done using a three-way split of the dataset into independent training, cross-validation, and test sets. On the other hand, the random forest algorithm is a bootstrap aggregation (bagging) of decision trees technique that has a convenient property. Given a sample x in the training dataset, x is used to train only about 2/3 of the decision trees, so that roughly 1/3 of the trees are trained on data which does not include x. An out-of-bag (OOB) estimate uses trees which have not been trained on x to make a prediction for x. Beyond a minor simplification in the dataset partition process, exploiting this property can lead to considerable resource advantages, without which, far less of this project could have succeeded using the resources available on the Kaggle Kernel platform. We elaborate on these details and discuss the implications for the hyperparameter search in Section 5.

The partition map is a transformation,

P: RawData
$$\rightarrow$$
 D^{DSets}

$$RawData \mapsto \{D_s\}_{s \in DSets},$$
(3.1)

where

DSets = {train, test, kaggle},

eval_set user_id
prior 206209
train 131209
test 75000

- RawData denotes the collection of tables of user orders and baskets in orders.csv and order_products*.csv,
- RawData is the set of possible collections of tables matching the column and relational structure of RawData,

eval_set counts

• P is the unique partition defined by a partition of the set of users, U, ordered by, say, user_id, into $\{U_s\}_{s \in DSets}$ where the sklearn.model_selection.train_test_split utility determines the partition between U_{train} and U_{test} , while U_{kaggle} consists of users whose user_id is in a row matching the condition eval_set == 'test' as follows

 U_{train} : 80% of the 131,209 users whose ultimate orders are available.

 U_{test} : 20% of the 131,209 users whose ultimate orders are available.

 U_{kaggle} : The 75,000 users whose ultimate orders are withheld by Kaggle. This project does not explicitly use this set; predictions on kaggle merely serve as a sanity check via submission to Kaggle.

- $\{D_s\}_{s \in DSets}$ is the image of RawData under P.
- D^{DSets} are possible sets of the form $\{D_s\}_{s \in DSets}$, that is, the collection of possible partitions of members of RawData over DSets.

The list of strings dsets = ['train', 'test', 'kaggle'], implements DSets. users is a dictionary of lists of user_ids keyed by dsets, initialized by

```
> users = dict.fromkeys(dsets)
so that
```

representation	implementation
$\overline{DSets = \{train, test, kaggle\}}$	dsets = ['train', 'test', 'kaggle']
$s \in DSets$	ds in dsets
D_s	orders[ds], prior[ds] # RawData
U_s	users[ds]
X_s	X[ds]
y_s	y[ds]

Table 8: Notation Dictionary: representation – implementation

> [users[ds] for ds in dsets]

implements $(U_s)_{s \in DSets}$. Similarly, this notebook constructs matrices X[ds] which implement design matrices X_s . Aside from the analogy between dictionary keys and subscripts, the dict type offers a coherent way to partition the dataset D_s of user orders and baskets in orders.csv and order_products*.csv into separate DataFrames orders[ds] and prior[ds], respectively, for ds in dsets at the outset, so as to avoid potential data leaks. Table 8 is a partial dictionary between mathematical abstractions and instantiations.

We often suppress the dataset decoration in subsequent discussion so that, for example, X_s is denoted X when the objects discussed do not depend on the value of s. Ideas to suppress [ds] in code are welcome.

4 Feature Design

Section 9.2.2 references the code described in this section.

Feature design is a transformation

$$F: D \to M_{n \times m}(\mathbb{R})$$

$$D \mapsto X$$

$$(4.1)$$

where $M_{n \times m}(\mathbb{R})$ is the space of $n \times m$ real-valued matrices and D is the space of possible user-basket data of the form D.

We describe F explicitly as an *m*-tuple of transformations

$$F(D) := (f_1(D), \dots, f_m(D)),$$
 (4.2)

or more succinctly $F = (f_i)_1^m$, where

$$f_i: D \to \mathbb{R}^n$$
 (4.3)

calculates the j^{th} column of $X \in M_{n \times m}(\mathbb{R})$ via the equivalence $(\mathbb{R}^n)^m \cong M_{n \times m}(\mathbb{R})$. Features may be implemented as int, bool, or float types though we consider them abstractly as being \mathbb{R} -valued.

For most $j \in \{1, ..., m\}$, f_j consists of aggregations, filtrations, arithmetic operations, though at times we employ more complex transformations. For example, some features are computed via an unsupervised learning technique, Latent Dirichlet Allocation (LDA), introduced in [1]. This is a probabilistic generative model we apply to the matrix of user-product purchase counts. Although

the random forest classifier already sees this data as a column of X, the distributional assumptions of LDA can yield a bit more predictive power. We can view this as a simple model-based collaborative filtering technique.

The features – columns of the design matrix X – we group into a few Profiles. This overall structure is inspired by the description of feature design in [7], in which the authors describe their approach to a related e-commerce buyer prediction competition. The User Profile, for example, consists of operations and aggregations grouped by user, so that the index for the user profile is U, the list of users. The rows of X are not merely users, but user-product pairs, which means that the User Profile is broadcast to the user-product multi-index, Γ , via a . join() operation. That is, the values of the User Profile are repeated across all products in the user-product index for any given user. An analogous statement holds for the Product Profile. Therefore, the User-Product profile will have the features with the greatest information content (and the Aisle and Department profiles the least). A list of Profiles and features is located in Section 9.1.

For each $u \in U$, let Prod(u) be the ordered sequence of products purchased by u during prior purchases with ordering induced by, say, $product_id$. Rows of X are multi-indexed by

$$\Gamma = ((u, p) \mid u \in U \& p \in \operatorname{Prod}(u)) \tag{4.4}$$

where the ordering is the lexicographic order defined by the ordering on U and $\operatorname{Prod}(u)$. If we denote $(u, p) \in \Gamma$ by γ , then we may denote the γ^{th} observation in $X \times y$ by (x^{γ}, y^{γ}) . Denote $n_s := |\Gamma_s|$ so that X_s is of size $n_s \times m$.

We were able to achieve as many as $m \approx 50$ features on the Kaggle platform on which the collection of notebooks comprising this project were developed and run. The limiting resource is memory, though the limitation occurs at the sklearn.ensemble.RandomForestClassifier calls of sub-

$n_{\rm train}$	n_{test}	n_{kaggle}	m
6760791	1713870	4833292	47

sequent notebooks. Kaggle provides instances with 16GB of memory; the instance provides no virtual memory (disk) so this is a hard limit on memory availability.

The model we construct phrases the labels as a vector *y* of binary classes

$$y^{\gamma} = \begin{cases} \text{True} & \text{if user } u \text{ purchased product } p \text{ in ultimate order} \\ \text{False} & \text{if user } u \text{ did not purchase product } p \text{ in ultimate order} \end{cases}$$
(4.5)

for all $\gamma = (u, p) \in \Gamma$. Recall that y_{kaggle} is withheld by Kaggle. Our aim is in the following sections is to predict the probability P((u, p)) that user u purchases product p in their ultimate order, for all $(u, p) \in \Gamma$ – or at least to predict a rank-ordering of these probabilities.

5 Random Forest Classifier

While random forests are well-known, we will review some details in Section 5.1 so as to explain, motivate, and justify the strategy of Section 5.4 and our choice of train-test rather than train-cv-test split in Section 3. We proceed with a discussion of the OOB samples in section 5.2, a list of metrics we examine in section 5.3, a hyperparameter search in section 5.4, and scores for the rank metrics AUC-PR and AUC-ROC in section 5.5.

Definition 2 amounts to a map of probabilistic predictions

$$\widehat{\mathsf{RFC}}_{\mathbf{n_0}}: \mathsf{M}_{n \times m}(\mathbb{R}) \times \mathcal{B}(\mathbb{R}^m) \to [0,1]^n \\ X \mapsto \hat{y}^*$$
 (5.1)

where n_0 is an optimal choice of hyperparameters. Section 6.3 discusses methods for mapping

$$\begin{bmatrix}
[0,1]^n \to \{0,1\}^n \\
\hat{y}^* \mapsto \hat{y}
\end{bmatrix} (5.2)$$

5.1 Algorithm Review

We begin with a concise review of decision trees to fix notation; Chapters 9.2 and 10.9 of [5] elaborate on the notions mentioned here.

Definition 1 (Decision Tree). Let $\mathcal{P}_{\Lambda}(\mathbb{R}^m)$ denote the space of partitions of the feature space \mathbb{R}^m into rectangular regions, $(R_{\lambda})_{\lambda \leq \Lambda}$, obtained via recursive binary splitting by hyperplanes parallel to coordinate axes. Λ is the *leaf node count* and we may refer to λ as the *leaf index*. Define the *space of binary decision tree parameters over* \mathbb{R}^m by

$$\mathcal{B}(\mathbb{R}^m) := \bigcup_{\Lambda \in \mathbb{N}} \left\{ (R_{\lambda}, \beta_{\lambda}) \mid (R_{\lambda}) \in \mathcal{P}_{\Lambda}(\mathbb{R}^m), (\beta_{\lambda}) \in \{0, 1\}^{\Lambda} \right\}. \tag{5.3}$$

Hence a *tree parameter* $\Theta \in \mathcal{B}(\mathbb{R}^m)$ is a partition $(R_{\lambda}) \in \mathcal{P}_{\Lambda}(\mathbb{R}^m)$ for some $\Lambda \in \mathbb{N}$ with a (boolean) class value β_{λ} associated to each R_{λ} . Given a tree parameter Θ , the associated *decision tree* on \mathbb{R}^m is formally

$$T: \mathsf{M}_{n \times m}(\mathbb{R}) \times \mathcal{B}(\mathbb{R}^m) \to \{0, 1\}^n$$

$$\mathsf{T}(x; \Theta) := \sum_{\lambda} \beta_{\lambda} \mathbf{1}_{R_{\lambda}}(x) \tag{5.4}$$

for $x \in \mathbb{R}^m$ and $\mathbf{1}_R$ the indicator function on $R \subset \mathbb{R}^m$.

Implementations of decision trees and random forests employ many hyperparameters to control the tree topology. For example, the sklearn.tree.DecisionTreeClassifier and sklearn.ensemble.RandomForestClassifier APIs expose

- the numbers of variables to consider during splits $(n_{\text{max features}})$,
- minimum samples in leaf nodes $(n_{\min \text{ samples leaf}})$,
- maximum tree depth (n_{max_depth}), etc.

Collect the hyperparameters into a vector,

$$\mathbf{n} = (n_{\text{max_features}}, n_{\text{min_samples_leaf}}, n_{\text{max_depth}}, \dots). \tag{5.5}$$

The space, **H**, of all such **n** parametrize a family of probability distributions, $\mathcal{T}(\mathbf{n})$, on $\mathcal{B}(\mathbb{R}^m)$, from which we sample tree parameters.

To grow a decision tree classifier, $\hat{T}(x; \Theta)$, on a training set $X_{train} \times y_{train}$ is to find tree parameters $\hat{\Theta}$ via empirical risk minimization

$$\hat{\Theta} = \arg\min_{\Theta} \sum_{\lambda < \Lambda} \sum_{x^{\gamma} \in R_{\lambda}} L(y^{\gamma}, \beta_{\lambda})$$
(5.6)

where L is a loss function (e.g. ordinary least squares) whose precise definition depends on the implementation. In addition, computing (R_{λ}) is combinatorially difficult so we must settle for $\tilde{\Theta}$, an approximation of the estimate. Practically, this means a procedure which recursively repeats the steps

- 1. Select $n_{\text{max_features}}$ features at random from the m features.
- 2. Use an information criterion such as Gini impurity to determine the best variable and split point among the $n_{\text{max}_{\text{features}}}$ features.
- 3. Split the node into two daughter nodes.

until the components of **n** determine the procedure stops. Section 1.10.7.1 of the scikit-learn documentation has more precise implementation details.

Bootstrap aggregation, or bagging, is essentially an averaging technique which is useful for high-variance, low-bias estimators, such as decision trees. Random forests are a modification of bagging trees which builds de-correlated trees by selecting a random subset of input variables from which to form decision nodes – that is, allowing $n_{\text{max_features}}$ to take values less than m.

Following the first definition of [2] and the exposition of Chapter 15 of [5], we can give a high-level overview of the random forest classifier algorithm as follows:

Definition 2 (Random Forest). Given a number of decision trees, B, draw bootstrap samples $(\mathbf{Z}_b^*)_{b \leq B}$ from $X_{\text{train}} \times y_{\text{train}}$ of size n_{train} and grow decision tree classifiers $(\hat{\mathsf{T}}(x;\Theta_b))_B$ on $(\mathbf{Z}_b^*)_B$. The resulting *random forest classifier* is the predictor

$$\widehat{\mathsf{RFC}}: \mathsf{M}_{n \times m}(\mathbb{R}) \times \mathcal{B}(\mathbb{R}^m) \to \{0,1\}^n$$

$$\widehat{\mathsf{RFC}}(x) := \mathsf{majority\text{-}vote}\left\{\left(\widehat{\mathsf{T}}\left(x; \Theta_b\right)\right)_B\right\}. \tag{5.7}$$

In fact, the implementation details of RandomForestClassifier differ from the above in that scikit-learn averages probabilistic predictions instead of using majority-vote; therefore \hat{T} , \widehat{RFC} , and \widehat{OOB} defined in section 5.2 below, are probability predictions rather than class predictions. In other words, the ranges of the maps (5.4), (5.7), and (5.10) are ordered n-tuples of intervals [0,1] instead of ordered n-tuples of boolean values $\{0,1\}$:

$$\hat{\mathsf{T}}, \widehat{\mathsf{RFC}}, \widehat{\mathsf{OOB}} : \mathsf{M}_{n \times m}(\mathbb{R}) \times \mathcal{B}(\mathbb{R}^m) \to [0, 1]^n$$
 (5.8)

We discuss various schemes for mapping $[0,1]^n \to \{0,1\}^n$ in Section 6.3. In the sklearn.ensemble.RandomForestClassifier API, B is called n_estimators.

5.2 Out of Bag Samples

Random forests have a convenient property which we exploited in hyperparameter tuning. In Definition 2, the bootstrap samples are chosen so that approximately 1/3 of instances are left out. Therefore, for any $\gamma \in \Gamma_{\text{train}}$, the observation $(x^{\gamma}, y^{\gamma}) \in X_{\text{train}} \times y_{\text{train}}$ is left out of approximately 1/3 of (\mathbf{Z}_{b}^{*}) .

Definition 3. Given a random forest classifier RFC, let

$$B(\gamma) = \{ b \in \{1, \dots, B\} \mid (x^{\gamma}, y^{\gamma}) \notin \mathbf{Z}_b^* \}$$
 (5.9)

be the set of indices in *B* for which observation γ is *not* in the bootstrap sample \mathbb{Z}_b^* .

For any $\gamma \in \Gamma_{\text{train}}$, the *out-of-bag* (OOB) classifier induced by $\widehat{\mathsf{RFC}}$ is

$$\widehat{\mathsf{OOB}}: \mathsf{M}_{n \times m}(\mathbb{R}) \times \mathcal{B}(\mathbb{R}^m) \to \{0,1\}^n$$

$$\widehat{\mathsf{OOB}}(x^\gamma) := \mathsf{majority\text{-}vote}\left\{ \left(\widehat{\mathsf{T}}\left(x^\gamma; \Theta_b \right) \right)_{b \in B(\gamma)} \right\}$$
(5.10)

that is, the prediction of the random forest constructed by averaging only those trees corresponding to \mathbf{Z}_b^* in which (x^γ, y^γ) does *not* appear. The out-of-bag (OOB) error is the error of OOB on $X_{\text{test}} \times y_{\text{test}}$.

The motivation for using OOB estimates instead of N-fold cross-validation is two-fold. First, this simplifies the phases of the overall project. Second, N-fold cross-validation with $sklearn.model_selection.GridSearchCV$ requires scikit-learn to split and copy the dataset N times, which, in addition to parallelization, causes a memory spike that the 16GB Kaggle Kernel cannot handle, even using N=3, for a feature set of reasonable size.

OOB error estimates are described in Chapter 15.3.1 of [5], which mentions that OOB errors are nearly identical to those obtained by N-fold cross-validation. As well, section 3.1 of [2] explains that, unlike in cross-validation, out-of-bag estimates are unbiased estimators once $n_{\rm estimators}$ is large enough that the test error converges. Otherwise, OOB *over*estimates error. This does not directly speak to how the difference between OOB error and test error varies with different choices of \mathbf{n} , which is a key question for understanding the results of hyperparameter tuning, especially in the low $B \ (\approx 40)$ domain. These errors are empirically close for the purposes of this project, so overall the OOB approach seems justified, though perhaps we should not trust fine differences in scores over different hyperparameters too much.

As before, the implementation details of RandomForestClassifier conveniently differ from the above in that $\hat{T}(x;\Theta_b)$ is a probability prediction rather than a class prediction (and scikit-learn averages probabilistic predictions instead of using majority-vote). Given the approximation between OOB estimates and test error, this feature allows us to use OOB estimates for rank metrics in addition to threshold metrics, as described in the next section.

A Stack Overflow post was insightful in devising the strategy to calculate OOB estimates using different metrics mentioned in Table 10. To use OOB estimates with the sklearn interface, we construct the hyperparameter search somewhat manually with sklearn.model_selection.ParameterGrid, as shown in Listing 2 which essentially creates a Python iterator from a dictionary of parameters, param_grid. Once we have trained a random forest classifier on a combination of parameters in param_grid, we expose the probabilistic OOB estimates with the RandomForestClassifier attribute oob_decision_function_. Then we can score all OOB estimates using the metrics described in Table 10.

5.3 Metrics

Sections 9.2.3 and 9.2.4 contain the code described in this section.

Not all of these metrics are necessarily relevant. In particular, Log Loss and Cohen's Kappa are included 1) out of curiosity and 2) because seven is prime; we should not pay much attention to these metrics except as an exploration into the behavior of the metrics themselves.

By threshold metrics, we mean those which score class values, e.g. precision, recall, and geometric mean (g-mean), while by rank metrics (threshold == False), we mean those which score probability orderings, e.g. AUC-ROC and AUC-PR.

One issue to be aware of when considering metrics is that the ratio between negative and positive classes is

$$skew = \frac{Negative Classes}{Positive Classes} \approx 10.$$
 (5.11)

Perhaps this is not exactly an imbalance, but certain metrics are more robust to skew than others. The discussion of [6] offers guidance on metric behavior with respect to skew and classifier performance. The simulations shown in Figure 1 of [6] suggest that, as far as rank metrics, it could

name	function	threshold
AUC-ROC	sklearn.metrics.roc_auc_score	False
AUC-PR	<pre>sklearn.metrics.average_precision_score</pre>	False
Log Loss	sklearn.metrics.log_loss	False
Precision	sklearn.metrics.precision_score	True
Recall	sklearn.metrics.recall_score	True
F1 Score	sklearn.metrics.f1_score	True
Balanced Accuracy	<pre>sklearn.metrics.balanced_accuracy_score</pre>	True
Geometric Mean	<pre>imblearn.metrics.geometric_mean_score</pre>	True
Cohen's Kappa	sklearn.metrics.cohen_kappa_score	True

Table 10: List of metrics

make sense to favor AUC-PR to AUC-ROC. Given the skew and the high misclassification rate in this problem relative to those the authors considered, perhaps AUC-PR scores have a greater spread than AUC-ROC scores with respect to misclassification rate.

To compute threshold metrics, we choose the probability threshold which predicts a skew for \hat{y} of 10. Threshold metrics are not relevant in judging hyperparameters, though it could be informative to view them. The Kaggle competition uses F1 Score, which is the harmonic mean of precision and recall. Balanced accuracy is the arithmetic mean of these while g-mean is the geometric mean of sensitivity and specificity.

We use the same set of metrics to score the tuned classifier on y_{test} . Note that scores for the model describe test error which is not exactly comparable to the OOB error we compute in hyperparameter tuning.

5.4 Hyperparameter Tuning

Section 9.2.3 references the code described in this section.

The hyperparameters we modify from the default values of RandomForestClassifier are various pairs of the following:

- max_features ∈ {5,...,9}
 Within the above range, there was little variation in scores.
- max_depth ∈ {4,...,64}
 This parameter actually seemed generally harmful to performance when varied (from None).
- $\bullet \ \mathtt{criterion} \in \{\mathtt{gini},\mathtt{entropy}\}$

The default is gini. Splitting criterions made no observable difference in model performance. Explanations as to why are contained in Figure 9.3 of [5] as well as the following StackOverflow posts:

- What is "entropy and information gain"?
- When should I use Gini Impurity as opposed to Information Gain?
- min_samples_leaf $\in \{4,\ldots,48\}$

Listing 1: The parameter grid responsible for the plot of optimal scores in Figure 5.

```
param1 = 'min_impurity_decrease'
param2 = 'min_samples_leaf'

param_grid = {
    param1: np.geomspace(1e-8, 1e-6, 5),
    param2: np.around(np.geomspace(12, 48, 3)).astype(int)
}
```

"The minimum number of samples required to be at a leaf node."

This is one of the two values adjusted from the defaults to train the model.

• min_impurity_decrease $\in [10^{-8}, 10^{-5}]$

"A node will be split if this split induces a decrease of the impurity greater than or equal to this value."

This is the other value adjusted from the defaults to train the model. In the context of decision trees, [5] mentions that modifying this hyperparameter (from None) is near-sighted, since there there may be higher information gain splits to be found beyond this threshold. Nonetheless, tuning this hyperparameter was more effective than the above and it has the benefit of making tree size easier to control than any of the previous hyperparameters, which is helpful to control resource usage. We have not attempted to vary max_leaf_nodes, which could achieve these goals more effectively.

In the notation of Definition 2 with a decoration added for the hyperparameter \mathbf{n} , we may consider a collection of random forest classifiers

$$\left\{\widehat{\mathsf{RFC}}_{\mathbf{n}}(x)\right\}_{\mathbf{n}\in\mathbf{G}}\tag{5.12}$$

where $G \subset H$ is a parameter grid instantiated by, say, the param_grid of Listing 1. Then Figure 5 displays the OOB scores of the $\widehat{\mathsf{OOB}}_n$ classifier associated to $\widehat{\mathsf{RFC}}_n$

$$\hat{y}^* = \widehat{\mathsf{OOB}}_{\mathbf{n}}(x) \text{ for all } \mathbf{n} \in \mathbf{G}.$$
 (5.13)

Listing 2: Hyperparameter search loop; decisions == y_predict_proba

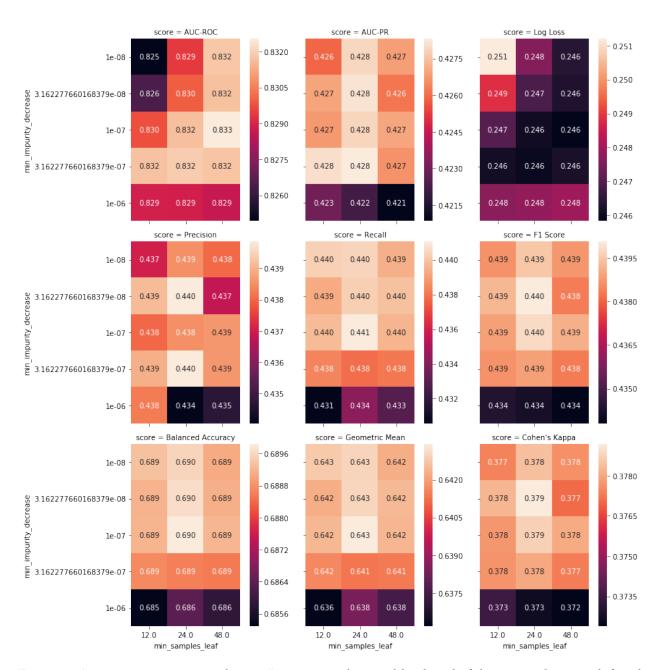


Figure 5: A ParameterGrid search as in Listing 2 in the neighborhood of the optimal scores defined by Listing 1 scored using the metrics of Table 10.

As mentioned in Section 5.1, the implementation details of RandomForestClassifier mean that \hat{y}^* is a probabilistic prediction rather than a boolean value. We examine variants to convert $\hat{y}^* \mapsto \hat{y}$ in section 6.3.

Fortunately, the optimal scores across metrics seem near enough, at least at this scale. The AUC-PR arg max occurs at a value \mathbf{n}_0 of

```
• min_impurity_decrease = 10^{-6.5},
```

• min_samples_leaf = 24

to the resolution displayed in Figure 5. Note that lower scores are better for Log Loss.

Those trees grown with the default values for RandomForestClassifier are "fully-grown" trees, in that those values for \mathbf{n} do little or nothing to 'interfere' with the tree topology, aside from max_features = 'sqrt', which is the default value for classification suggested by the creators. Such fully-grown trees have $\Lambda \approx 10^6$ on $X_{\text{train}} \times y_{\text{train}}$, whereas in the neighborhood defined by Listing $\mathbf{1}$, $\Lambda \approx 10^{4.5}$ — $\mathbf{10}^5$.

The search performed in Figure 5 used $B = n_{estimators} = 35$ trees, which is admittedly few, though samples roughly every observation in 'train'. We used this value for n_estimators to obtain a runtime less than the six hours provided by Kaggle Kernels. A search on a smaller parameter grid with roughly double the n_estimators indicates a bit of empirical stability in optimal hyperparameters as we increase the number of trees.

5.5 Rank Scores

Section 9.2.4 references the code described in this section.

Listing 3: Call and fit RandomForestClassifier

Now that we have decided on hyperparameters, we fit the classifier as in Listing 3. The decision to increase n_estimators to 600 decreases error at the cost of compute time. More trees decreases variance without increasing bias; the only reason we do not use more trees in Listing 2 is the six hour compute time limit of Kaggle Kernels. Listing 3 has a runtime of approximately four hours.

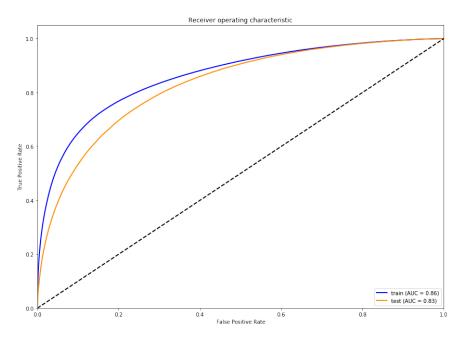


Figure 6: Receiver Operating Characteristic (ROC) curve; AUC-ROC = 0.83.

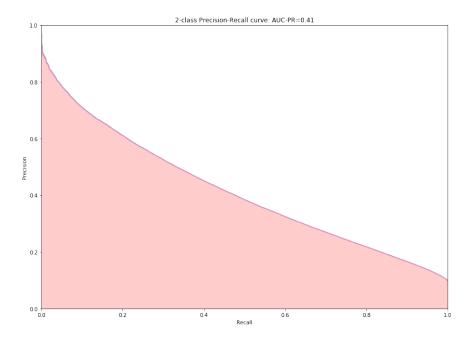


Figure 7: Precision-Recall Curve; AUC-PR = 0.41.

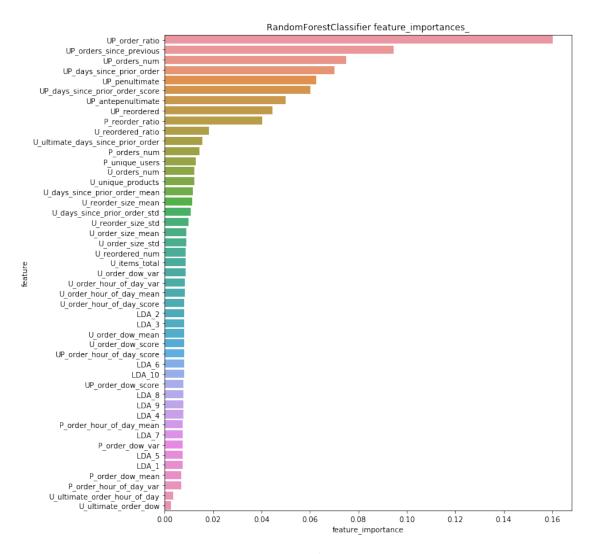


Figure 8: The RandomForestClassifier uses an information criterion to determine variable importances.

5.5.1 ROC Curve

An issue with changing n_estimators to a different value after hyperparameter tuning is that there is not necessarily reason to think that the optimal hyperparameters for n_estimators = 35 are the same as the optimal hyperparameters for n_estimators = 600. On the other hand, changing the value of n_estimators does not alter $\mathcal{T}(\mathbf{n})$, the decision tree distribution. Also, there is a small amount of empirical evidence that the optimal hyperparameters are relatively stable in the range n_estimators \approx 25—75. Finally, given that notebooks of both Sections 9.2.3 and 9.2.4 must run in six hours, this seems like the best strategy since the hyperparameters found in Section 5.4 are the best we are able to compute.

5.5.2 Precision-Recall Curve

Now we can examine the probabilistic predictions from the RandomForestClassifier of Listing 3. The ROC Curve shown in Figure 6 displays decent classifier performance. On the other hand, a

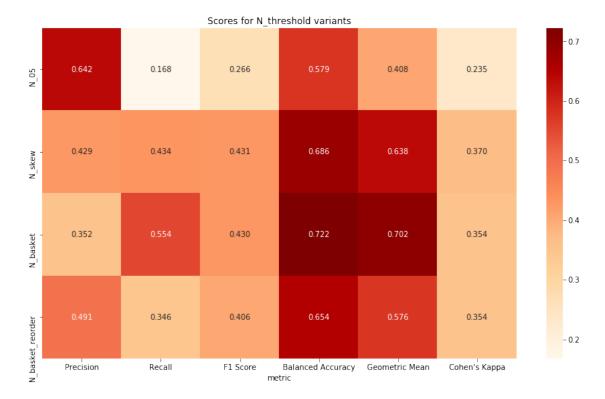


Figure 9: Scores for TopN_{threshold} variants.

skew of 10 means that it is a bit 'easier' to find negatives and 'suppress' the false positive rate. The performance displayed in Figure 6 seems overly optimistic when compared to the Precision-Recall Curve of Figure 7. [3] contains an informative review and argument for using AUC-PR rather than AUC-ROC given an imbalance.

5.5.3 Variable Importances

Figure 8 describes the importances of the features listed in Table 12. Variable importance is another nice feature of random forest classifiers. The importances are computed via the information criterion; the idea is described in 15.3.2 of [5]. One of the most fruitful avenues to pursue to improve classifier performance is to focus on manually creating additional user-product features which capture more complex user-product interactions.

6 TopN Variants

Section 9.2.4 references the code described in this section.

Finally, we define various maps

$$\mathsf{TopN}: [0,1]^n \to \{0,1\}^n$$

$$\hat{y}^* \mapsto \hat{y}$$
(6.1)

to make binary predictions. The structure of the definitions is to define a subset of user-product

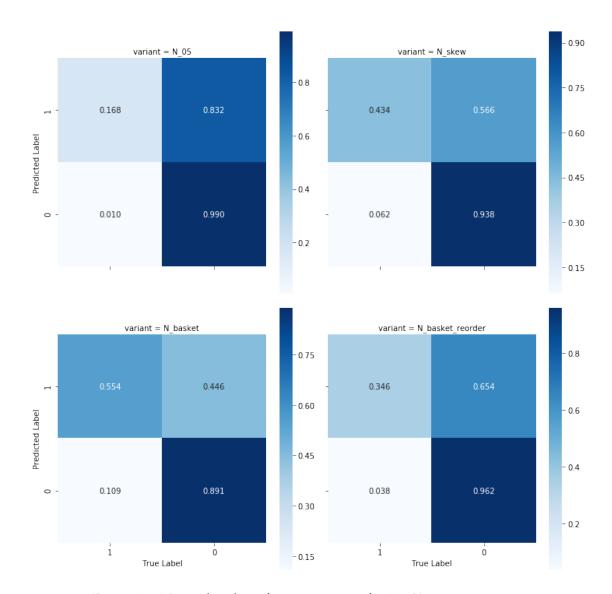


Figure 10: Normalized confusion matrices for TopN_{threshold} variants.

pairs $N_{\text{variant}} \subset \Gamma$ and throughout let

$$\mathsf{TopN}_{\mathrm{variant}}((\hat{y}^{\star})^{\gamma}) = \begin{cases} 1 & \text{if } \gamma \in N_{\mathrm{variant}}, \\ 0 & \text{if } \gamma \notin N_{\mathrm{variant}}. \end{cases}$$
(6.2)

6.1 TopN_{threshold} Variants

If we choose the $N_{\text{threshold}}$ user-product pairs $(u, p) \in \Gamma$ with the greatest $(\hat{y}^{\star})^{(u, p)}$, then this top-N variant is a reparamaterization of the classification threshold, p_0 , via

$$N_{\mathrm{threshold}} = \left\{ (u, p) \mid (\hat{y}^{\star})^{(u, p)} > p_0 \right\}.$$

An advantage of this variant is that it recommends the items users are, in aggregate, most likely to purchase. Therefore, we can, overall, make the 'best' recommendations. A disadvantage is that

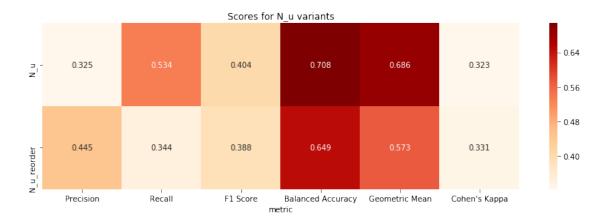


Figure 11: Scores for TopN_u variants.

there is a lot variation in the number of recommended products. Some proposals for principled choices of $N_{\text{threshold}}$ follow.

$N_{0.5}$

A direct interpretation of \hat{y} in terms of probabilities would make a threshold of $p_0 = 0.5$ the most principled choice. On the other hand, choices made in the model definition and implementation make this interpretation dubious. Nonetheless, we can define

$$N_{0.5} = \{(u, p) \mid P((u, p)) > 0.5\}$$

to explore scores. Figures 9 and 10 show scores and normalized confusion matrices.

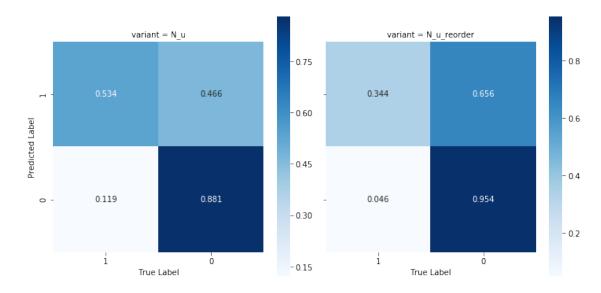


Figure 12: Normalized confusion matrices for TopN_u variants.

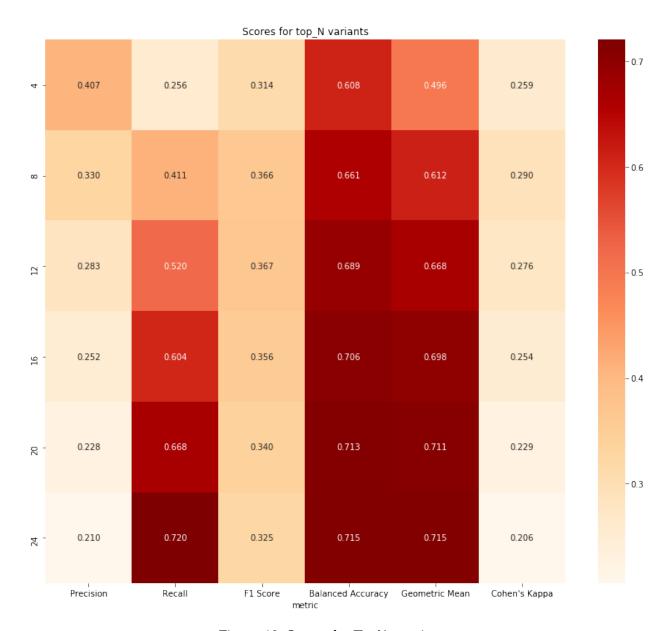


Figure 13: Scores for $TopN_N$ variants.

$N_{\mathbf{skew}}$

It may instead be most principled to choose N such that the skew of \hat{y} equals the train skew.

$N_{\rm basket}$

A couple other values we may consider to be principled are

$$N_{\mathsf{basket}} = \sum_{u \in U} \overline{b(u)}$$

$$N_{\text{basket reorder}} = \sum_{u \in U} \overline{r(u)}$$

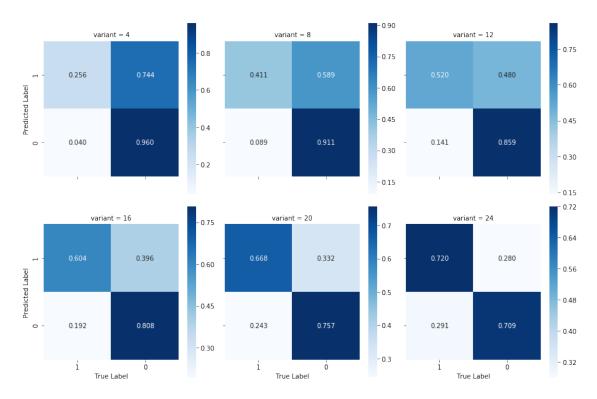


Figure 14: Normalized confusion matrices for TopN_N.

where $\overline{b(u)}$ is the mean basket size for user u and $\overline{r(u)}$ is the mean reordered items per basket for user u.

6.2 TopN_u Variants

If we want to avoid the high variation of basket sizes in the TopN_{threshold} variant, we can define ultimate basket sizes by user. Let

$$N(u) = \left\lceil \overline{b(u)} \right\rceil$$
$$N_{\text{reorder}}(u) = \left\lceil \overline{r(u)} \right\rceil$$

for all $u \in U$, that is, the ceiling of the mean (re)orders per basket for user u. Using the ceiling rather than round or floor offers the advantage of recommending at least one item to users in a straight-forward way. The mean reorders per basket is biased even as a predictor of ultimate reorders since user's initial orders have zero reorders. On the other hand, since we are predicting fewer positives, the precision of $N_{\text{reorder}}(u)$ is better.

For the curious reader, we can be formal about this by defining a maximum-N function recursively as

$$M_1(A) = {\max(A)}, \qquad M_{N+1}(A) = {\max(A \setminus M_N(A))} \cup M_N(A)$$
 (6.3)

where A and $M_N(A)$ are ordered sets. Then

$$N_u = \bigcup_{u \in U} M_{N(u)}(\Gamma|_u)$$
(6.4)

$$\mathsf{TopN}_{\mathsf{U}} : [0,1]^n \times \mathcal{D} \to \{0,1\}^n$$
 (6.5)

which depends on the raw data since N(u) depends on the raw data.

These kinds of variants, or those which offer control of ultimate basket size while offering more flexibility in that control, may be useful for product applications like auto-populating user carts with items we most expect users to reorder. For such an application we would prefer models with higher precision. Figures 11 and 12 show scores and normalized confusion matrices.

6.3 TopN_N Variants

While the top- N_u model gives better predictions, a top-N model with a fixed N for all users may be useful, for example, in displaying previously purchased product recommendations on a web page of fixed size. For an application like this one would prefer higher recall models. Figures 13 and 14 show scores and normalized confusion matrices for $N \in \{4, 8, 12, 16, 20, 24\}$. Using (6.3) it is straight-forward to write explicit formulae for the TopN $_N$ maps.

7 Prediction Explorer

Section 9.2.5 references the code described in this section.

For a user and a model variant, we construct a utility to visualize the model prediction, true order, and basket history, along with colorings for

- True Positives: Ordered and Predicted
- False Positives: Predicted but not Ordered
- False Negatives: Ordered but not Predicted
- True Negatives: neither Ordered nor Predicted

A model with greater **precision** has fewer False Positives while a model with greater **recall** has fewer False Negatives. Note: 'add_to_cart_order' is not meaningful for the top rows of predictions and true orders.

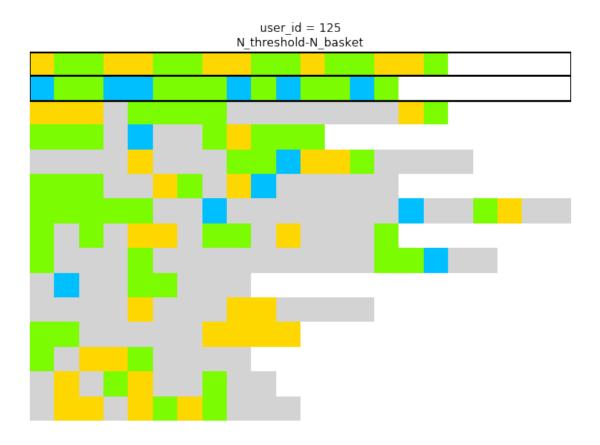
Listing 4: Model choices for Figure 17

```
models_list = [
          ('N_threshold', 'N_basket'),
          ('N_u', 'N_u'),
          ('top_N', '8'),
          ('top_N', '20')
]
```

add_to_cart_order	1	2	3	4	5	6	7	8
order_number								
prediction	Hampshire 100% Natural Sour Cream	Cut & Peeled Baby Carrots	Bistro Bowl Chicken Caesar Salad	Salisbury Steak with macaroni and cheese Salisbury Steak with macaroni and cheese	Multi- Grain Club Crackers	Sliced Sourdough Bread	Organic Fat- Free Milk	Blueberry on the Bottom Nonfat Greek Yogurt
true	Chicken Thighs	Cut & Peeled Baby Carrots	Bistro Bowl Chicken Caesar Salad	Deluxe Plain Bagels	Ritz Crackers	Sliced Sourdough Bread	Organic Fat- Free Milk	French Onion Dip
13	Strawberry on the Bottom Nonfat Greek Yogurt	Blueberry on the Bottom Nonfat Greek Yogurt	Non Fat Black Cherry on the Bottom Greek Yogurt	Colagate Total Whitening Toothpaste	Cut & Peeled Baby Carrots	Sliced Sourdough Bread	Poppycock Cashew Lovers	Butter Toffee Peanuts
12	Cut & Peeled Baby Carrots	French Onion Dip	Sliced Sourdough Bread	Original Cream Cheese	Deluxe Plain Bagels	Ultra Plush® 3 Ply Double Toilet Paper Rolls	Select-a-Size Rolls Paper Towels Tissue	Coke
11	Roma Tomato	French Bread	Organic Navel Orange	Whole Grains Oatnut Bread	Hampshire 100% Natural Sour Cream	Broccoli Crown	Cooking Beef Stock	Horseradish
10	Spiced Rum	French Onion Dip	Bistro Bowl Chicken Caesar Salad	Complete Clean Power Toilet Bowl Cleaner Value Pack	Assorted Chocolate Miniatures Chocolate Candy Bars	Multi- Grain Club Crackers	Cut & Peeled Baby Carrots	Classic Mix Variety
9	Coke	Spiced Rum	Sliced Sourdough Bread	Cut & Peeled Baby Carrots	French Onion Dip	Rigatoni Pasta	Crackers	Chicken Thighs
8	Spiced Rum	Butter	Coke	Original Citrus Sparkling Flavored Soda	Meatloaf and Mashed Potatoes	Salisbury Steak with macaroni and cheese Salisbury Steak with macaroni and cheese	360 Dusters Refills Unscented	French Onion Dip

Figure 15: A portion of a styled DataFrame of Predictions, Ultimate Orders, and Basket History for user_id == 125; model == ('N_threshold', 'N_basket').

Figure 16: "Zoom out" on Figure 15 by ignoring product names.



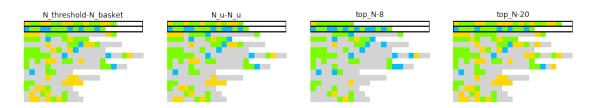


Figure 17: "Zoom out" further by displaying predictions for user_id == 125 using the model choices of Listing 4. By fixing a user, we can inspect the behavior of different models.



Figure 18: Zoom out on Figure 17 to include more users.

8 Prospects

There are a number of avenues to pursue in future versions of this project:

Feature Design: The first suggestions listed may be the most urgent to improve performance.

- Design more User-Product features as a first step. Figure 8 demonstrates how much more effective these features are than those which come from Profiles with lower information content.
- User-Aisle and User-Department Profiles may be the next reasonable Profiles to build if the User-Product profile is exhausted.
- As well, there are additional sorts of complex features which require a modest increase in memory. For example, non-negative matrix factorization (NMF) techniques have traditionally been used in recommendation systems. Such techniques may be appropriate for the user-user matrix of, say, counts of common product purchases. One application of NMF to this matrix is dimensionality reduction to create a relatively small number of user "topics" based on the common purchase count matrix. Experimentation along the lines of Listing 5 on subsets of the overall dataset suggest the matrix is tractable at a size of perhaps roughly 10GB for s = train. The value of n_components requires a search (scored by factor.reconstruction_err_).

Listing 5: NMF Mock-up

```
from sklearn.decomposition import NMF
from itertools import combinations
def col_comb(gp, r):
    return pd.DataFrame(list(combinations(gp.values, r)),
                        columns=['row', 'col'])
product_user = dict.fromkeys(dsets)
product_similarity = dict.fromkeys(dsets)
for ds in dsets:
    product_user[ds] = (prior[ds][['user_id', 'product_id']]
                        .drop_duplicates()
                        .sort_values(by=['user_id', 'product_id']))
product_similarity = (product_user[ds]
                       .groupby('user_id').product_id
                      .apply(col_comb, 2)
                      .reset_index(level=1, drop=True).reset_index()
                      .groupby(['row','col']).count())
factor = NMF(n_components=10)
W = factor.fit_transform(product_similarity)
H = factor.components_
```

• There are many approaches to incorporate interactions between baskets. The factorizing personalized Markov chains model in [9] is a tensor factorization approach which improves on matrix factorization alone by introducing a "personalized Markov chain" product-product transition matrix for each user. These papers are mentioned in [8], which provides an excellent overview of these more complex techniques.

Prediction Explorer: Some ideas to improve section 7 would be

- a product information highlight display on mouse hover (using Bokeh)
- an API allowing for interactivity in user choice, model variant, etc.
- a simple web app front-end

Random Forest Classifier Alterations related to the classifier itself may improve performance somewhat.

- Adjust train/test split proportion to 70%/30%; check if this lowers the difference between train and test AUC-ROC.
- Experiment with max_leaf_nodes.
- Instead of random forests, experiment with gradient boosting or XGBoost.
- A couple variants of random forests were introduced in [4] to better handle imbalanced data. These may offer marginal improvements.
 - Balanced Random Forests are an under/over-sampling technique to either oversample the minority class or undersample the majority class; the imbalanced-learn package has an implementation imblearn.ensemble.BalancedRandomForestClassifier though the results of early experiments have been difficult to interpret.
 - Weighted Random Forests penalize the majority class more or the minority class less; despite the name, they appear to be implemented in scikit-learn as class_weight='balanced'.

9 Appendices

9.1 Appendix I: Features List

Table 11: Profiles

prefix	name
U	User Profile
P	Product Profile
UP	User-Product Profile
AD	Aisle and Department Profiles (ignored)
LDA	Latent Dirichlet Allocation User Features

Table 12: List of features

feature	dtype	description
U_ultimate_order_dow	float16	dow of user's ultimate order
U_ultimate_order_hour_of_day	float16	hour of user's ultimate order
U_ultimate_days_since_prior_order	float16	days since user's previous order (from ul-
		timate)
U_orders_num	uint8	number of orders a given user has placed
U_items_total	uint16	number of total items a given user has pur-
		chased
U_order_size_mean	float16	mean basket size for a given user
U_order_size_std	float16	std basket size for a given user
U_unique_products	uint16	number of unique products a given user
		has purchased
U_reordered_num	uint16	number of total items a given user has pur-
		chased which are reorders
U_reorder_size_mean	float16	mean reorders per basket
U_reorder_size_std	float16	std reorders per basket
U_reordered_ratio	float16	proportion of items a given user has pur-
		chased which are reorders
U_order_dow_mean	float16	mean order_dow
U_order_dow_var	float16	var order_dow
U_order_dow_score	float16	ultimate score for order_dow using circstd
		= sqrt(-2ln(circvar))
U_order_hour_of_day_mean	float16	mean order_hour_of_day
U_order_hour_of_day_var	float16	var order_hour_of_day
U_order_hour_of_day_score	float16	ultimate score for order_hour_of_day us-
		ing circstd = sqrt(-2ln(circvar))
U_days_since_prior_order_mean	float16	mean days since prior order (mean user or-
		der time interval)

U_days_since_prior_order_std	float16	std days since prior order (std user order time interval)
P_orders_num	uint32	number of total purchases
P_unique_users	uint16	number of purchasers
P_reorder_ratio	float16	reorder ratio
P_order_hour_of_day_mean	float16	mean order_hour_of_day
P_order_hour_of_day_var	float16	var order_hour_of_day
P_order_dow_mean	float16	mean order_dow
P_order_dow_var	float16	var order_dow
UP_orders_num	uint8	number of times particular user has or- dered particular product
UP_orders_since_previous	uint8	number of orders since previous purchase of product by user
UP_days_since_prior_order	uint16	days since user last ordered product
UP_days_since_prior_order_score	float16	normalize above by user's days_since_prior_order
UP_reordered	bool	boolean indicating whether the product was ever reordered by user
UP_order_ratio	float16	fraction of baskets in which a given prod- uct appears for a given user (count of or- ders in which product appears divided by total orders)
UP_penultimate	bool	products in user's penultimate (previous) order as bool (train and test sets contain ultimate order)
UP_antepenultimate	bool	products in user's antepenultimate order as bool
UP_order_dow_score	float16	ultimate score for order_dow using (U_ultimate - P_order_dow_mean) / P_order_dow_std (intuitively, how 'far' is a user's ultimate order dow from the mean dow product is ordered)
UP_order_hour_of_day_score	float16	ultimate score for order_hour_of_day using (U_ultimate - P_order_hour_of_day_mean) / P_order_hour_of_day_std (intuitively, how 'far' is a user's ultimate order hour_of_day from the mean hour_of_day product is ordered)
LDA_1	float16	Latent Dirichlet Allocation Feature 1
LDA_2	float16	Latent Dirichlet Allocation Feature 2
LDA_3	float16	Latent Dirichlet Allocation Feature 3
LDA_4	float16	Latent Dirichlet Allocation Feature 4
LDA_5	float16	Latent Dirichlet Allocation Feature 5

LDA_6	float16	Latent Dirichlet Allocation Feature 6
LDA_7	float16	Latent Dirichlet Allocation Feature 7
LDA_8	float16	Latent Dirichlet Allocation Feature 8
LDA_9	float16	Latent Dirichlet Allocation Feature 9
LDA_10	float16	Latent Dirichlet Allocation Feature 10

9.2 Appendix II: Notebooks

The following notebooks contain the code for this project as well as additional discussion particular to the code itself. Some of the linked notebooks repeat parts of the above discussion in order to be more readable as independent documents.

9.2.1 Instacart: Exploratory Data Analysis

Examines the raw data prior to making any predictions.

9.2.2 Instacart: Feature Engineering

Designs nearly 50 features from the raw data. These features are columns of X.

- Instacart: LDA GridSearchCV (Course) is a coarse parameter search for Latent Dirichlet Allocation parameters.
- Instacart: LDA GridSearchCV (Fine) is a fine parameter search for Latent Dirichlet Allocation parameters.
- Instacart: Non-negative Matrix Factorization is a work in progress aimed at constructing features derived from matrix factorization of user-user product counts and variants.

9.2.3 Instacart: Random Forest ParameterGrid Search

Conducts a hyperparameter search using sklearn.model_selection.ParameterGrid, which permits sufficient flexibility for out-of-bag (OOB) samples to be used in cross-validation. A history of previous searches is available at Kaggle.

9.2.4 Instacart: Top-N Random Forest Model

Trains a random forest classifier using the best parameters found in Section 9.2.3. In fact, sklearn.ensemble.RandomForestClassifier provides an array of probabilities. From the ranking determined by this array, Instacart: Top-N Random Forest Model picks the top-N user-product pairs, for various meanings of N.

9.2.5 Instacart: Prediction Explorer

Constructs a visualization utility to inspect model performance for a given model and user.

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