

Lab Section: T 3-5

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Lab 5 – Active Gimbal Control– Dual-Axis Gimbal

Prelab

$$s^2 + \frac{B}{J}s + \frac{K_p K}{J} = s^2 + 2\zeta \omega_n s + \omega_n^2 = 0 \quad \text{char. eqn of CL P controlled system}$$

$$\frac{B}{J} = 2\zeta \omega_n \quad \frac{K_p K}{J} = \omega_n^2 \quad \frac{K}{J} = \frac{\omega_n^2}{K_p}$$

$$J s^2 + (B + K K_d) s + K K_p = 0$$

char. eqn of
CL PD controlled
system

ω_n, ζ are measured
= known

$$s^2 + \left(\frac{B + K K_d}{J}\right)s + \frac{K K_p}{J} = s^2 + 2\zeta' \omega_n' s + \omega_n'^2 = 0$$

$$\frac{B}{J} + \frac{K}{J} K_d' = 2\zeta' \omega_n'$$

$$\frac{K}{J} K_p' = \omega_n'^2$$

$$2\zeta \omega_n + \frac{\omega_n^2}{K_p} K_d' = 2\zeta' \omega_n'$$

$$\frac{\omega_n^2}{K_p} K_p' = \omega_n'^2$$

$$K_d' = \frac{2\zeta' \omega_n' - 2\zeta \omega_n}{\omega_n^2} K_p$$

$$K_p' = \frac{\omega_n'^2 K_p}{\omega_n^2}$$

Experiment #1

Record your Gimbal #.

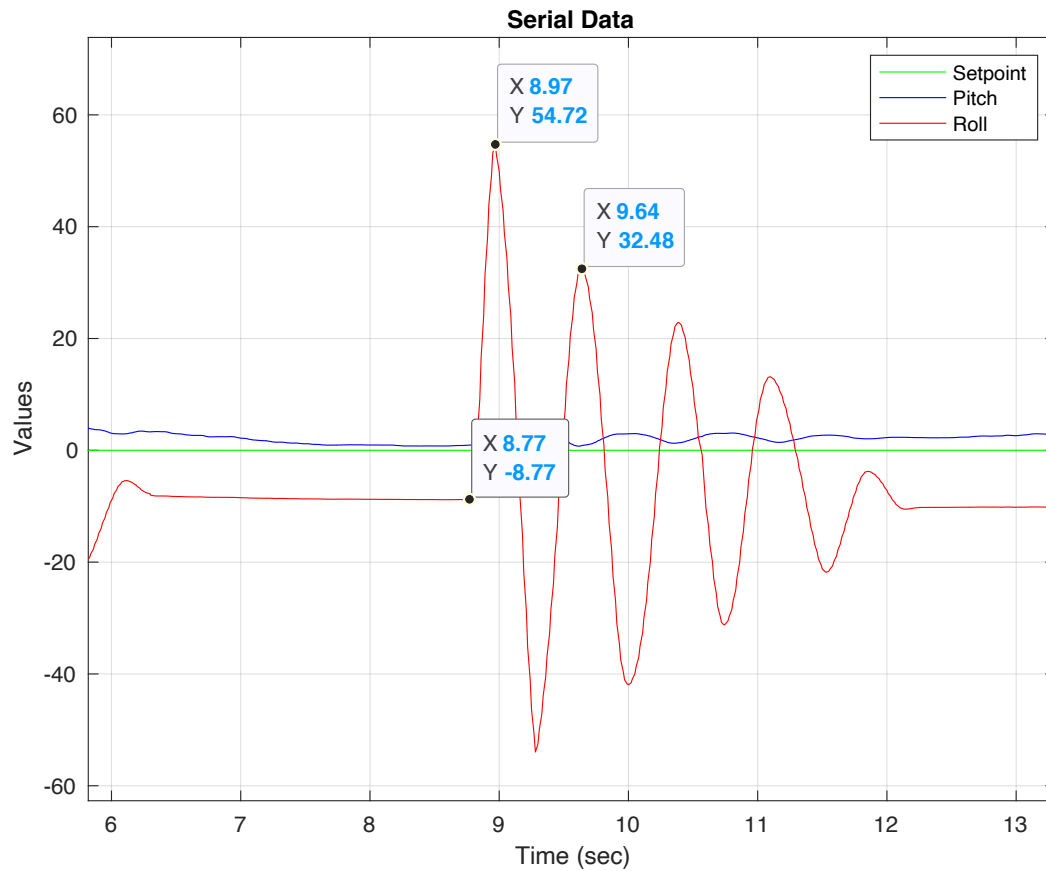
#7

Experiment #2

1. Roll axis:

(a) Damping ratio and natural frequency of P control with $K_p = 10$ (or some other value) and impulse response plot.

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$$\zeta = 0.07$$

$$\omega_n = 9.40$$

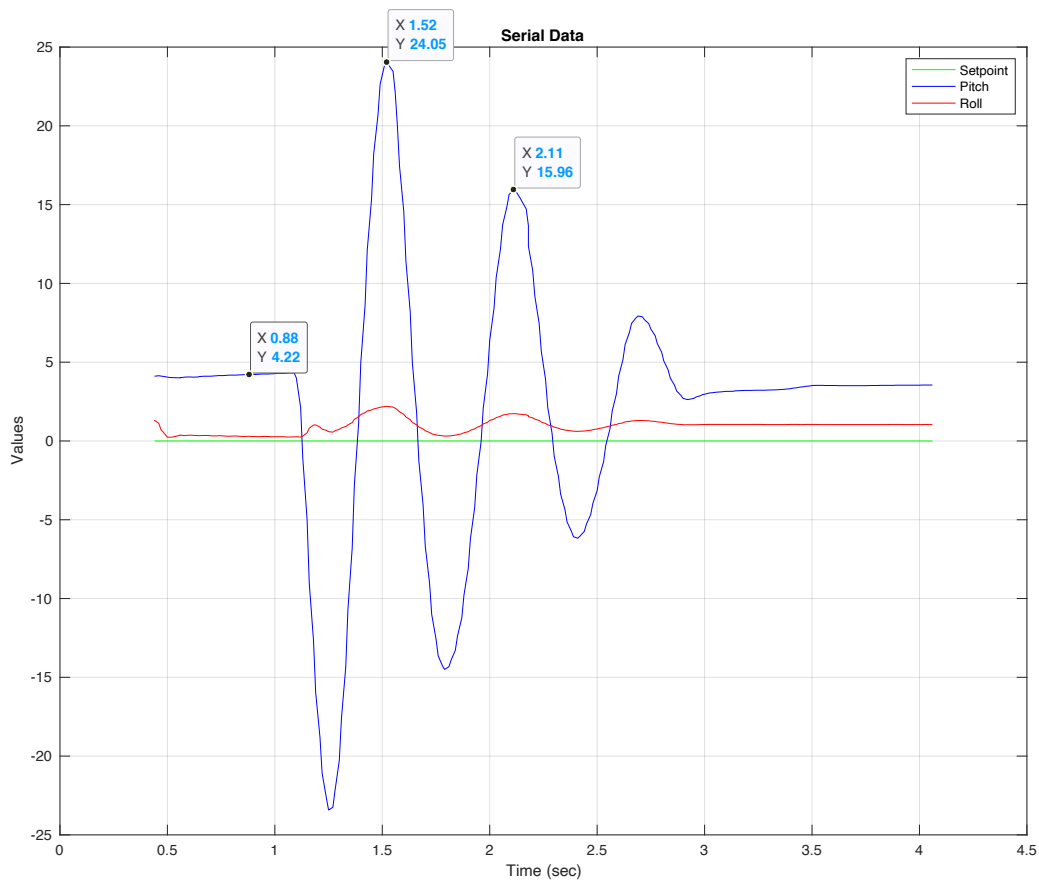
(b) K_p and K_d of PD controller.

$$G_c(s) = K_p + K_d s = 40.21 + 4.12s$$

2. Pitch axis:

(a) Damping ratio and natural frequency of P control with $K_p = 5$ (or some other value) and impulse response plot.
(graph)

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$$\zeta = 0.08$$

$$\omega_n = 10.69$$

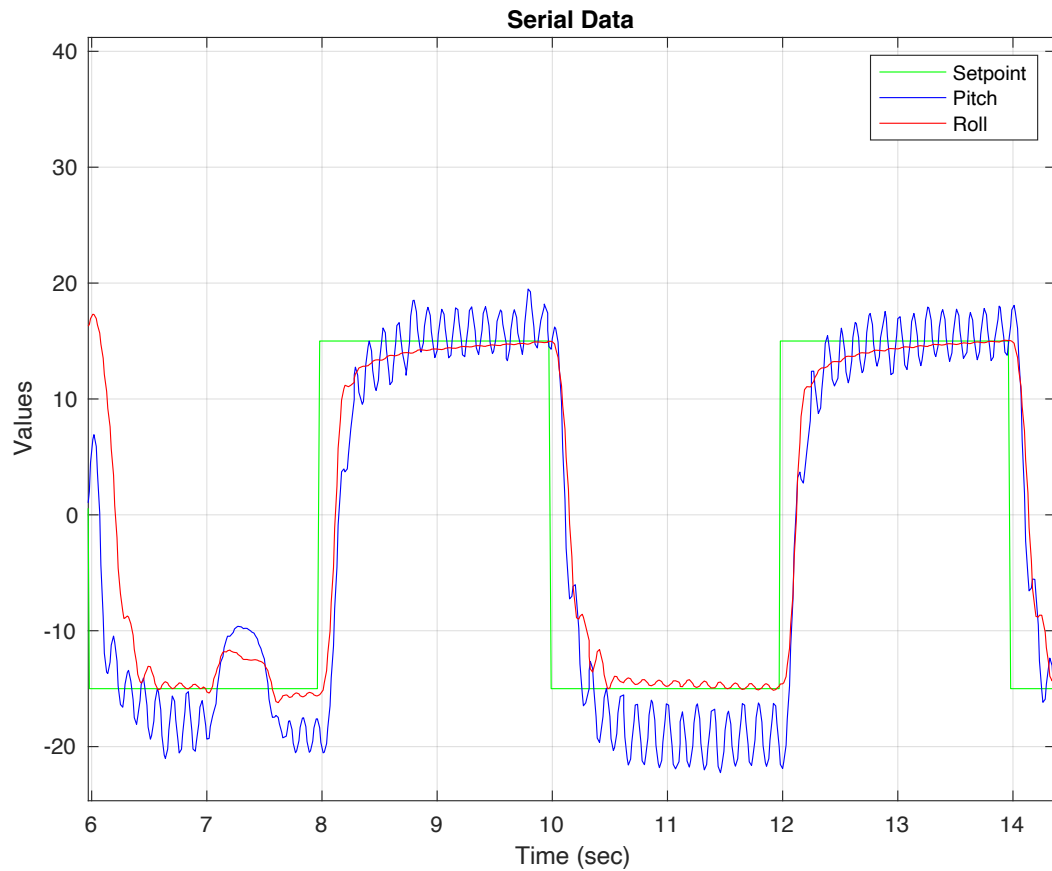
(b) K_p and K_d of PD controller.

$$G_c(s) = K_p + K_d s = 31.11 + 3.15s$$

Explain why pitch and roll axes have different controller gains.
The moment of inertia in roll is greater than that of pitch.

- Implement both PD controllers. Insert a closed-loop step response plot of both pitch and roll responses when driven by a square wave. Use `d_error_1` and `d_error_2` for this task.

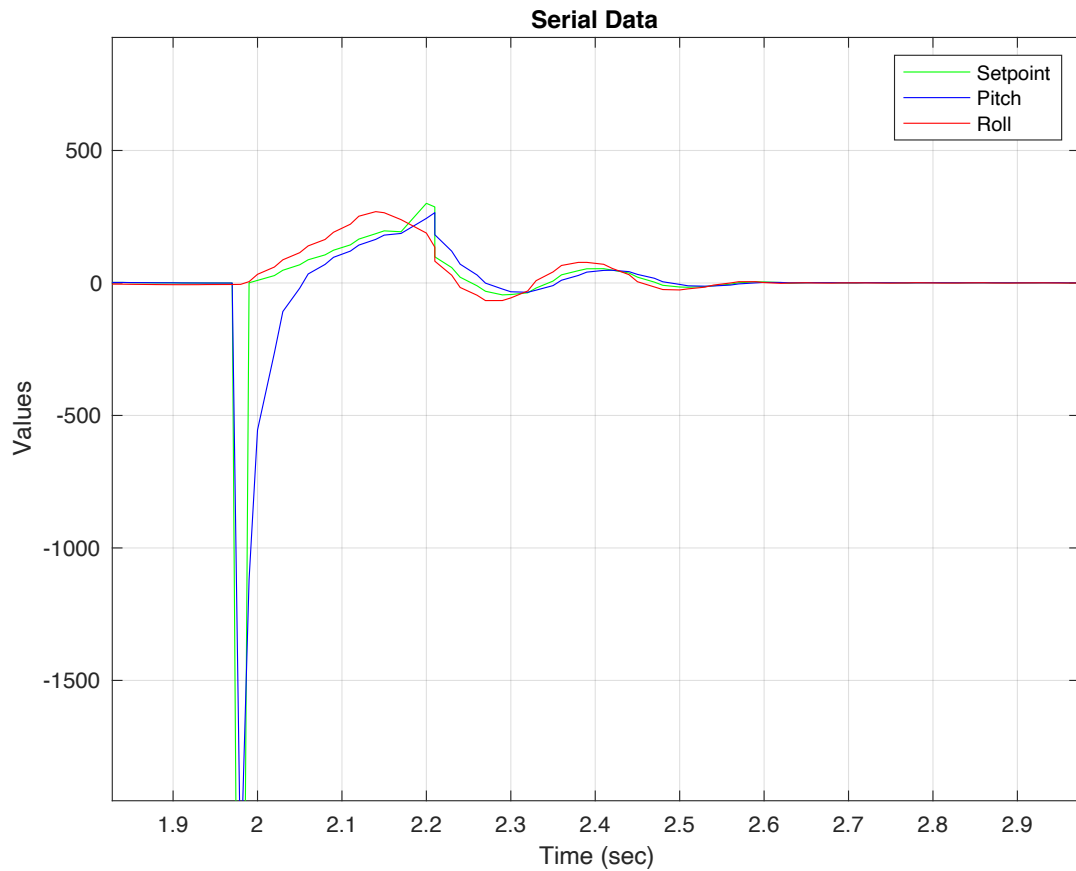
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Experiment #3

1. Insert a plot showing d_error_2 , $filt_d_error_2$, and $roll_rate$ for the roll axis when subject to a square wave input. Comment on the three signals. Use $\alpha = 0.5$ for the low-pass filter.

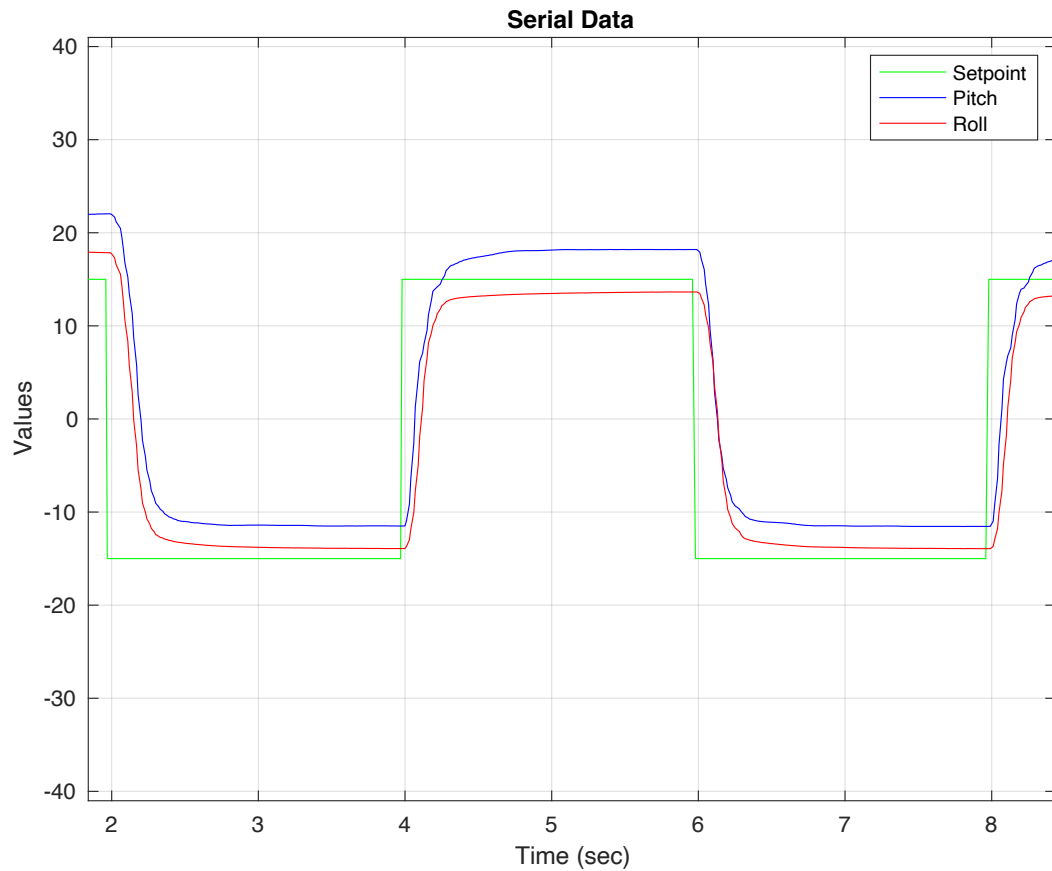
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***** Use *pitch_rate* and *roll_rate* for D control actions for the following tasks.**

2. Insert a closed-loop step response plot of both pitch and roll responses when driven by a square wave. Use *pitch_rate* and *roll_rate* for this task. Compare the responses to the ones in Exp. #2.3 above, and comment on the responses.

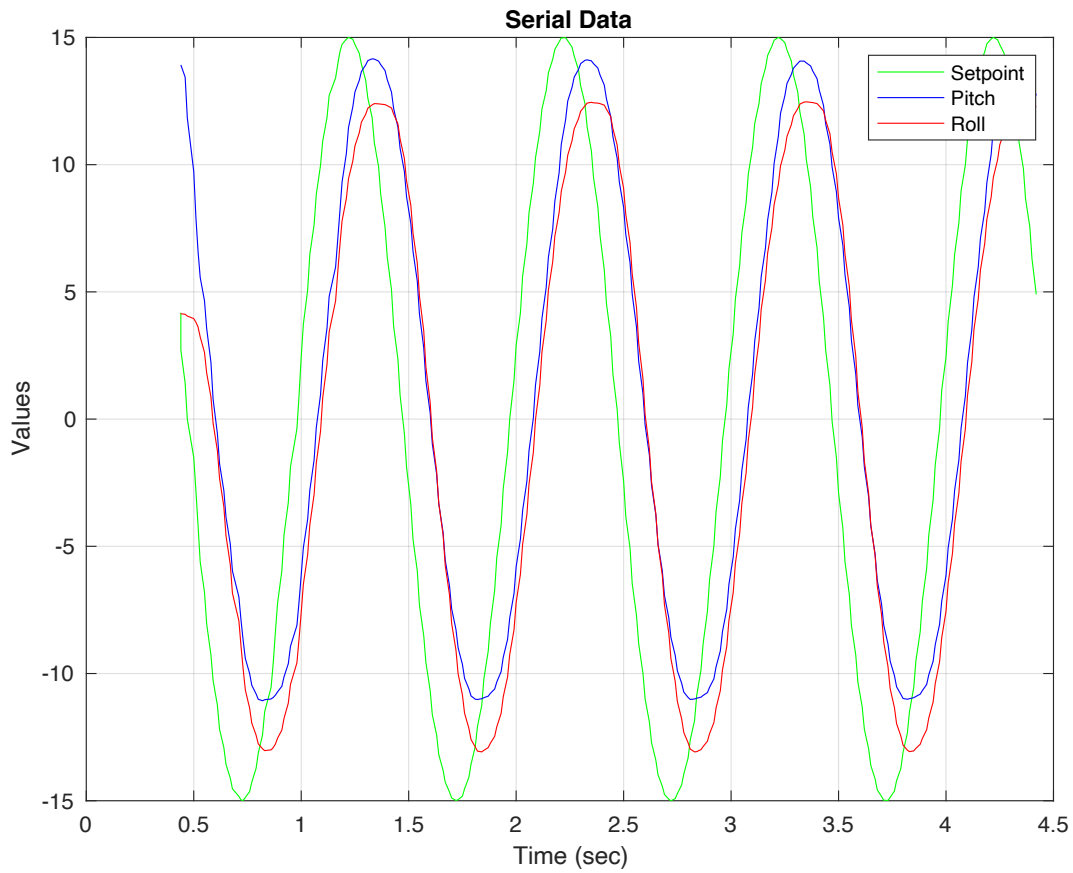
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The response is a lot smoother, a little faster, and without any oscillations.

3. Include a plot showing roll response when subject to a 1 Hz sine wave input. Make comments on the behavior of the gimbal based on your observations.

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The gimbal appears to be consistently rocking.

★Additional Task★

1. *Estimated spring constant and oscillation frequency of the mass-spring setup.*
2. *Demonstrate your tracking system to a staff member.*