

## Exercise 2

a)

Found out that spline interpolation gives the best graph.

```
close all
clear all
clc

motor = [0, 400, 800, 1200, 1600, 1763;
         8, 8.5, 9.0, 9.90, 7.15, 0];

fan    = [0, 400, 800, 1200;
         2, 3.8, 7.5, 14];

interpolation_type = 'spline';

graphSpeed = linspace(0,1800,1801);

MotorTorque = interp1(motor(1,:),motor(2,:),graphSpeed,interpolation_type);
FanTorque    = interp1(fan(1,:),fan(2,:),graphSpeed,interpolation_type);
```

The speed (in RPM) that gives the maximum allowed power, is the speed that gives

$$T_{motor} = 4.0 \text{ [in} \cdot \text{lb]}$$

We find interception between the motor torque curve and the straight line  $T(v) = 4$ .

```
[MaxAllowedMotorSpeed, MaxAllowedMotorTorque] = interception(graphSpeed,MotorTorque,graphSpeed,4);
```

```
MaxAllowedMotorSpeed = 1.6870e+03
MaxAllowedMotorTorque = 4.0000
```

This gives max allowed Power [lb in rpm]

```
MaxAllowedPower = MaxAllowedMotorSpeed*MaxAllowedMotorTorque
```

```
MaxAllowedPower = 6.7479e+03
```

b)

Power is conserved in the system, so we need to find a set of torque and speed for the fan that matches the power output from the motor

```
PowerFan = FanTorque .* graphSpeed;
[MaxAllowedFanSpeed,~] = interception(graphSpeed,PowerFan,[0 1800],[MaxAllowedPower MaxAllowedPower]);
```

```
MaxAllowedFanSpeed = 841.0620
```

```
[~,MaxAllowedFanTorque] = interception(graphSpeed, FanTorque,[MaxAllowedFanSpeed MaxAllowedFanSpeed]);
```

```
MaxAllowedFanTorque = 8.0231
```

Ratio for the motor and fan can be found by

$$i = \frac{D_m}{D_f} = \frac{\omega_f}{\omega_m} = \frac{P T_m}{P T_f} = \frac{T_m}{T_f}$$

```
beltRatio = MaxAllowedMotorTorque/MaxAllowedFanTorque
```

```
beltRatio = 0.4986
```

c)

```
Iv = 1.2 % lb*in*s^2
```

```
Iv = 1.2000
```

## Functions

*Interception(x1,y1,x2,y2)*

Find the interception point of two graphs on vector form.

```
function [xcross,ycross] = interception(x1,y1,x2,y2)
% Find intersections between two arrays y1 and y2

xstart = max(x1(1),x2(1));
xstop  = min(x1(end),x2(end));
x      = linspace(xstart,xstop,(xstop-xstart)*1000 + 1);
y1_int = interp1(x1,y1,x,'linear');
y2_int = interp1(x2,y2,x,'linear');

diff_vec = abs(y2_int-y1_int);
minDiff  = min(diff_vec);
minIndex = find(diff_vec == minDiff);

xcross = x(minIndex);
ycross = y1_int(minIndex);
end
```