

**AN HYBRID EVOLUTIONARY ALGORITHM FOR  
STOCHASTIC VEHICLE ROUTING PROBLEM WITH  
STOCHASTIC DEMANDS**

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# **ABSTRACT**

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by

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Abstract here

## ACKNOWLEDGMENTS

Last thing to do :-)

## DEDICATION

To Hari

## Contents

List of Figures	vi
List of Tables	vii
Notation	viii
Bibliography	1

## List of Figures

## List of Tables



## Notation

Symbol	Definition
$n$	Number of customers
$d_{ij}$	Distance between a pair of customers $i$ and $j$
$E[L_\tau]$	Expected distance of an apriori solution (base sequence) $\tau$
$l$	Location of vehicle
$q_l$	Vehicle capacity when customer $l$ has already been served.
$p_i(j)$	Probability of customer $i$ take the demand value $j$
$K$	Maximal demand
$\bar{D}_i$	Maximal demand of customer $i$
$Q$	Maximal capacity of vehicle

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