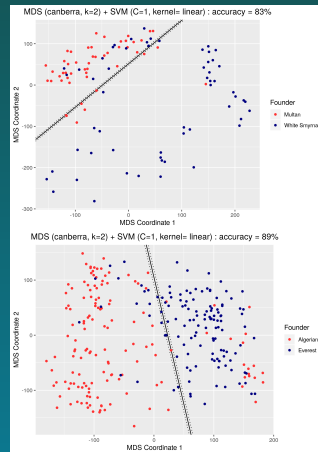
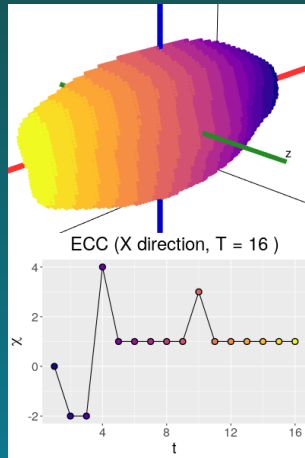


# Using topology to analyze the shape of barley

↓ Animated version! ↓

[bit.ly/eccb21\\_tda](https://bit.ly/eccb21_tda)



## Preprint [QR below]

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## Euler meets plant science

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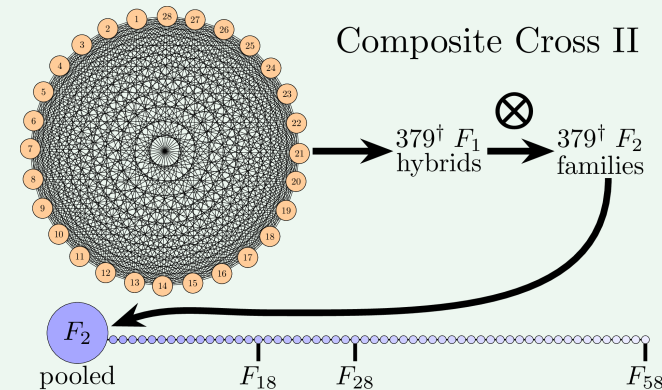
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<sup>3</sup> Mathematics and Computer Science, TU Eindhoven

<sup>4</sup> Integrative Plant Science, Cornell University

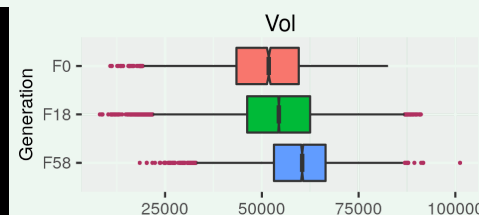
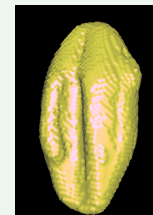
<sup>5</sup> Botany and Plant Sciences, University of California, Riverside

### Barley Experimental Design



- 28 founders (land races). 58 generations.

### Image processing to measure seeds



- 3D X-ray CT scan data: 875 barley spikes.
- 38,000 seeds: generations F0, F18, and F58.
- Distribution of length, height, width, volume, etc.

### SVM Classification Results

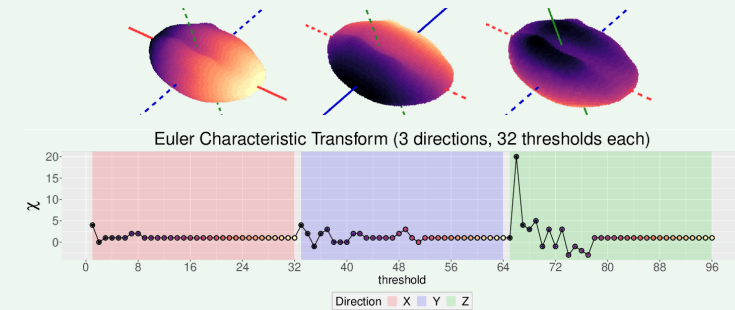
Shape descriptors	# descr	F1 Score
Traditional	11	0.55 ± 0.019
Topological (ECT + UMAP)	12	0.74 ± 0.016
Combined (Trad + Topo)	23	0.86 ± 0.010

- SVM to classify 3,000 seeds from the 28 founders
- (75% training vs 25% testing) × 50 times
- Up to 84% classification accuracy

## Euler characteristic transform (ECT)

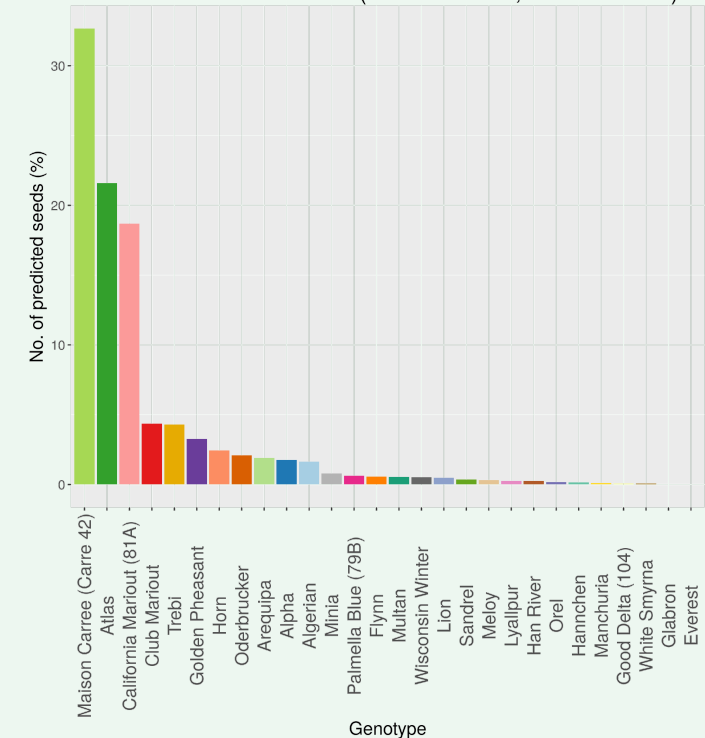
$$\chi = \#(\text{Vertices}) - \#(\text{Edges}) + \#(\text{Faces})$$

- ECT is the record of how the EC changes as we reconstruct a given object in all possible directions.
- The ECT summarizes all shape information [1].



### Semi-supervised learning

SVM Results for Gen 58 (158 directions, 16 thresholds)



- Train with 100% of the founder seeds
- Classify 6000 unlabeled seeds from F58
- Three morphologies are enriched through time.
- Similar conclusion with genomic analysis!

### Acknowledgements

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### References

[1] K. Turner, S. Mukherjee, and D. M. Boyer, "Persistent homology transform for modeling shapes and surfaces," *Information and Inference*, vol. 3, no. 4, pp. 310–344, Dec. 2014.