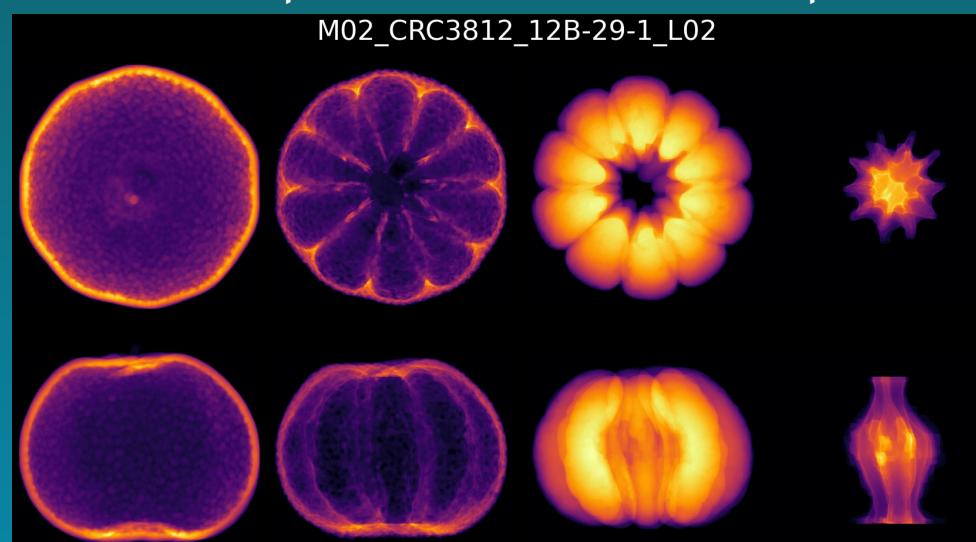
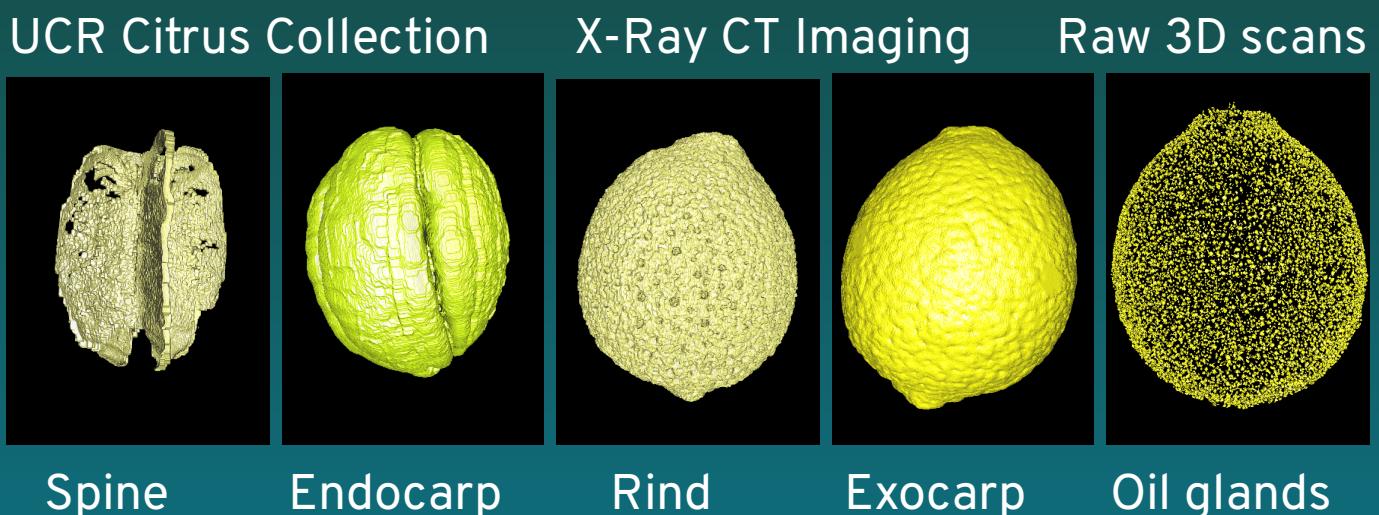
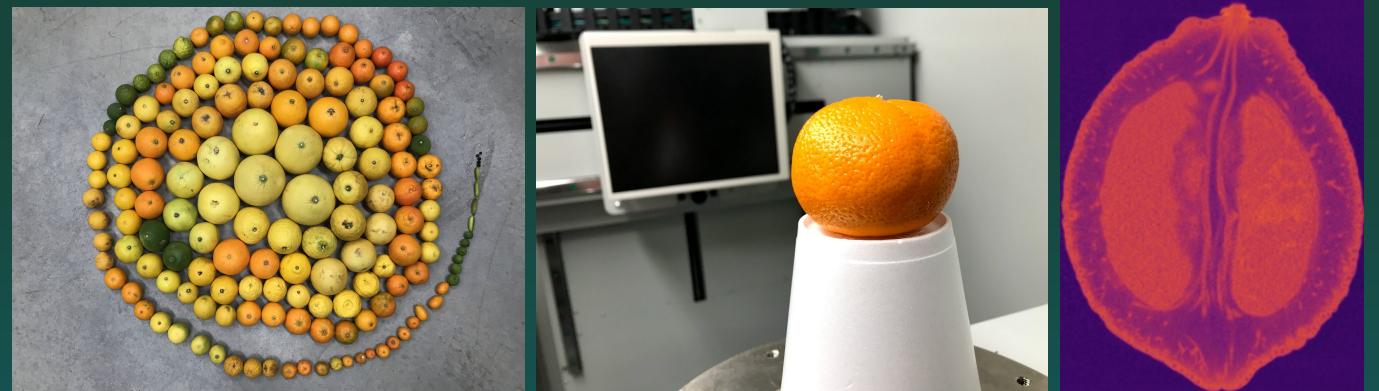


Modeling the shape of citrus and their oil gland distribution



↓ Animated version! ↓

bit.ly/osu_pss22



The shape of aroma

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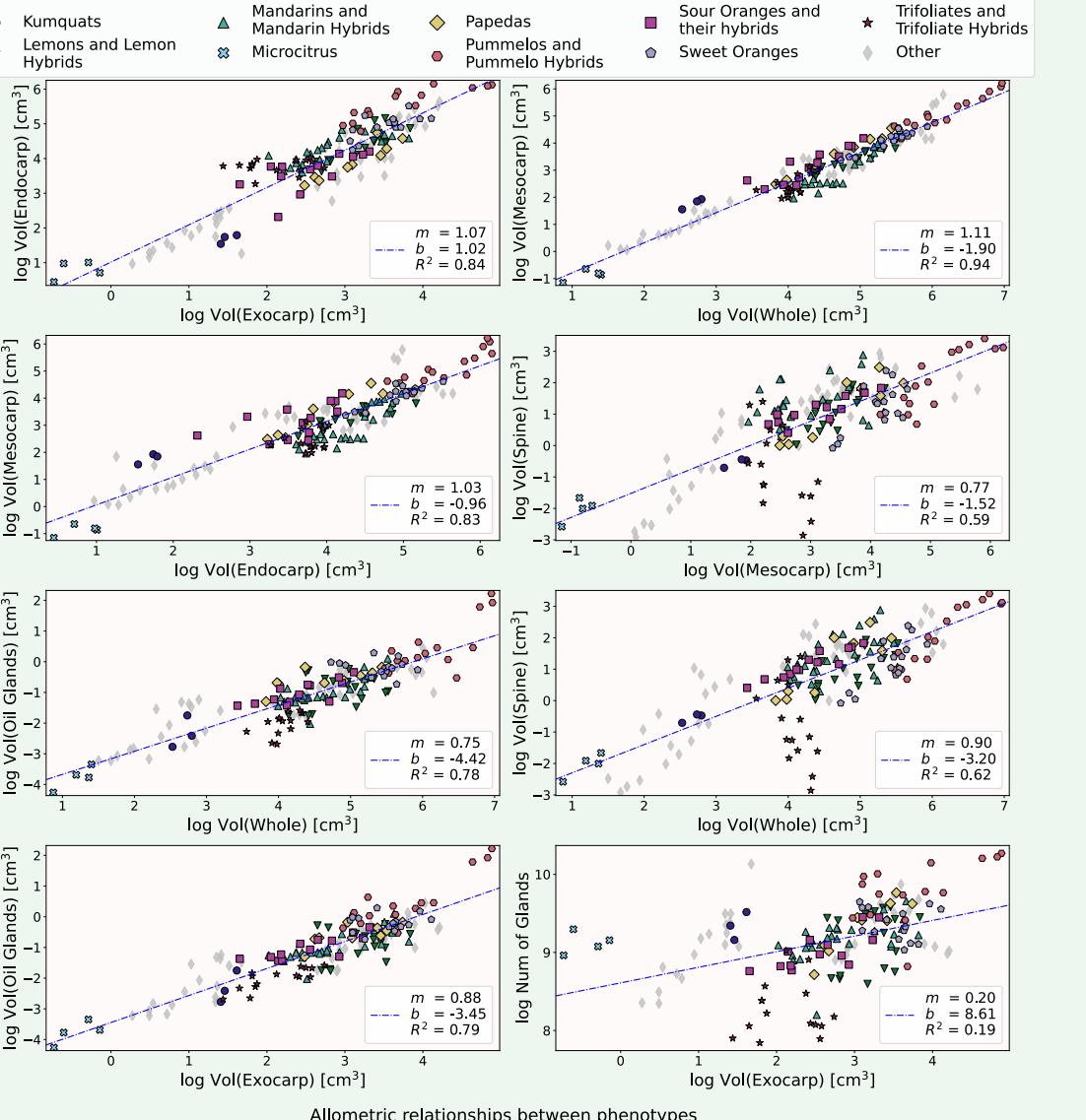
³ Mathematics and Computer Science, TU Eindhoven

⁴ Botany and Plant Sciences, University of California, Riverside

51 different citrus varieties

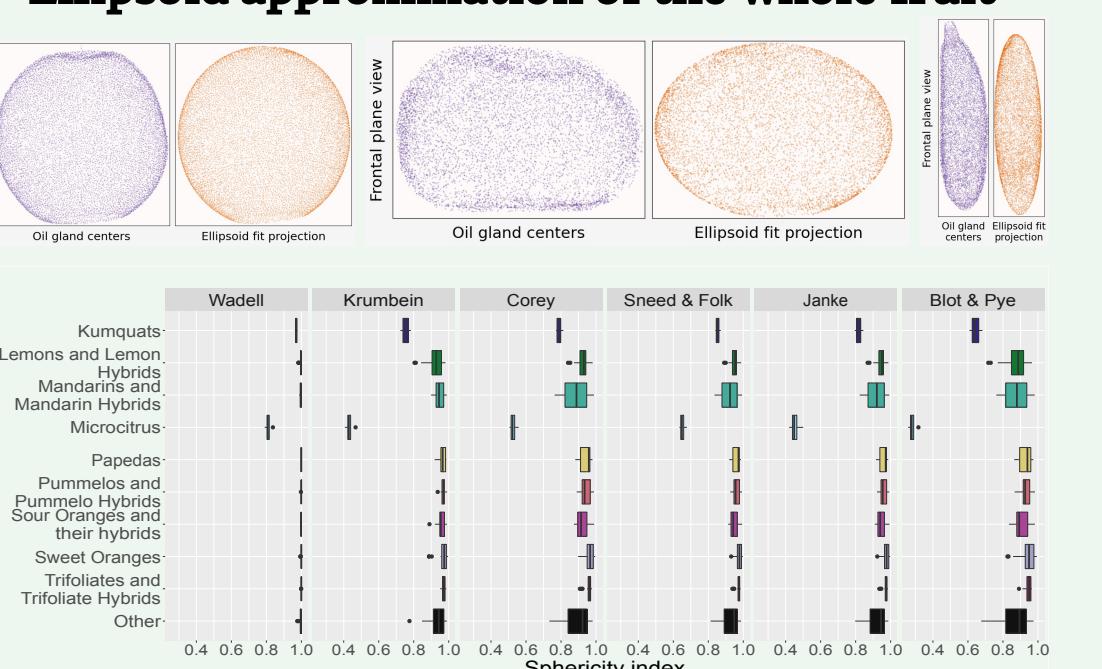
- 166 samples X-ray CT scanned (90 micron resolution)
- Extracted 5 tissues for all samples

Significant allometry across tissues' volumes



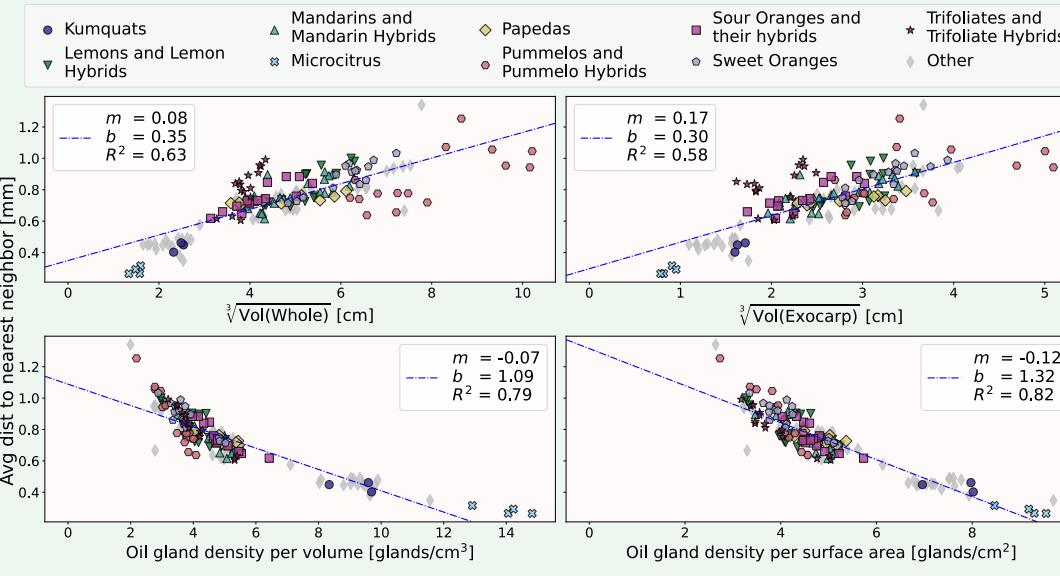
- Size relationships correspond to hybridization patterns
- E.g. Sour oranges are between mandarins and pummelos

Ellipsoid approximation of the whole fruit



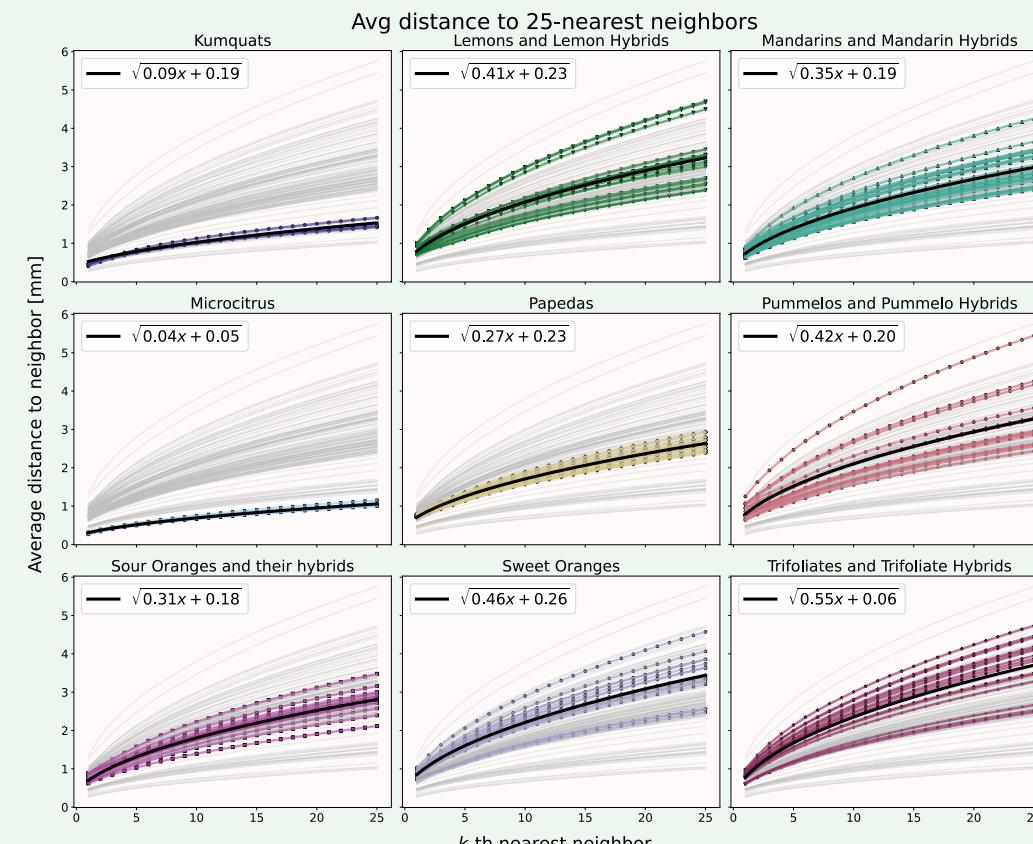
- Fruit sphericity with various indices: 0 (line/plane) → 1 (sphere)

Size and average distance between closest glands has high R² correlation coefficients



- Smaller fruits report higher density of oil glands
- Similar results when looking at the average distance between each oil gland and its 2nd, 3rd, ..., 25th nearest neighbors

The average distance to the oil gland nearest neighbors follows a square root relationship



- The average distance from each oil gland to its k-th nearest neighbor follows a square root formula

$$\text{Avg.dist}(k) = \sqrt{Mk + B}$$

- M is the distance increase rate; B an adjusting intercept
- This formula suggests that oil glands might be distributing themselves following **normal diffusion** mechanics
- Distance increase **rate** is related to oil gland **density**
- The **outliers** for citrus groups usually correspond to **hybrids**
- E.g. lemon outliers are Interdonatos, lemon x pummelo hybrids

Conclusions and takeaways

- X-ray CT technology offers a new powerful lens to study citrus shape at a much more granular level, even oil glands!
- Oil gland distribution can shed new light in **citrus development**
- Shape patterns can give us insight into **citrus hybridization**

Acknowledgements

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