

QUIZ 9 (GROUP WORK)

GOOD LUCK

- Show all your work and indicate your final answer clearly. You will be graded not merely on the final answer, but also on the work leading up to it.

+3 for trying to for not.

1. (3pts) Let $f(x) = \cot(x)$. Show that there is no value c in the interval $(-\frac{\pi}{2}, \frac{\pi}{2})$ such that $f'(c) = \frac{f(\frac{\pi}{2}) - f(-\frac{\pi}{2})}{\frac{\pi}{2} - (-\frac{\pi}{2})}$ and explain why this does not contradict the Mean Value Theorem.

- First note that $\cot(x)$ is not continuous on $(-\frac{\pi}{2}, \frac{\pi}{2})$, so MVT doesn't ~~even~~ apply.

- Try to find c anyway! Plug $f(x)$ into formula so

$$f'(x) = -\csc^2(x) = -\frac{1}{\sin^2(x)} = 0, \text{ so no } c \text{ exists}$$

2. (4pts) Sketch the graph of $f(x) = e^{\frac{1}{x^2}}$.

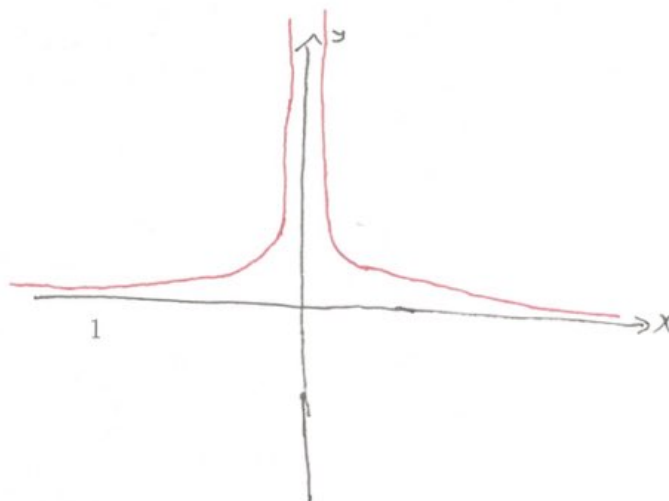
but this does not

contradict MVT because

$\cot(x)$ isn't continuous in interval.

- Note that as $x \rightarrow 0$, $e^{\frac{1}{x^2}} \rightarrow \infty$,
as $x \rightarrow \pm\infty$, $e^{\frac{1}{x^2}} \rightarrow 0$.

+4 for correct graph



3. (3pts) Compute $\lim_{x \rightarrow 1} \frac{x}{x-1} - \frac{1}{\ln(x)}$.

$$\bullet \quad \frac{x}{x-1} - \frac{1}{\ln(x)} = \frac{x \ln(x) - x + 1}{(x-1) \ln(x)} \quad +1$$

• Note that at $x=1$, we get form $\frac{0}{0}$, so we can use L'Hopital's rule.

$$\begin{aligned} \bullet \quad \lim_{x \rightarrow 1} \frac{x \ln(x) - x + 1}{(x-1) \ln(x)} &= \lim_{x \rightarrow 1} \frac{\frac{d}{dx}(x \ln(x) - x + 1)}{\frac{d}{dx}((x-1) \ln(x))} \\ &= \lim_{x \rightarrow 1} \frac{x \ln(x)}{\ln(x) + x - 1} \quad +1 \\ &\stackrel{\text{L'Hopital's rule}}{=} \lim_{x \rightarrow 1} \frac{1 + \ln(x)}{1 + \frac{1}{x}} \\ &= \frac{1}{2} \quad +1 \end{aligned}$$