

```
years =  
16  
months =  
5
```

the end of any of the commands that calculate the values).

## 1.10 PROBLEMS

The following problems can be solved by writing commands in the Command Window or by writing a program in a script file and then executing the file.

1. Calculate:

$$(a) \left(5 - \frac{19}{7} + 2.5^3\right)^2$$

$$(b) 7 \times 3.1 + \frac{\sqrt{120}}{5} - 15^{5/3}$$

2. Calculate:

$$(a) \sqrt[3]{8 + \frac{80}{2.6}} + e^{3.5}$$

$$(b) \left(\frac{1}{\sqrt{75}} + \frac{73}{3.1^3}\right)^{1/4} + 55 \times 0.41$$

$$(a) 0.4z^4 + 3.1z^2 - 162.5z$$

7. Define the variable  $t$  as  $t = 3.2$ ; then evaluate:

$$(a) \frac{1}{2}e^{2t} - 3.8 \ln t^3$$

$$(b) \frac{6t^2 + 6t - 2}{t^2 - 1}$$

8. Define the variables  $x$  and  $y$  as  $x = 6.5$  and  $y = 3.8$ ; then evaluate:

$$(a) (x^2 + y^2)^{2/3} + \frac{xy}{y-x}$$

$$(b) \frac{\sqrt{x+y}}{(x-y)^2} + 2x^2 - xy^2$$

9. Define the variables  $a$ ,  $b$ ,  $c$ , and  $d$  as:

$c = 4.6$ ,  $d = 1.7$ ,  $a = cd^2$ , and  $b = \frac{c+a}{c-d}$ ; then evaluate:

$$(a) e^{d-b} + \sqrt[3]{c+a} - (ca)^d$$

$$(b) \frac{d}{c} + \left(\frac{ct}{b}\right)^2 - c^d - \frac{a}{b}$$

10. Two trigonometric identities are given by:

$$(a) \cos^2 x - \sin^2 x = 1 - 2 \sin^2 x$$

degree.

- (b) Determine the area of the triangle  $ABC$  to the nearest tenth of a centimeter.

Law of cosines:  $c^2 = a^2 + b^2 - 2ab \cos \gamma$

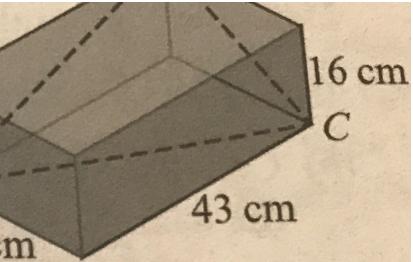
Heron's formula for triangular area:

$$A = \sqrt{p(p-a)(p-b)(p-c)}, \text{ where } p = (a+b+c)/2.$$

15. The arc length of a segment of a parabola  $ABC$  is given by:

$$L_{ABC} = \sqrt{a^2 + 4h^2} + \frac{a^2}{2h} \ln \left( \frac{2h}{a} + \sqrt{\left( \frac{2h}{a} \right)^2 + 1} \right)$$

Determine  $L_{ABC}$  if  $a=8$  in. and  $h=13$  in.

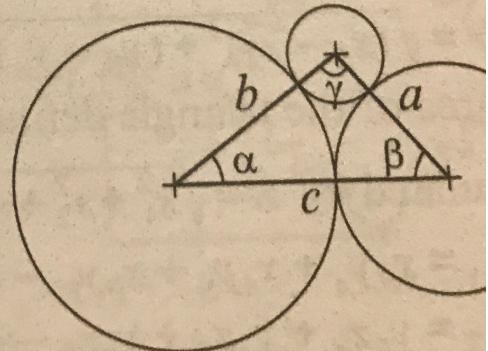
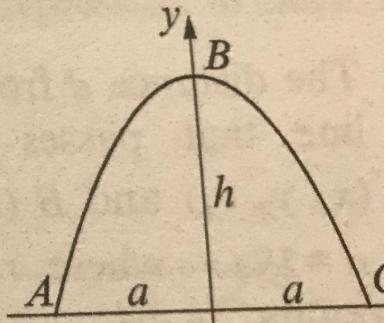


16. The three shown circles, with radius 15 in., 10.5 in., and 4.5 in., are tangent to each other.

- (a) Calculate the angle  $\gamma$  (in degrees) by using the law of cosines.

(Law of cosines:  $c^2 = a^2 + b^2 - 2ab \cos \gamma$ )

- (b) Calculate the angles  $\gamma$  and  $\alpha$  (in degrees) using the law of sines.



30

18. In the triangle shown  $a = 27$  in.,  $b = 43$  in., and  $c = 57$  in. Define  $a$ ,  $b$ , and  $c$  as variables, and then:

- (a) Calculate the angles  $\alpha$ ,  $\beta$ , and  $\gamma$  by substituting the variables in the law of cosines.

$$\text{Law of cosines: } c^2 = a^2 + b^2 - 2ab \cos \gamma$$

- (b) Verify the law of tangents by substituting the results into the right and left sides of:

$$\text{law of tangents: } \frac{b-c}{b+c} = \frac{\tan \left[ \frac{1}{2}(\beta - \gamma) \right]}{\tan \left[ \frac{1}{2}(\beta + \gamma) \right]}$$

19. For the triangle shown,  $\alpha = 72^\circ$ ,  $\beta = 43^\circ$ , and its perimeter is  $p = 114$  mm. Define  $\alpha$ ,  $\beta$ , and  $p$ , as variables, and then:

- (a) Calculate the triangle sides (Use the law of sines).

- (b) Calculate the radius  $r$  of the triangle.

