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Spacial convergence with varying (dx, dx/2, dx/4) , different domain size (smaller domains)
time convergence -
use just 10 cubes

All chapter 3 send by 5/24

For 50 cubes, clean up the figures that I have now by 5/10

SEND 3.4 BY 5/17

3.5 Validation (convergence) 5/12
3.6 results (what are we running? parameters) -> different shapes (with the same number of cubes) + varying NC
we need 100 cubes different shapes

3.7 Discussion (tie back to the motivation) -
-> by 5/19: with figures and discussion

edit these by 5/24

4.1 - 4.2 : needs edit by 5/31

by 6/2 (add text)

4.6 Discussion (conclusion)

check the notations!

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