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**Spatial convergence with varying (dx, dx/2, dx/4) , different domain size (smaller domains)  
time convergence -  
use just 10 cubes**

**All chapter 3 send by 5/24**

**For 50 cubes, clean up the figures that I have now**

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