

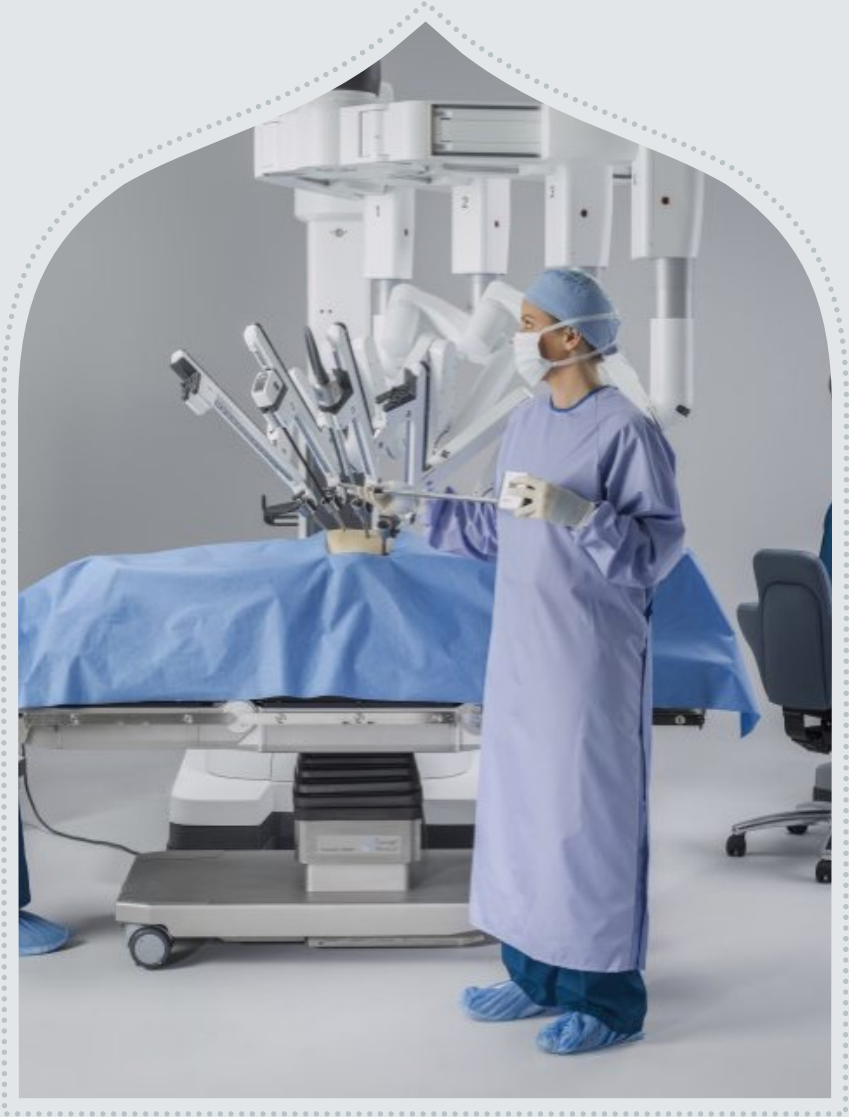


# Robot Autonomy

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# Introduction

- Robotics is the science of perceiving and manipulating the physical world through computer-controlled devices
- Robotics systems are situated in the physical world, perceive information on their environments through sensors, and manipulate through physical forces.
- While much of robotics is still in its infancy, the idea of “intelligent” manipulating devices has an enormous potential to change society.





From automation ...



... to autonomy

Waymo Self-Driving Car



Intuitive DaVinci  
Surgical Robot



Apollo Robot at MPI for Intelligent  
Systems



Boston Dynamics – Spot Mini



Astrobee - NASA



Zipline

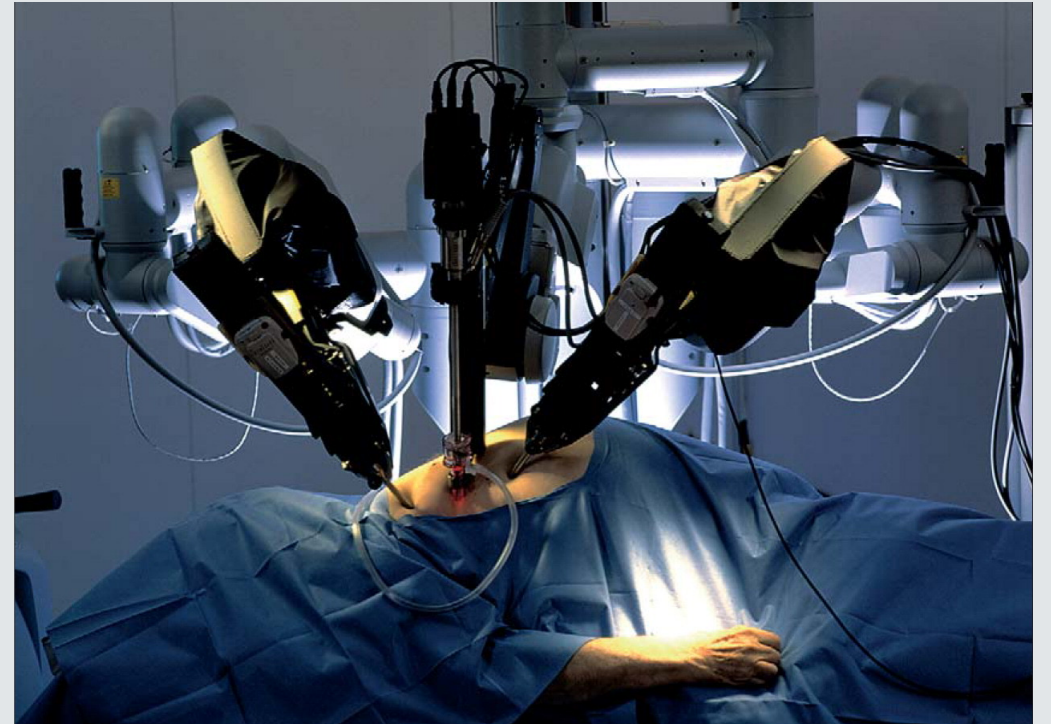


# Robot's Uncertainty

**Think of a medical robot.** The robot has to be able to accommodate the enormous uncertainty that exists in “the physical world”. Factors that contribute robot’s uncertainty:

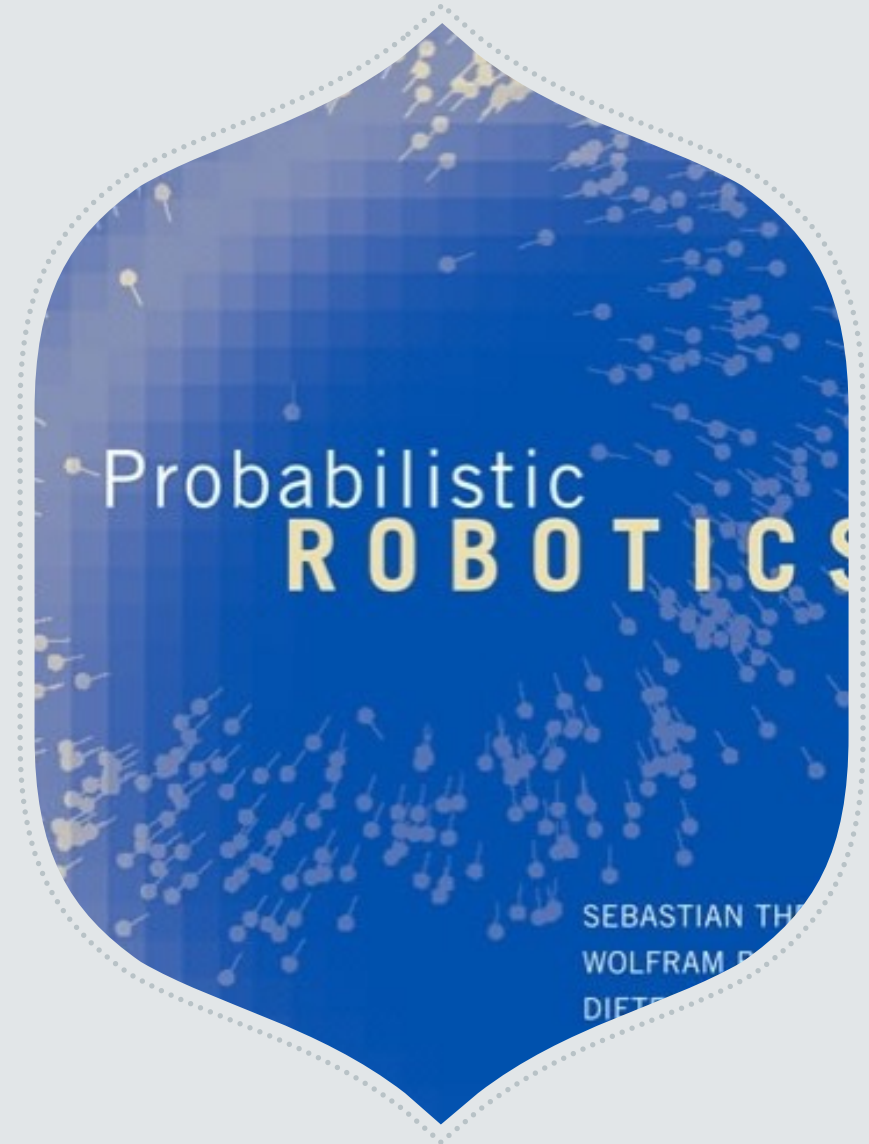
- ***Robot environment*** is inherently unpredictable especially in the proximity of people.
- ***Sensors*** are limited in what they can perceive, sensors are also subject to noise and can break.
- ***Robot actuation*** involves motors that are, at least to some extent, unpredictable.
- ***Robot software*** uses *internal models* of the world as abstractions of the real world.
- ***Robots are real-time systems*** with algorithmic approximations.

The level of uncertainty depends on the application domain. Managing uncertainty is possibly the most important step towards robust real-world robot systems (eq. environment, sensor, action, software, realtime, etc)



# Probabilistic Robotics

- ♦ The key idea in probabilistic robotics is to represent uncertainty explicitly using **the calculus of probability theory**.
- ♦ Probabilistic algorithms represent information by probability distributions over a whole space of guesses. Hence, they can represent ambiguity and degree of belief in a mathematically sound way.



# Implications

## Advantages:

- Probabilistic robotics seamlessly integrates models with sensor data, overcoming the limitations of both at the same time.
- Probabilistic approaches tend to be more robust in the face of sensor limitations and model limitations.
- Probabilistic algorithms have weaker requirements on the accuracy of the robot's models, thereby relieving the programmer from the insurmountable burden to come up with accurate models.

## Disadvantages:

- **Computation complexity:** Probabilistic algorithms are inherently less efficient than their non-probabilistic counterparts.
- **Need to approximate:** In some cases approximations are too crude to be of use, and more complicated representations must be employed.



# Goals of This Course

To learn the “Fundamental, Conceptual and Practical” aspects of Robot Autonomy covering basic non-probabilistic ideas:

- Motion control and planning
- Robotic perception
- Localization and SLAM
- State machines and system architecture

Specifically, you will:

1. Gain a fundamental knowledge of the “autonomy stack”
2. Be able to apply such knowledge in applications / research by using ROS
3. Devise novel methods and algorithms for robot autonomy

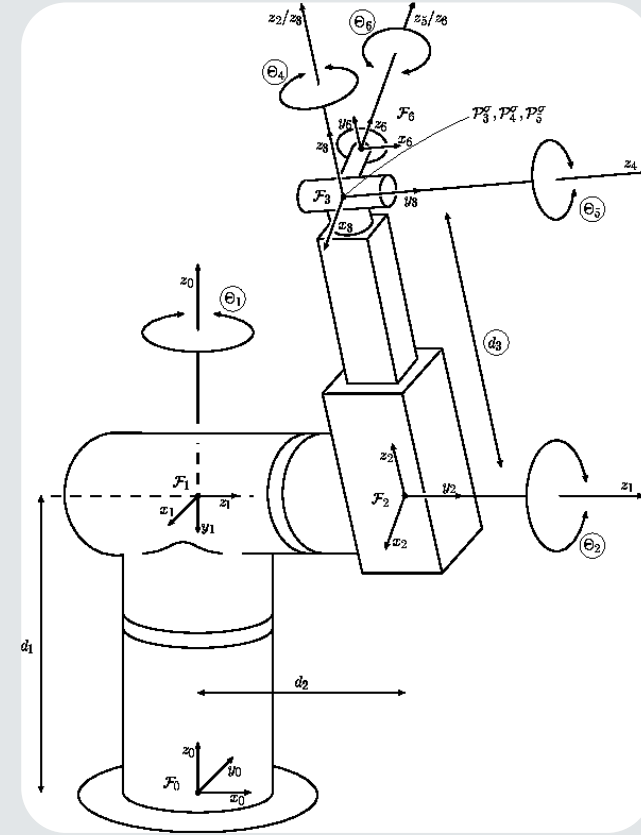




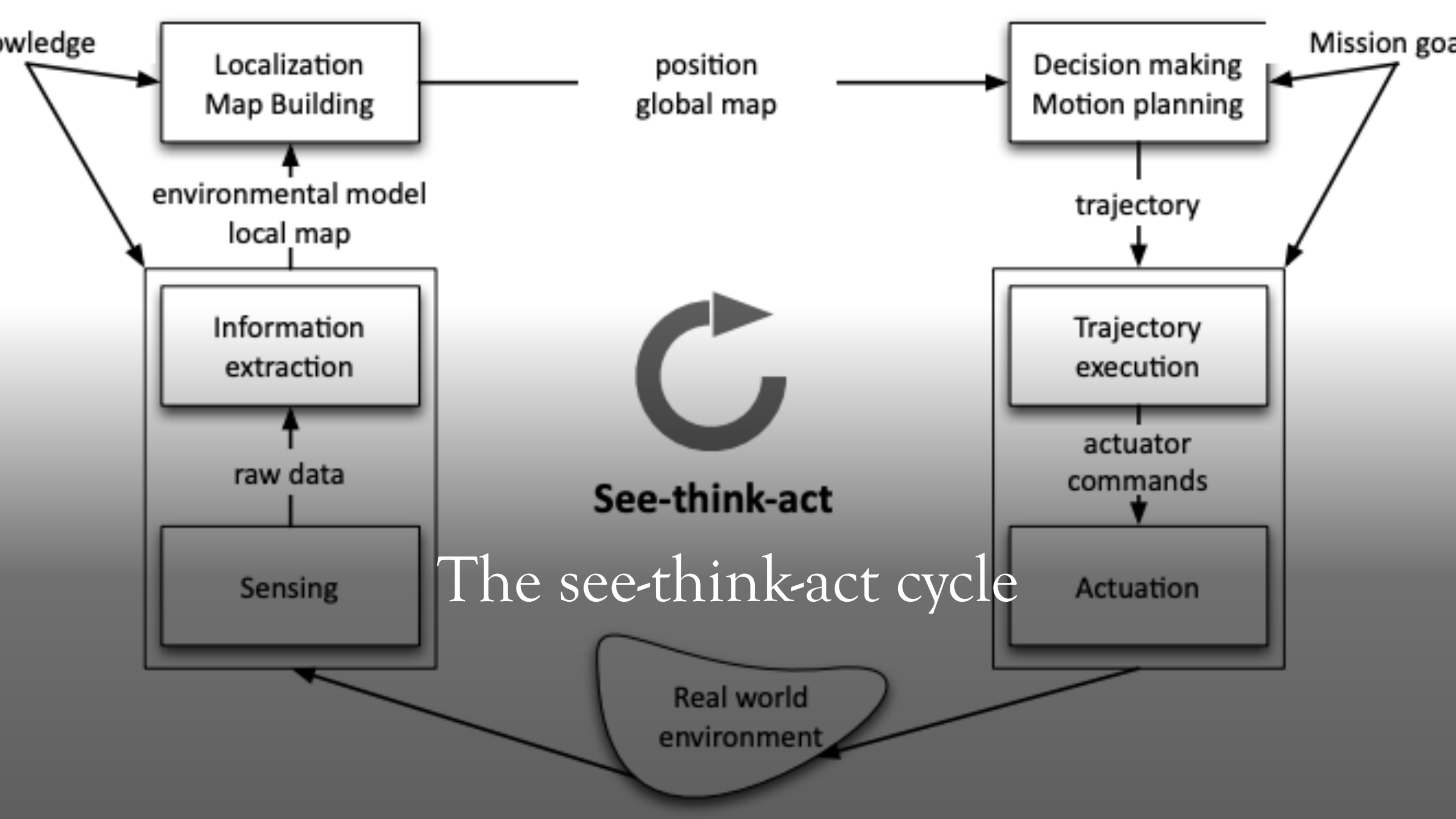
# Principles of Robot Autonomy I

## W1: Introduction to Robot Kinematics

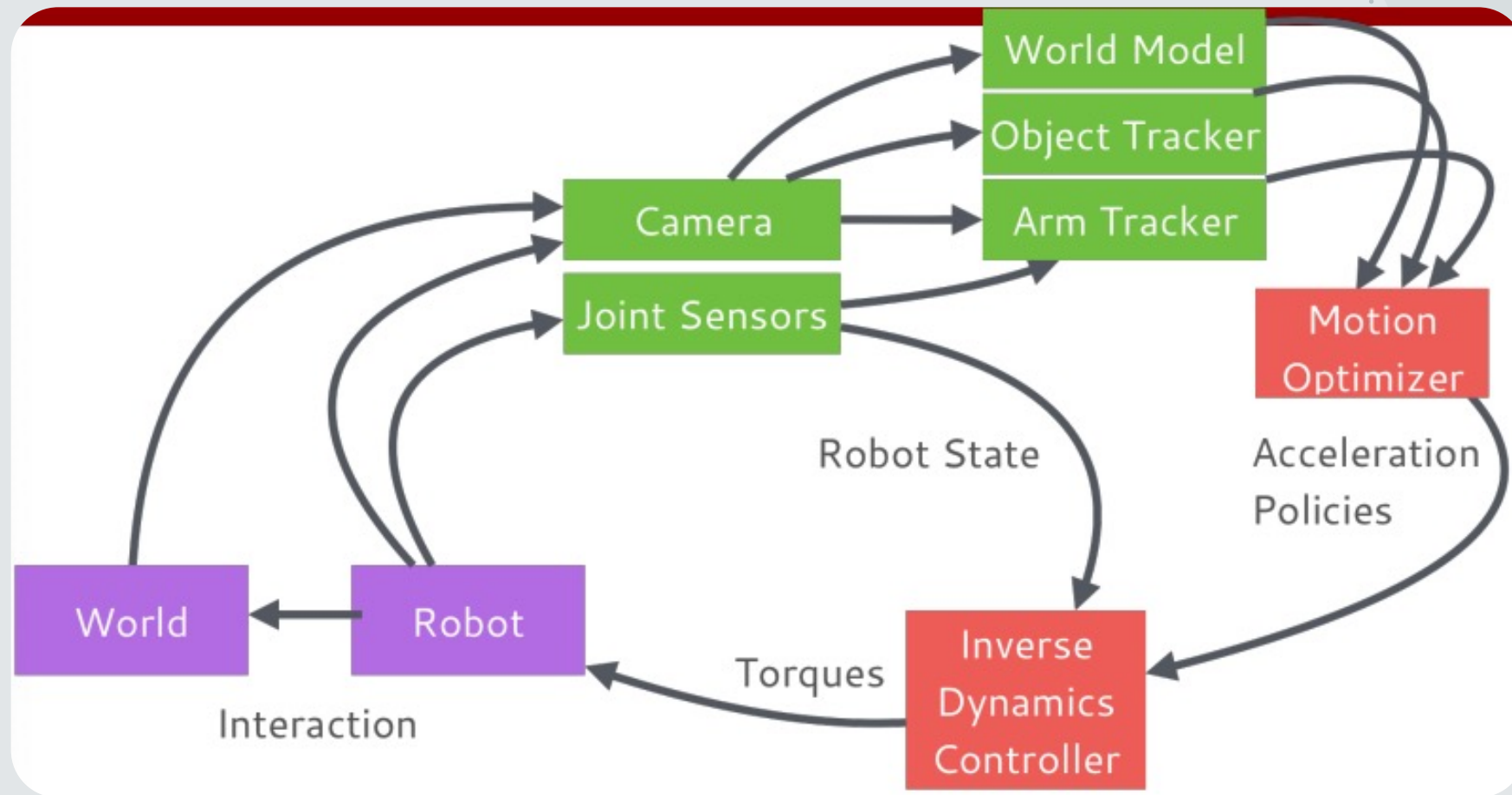
- Mobile Kinematics Robot
- Generalized Coordinates
- Kinematic Constraint
- Holonomic and Nonholonomic Constraints
- Kinematic Model
- Kinematic Model of Wheeled Robots
- Dynamic Models



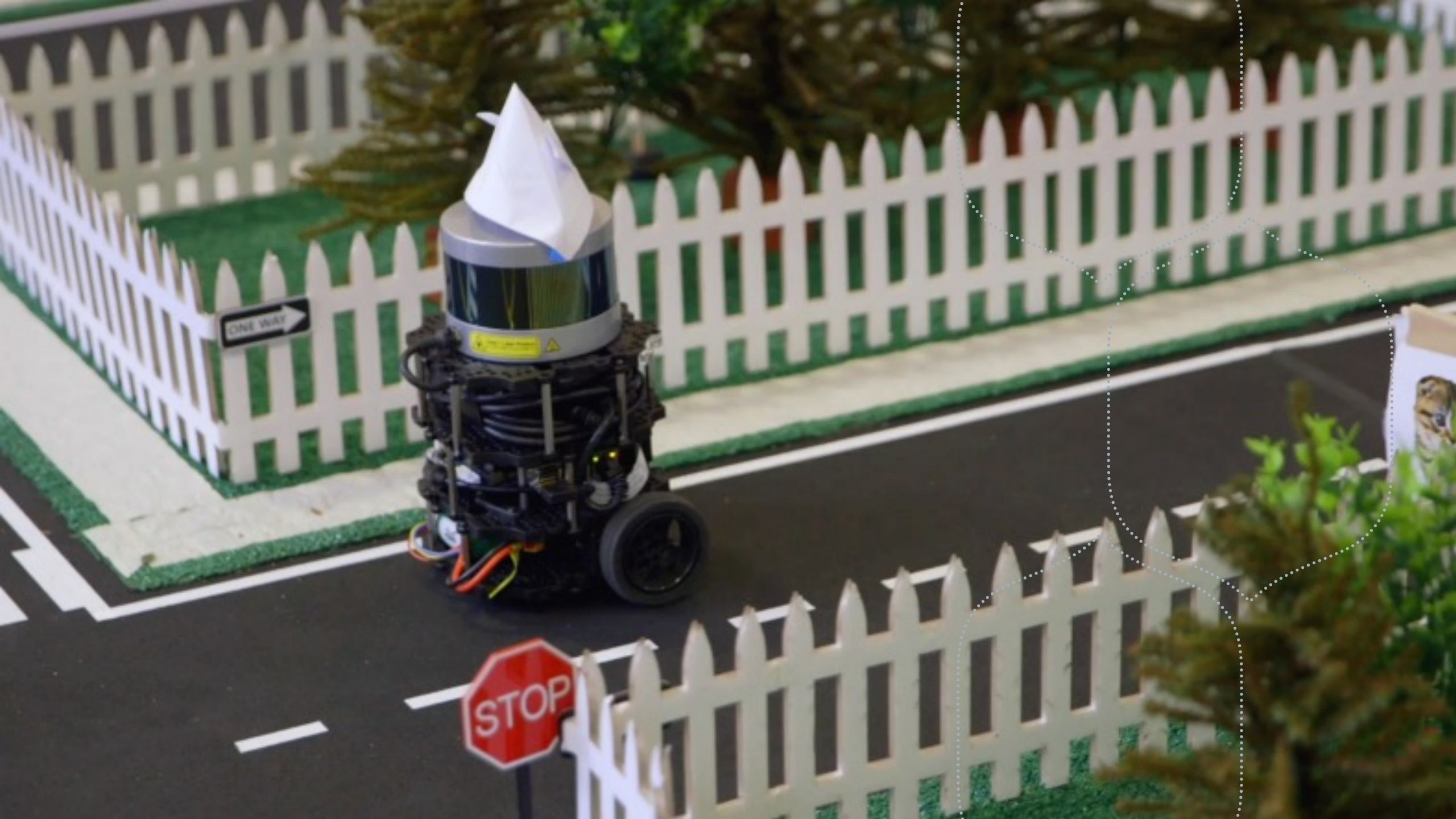
Stanford Arm Robot



# Real-time Perception meets Reactive Motion Generation





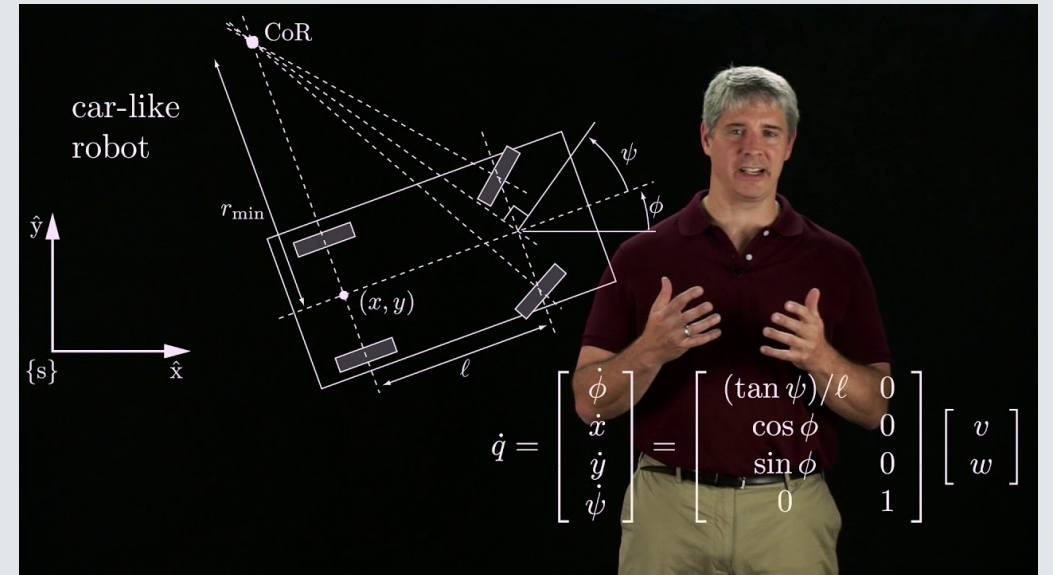






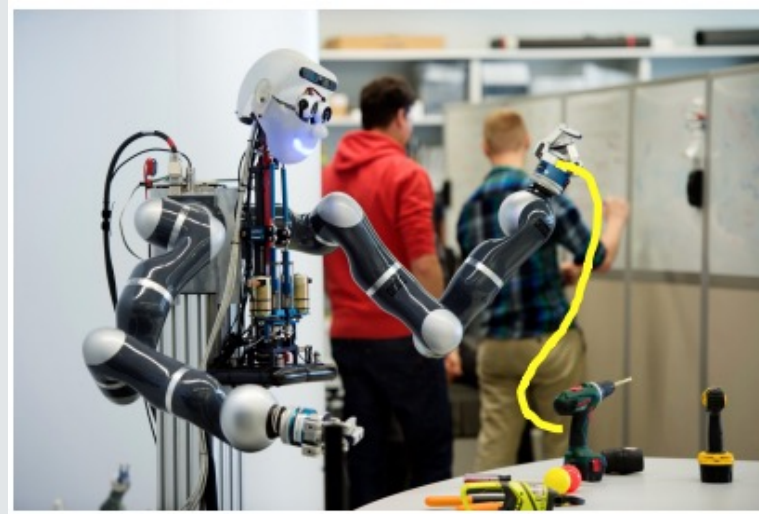
# Mobile Robot Kinematics

- Aim
  - Understand motion constraints
  - Learn about basic motion models for wheeled vehicles
  - Gain insights for motion control

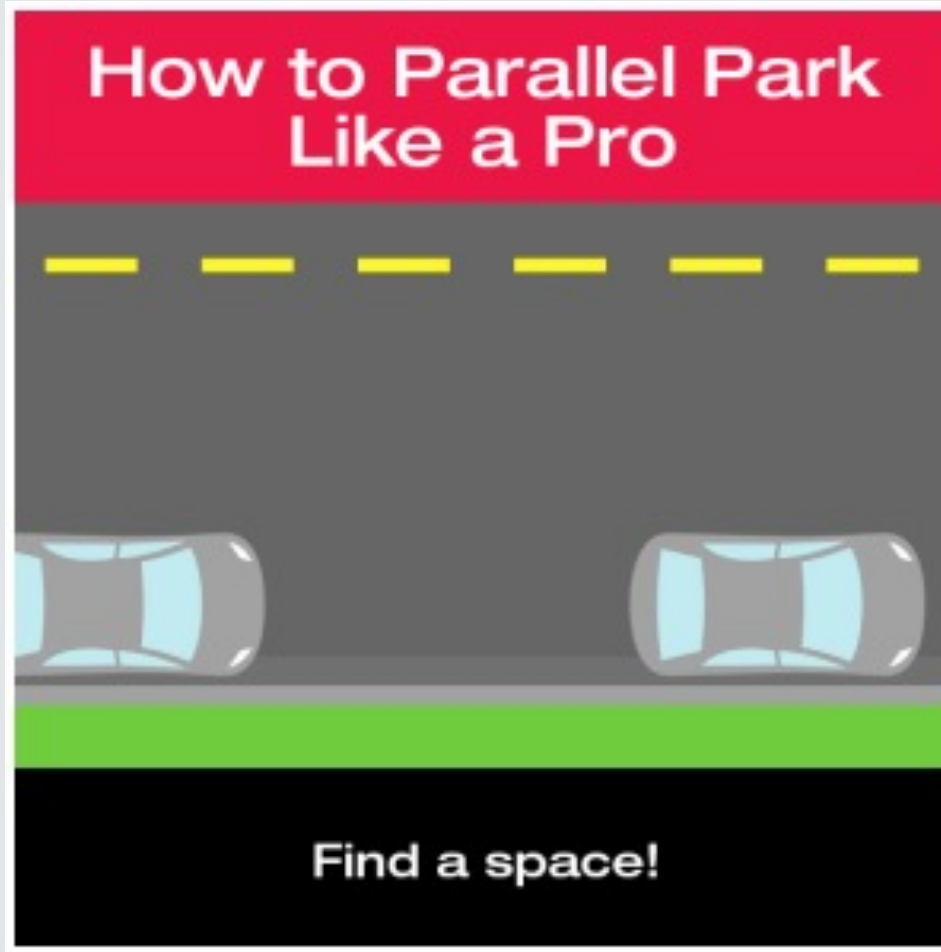




# Motion Planning and Control



# Constraint in Motion Planning and Control



<https://tenor.com/view/parallel-park-parking-proper-gif-13789379>



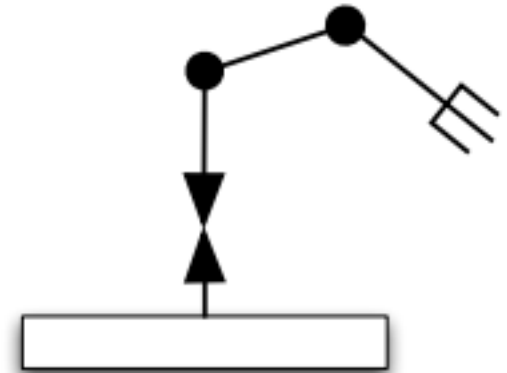
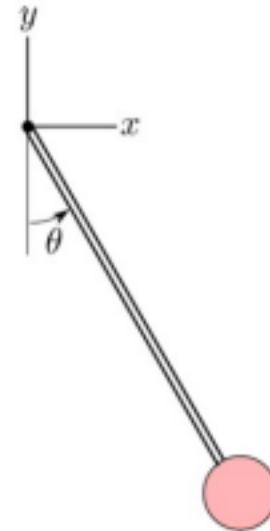
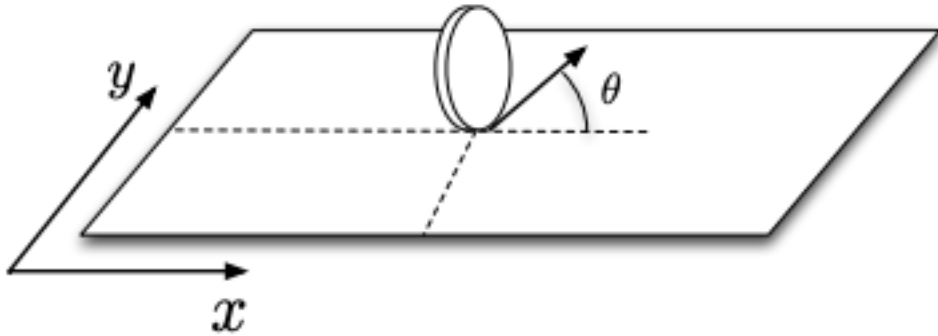
Futurama - Put Your Head on My Shoulders [S02E10]

<https://tenor.com/view/parallel-park-parking-proper-gif-13789379>

Futurama - Put Your Head on My Shoulders [S02E10] : <https://getyarn.io/tv-series/6e5aa01e-9637-11e7-a34c-42010af00cf6>

# Generalized Coordinates

- Let  $\xi = [\xi_1, \dots, \xi_n]^T$  denote the configuration of a robot (e.g.,  $\xi = [x, y, \theta]^T$  for a wheeled mobile robot)



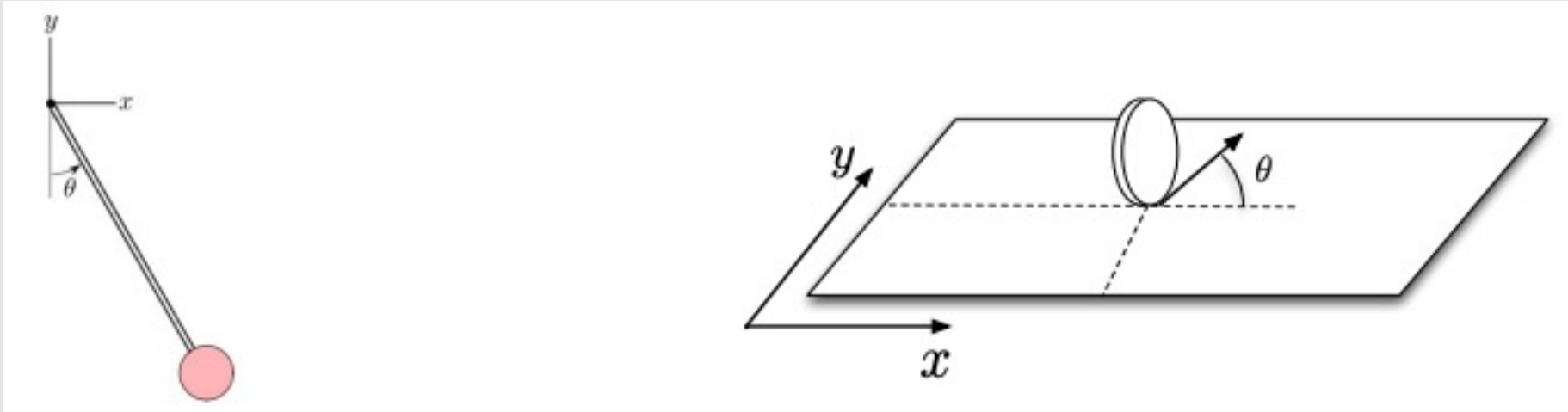


# Kinematics Constraints

$$a_i(\xi, \dot{\xi}) = 0, \quad i = 1, \dots, k < n$$

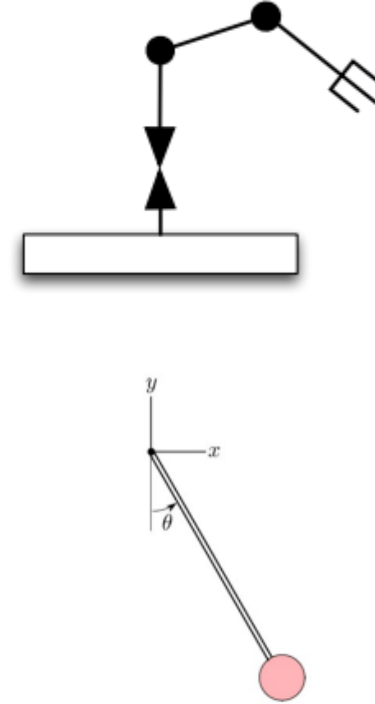
- Constrain the instantaneous admissible motion of the mechanical system
- Generally expressed in Pfaffian form, i.e., linear in the generalized velocities

$$a_i^T(\xi) \dot{\xi} = 0, \quad i = 1, \dots, k < n$$



# Holonomic Constraints

- $h_i(\xi) = 0$ , for  $i = 1, \dots, k < n$
- Reduce space of accessible configurations to an  $n - k$  dimensional subset
- If all constraints are holonomic, the mechanical system is called holonomic
- Generally, the result of mechanical interconnections



# Examples of Holonomic Constraints

Xiang, Qin, Mo et al., “SAPIEN: A SimulAted Part-based Interactive ENvironment”, CVPR 2020





# Kinematics Constraints

$$a_i(\xi, \dot{\xi}) = 0, \quad i = 1, \dots, k < n$$

- Constrain the instantaneous admissible motion of the mechanical system
- Generally expressed in Pfaffian form, i.e., linear in the generalized velocities

$$a_i^T(\xi) \dot{\xi} = 0, \quad i = 1, \dots, k < n$$

- $k$  holonomic constraints imply the existence of an equal number of kinematic constraints

$$\frac{d h_i(\xi)}{dt} = \frac{\partial h_i(\xi)}{\partial \xi} \dot{\xi} = 0, \quad i = 1, \dots, k < n$$

- However, the converse is not true in general...

# Nonholonomic Constraints

- If a kinematic constraint is not integrable in the form  $h_i(\xi) = 0$ , then it is said *nonholonomic*  $\rightarrow$  nonholonomic mechanical system
- Nonholonomic constraints reduce mobility in a completely different way. Consider a single Pfaffian constraint

$$a^T(\xi)\dot{\xi} = 0$$

- Holonomic
  - Can be integrated to  $h(\xi) = 0$
  - Loss of accessibility, motion constrained to a level surface of dimension  $n - 1$
- Nonholonomic
  - Velocities constrained to belong to a subspace of dimension  $n - 1$ , the null space of  $a^T(\xi)$
  - No loss of accessibility

# Example of Nonholonomic Constraints

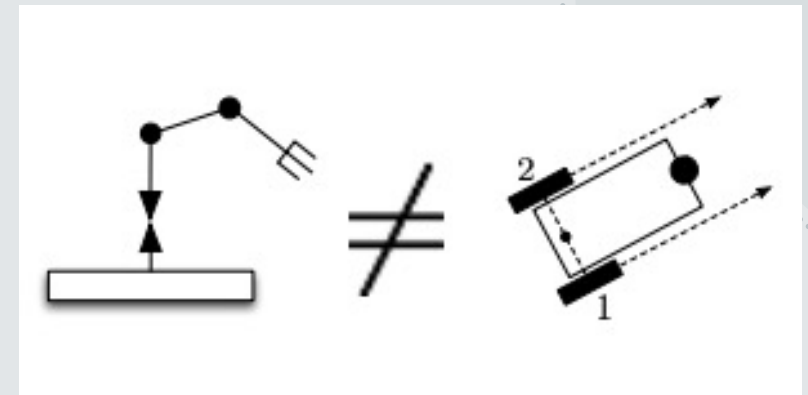
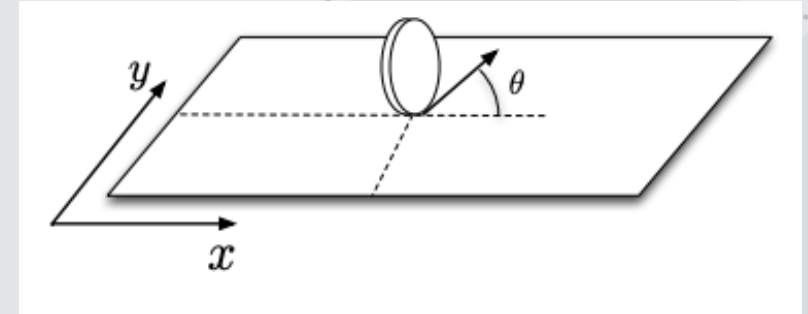
- **System:** disk that rolls without slipping

$$\xi = [x, y, \theta]^T$$

- No side slip constraints

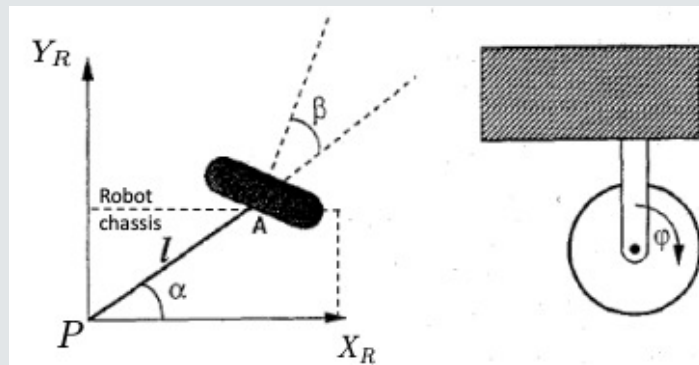
$$[\dot{x}, \dot{y}] \cdot \begin{bmatrix} \sin \theta \\ -\cos \theta \end{bmatrix} = \dot{x} \sin \theta - \dot{y} \cos \theta = [\sin \theta, -\cos \theta, 0] \dot{\xi} = 0$$

- **Facts:**
  - No loss of accessibility
  - Wheeled vehicles are generally nonholonomic

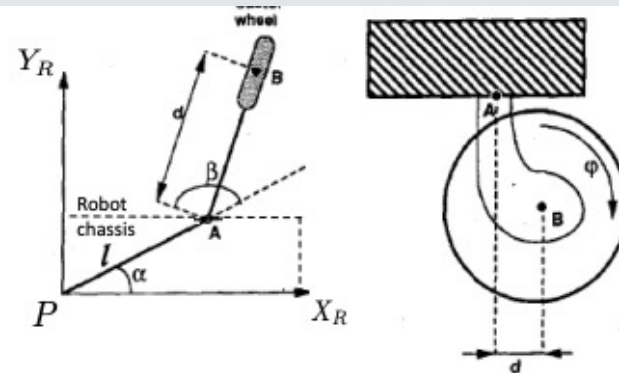


# Types of Wheels

- Standard wheels (four types)



Standard wheel -- fixed or steerable



Standard, off-centered wheel (caster)  
-- passive or active

- Special wheels:** achieve omnidirectional motion (e.g., Swedish or spherical wheels)



# Kinematic models

- Assume the motion of a system is subject to  $k$  Pfaffian constraints

$$\begin{bmatrix} a_1^T(\xi) \\ \vdots \\ a_k^T(\xi) \end{bmatrix} \dot{\xi} := A^T(\xi) \dot{\xi} = 0$$

- Then, the admissible velocities at each configuration  $\xi$  belong to the  $(n - k)$ -dimensional null space of matrix  $A^T(\xi)$
- Denoting by  $\{g_1(\xi), \dots, g_{n-k}(\xi)\}$  a basis of the null space of  $A^T(\xi)$ , admissible trajectories can be characterized as solutions to

$$\dot{\xi} = \sum_{j=1}^{n-k} g_j(\xi) u_j = G(\xi) u$$

Input vector

# Example : Unicycle

- Consider pure rolling constraint for the wheel:

$$\dot{x} \sin \theta - \dot{y} \cos \theta = [\sin \theta, -\cos \theta, 0] \dot{\xi} = a^T(\xi) \dot{\xi} = 0$$

- Consider the matrix

$$G(\xi) = [g_1(\xi), g_2(\xi)] = \begin{bmatrix} \cos \theta & 0 \\ \sin \theta & 0 \\ 0 & 1 \end{bmatrix}$$

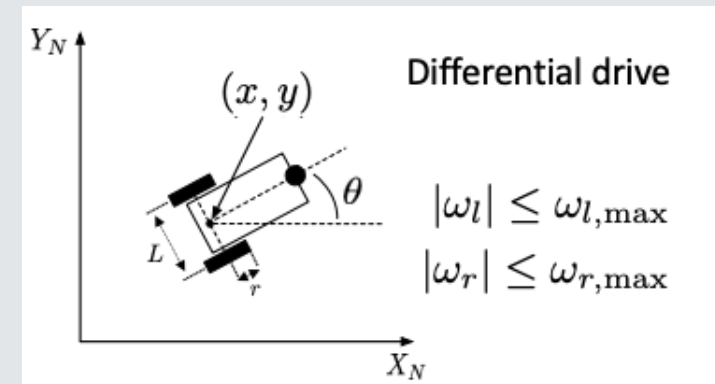
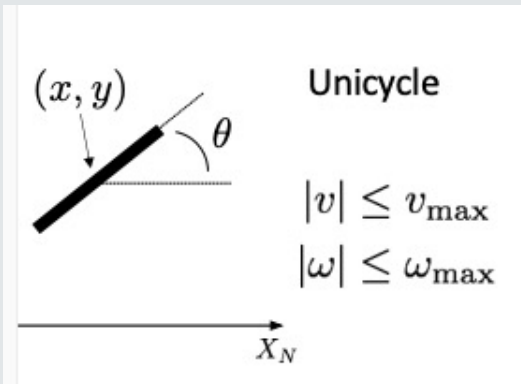
where  $[g_1(\xi), g_2(\xi)]$  is a basis of the null space of  $a^T(\xi)$

- All admissible velocities are therefore obtained as linear combination of  $g_1(\xi)$ , and  $g_2(\xi)$

# Unicycle and differential drive models

$$\begin{pmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{pmatrix} = \begin{pmatrix} \cos \theta \\ \sin \theta \\ 0 \end{pmatrix} v + \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \omega$$

$$\begin{pmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{pmatrix} = \begin{pmatrix} \frac{r}{2}(\omega_l + \omega_r) \cos \theta \\ \frac{r}{2}(\omega_l + \omega_r) \sin \theta \\ \frac{r}{L}(\omega_r - \omega_l) \end{pmatrix}$$



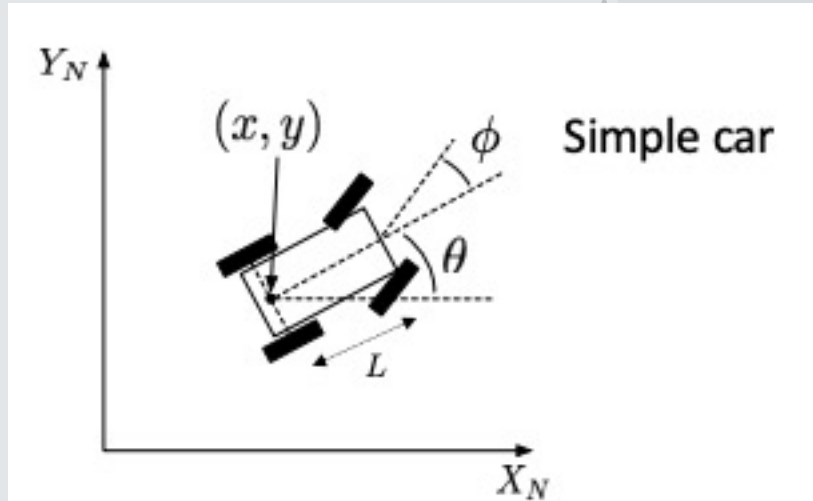
The kinematic model of the unicycle also applies to the differential drive vehicle, via the one-to-one input mappings:

$$v = \frac{r}{2} (\omega_r + \omega_l) \quad \omega = \frac{r}{L} (\omega_r - \omega_l)$$



# Simplified Car Model

$$\begin{pmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{pmatrix} = \begin{pmatrix} v \cos \theta \\ v \sin \theta \\ \frac{v}{L} \tan \phi \end{pmatrix}$$



$$|v| \leq v_{\max}, \quad |\phi| \leq \phi_{\max} < \frac{\pi}{2}$$

$$v \in \{-v_{\max}, v_{\max}\}, \quad |\phi| \leq \phi_{\max} < \frac{\pi}{2}$$

$$v = v_{\max}, \quad |\phi| \leq \phi_{\max} < \frac{\pi}{2}$$

- Simple car model
- Reeds&Shepp's car
- Dubins' car

References: (1) J.-P. Laumond. Robot Motion Planning and Control. 1998. (2) S. LaValle. Planning algorithms, 2006.

# From kinematic to dynamic models

- A kinematic state space model should be interpreted only as a subsystem of a more general dynamical model
- Improvements to the previous kinematic models can be made by placing **integrators** in front of action variables
- For example, for the unicycle model, one can set the speed as the integration of an action  $a$  representing acceleration, that is
$$\dot{x} = v \cos \theta, \quad \dot{y} = v \sin \theta, \quad \dot{\theta} = \omega, \quad \dot{v} = a$$





## Aim

Understand motion constraints

Learn about basic motion models for wheeled vehicles

Gain insights for motion control



## Readings

Please read the mandatory chapter and explore more in other books

# Your Home Work