

Flares in Open Clusters with K2.

II. M35, Hyades, and Ruprecht 147

Ekaterina Ilin¹, Sarah J. Schmidt¹, Katja Poppenhäger¹, James R. A. Davenport² and Klaus G. Strassmeier¹

¹ Leibniz Institut für Astrophysik Potsdam

e-mail: eilin@aip.de

² University of Washington e-mail: jrad@uw.edu

Received XXX; accepted XXX

ABSTRACT

Context. Flares can help us trace magnetic activity because are bright and high-contrast on low mass stars.

Aims. This study aims to quantify flaring activity on these stars as a function of mass and age.

Methods. We automatically detected flares in K2 time-domain photometry, using the open-source software K2SC to remove instrumental and astrophysical variability from K2 light curves. We used injection and recovery of synthetic flares to assess detection thresholds, time sampling and de-trending effects on the inferred flare energies. With additional data from the full K2 archive we added stars with a larger variety of ages and spectral types to the analysis of the previous study (Ilin et al. 2019). We compared previous results from the Pleiades and Praesepe to the flare frequency distributions (FFDs) in M35 and the Hyades, respectively. Ruprecht 147 filled in the age gap at 2.5 Gyr between the aforementioned young clusters and the solar age cluster M67.

Results. We find that the flare production mechanism is similar for the entire parameter space, following a power law relation with exponent $\alpha \approx 2$, but the flaring frequencies depend on both mass, and age. We discuss X and Y.

Key words. Methods: data analysis, Stars: activity, Stars: flare, Stars: low-mass

Use \titlerunning to supply a shorter title and/or \authorrunning to supply a shorter list of authors.

1. Introduction

Flares are explosions on stellar surfaces with a complex spatio-temporal and energetic phenomenology. We know that flares are magnetic re-connection events that lead to a change in field line topology and subsequent energy release (Priest & Forbes 2002). We can observe flares in nearly all electromagnetic bands, from radio to X-rays, and on all stars that possess a convection zone. From late F type stars to ultracool dwarfs (Gizis 2013). But even with continuous monitoring at high temporal resolution, the random occurrence of solar flares makes them costly observing targets, especially in coordinated multi-band observations. In integrated light, most solar flares have a far too low contrast and intensity to be observable. Stellar flares on cool stars have two advantages in this respect. They are often bright, enhancing stellar flux by up to several orders of magnitude, and they typically exhibit blackbody emission at temperatures significantly higher than their stars' photospheres. With the evidence that the physical processes that cause flares on the Sun and other stars are the same (Karoff 2016), solar and stellar flares can inform each other (Shibayama et al. 2013). Inconsistencies in extrapolations from solar to stellar conditions (Aarnio et al. 2011; Aarnio et al. 2012; Drake et al. 2012; Alvarado-Gómez et al. 2018). Large surveys like Kepler and TESS enable statistical flare studies of stars that were not pre-selected for their activity (Walkowicz et al. 2011). Statistical studies of stellar flaring activity can help us understand the underlying physical processes CITE stellar surface magnetic fields, starspots (Davenport 2015; Howard

et al. 2019b), how flares relate to stellar angular momentum evolution (Mondrik et al. 2019; Howard et al. 2019b), how they affect the atmospheres of exoplanets (Lecavelier des Etangs et al. 2012; Loyd et al. 2018; Tilley et al. 2019; Howard et al. 2019a), and inform galactic archaeology (Howard et al. 2019a).

Basic parameters that affect flaring behaviour on stars are their masses, and ages. Ages can be controlled for in coeval groups of stars, and flaring-age studies in binaries showed consistency in activity for both components in the majority of targets (Lurie et al. 2015; Clarke et al. 2018). Open clusters present other coeval groups of stars with well-determined ages. Ilin et al. (2019) (hereafter PaperI) investigated the flaring activity of late-K to mid-M dwarfs in three open clusters (OCs), the Pleiades, Praesepe, and M67, using K2 time domain photometry. They analysed the flare frequency distributions (FFDs), with respect to different masses and cluster ages. For the cluster members, the light curves revealed that their flaring activity declines both with age and mass. The decline is faster for higher mass stars. Recently, Davenport et al. (2019) put forward an empirical parametrization of this flaring-mass-age relation based on FFDs. The present study aims to extend the results in PaperI to the age of Ruprecht 147 (2.5 Gyr), and both higher and lower masses than in the previous study. We also test the previous results from the Pleiades on M35, and the results from Praesepe on the Hyades, as both OC pairs have approximately the same ages. Because the Kepler satellite retired in fall 2018, we can now use the complete K2 data set, and supplement all three OCs in PaperI with additional light curves. Additionally, we use high quality K2 light curves available for M67 (Nardiello et al. 2016) and M35 (Soares-Furtado et al. 2017). We discuss our results with

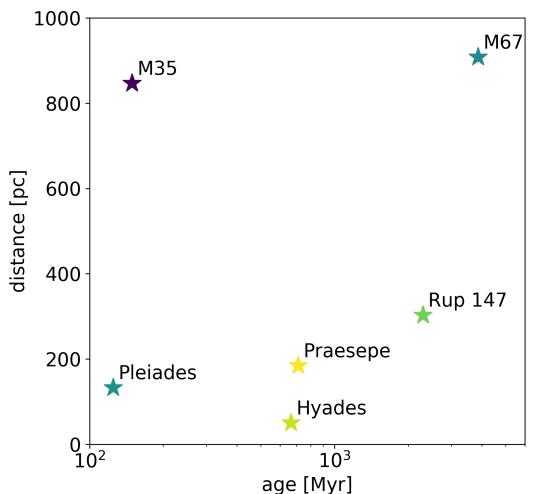


Fig. 1. The values for age, metallicity, and distance are approximate values from a compilation of existing literature, see Appendix B.1.

respect to potential breaks in the power law distribution at high energies. Finally, we use the results to test the parametrizability in Davenport et al. (2019).

2. Data

Our main data are K2 target pixel files that were provided by the Kepler archives hosted at MAST, and light curves derived from them (Aigrain et al. 2016; Soares-Furtado et al. 2017; Vinícius et al. 2018). To assign T_{eff} to the targeted stars we used multi-band photometry obtained from Tycho, UCAC4, 2MASS, Pan-STARRS, and Gaia catalogs. To assign ages to the targeted stars OC membership information was compiled from the literature. An overview over the cluster sample is presented in Table ?? and illustrated in Figure 1.

2.1. K2 light curves

The Kepler (Koch et al. 2010) spacecraft finished its follow-on mission K2 (Howell et al. 2014) in September 2018, after having completed nearly 20 80-day observing campaigns. Even though Kepler and K2 data are used in more than 2 400 publications to date, the public archive can still be considered understudied (Barentsen et al. 2018). In this spirit we took up the analysis of about 4 000 Kepler target pixel files that each contain up to 80 days of 30 min cadence observations in white light ($4, 200 - 9, 000 \text{ \AA}$). We also used light curves extracted from the K2 C0 super stamp. A super stamp is an aggregated set of typical Kepler postage stamps placed over a densely populated field, that also covers M35 (Soares-Furtado et al. 2017).

As K2 was conducted on the two-wheeled Kepler satellite, it was subjected to substantial drift motion (spacecraft roll, Van Cleve et al. 2016) and had an overall reduced pointing accuracy. To mitigate these effects, various solutions were developed (Vanderburg & Johnson 2014; Aigrain et al. 2016; ?; Luger et al. 2018)

2.2. Membership matching

We obtained membership information from multiple catalogs for each cluster. We cross-matched these catalogs on RA and

declination within 3 arcsec. The resulting target lists were used to search the K2 archive, or were matched to the catalogs of extracted light curves from crowded fields in the case of M35 (Soares-Furtado et al. 2017) and M67 (Nardiello et al. 2016).

One part of the membership catalogs provided membership probabilities (Douglas et al. 2014; Bouy et al. 2015; Cantat-Gaudin et al. 2018; Olivares et al. 2018; Reino et al. 2018; Gao 2018; Olivares et al. 2019). For the other part no probability was provided (Rebull et al. 2016a; Douglas et al. 2017; Gaia Collaboration et al. 2018a), or qualitative classifiers were given (Curtis et al. 2013; Gonzalez 2016; Rebull et al. 2017). In the latter cases we assigned approximate probabilities anchored to the set threshold for inclusion into our final sample. Absence in a catalog did not decrease the likelihood of membership, as each catalog shows different selection biases which we did not address in this study. We set the threshold mean membership probability p for a target in our sample to 0.8.

2.3. Open Clusters

We studied flaring activity in the low mass stars in six open clusters spanning from ZAMS to solar age. Table 1 provides an overview over the final sample. The literature overview of age, distance, and metallicity determinations is given in Table ?? in the Appendix. Membership probability histograms of the final sample are displayed in Figure ??.

2.3.1. Pleiades

The Pleiades, a nearby ZAMS cluster, were observed in Campaign 4, and were treated in PaperI. We include the cluster in this work for completeness and to illustrate improvements to (PaperI). We revisited the memberships from Rebull et al. (2016a), which were your in the previous work, and merged them with lists of members determined by Olivares et al. (2018); Gaia Collaboration et al. (2018a); and Cantat-Gaudin et al. (2018).

2.3.2. M35

M35 is a ZAMS cluster 900 pc away, observed during Campaign 0 in K2. We merged membership lists from Cantat-Gaudin et al. (2018); Gaia Collaboration et al. (2018a); and Bouy et al. (2015). There are only five K2 light curves, but we identified multiple additional members with publicly available¹ light curves obtained from Soares-Furtado et al. (2017). They used an image subtraction technique in the campaign's super stamps, a self flat-fielding de-trending inspired by K2SFF (Vanderburg & Johnson 2014), and a trend-filtering algorithm developed by Kovács et al. (2005). We preferred PSF photometry in cases where both aperture K2 and PSF LCs were available. We took the raw extracted PSF light curves and de-trended them using K2SC.

2.3.3. Hyades

The Hyades are a 0.6 Gyr old OC observed during Campaigns 4 and 13 with K2. It is about as old as Praesepe. We merged membership tables obtained from Douglas et al. (2014); Reino et al. (2018); and Gaia Collaboration et al. (2018a).

¹ <https://k2.hatsurveys.org/archive/>

Table 1. Open clusters.

cluster	<i>n</i>	LCs	SLCs	LLCs	PSF LCs	age[Myr]	distance[pc]	[Fe/H]
Pleiades	2033	944	33	911	0	125		
M35	1614	5	0	5	158			
Hyades	655	301	42	259	0			
Praesepe	1281	2500	68	2432	0			
Rup 147	213	97	25	72	0			
M67	1344	1141	118	1023	1019			

Notes. *n* is the approximate number of members with $p > 0.8$. LCs, SLCs, LLCs, and PSF LCs denote the number of available light curves, short cadence light curves, long cadence light curves, and PSF de-detrended light curves, respectively. The values for age, [Fe/H], and distance are approximate values from a comparison of existing literature, detailed in Appendix B.1.

149 2.3.4. Praesepe

150 Praesepe appeared in Campaign 5, and was previously treated
151 in PaperI. It was then observed again during Campaign 13. We
152 revisited the memberships obtained by Douglas et al. (2014), and
153 matched them to the members identified in Douglas et al. (2017)
154 Rebull et al. (2017); Cantat-Gaudin et al. (2018); and Gaia Col-
155 laboration et al. (2018a).

191 used the average extinction value of the respective cluster. We
192 accounted for extinction in Gaia BP and RP using the reddening
193 $E(B_P - R_P)$ derived from Gaia photometry and parallax from
194 Gaia DR2 (Andrae et al. 2018). We dropped targets that were
195 too bright (Kepler magnitude $K_p \leq 9$).
196

197 2.3.5. Ruprecht 147

198 Ruprecht 147 is a 2.5 Gyr old OC observed during Campaign 5
199 with K2. We used the mean membership probabilities obtained
200 from a number of studies (Curtis et al. 2013; Cantat-Gaudin et al.
201 2018; Olivares et al. 2019) combined with the members found
202 by Gaia Collaboration et al. (2018a) to identify the most likely
203 members.

204 2.4.2. Effective temperatures

205 2.3.6. M67

206 M67 is a solar-age, solar metallicity OC about 900 pc away.
207 Multiple members were observed during Campaign 5, and 208 visited in Campaigns 16 and 18. We did not find any flares 209 in Campaign 5 (PaperI) observing the members identified 210 by Gonzalez (2016). The recent campaigns brought both ad-211 tional observations, and entirely new targets to the sample. We 212 merged the members from Gonzalez (2016) with a recent study 213 based of Gaia DR2 data (Gao 2018). Additionally, we obtained 214 PSF-detrended light curves for Campaign 5 from Nardiello et al. 215 (2016).

216 We applied several methods and color-temperature relations
217 (CTRs) to determine robust T_{eff} . We used CTRs from Boyajian et al. (2013) and Mann et al. (2016) (erratum to Mann et al. 218 2015), and T_{eff} derived from Gaia DR2 using the StarHorse algorithm (Queiroz et al. 2018) and inferred from Gaia DR2 using the Apsis pipeline (Bailer-Jones et al. 2013; Andrae et al. 2018).
219 Boyajian et al. (2013) determined CTRs from a range of inter-220 ferometrically characterized stars using $g - z$, $g - i$, $g - r$,
221 $g - J$, $g - H$, and $g - K$ colors from SDSS and Johnson magni-222 tudes for A to K stars. Their sample is centered on solar metal-223 licity, so we constrained the use of these CTRs to stars with
224 $-0.25 < [\text{Fe}/\text{H}] < 0.25$. We transformed 2MASS JHK to $J - H$,
225 $H - K$, and $J - K$ in the Johnson system as the authors from
226 2MASS to the Bessell-Brett system (Carpenter 2001), and from
227 Bessell-Brett to Johnson using the relations in Bessell & Brett
228 (1988).

229 Mann et al. (2015) provide CTRs from absolutely calibrated
230 spectra to which they fitted atmospheric models to obtain T_{eff} .
231 Alternatively, they determined T_{eff} from long-baseline optical
232 interferometry measurements using the bolometric flux. Among
233 others, they note transformations for SDSS/2MASS $r - z$ and
234 $r - J$, or Gaia $BP - RP$ where extra information can be added
235 from metallicity or 2MASS $J - H$. The relations in Mann et al.
236 (2015) are only valid if metallicity is sufficiently close to solar,
237 which is satisfied for all clusters in this paper (see Table ??).
238 M35 may be an exception to this rule.

239 We supplemented our estimates with T_{eff} estimates from ? who
240 used the StarHorse pipeline (Queiroz et al. 2018) on Gaia DR2.
241 Gaia DR2 published effective temperatures for over 160 million
242 sources (Gaia Collaboration et al. 2018b). The typical uncer-
243 tainty is quoted at 324 K, but it is lower for stars above ~ 4100
244 K and below ~ 6700 K, so that we adopt 175 K which is above
245 the quoted root-median-squared error in this T_{eff} range (Andrae
246 et al. 2018), and use provided values only in this range.

247 Empirical CTRs suffer from systematic errors that stem both
248 from the different methods applied, and from sample selection
249 biases. We used as many empirical relations as possible in their
250 appropriate ranges to obtain multiple T_{eff} estimates from which
251 we then drew a more reliable median value. Targets that were
252 lacking sufficient photometric data to derive T_{eff} , or were too hot
253

254 2.4. Effective temperatures, stellar radii, and luminosities

255 2.4.1. Photometry and extinction correction

256 We determined effective temperatures T_{eff} using broadband
257 photometry the Two Micron All Sky Survey (2MASS; Skrutskie
258 et al. 2006), the Panoramic Survey Telescope and Rapid
259 Response System (Pan-STARRS) Data Release 1 (Chambers et al.
260 2016), and Gaia DR2 (Gaia Collaboration et al. 2018b). We
261 applied quality cuts to 2MASS, Pan-STARRS DR1, and Gaia DR2
262 data, as described in Appendix C, and removed foreground
263 stars using Gaia DR2 parallaxes. We corrected the 2MASS
264 and PanSTARRS photometry in M35, M67, and Ruprecht
265 147 for extinction using the most recent version (Green et al.
266 2019) of the dustmaps package that provides 3D dust maps
267 derived from 2MASS and PanSTARRS photometry together
268 with Gaia distances (Green et al. 2018). If there was no
269 parallax available we used the cluster median distance instead.
270 If an extinction value was not available for a given star
271

238 to be expected to have a convective envelope ($T_{\text{eff}} \geq 7000$ K),
 239 were flagged accordingly, and removed from the sample. We
 240 dropped all targets where the uncertainty on the weighted mean
 241 T_{eff} was greater than 10%. Only targets that were assigned a T_{eff}
 242 were searched for flares.

243 2.4.3. Stellar radii

244 We used a catalog of empirically characterised stars (Yee et al.
 245 2017) to derive R_* from T_{eff} (Fig. 4). Yee et al. (2017) collected
 246 404 stars with high-resolution spectra from the literature, and
 247 own observations of mid to late K-dwarfs, spanning low mass
 248 stars from 7000 K down to 3000 K. For these stars, the resulting
 249 catalog is accurate to 100 K in T_{eff} , 15 % in R_* , and 0.09 dex
 250 in [Fe/H]. We interpolated between stars from the catalog to our
 251 derived T_{eff} , and propagated the resulting scatter to the uncer-
 252 tainty in R_* if $T_{\text{eff}} > 3500$ K. For stars with $T_{\text{eff}} < 3500$ K we
 253 used $T_{\text{eff}} - R_*$ relations derived by (Mann et al. 2015, 2016).

254 2.4.4. Spectra

255 We assigned spectra to our targets from the SpecMatchEmp Yee
 256 et al. (2017) and the FlareSpecPhot libraries (Schmidt 2014;
 257 Kirkpatrick et al. 2010; Burgasser et al. 2007, 2008, 2010, 2004;
 258 Cruz et al. 2004; Burgasser & McElwain 2006; Rayner et al.
 259 2009; Doi et al. 2010; Filippazzo et al. 2015; Cruz et al. 2003;
 260 West et al. 2011; Bochanski et al. 2010, 2007; Schmidt et al.
 261 2010, 2015, 2014; Mann et al. 2015). When a spectrum was
 262 available for the derived spectral type in FlareSpecPhot, we pre-
 263 ferred it over SpecMatchEmp, which was the case for all stars
 264 cooler than M0, where we mapped spectral type to effective tem-
 265 perature as appears in Pecaut & Mamajek (2013). We then com-
 266 bined stellar radii R_* , T_{eff} , and spectra to projected bolome-
 267 luminosities $L_{\text{bol},*}$, and projected luminosities in the Kepler ba-
 268 $L_{Kp,*}$ (Shibayama et al. 2013; Ilin et al. 2019). Uncertainties
 269 $L_{Kp,*}$ ranged from 9 % to 52 % with a median value of 17 %.
 270 293
 294
 295
 296
 297
 298
 299
 300
 301
 302
 303
 304
 305
 306
 307
 308
 309
 310
 311
 312
 313
 314
 315
 316
 317
 318
 319
 320
 321
 322
 323
 324
 325
 326
 327
 328
 329
 330
 331
 332
 333
 334
 335
 336
 337
 338
 339
 340
 341
 342
 343
 344
 345
 346
 347
 348
 349
 350
 351
 352
 353
 354
 355
 356
 357
 358
 359
 360
 361
 362
 363
 364
 365
 366
 367
 368
 369
 370
 371
 372
 373
 374
 375
 376
 377
 378
 379
 380
 381
 382
 383
 384
 385
 386
 387
 388
 389
 390
 391
 392
 393
 394
 395
 396

270 3. Methods

271 We detected flare candidates automatically, and validated them
 272 by eye. We attempted to assign recovery probabilities and cor-
 273 rected for sampling effects using injection/recovery tests but the
 274 procedure was not scalable due to computational costs. We per-
 275 formed injection recovery on a handful of example light curves
 276 to see that de-trending and intrinsic light curve properties smear
 277 out the ED recovery with varying distributions that add an uncer-
 278 tainty of about 30%. Most of the candidates are expected to have
 279 a complex shape that deviates from the classical flare template.
 280 The validation yielded an estimate on the uncertainty on the flare
 281 energy released in the Kepler band. The frequency distributions
 282 of these flare energies are believed to follow a power law that
 283 spans multiple orders of magnitude. We adopted this model, and
 284 used two different Maximum Likelihood estimators to obtain the
 285 power law exponents. We tested the best fit parameters with the
 286 Kolmogorov-Smirnov test, and probed possible truncation of the
 287 power law relation with an exceedance test.

288 3.1. Flare finding

289 We used the open source software AltaiPony² to automatically
 290 detect and characterize flares in our sample. The code base

lies on K2SC³ (Aigrain et al. 2016) to remove instrumental and
 astrophysical variability from K2 light curves. We did not use the
 pre-detrended light curves available on MAST, but used K2SC to
 derive our own, because we clipped outliers at 3σ iteratively, as
 compared to the original work, where outliers were clipped at
 5σ (Aigrain et al. 2016).

After de-trending, the flare finder algorithm looked for continuous
 observing periods, defined as being longer than 10 data
 points at a minimum cadence of 2 h. All further routines were
 run on these observing periods. The finder iteratively clipped
 excursions from the median value at 3σ rolling window noise
 above median plus uncertainty given from K2SC de-trending.
 After each iteration, outliers were cut down to the current
 median value. Either after convergence, or 50 iterations, the result-
 ing median value was adopted. With this median as quiescent
 flux, flare candidates were identified with the same procedure
 as during the median value calculation, but now we addition-
 ally required at least three consecutive data points to fullfil the
 σ -criterion. Flare candidates were merged into single candidate
 events if they were no more than three data points apart. For
 each of these candidates occurrence time, amplitude and equiv-
 alent duration (ED) was returned.

The Kepler flare sample has shown to be difficult to treat in a
 fully automated way. Without manual vetting, the event samples
 remain significantly contaminated (Yang & Liu 2019).

ED is the area between the LC and the quiescent flux, that is,
 the integrated flare flux divided by the median quiescent flux F_0
 of the star, integrated over the flare duration (Hunt-Walker et al.
 2012):

$$ED = \int dt \frac{F_{\text{flare}}(t)}{F_0}. \quad (1)$$

ED is a quantity independent of calibration and distance that is
 suited to compare flaring activity on stars where these properties
 are uncertain. It describes the time during which a star releases
 as much energy as the flare itself. This time can be shorter or
 longer than the actual flare duration.

The uncertainty in ED depends on the light curve noise proper-
 ties, time sampling, and other intrinsic characteristics. Moreover,
 K2SC de-trending and the flare finding procedure introduce ad-
 ditional uncertainty that dominates the photometric noise. Car-
 rying out injection and recovery that takes into account the ef-
 fect of GP regression that underlies K2SC. We only performed
 injection-recovery on a small number of light curves with flares
 to estimate the .

3.2. Kepler flare energies

(see PaperI for details).

Multiband time resolved observations of active M dwarfs have
 shown that continuum flux accounts for the majority of the
 energy radiated by flares (Kowalski et al. 2013). The effective
 temperature of this blackbody, however, varies by a great degree,
 with, to date, no robust predictor of that temperature:

While solar flares are relatively cool, with
 $T_{\text{eff}} \approx 5000 - 7000$ K (Kleint et al. 2016; Kerr & Fletcher
 2014; Watanabe et al. 2013; Namekata et al. 2017), at least one
 M dwarf flare reached 40 000 K as seen in FUV spectra (Fron-
 ing et al. 2019), and most events exhibit temperatures of about
 9 000 – 10 000 K (Hawley & Fisher 1992; Kretzschmar 2011;
 Shibayama et al. 2013). A dependence of flare temperature on
 stellar age, or mass, or both, will enter our analysis if we attempt

² <https://github.com/ekaterinailin/AltaiPony>

³ <https://github.com/OxEs/k2sc>

317 to quantify bolometric flare energy. At about 6 200 K, the Kepler
 318 pass band captures the largest flux fraction, at 10 000 K 72 %
 319 at 40 000 K only 4% of this value is transmitted. Another effect
 320 is that flares of equal flare energy but hotter SED would not be
 321 seen in the Kepler band at all.

322 We propagated the uncertainties σ_{ED} and σ_L (on $L_{*,Kp}$)
 323 quadrature to $E_{Kp,\text{flare}}$.

325 3.3. Power law fits

326 Flare frequency distributions follow power law relations that
 327 cover several orders of magnitude, from solar microflares to stellar
 328 superflares. We fitted power law functions to the FFDs using
 329 three different approaches.

330 The first method was a maximum likelihood estimator (MLE)
 331 from Maschberger & Kroupa (2009).

332 The second method used the MLE result as a prior for α . Following
 333 Wheatland (2004), we defined the joint posterior distribution
 334 for the probability ϵ that a flare with ED or energy above some
 335 value S_2 occurs within a time period ΔT :

$$p(\epsilon, \alpha) = C \cdot (-\ln(1 - \epsilon)^M) \\ \cdot (\alpha - 1)^M \cdot \Gamma(\alpha) \left[\frac{(S_2/S_1)^{M+1}}{\pi} \right]^\alpha \\ \cdot (1 - \epsilon)^{(T/\Delta T) \cdot (S_2/S_1)^{\alpha-1} - 1}.$$

336 C is the normalisation constant, M is the number of events,
 337 the total observation time. Γ contains the prior distribution for
 338 and S_1 denotes the detection threshold above which all flares
 339 detected. π encapsulates the flare energies as

$$\pi = \prod_{i=1}^M \frac{s_i}{S_1}$$

340 , where $\{s_1, s_2, \dots, s_m\}$ are the flare energies or ED .

341 The posterior distribution in Wheatland (2004) captures both the
 342 Poissonian distribution of flare events in time, and their power
 343 law distribution in energy, simultaneously. Wheatland (2004)
 344 derived this model to be able to predict the flaring rate of a
 345 given active region on the sun, and offered an extension to Eq.
 346 2 that treated changing flaring activity rates as the active region
 347 evolves, and also characteristics of the active region itself, such
 348 as sunspot classifiers. In our simplification of the model, we
 349 assumed that the flare generating process did not change within
 350 the observation time span in any star in our sample ($M = M'$ in
 351 Eq. 24 in Wheatland (2004)). Another assumption was that this
 352 process was the same for all stars in the sample ($\Lambda_{MC} = 1$ in Eq.
 353 24). Thus the information gained from the light curves could be
 354 stacked together.

355 While in the case of a uniform prior for α the results from the MLE and
 356 Markov Chain Monte Carlo (MCMC)⁴ sampling from the posterior distribution are the same, the latter
 357 allowed us to fit for ϵ and α simultaneously. Additionally, the
 358 MCMC approach can be extended to incorporate further information
 359 about the stars in the sample in the future.

360 Another advantage of the latter approach is that we could use
 361 more informative priors. We also used a Gaussian fit to α obtained
 362 from the posterior distribution using the full sample of flares as the
 363 prior for a subsequent Bayesian analysis of individual age and T_{eff}
 364 bins. Assuming that α is universal for all spectral types, ages,
 365 and flare energy ranges, we used this more informative, Gaussian
 366 prior to further constrain the flaring rates.

367 The uncertainties on α were computed using the jackknife algorithm,
 368 which is well suited if we suspect false positives among the
 369 flare candidates. The resulting uncertainty estimate reflects
 370 the weight of outliers in the data. To show this, we sampled
 371 100 random FFDs of the same size, best fit power law parameters,
 372 and minimum and maximum observed ED for each power
 373 law fit we performed. We compared the power law parameters
 374 derived for these FFDs with the above methods to the original
 375 value, and found that the jackknife uncertainty captures XX% of
 376 random FFDs' results. With all methods, we fitted the intercept
 377 β_{cum} using non-linear least squares to the cumulative FFD and
 378 converted the result to $\beta = \beta_{\text{cum}} \cdot |\alpha - 1|$. As with α , we calculated
 379 the uncertainty $\sigma_{\beta_{\text{cum}}}$ using the jackknife algorithm, and propagated
 380 uncertainties from α for the final result on β .

381 Additionally we calculated the exceedance statistic tr to test if
 382 the power law distribution was truncated. If tr is 1, the power
 383 law distribution is truncated at the high energy end. If tr is 0,
 384 no information was gained from the calculation. To derive tr ,
 385 given a number n of observations X_n and a best fit value for the
 386 power law exponent, we generated 500 samples with n values
 387 from this best-fit distribution assuming no truncation, i.e. choosing
 388 an upper limit several orders of magnitude higher than X_{max} .
 389 We then proceeded to truncate the samples at thresholds T below
 390 the maximum observed value X_{max} and determined the average
 391 number N_{ex} of generated values that will exceed T . If the underly-
 392 ing power law is not truncated, N_{ex} declines with larger n ,
 393 as larger X_{max} will be present in the original data. If the best fit
 394 power law exponent is steeper, N_{ex} will be underestimated. If the
 395 best fit power law exponent is flatter, N_{ex} will be overestimated.
 396 If the power law is not truncated, for $n \geq 100$ N_{ex}/n will be
 397 < 5%, for $20 < n < 100$, typically $N_{\text{ex}}/n < 15\%$.

398 As recommended by Maschberger & Kroupa (2009), we applied
 399 the stabilized Kolmogorov-Smirnov (KS) test at 95% significance
 400 level to all power law fits in the sample. If the test fails
 401 the power law model does not fit the data at the given significance
 402 level. If the test passes, this does not give any information
 403 whether the power law model is the correct assumption. The
 404 goodness of fit can be estimated from the visual inspection of
 405 percentile-percentile plots, given in the online material⁴.

4. Results

Fig. ?? shows the $E_{Kp,\text{flare}}$ and ED detection thresholds, as defined by the recovery probability (see Sec. ??). The thresholds in ED reflect the noise level in the light curves.

4.1. Flaring activity as a function of age and T_{eff}

Flaring activity decays with age. Flaring fraction was observed to decline with galactic latitude for M dwarfs (Hilton et al. 2010) Howard+2019. Short rotation periods and high magnetic activity measured in H α are strongly correlated (West et al. 2015). According to gyrochronology, fast rotation indicates young age (Barnes 2003), and slows down as the star ages. Here, we quantify how this decline unfolds for different spectral types. Except for the stars in our coolest temperature bin (M5.5-M8, 2 500-3 000 K), stellar flaring activity at a given age is always stronger for a cooler star. The exception is seen at cluster ages around 120 Myr.

⁴ <https://github.com/ekaterinailin/flare-in-clusters-with-k2-ii>

423 4.2. M67

424 We found one very likely flare candidate in the PSF-detrended
 425 light curves (Nardiello et al. 2016). After having searched the
 426 entire sample we identified about 250 candidates. We excluded
 427 those candidates that clustered spatio-temporally in different
 428 light curves as systematics. After vetting the remaining 25
 429 eye, we excluded false positives judging by their morphology,
 430 leaving a mere ten light curves with flare-like shape. One target
 431 appeared to be an echo from one of the other light curves.
 432 Five targets were foreground stars, two are more likely back-
 433 ground stars, one target is probably a giant and does not ap-
 434 pear in Gaia photometry (IR source). Only one target appears
 435 to reside at M67 distance and is a $p = 0.997$ member according
 436 to Gao (2018). The 2MASS and Gaia BP and RP colors indicate
 437 an M2V dwarf (Pecaut & Mamajek 2013). If the spectral class is
 438 correct, the flare releases about $6.1 \cdot 10^{33}$ erg ($ED = 1391 \pm 548$
 439 s) in the Kepler band.

440 4.3. Flaring Activity Indicators

441 Flaring rates: FR and flaring fraction We define FR as the flare
 442 rate above detection thresholds on $E_{Kp,\text{flare}}$ and ED in each
 443 bin, respectively (Figs. ?? and ??).

444 Flaring energy: FA and $L_{Kp,\text{flare}}$ The energy released in flares
 445 was inferred using our derived stellar luminosities. It declines
 446 with age for every T_{eff} bin considered for both the total lumino-
 447 sity and relative to the quiescent flux (Fig. ??).

448 $L_{Kp,\text{flare}}$ is the luminosity in flares in the Kepler band. We can relate
 449 this to the quiescent bolometric luminosity of the star when
 450 we define the fractional flare luminosity FA as in PaperI:

$$451 FA = \frac{1}{N} \sum_i^N FA_i = \frac{1}{N} \sum_i^N \frac{E_{Kp,\text{flare,tot},i}}{t_i \cdot L_{\text{bol},*,i}}$$

452 We determine $L_{\text{bol},*}$ from R_* and T_{eff} , as described in Sec. 2.4.
 453 This is a meaningful measure of relative stellar activity as long
 454 as only the flux portion of the quiescent star in the Kepler band
 455 roughly constant. It is therefore sensible to compare FA values
 456 across ages, but not across T_{eff} .

457 FFD Power law fit parameters to the FFDs (Figs. 5 and 6)
 458 sensitive to the low-energy cutoff, where most observations
 459 side. The goodness of fit strongly depends on the sample size
 460 Power law fit parameters derived using MLEs, as described
 461 Sec. 3.3, are mostly consistent with each other but often deviate
 462 from $\alpha = 2$. A smaller sample size tends to create a flatter
 463 distribution (Figs. 7 and 8). Truncation was not detected for FFDs
 464 with more than 50 flares (Tables 2 and 3) For these results,
 465 extrapolations outside of the observed energy range are clearly off.
 466 If we assume $\alpha \equiv 2$, different distributions can be compared. For
 467 fixed α , in the ED domain, β_2 is the flare frequency at $ED = 1$ s,
 468 and shows a trend in both T_{eff} , and age (see Fig. ??). In the
 469 energy domain, the picture is less clear (Fig. ??).

470 Compare to other FFD values, e.g., from Ward's Evryscope
 471 survey, see table in Appendix, and maybe convert it to a plot Howard
 472 et al (2019) monitored superflares on cool stars with bolometric
 473 energies above 10^{33} erg and up to 10^{36} erg. They find power
 474 exponent values around ~ 2 resolved by spectral types. Similar
 475 values are found for individual flare stars (Lurie et al. 2015).
 476 Howard+18, Loyd+18, Tilley+19 show that flares can erode
 477 oplanetary atmospheres. If a flare is assumed to deposit its
 478

479 energy in an instant a single superflare can completely remove
 480 the ozone layer at the substellar point Loyd+18. Associated pro-
 481 tons are safer way to ozone destruction if they are associated
 482 with reoccurring large flares Tilley+19

5. Discussion

5.1. Consistency with other studies

EvryFlare, mass-dependence,

5.2. Flaring and rotation

More energetic flares can be expected from faster rotating stars (Candelaresi et al. 2014; Doorsselaere et al. 2017; Yang et al. 2017). Findings that flares with intermediate Rossby number appear to flare more than fast and slow rotators (Mondrik et al. 2019) could not be reproduced here or in the EvryFlare survey (Howard et al. 2019b). If enhanced flaring can be interpreted as an increase in the stellar angular momentum loss rate flaring activity can be used to inform the cause of variation in the spin-down efficiency. An example of such variations is the apparent temporary stalling of spin-down seen in K dwarfs in NGC 6811 (Curtis+2019). The authors favored a scenario in which the stellar core transfers momentum onto the envelope but did not rule out the possibility of a decreased magnetic braking efficiency. In the latter scenario, these stars should flare less.

We used rotation periods derived from K2 light curves for the Pleiades (Rebull et al. 2016b), the Hyades (Douglas et al. 2016), and Praesepe (Rebull et al. 2017), to illuminate the rotation-flaring relation at fixed ages. In the Pleiades, most flaring stars are found on the fast rotator branch at or below one day, and flaring activity peaks in this regime. For Praesepe, flaring rates appear to ... In the Hyades, all of the 11 stars with rotation periods that overlapped with our sample were found flaring, but the number were too low to provide statistical insight. For Rup 147, M35 and M67, no rotation rates were available at the time.

5.3. M37

Comparing our results to a similar study of photometric flares in M37 (Chang et al. 2015) we find the results somewhat discrepant. M37 is 300-600 Myr old and appears less active than Praesepe and Hyades in individual Teff bins, which are of coeval or older. We attribute the difference to the loose membership requirement of $pmem \geq 0.2$ in Chang et al. (2015) as compared to our stricter cuts at 0.8. We expect the M37 to be contaminated with field stars that systematically reduce the flaring rates. Applying our own restriction the M37 sample (Chang et al. 2016) leaves very few flares that hamper a statistical description of their distributions.

5.4. Division at 3000 K

The lowest T_{eff} bin at Pleiades age in our sample reflects the division between fully convective stars and those with a radiative core (Reid & Hawley 2005). At this age, the coolest dwarfs may still be accreting angular momentum on the PMS, instead of spinning down on the MS. We suggest that a regime change occurs around 120 Myr for stars with $T_{\text{eff}} = 2500 - 3250$ K. Below 3000 K, an analysis of 66 ZDI maps show that magnetic field configurations can be strong and dipolar or weak and multipolar (Morin et al. 2008; See et al. 2017). If these stars can be distinguished by age, this should be reflected in our age-resolved

Table 2. Summary of activity parameters of all clusters and T_{eff} bins in energy distributions.

cluster	T_{\min} [K]	T_{\max} [K]	n_*	n_{flares}	age [Myr]	[Fe/H]	$E_{\text{Kp,flare,min}}$ [erg]	σ_{B}	α_{MK}	β_2 [yr^{-1}]	β_{MK} [yr^{-1}]	tr_2	tb_{B} , tr_{MK}
Pleiades	4000	4999	87	148	125 ± 25	-0.02 ± 0.03	$1 \cdot 10^{34}$	1.70 ± 0.24	1.58 ± 0.20	$7.19 \cdot 10^{33} \pm 2.32 \cdot 10^{32}$	$2.07 \cdot 10^{23} \pm 5.12 \cdot 10^{22}$	$1.39 \cdot 10^{19} \pm 2.87 \cdot 10^{18}$	0
Pleiades	3000	3249	353	420	125 ± 25	-0.02 ± 0.03	$4.6 \cdot 10^{33}$	-	1.35 ± 0.42	$6.57 \cdot 10^{32} \pm 1.60 \cdot 10^{31}$	-	$1.09 \cdot 10^{10} \pm 4.74 \cdot 10^9$	0
Pleiades	3250	3499	168	324	125 ± 25	-0.02 ± 0.03	$4.8 \cdot 10^{32}$	2.08 ± 0.12	2.06 ± 0.11	$1.71 \cdot 10^{33} \pm 6.95 \cdot 10^{30}$	$8.03 \cdot 10^{35} \pm 9.34 \cdot 10^{34}$	$1.97 \cdot 10^{35} \pm 2.25 \cdot 10^{34}$	0
Pleiades	3750	3999	52	92	125 ± 25	-0.02 ± 0.03	$5.2 \cdot 10^{32}$	1.86 ± 0.12	1.83 ± 0.11	$4.01 \cdot 10^{33} \pm 4.99 \cdot 10^{31}$	$7.09 \cdot 10^{28} \pm 8.49 \cdot 10^{27}$	$8.29 \cdot 10^{27} \pm 9.52 \cdot 10^{26}$	0
Pleiades	5000	5999	53	23	125 ± 25	-0.02 ± 0.03	$3.7 \cdot 10^{32}$	-	1.28 ± 0.31	$1.51 \cdot 10^{33} \pm 1.56 \cdot 10^{32}$	-	$1.66 \cdot 10^8 \pm 5.19 \cdot 10^7$	0
Pleiades	3500	3749	50	127	125 ± 25	-0.02 ± 0.03	$3.8 \cdot 10^{32}$	1.74 ± 0.09	1.72 ± 0.09	$4.44 \cdot 10^{33} \pm 8.32 \cdot 10^{31}$	$7.47 \cdot 10^{24} \pm 6.80 \cdot 10^{23}$	$1.93 \cdot 10^{24} \pm 1.70 \cdot 10^{23}$	0
M35	4000	4999	216	23	149 ± 13	-0.21 ± 0.06	$1.6 \cdot 10^{33}$	1.23 ± 0.32	1.24 ± 0.27	$3.15 \cdot 10^{33} \pm 5.31 \cdot 10^{32}$	$2.20 \cdot 10^6 \pm 7.14 \cdot 10^5$	$4.81 \cdot 10^6 \pm 1.34 \cdot 10^6$	0
Hyades	4000	4999	32	24	665 ± 70	0.13 ± 0.01	$1.2 \cdot 10^{32}$	-	1.06 ± 0.14	$8.40 \cdot 10^{32} \pm 1.54 \cdot 10^{32}$	-	$1.07 \cdot 10^6 \pm 1.83 \cdot 10^4$	0
Hyades	3000	3249	54	115	665 ± 70	0.13 ± 0.01	$2.5 \cdot 10^{32}$	1.89 ± 0.18	1.85 ± 0.17	$1.15 \cdot 10^{33} \pm 6.45 \cdot 10^{30}$	$1.93 \cdot 10^{29} \pm 3.51 \cdot 10^{28}$	$1.33 \cdot 10^{28} \pm 2.28 \cdot 10^{27}$	0
Hyades	3250	3499	42	140	665 ± 70	0.13 ± 0.01	$2.2 \cdot 10^{33}$	2.09 ± 0.65	1.90 ± 0.47	$2.19 \cdot 10^{33} \pm 9.70 \cdot 10^{31}$	$2.06 \cdot 10^{36} \pm 1.33 \cdot 10^{36}$	$1.13 \cdot 10^{30} \pm 5.36 \cdot 10^{29}$	0
Hyades	3750	3999	5	25	665 ± 70	0.13 ± 0.01	$6.3 \cdot 10^{31}$	1.47 ± 0.23	1.45 ± 0.19	$2.12 \cdot 10^{33} \pm 9.71 \cdot 10^{31}$	$5.41 \cdot 10^{15} \pm 1.24 \cdot 10^{15}$	$1.02 \cdot 10^{15} \pm 2.01 \cdot 10^4$	0
Hyades	5000	5999	11	11	665 ± 70	0.13 ± 0.01	$1.9 \cdot 10^{32}$	-	1.06 ± 0.28	$7.75 \cdot 10^{34} \pm 7.76 \cdot 10^{33}$	-	$1.36 \cdot 10^6 \pm 4.59 \cdot 10^4$	0
Hyades	3500	3749	14	31	665 ± 70	0.13 ± 0.01	$8.8 \cdot 10^{31}$	1.13 ± 0.24	1.16 ± 0.20	$1.54 \cdot 10^{33} \pm 2.27 \cdot 10^{32}$	$2.29 \cdot 10^3 \pm 5.82 \cdot 10^2$	$2.38 \cdot 10^4 \pm 5.14 \cdot 10^3$	0

Table 3. Summary of activity parameters of all clusters and T_{eff} bins in equivalent duration distributions.

cluster	$T_{\text{min}} [\text{K}]$	$T_{\text{max}} [\text{K}]$	n_*	n_{flares}	age [Myr]	[Fe/H]	$ED_{\text{min}} [\text{s}]$	α_B	α_{MK}	$\beta_2 [\text{yr}^{-1}]$	$\beta_B [\text{yr}^{-1}]$	$\beta_{\text{MK}} [\text{yr}^{-1}]$	tr_2	tr_B	tr_{MK}	
Pleiades	4000	4999	87	110	$125 \pm^{25}_{25}$	-	$2.3 \cdot 10^1$	1.68 ± 0.07	1.68 ± 0.07	175.40 ± 3.06	26.23 ± 1.80	26.08 ± 1.74	0	0	0	
Pleiades	3000	3249	353	129	$125 \pm^{25}_{25}$	-	$9.1 \cdot 10^2$	2.26 ± 0.12	2.24 ± 0.12	1663.97 ± 8.43	16801.52 ± 1988.56	14323.95 ± 1675.01	0	0	0	
Pleiades	3250	3499	168	185	$125 \pm^{25}_{25}$	-	$2.2 \cdot 10^2$	2.03 ± 0.09	2.02 ± 0.09	1250.16 ± 3.32	1524.74 ± 130.65	1437.66 ± 122.52	0	0	0	
Pleiades	2500	2999	63	28	$125 \pm^{25}_{25}$	-	$2 \cdot 10^2$	1.40 ± 0.32	1.38 ± 0.26	732.64 ± 89.39	3.07 ± 0.97	2.55 ± 0.68	0	1	1	
Pleiades	3750	3999	52	61	$125 \pm^{25}_{25}$	-	$4.6 \cdot 10^1$	1.86 ± 0.12	1.84 ± 0.11	337.15 ± 3.77	133.53 ± 15.57	118.85 ± 13.38	0	0	0	
Pleiades	5000	5999	53	14	$125 \pm^{25}_{25}$	-	0.02 ± 0.03	4.9	1.27 ± 0.25	1.32 ± 0.17	9.24 ± 1.16	0.13 ± 0.03	0.20 ± 0.04	1	1	1
Pleiades	3500	3749	50	47	$125 \pm^{25}_{25}$	-	-0.02 ± 0.03	$1.6 \cdot 10^2$	1.88 ± 0.11	838.25 ± 8.01	338.29 ± 38.96	256.41 ± 28.27	0	0	0	
M35	4000	4999	221	7	$149 \pm^{13}_{13}$	-	-0.21 ± 0.06	$5.2 \cdot 10^2$	-	1.34 ± 0.76	202.70 ± 21.23	-	0.26 ± 0.20	1	0	1
Rup 147	5000	5999	39	7	$2301 \pm^{380}_{257}$	-	0.08 ± 0.04	4.0	-	1.95 ± 0.30	3.07 ± 0.21	-	2.58 ± 0.79	0	0	0
Hyades	4000	4999	32	22	$665 \pm^{76}_{76}$	-	0.13 ± 0.01	4.4	-	1.13 ± 0.25	30.87 ± 8.30	-	0.05 ± 0.01	0	0	1
Hyades	3000	3249	56	14	$665 \pm^{70}_{70}$	-	0.13 ± 0.01	$9.8 \cdot 10^2$	1.87 ± 0.60	1.78 ± 0.48	1037.31 ± 28.99	316.11 ± 191.27	132.35 ± 63.88	0	1	1
Hyades	3250	3499	42	20	$665 \pm^{70}_{70}$	-	0.13 ± 0.01	$5.5 \cdot 10^2$	1.82 ± 0.37	1.77 ± 0.30	1281.92 ± 18.75	264.94 ± 97.28	156.31 ± 46.78	0	1	1
Hyades	3750	3999	5	21	$665 \pm^{70}_{70}$	-	0.13 ± 0.01	3.9	1.46 ± 0.29	1.49 ± 0.27	157.65 ± 8.25	8.37 ± 2.48	10.09 ± 2.71	0	1	1
Hyades	5000	5999	11	8	$665 \pm^{70}_{70}$	-	0.13 ± 0.01	$2.4 \cdot 10^1$	-	1.06 ± 0.28	182.82 ± 18.30	-	0.01 ± 0.00	1	0	1
Hyades	3500	3749	14	30	$665 \pm^{70}_{70}$	-	0.13 ± 0.01	6.5	-	1.14 ± 0.16	172.86 ± 33.54	-	0.18 ± 0.03	0	0	1

flaring activity. If the difference is not a function of age, ⁵⁷⁸ should see a similar bimodal distribution of very inactive and ⁵⁷⁹ very active stars in the lowest mass bins. If the difference ⁵⁸⁰ between the two configurations is a function of age, we should only ⁵⁸¹ see one type of stars with correspondingly similar behaviour in ⁵⁸² these T_{eff} bins. ⁵⁸³
The lowest mass bin appears underactive compared to the rest of ⁵⁸⁴ the flaring-age- T_{eff} relation in the ED domain. Physical explana- ⁵⁸⁵ tions for this peculiarity include: A different magnetic structure ⁵⁸⁶ A truncation of the power law that reflects the maximum ED an ⁵⁸⁷ active region can produce on these stars. ⁵⁸⁸
West et al. (2015) found that all M1-M4 dwarfs with rotation pe- ⁵⁸⁹ riods shorter than 26 days, and all M5-M8 dwarfs with periods ⁵⁹⁰ shorter than 86 days show $H\alpha$ emission, indicating their mag- ⁵⁹¹ netic activity. ⁵⁹²
Assuming a typical binary fraction for early and mid M ⁵⁹³ dwarfs (Fischer & Marcy 1992), we can expect some of the flares ⁵⁹⁴ on stars at $T_{\text{eff}} > 3000$ K to belong to unresolved binary com- ⁵⁹⁵ panions with $T_{\text{eff}} < 3000$ K. A misattributed flare on an early M ⁵⁹⁶ dwarf then will be assigned a too small ED , but still a correct ⁵⁹⁷ $E_{Kp,\text{flare}}$ because the count ratios are equal to the L_{Kp} ratios. ⁵⁹⁸

5.5. Consistency of Hyades' and Praesepe's results

HRDs constructed in Gaia Collaboration et al. (2018a) indicate ⁵⁹⁹ only slightly older ages for Hyades and Praesepe. We expect our ⁶⁰⁰ results to reflect this similarity. ⁶⁰¹
Are the samples comparable? Membership determination may differ. Can we frame this as a statistical test, i.e. answer the question: What is the probability that the activity distributions for both clusters were drawn from the same underlying distribution for a given age and mass bin? ⁶⁰²
Metallicity is controlled for ([Fe/H](Praesepe) = ⁶⁰³ [Fe/H](Hyades) = 0.13, Netopil et al. 2016). ⁶⁰⁴

5.6. Consistency of Pleiades and M35 results

M35 is has subsolar metallicity, while Pleiades are roughly solar. ⁶⁰⁵

5.7. Jim's section(s)

Flaring activity function of mass and age – a gyrochronology ⁶¹⁷ analog? ⁶¹⁸
Results in the context of Davenport et al. (2019): How well does ⁶¹⁹ the model fit if we have isochronal and not rotational ages ⁶²⁰ for ⁶²¹ our stars? ⁶²²
Davenport et al. (2019) note a sample bias towards more active ⁶²³ stars. Their models overpredicts the superflaring rate of the ⁶²⁴ average Sun-like sample from Shibayama et al. (2013) and more ⁶²⁵ resembles the rate for their most active sub-sample. *Do we see ⁶²⁶ the same effect in our OC sample? We should not. Or do our ⁶²⁷ memberships depend on activity.* ⁶²⁸

5.8. Universality of α

Takin into account uncertainties and systematic errors resulting ⁶²⁹ power law fitting methods, the power law exponent $\alpha \sim 2$ ⁶³⁰ pears to be the same for all studies on flare statistics so far, ⁶³¹ irrespective of spectral type. A noteable exception are A stars in ⁶³² Kepler that follow a power law with $\alpha \sim 1$ that may indicate ⁶³³ different physical process (Yang & Liu 2019). ⁶³⁴

5.9. Deviations from single power law

Spots can survive on the stellar surface from a few days to nearly a year (Namekata et al. 2017; Davenport 2015). Namekata et al. (2017) find conceivable that spots evolve on timescale shorter than the estimated lifetimes. Complex spot geometry is correlated with the strongest X-class flares on the Sun (Toriumi et al. 2017; Sammis et al. 2000). This support the idea that flares are associated with the presence of certain types of starspots, or more generally, certain types of active regions. Since we can reasonable expect that there is a maximum flare energy a spot can produce, the underlying power law relation must break a some ED_{max} . We tested a possible truncation of our FFDs, but find no conclusive evidence for it in any FFD with > 50 data points. As we stack multiple targets, each potentially with multiple, evolving spots of various sizes on their surfaces, into one FFD at a time, we might observe a deviation but no truncation. A different explanation is simply that we do not sample the maximum energies, as extremely high relative fluxes have been observed in the past (Paudel et al. 2018; Jackman et al. 2019; Schmidt et al. 2016).

6. Summary and Conclusions

Is there or will be there more data available to further extend the sample?

Acknowledgements. This work made use of the `gaia-kepler.fun` crossmatch database created by Megan Bedell. Kepler-affiliated tools were used in the process: `lightkurve`, `K2SC`, `AltaIPony`. Also: `numpy`, `pandas`, `astroML`, `astropy`, `specmatch-emp`, `bokeh` (Bokeh Development Team 2019)... `TOPCAT`: This research made use of the cross-match service provided by CDS, Strasbourg. This work has made use of data from the European Space Agency (ESA) mission `Gaia` (<https://www.cosmos.esa.int/gaia>), processed by the `Gaia` Data Processing and Analysis Consortium (DPAC, <https://www.cosmos.esa.int/web/gaia/dpac/consortium>). Funding for the DPAC has been provided by national institutions, in particular the institutions participating in the `Gaia` Multilateral Agreement. If you have used `Gaia` DR2 data in your research, please cite both the `Gaia` mission paper and the `Gaia` DR2 release paper: Gaia Collaboration et al. (2016): Description of the `Gaia` mission (spacecraft, instruments, survey and measurement principles, and operations), Gaia Collaboration et al. (2018b): Summary of the contents and survey properties.

References

- Aarnio, A. N., Matt, S. P., & Stassun, K. G. 2012, *ApJ*, 760, 9
- Aarnio, A. N., Stassun, K. G., Hughes, W. J., & McGregor, S. L. 2011, *Sol. Phys.*, 268, 195
- Aigrain, S., Parviainen, H., & Pope, B. J. S. 2016, *MNRAS*, 459, 2408
- Alvarado-Gómez, J. D., Drake, J. J., Cohen, O., Moschou, S. P., & Garraffo, C. 2018, *ApJ*, 862, 93
- Anders, F., Khalatyan, A., Chiappini, C., et al. 2019, *A&A*, 628, A94
- Andrae, R., Fouesneau, M., Creevey, O., et al. 2018, *A&A*, 616, A8
- Bailer-Jones, C. A. L., Andrae, R., Arcay, B., et al. 2013, *A&A*, 559, A74
- Barentsen, G., Hedges, C., Saunders, N., et al. 2018, arXiv e-prints, arXiv:1810.12554
- Barnes, S. A. 2003, *ApJ*, 586, 464
- Bauke, H. 2007, *European Physical Journal B*, 58, 167
- Bessell, M. S. & Brett, J. M. 1988, *Publications of the Astronomical Society of the Pacific*, 100, 1134
- Bochanski, J. J., Hawley, S. L., Covey, K. R., et al. 2010, *AJ*, 139, 2679
- Bochanski, J. J., West, A. A., Hawley, S. L., & Covey, K. R. 2007, *AJ*, 133, 531
- Bokeh Development Team. 2019, Bokeh: Python library for interactive visualization
- Bouy, H., Bertin, E., Barrado, D., et al. 2015, *Astronomy and Astrophysics*, 575, A120
- Boyajian, T. S., von Braun, K., van Belle, G., et al. 2013, *The Astrophysical Journal*, 771, 40
- Burgasser, A. J., Cruz, K. L., Cushing, M., et al. 2010, *ApJ*, 710, 1142
- Burgasser, A. J., Liu, M. C., Ireland, M. J., Cruz, K. L., & Dupuy, T. J. 2008, *ApJ*, 681, 579

- 643 Burgasser, A. J.,Looper, D. L., Kirkpatrick, J. D., & Liu, M. C. 2007, ApJ, 6557
644 557
645 Burgasser, A. J. & McElwain, M. W. 2006, AJ, 131, 1007
646 Burgasser, A. J., McElwain, M. W., Kirkpatrick, J. D., et al. 2004, AJ, 127, 2826
647 Candelaresi, S., Hillier, A., Maehara, H., Brandenburg, A., & Shibata, K. 20127
648 ApJ, 792, 67
649 Cantat-Gaudin, T., Jordi, C., Vallenari, A., et al. 2018, A&A, 618, A93
650 Carpenter, J. M. 2001, The Astronomical Journal, 121, 2851
651 Chambers, K. C., Magnier, E. A., Metcalfe, N., et al. 2016, ArXiv e-prints [arXiv:1612.05560]
652 Chang, S.-W., Byun, Y.-I., & Hartman, J. D. 2015, ApJ, 814, 35
653 Chang, S. W., Byun, Y. I., & Hartman, J. D. 2016, VizieR Online Data Catalogue, 734
654 J/ApJ/814/35
655 Clarke, R. W., Davenport, J. R. A., Covey, K. R., & Baranec, C. 2018, ApJ, 873
656 59
657 Cruz, K. L., Burgasser, A. J., Reid, I. N., & Liebert, J. 2004, ApJ, 604, L61
658 Cruz, K. L., Reid, I. N., Liebert, J., Kirkpatrick, J. D., & Lowrance, P. J. 2009
659 AJ, 126, 2421
660 AJ, 145, 134
661 Curtis, J. L., Wolfgang, A., Wright, J. T., Brewer, J. M., & Johnson, J. A. 20124
662 AJ, 145, 134
663 Davenport, J. 2015, PhD thesis, University of Washington
664 Davenport, J. R. A., Covey, K. R., Clarke, R. W., et al. 2019, ApJ, 871, 241
665 Davenport, J. R. A., Hawley, S. L., Hebb, L., et al. 2014, ApJ, 797, 122
666 Doi, M., Tanaka, M., Fukugita, M., et al. 2010, AJ, 139, 1628
667 Doorsselaere, T. V., Shariati, H., & Debosscher, J. 2017, ApJS, 232, 26
668 Douglas, S. T., Agüeros, M. A., Covey, K. R., et al. 2014, ApJ, 795, 161
669 Douglas, S. T., Agüeros, M. A., Covey, K. R., et al. 2016, ApJ, 822, 47
670 Douglas, S. T., Agüeros, M. A., Covey, K. R., & Kraus, A. 2017, ApJ, 842, 849
671 Drake, J. J., Cohen, O., Yashiro, S., & Gopalswamy, N. 2013, ApJ, 764, 170
672 Filippazzo, J. C., Rice, E. L., Faherty, J., et al. 2015, ApJ, 810, 158
673 Finkbeiner, D. P., Schlafly, E. F., Schlegel, D. J., et al. 2016, ApJ, 822, 66
674 Fischer, D. A., & Marcy, G. W. 1992, ApJ, 396, 178
675 Froning, C. S., Kowalski, A., France, K., et al. 2019, ApJ, 871, L26
676 Gaia Collaboration, Babusiaux, C., van Leeuwen, F., et al. 2018a, A&A, 615
677 A10
678 Gaia Collaboration, Brown, A. G. A., Vallenari, A., et al. 2018b, A&A, 616, 757
679 Gao, X. 2018, ApJ, 869, 9
680 Gao, X. 2018, The Astrophysical Journal, 869, 9
681 Gizis, J. E. 2013, ApJ, 779, 172
682 Gonzalez, G. 2016, MNRAS, 459, 1060
683 Green, G. M., Schlafly, E. F., Finkbeiner, D., et al. 2018, MNRAS, 478, 651
684 Green, G. M., Schlafly, E. F., Zucker, C., Speagle, J. S., & Finkbeiner, D. P. 201763
685 arXiv e-prints, arXiv:1905.02734
686 Hawley, S. L. & Fisher, G. H. 1992, ApJS, 78, 565
687 Hilton, E. J., West, A. A., Hawley, S. L., & Kowalski, A. F. 2010, AJ, 140, 1768
688 Howard, W. S., Corbett, H., Law, N. M., et al. 2019a, ApJ, 881, 9
689 Howard, W. S., Corbett, H., Law, N. M., et al. 2019b, arXiv e-prints [arXiv:1907.10735]
690 769
691 Howell, S. B., Sobeck, C., Haas, M., et al. 2014, PASP, 126, 398
692 Hunt-Walker, N. M., Hilton, E. J., Kowalski, A. F., Hawley, S. L., & Matthews, J. M. 2012, PASP, 124, 545
693 Ilin, E., Schmidt, S. J., Davenport, J. R. A., & Strassmeier, K. G. 2019, A&A, 622, A133
694 Jackman, J. A. G., Wheatley, P. J., Bayliss, D., et al. 2019, arXiv e-prints, arXiv:1902.00900
695 Karoff, C. 2016, Nature Communications, 7, 11058
696 Kerr, G. S. & Fletcher, L. 2014, ApJ, 783, 98
697 Kirkpatrick, J. D.,Looper, D. L., Burgasser, A. J., et al. 2010, ApJS, 190, 100
698 Kleint, L., Heinzel, P., Judge, P., & Krucker, S. 2016, ApJ, 816, 88
699 Koch, D. G., Borucki, W. J., Basri, G., et al. 2010, ApJ, 713, L79
700 Kovács, G., Bakos, G., & Noyes, R. W. 2005, MNRAS, 356, 557
701 Kowalski, A. F., Hawley, S. L., Wisniewski, J. P., et al. 2013, ApJS, 207, 15
702 Kretzschmar, M. 2011, A&A, 530, A84
703 Lecavelier des Etangs, A., Bourrier, V., Wheatley, P. J., et al. 2012, A&A, 543,
704 L4
705 Loyd, R. O. P., France, K., Youngblood, A., et al. 2018, ApJ, 867, 71
706 Luger, R., Kruse, E., Foreman-Mackey, D., Agol, E., & Saunders, N. 2018, AJ, 156, 99
707 Lurie, J. C., Davenport, J. R. A., Hawley, S. L., et al. 2015, ApJ, 800, 95
708 Mann, A. W., Feiden, G. A., Gaidos, E., Boyajian, T., & von Braun, K. 2015,
709 ApJ, 804, 64
710 Mann, A. W., Feiden, G. A., Gaidos, E., Boyajian, T., & von Braun, K. 2016,
711 The Astrophysical Journal, 819, 87
712 Maschberger, T. & Kroupa, P. 2009, MNRAS, 395, 931
713 Mondrik, N., Newton, E., Charbonneau, D., & Irwin, J. 2019, ApJ, 870, 10
714 Morin, J., Donati, J. F., Petit, P., et al. 2008, MNRAS, 390, 567
715 Namekata, K., Sakaue, T., Watanabe, K., et al. 2017, ApJ, 851, 91
716 Nardiello, D., Libralato, M., Bedin, L. R., et al. 2016, MNRAS, 463, 1831
717 Olivares, J., Bouy, H., Sarro, L. M., et al. 2019, A&A, 625, A115
718 Olivares, J., Sarro, L. M., Moraux, E., et al. 2018, A&A, 617, A15
719 Paudel, R. R., Gizis, J. E., Mullan, D. J., et al. 2018, ApJ, 861, 76
720 Pecaut, M. J. & Mamajek, E. E. 2013, ApJS, 208, 9
721 Priest, E. & Forbes, T. 2002, A&A Rev., 10, 313
722 Queiroz, A. B. A., Anders, F., Santiago, B. X., et al. 2018, MNRAS, 476, 2556
723 Rayner, J. T., Cushing, M. C., & Vacca, W. D. 2009, ApJS, 185, 289
724 Rebull, L., Stauffer, J., Bouvier, J., et al. 2016a, Astronomical Journal, 152, 113,
725 bibtext: 2016AJ....152..113R bibtex[eid=113;adsurl=https://ui.adsabs.harvard.edu/abs/2016AJ....152..113R;adsnote=Provided by the SAO/NASA
726 Astrophysics Data System]
727 Rebull, L. M., Stauffer, J. R., Bouvier, J., et al. 2016b, AJ, 152, 113
728 Rebull, L. M., Stauffer, J. R., Hillenbrand, L. A., et al. 2017, ApJ, 839, 92
729 Reid, I. N. & Hawley, S. L. 2005, New Light on Dark Stars: Red Dwarfs, Low-
730 Mass Stars, Brown Dwarfs, 2nd edn., Springer-Praxis books in astronomy and
731 astrophysics (Berlin ; New York : Chichester, UK: Springer ; Praxis)
732 Reino, S., de Bruijne, J., Zari, E., d'Antona, F., & Ventura, P. 2018, MNRAS,
733 477, 3197
734 Sammis, I., Tang, F., & Zirin, H. 2000, ApJ, 540, 583
735 Schmidt, S. J. 2014, Mem. Soc. Astron. Italiana, 85, 741
736 Schmidt, S. J., Hawley, S. L., West, A. A., et al. 2015, AJ, 149, 158
737 Schmidt, S. J., Shappee, B. J., Gagné, J., et al. 2016, ApJ, 828, L22
738 Schmidt, S. J., West, A. A., Bochanski, J. J., Hawley, S. L., & Kielty, C. 2014,
739 PASP, 126, 642
740 Schmidts, S. J., West, A. A., Hawley, S. L., & Pineda, J. S. 2010, AJ, 139, 1808
741 See, V., Jardine, M., Vidotto, A. A., et al. 2017, MNRAS, 466, 1542
742 Shibayama, T., Maehara, H., Notsu, S., et al. 2013, The Astrophysical Journal
743 Supplement Series, 209, 5
744 Shibayama, T., Maehara, H., Notsu, S., et al. 2013, ApJS, 209, 5
745 Skrutskie, M. F., Cutri, R. M., Stiening, R., et al. 2006, AJ, 131, 1163
746 Soares-Furtado, M., Hartman, J. D., Bakos, G. Á., et al. 2017, Publications of
747 the Astronomical Society of the Pacific, 129, 044501
748 Tilley, M. A., Segura, A., Meadows, V., Hawley, S., & Davenport, J. 2019, As-
749 trobiology, 19, 64
750 Toriumi, S., Schrijver, C. J., Harra, L. K., Hudson, H., & Nagashima, K. 2017,
751 ApJ, 834, 56
752 Van Cleve, J. E., Howell, S. B., Smith, J. C., et al. 2016, PASP, 128, 075002
753 Vanderburg, A. & Johnson, J. A. 2014, Publications of the Astronomical Society
754 of the Pacific, 126, 948
755 Vanderplas, J., Connolly, A., Ivezić, Ž., & Gray, A. 2012, in Conference on In-
756 telligent Data Understanding (CIDU), 47–54
757 Vinícius, Z., Barentsen, G., Hedges, C., Gully-Santiago, M., & Cody, A. M. 2018
758 Walkowicz, L. M., Basri, G., Batalha, N., et al. 2011, AJ, 141, 50
759 Watanabe, K., Shimizu, T., Masuda, S., Ichimoto, K., & Ohno, M. 2013, ApJ,
760 776, 123
761 West, A. A., Morgan, D. P., Bochanski, J. J., et al. 2011, AJ, 141, 97
762 West, A. A., Weisenburger, K. L., Irwin, J., et al. 2015, ApJ, 812, 3
763 Wheatland, M. S. 2004, ApJ, 609, 1134
764 Yang, H. & Liu, J. 2019, ApJS, 241, 29
765 Yang, H., Liu, J., Gao, Q., et al. 2017, ApJ, 849, 36
766 Yee, S. W., Petigura, E. A., & von Braun, K. 2017, ApJ, 836, 77

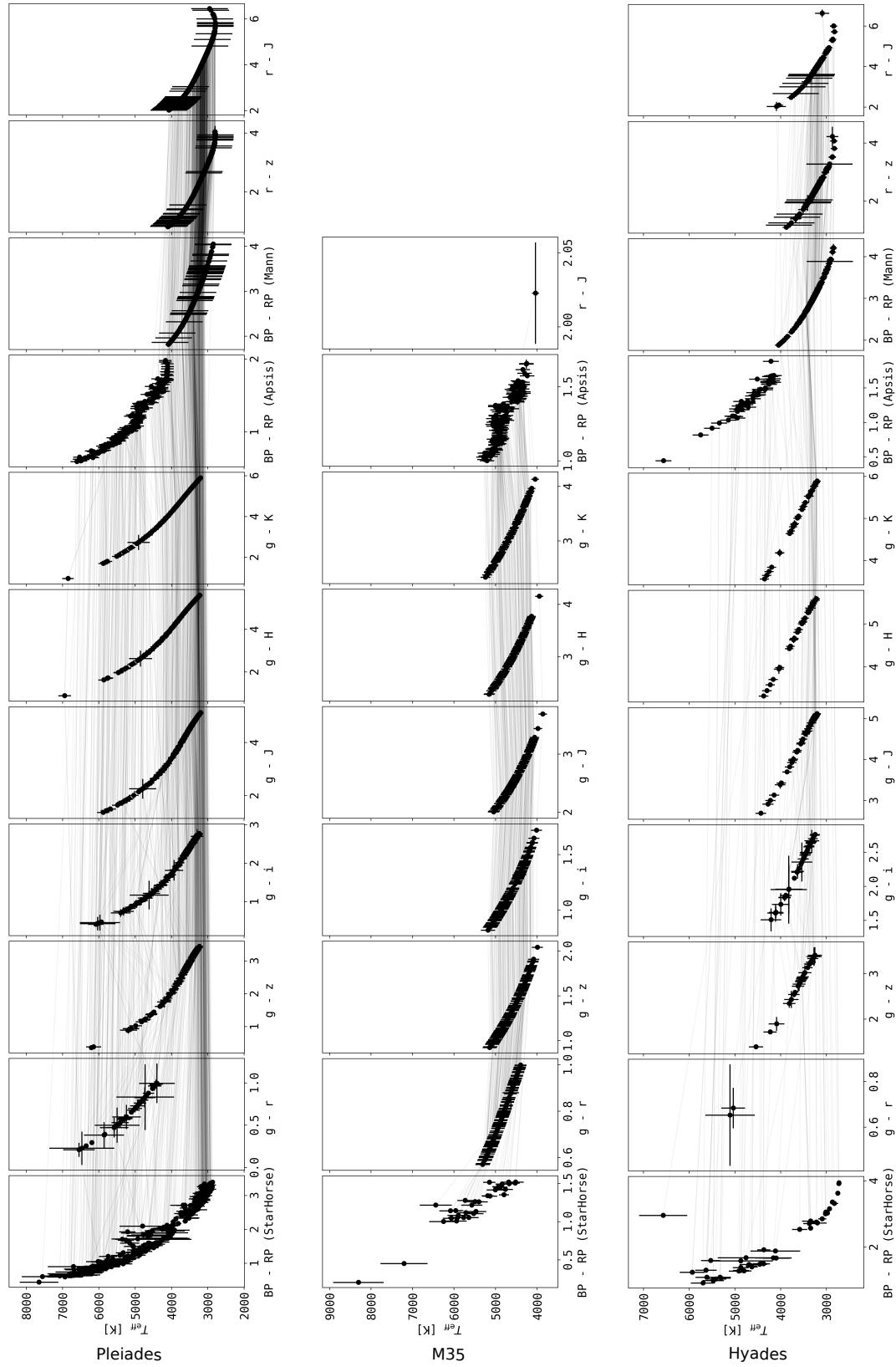


Fig. 2. Color-temperature relations for Pleiades, M35, and Hyades.

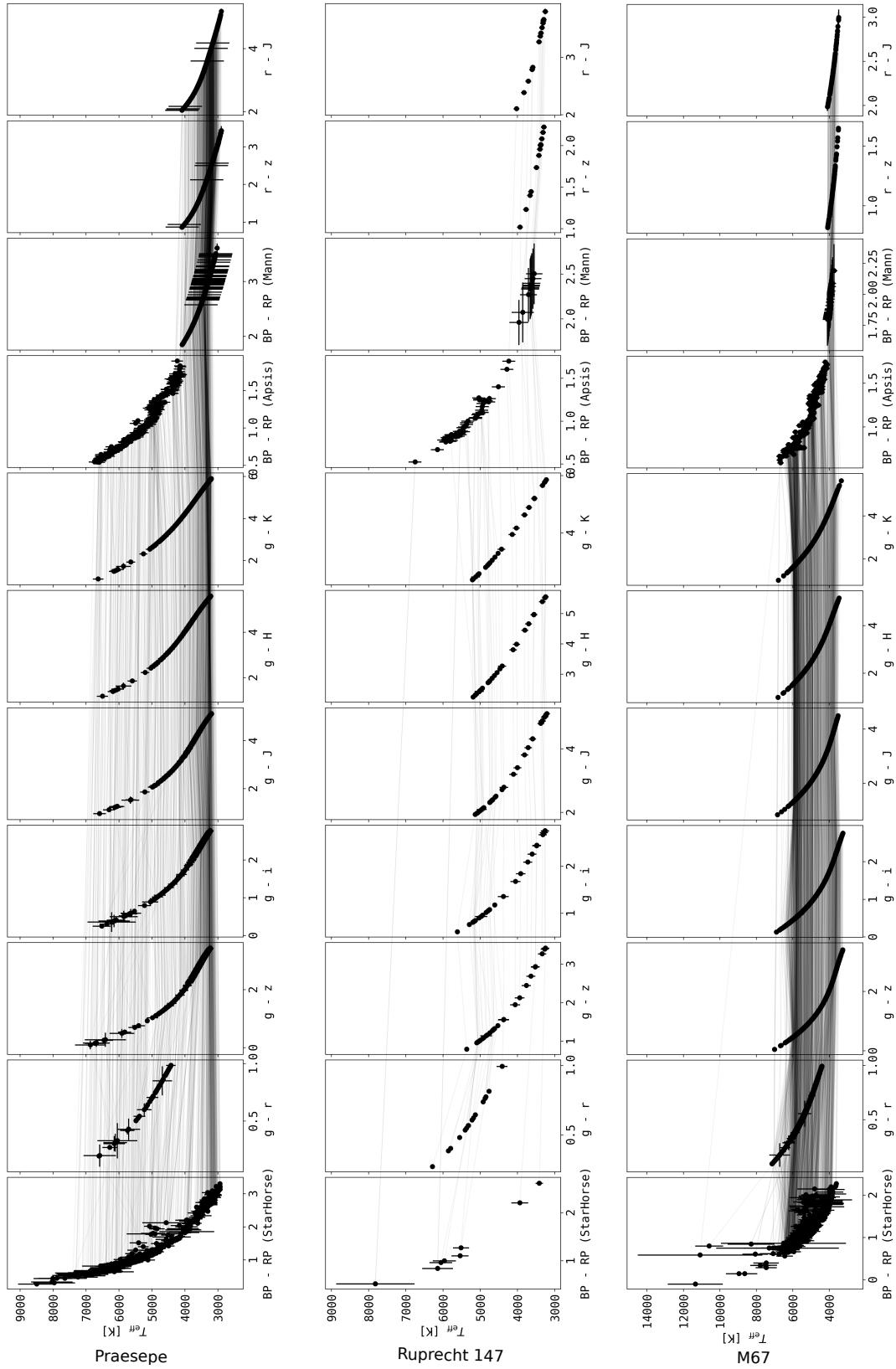


Fig. 3. Color-temperature relations for Praesepe, Ruprecht 147, and M67. Description as in Fig. 2.

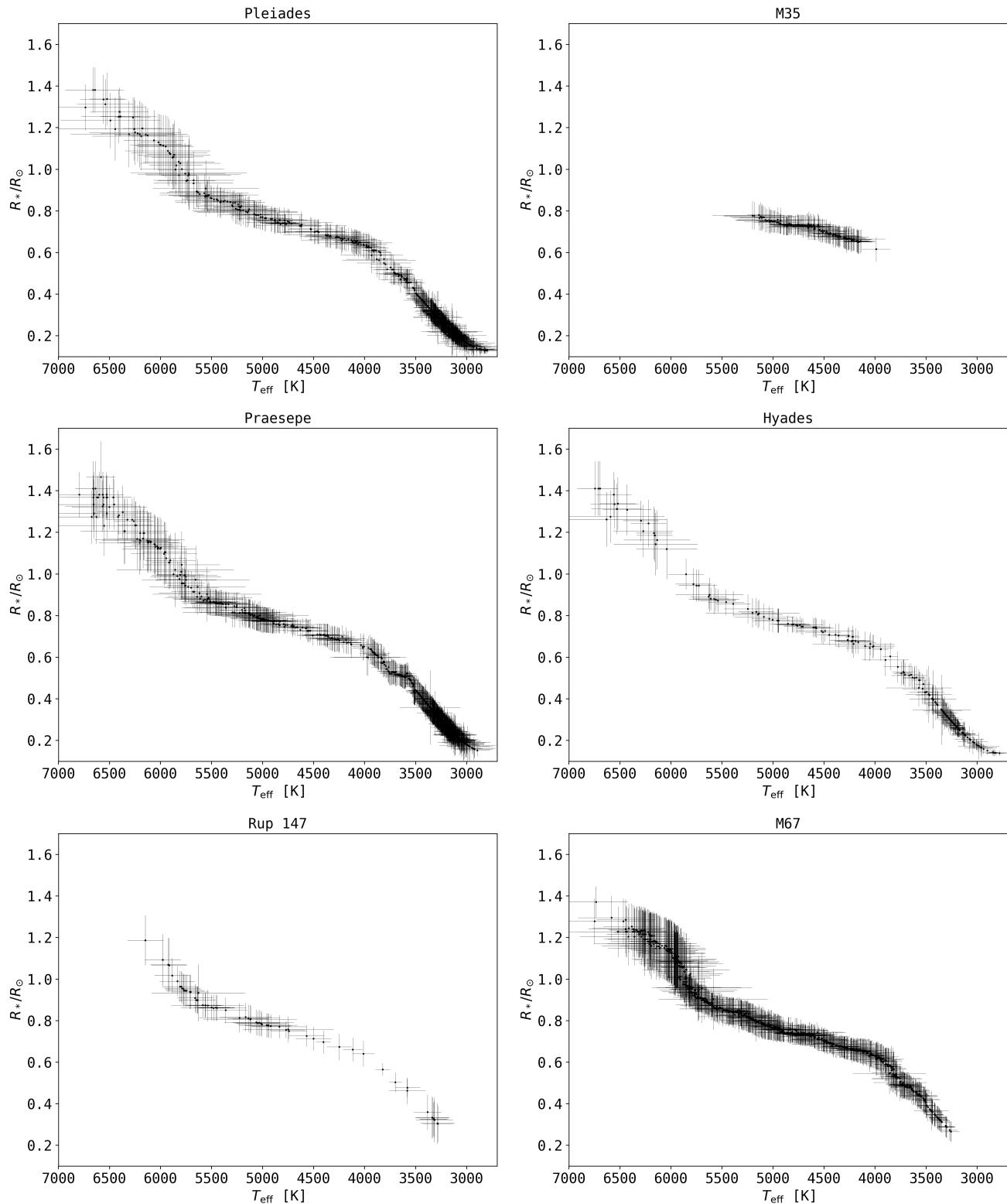


Fig. 4. T_{eff} – R_* relation for all clusters in this study.

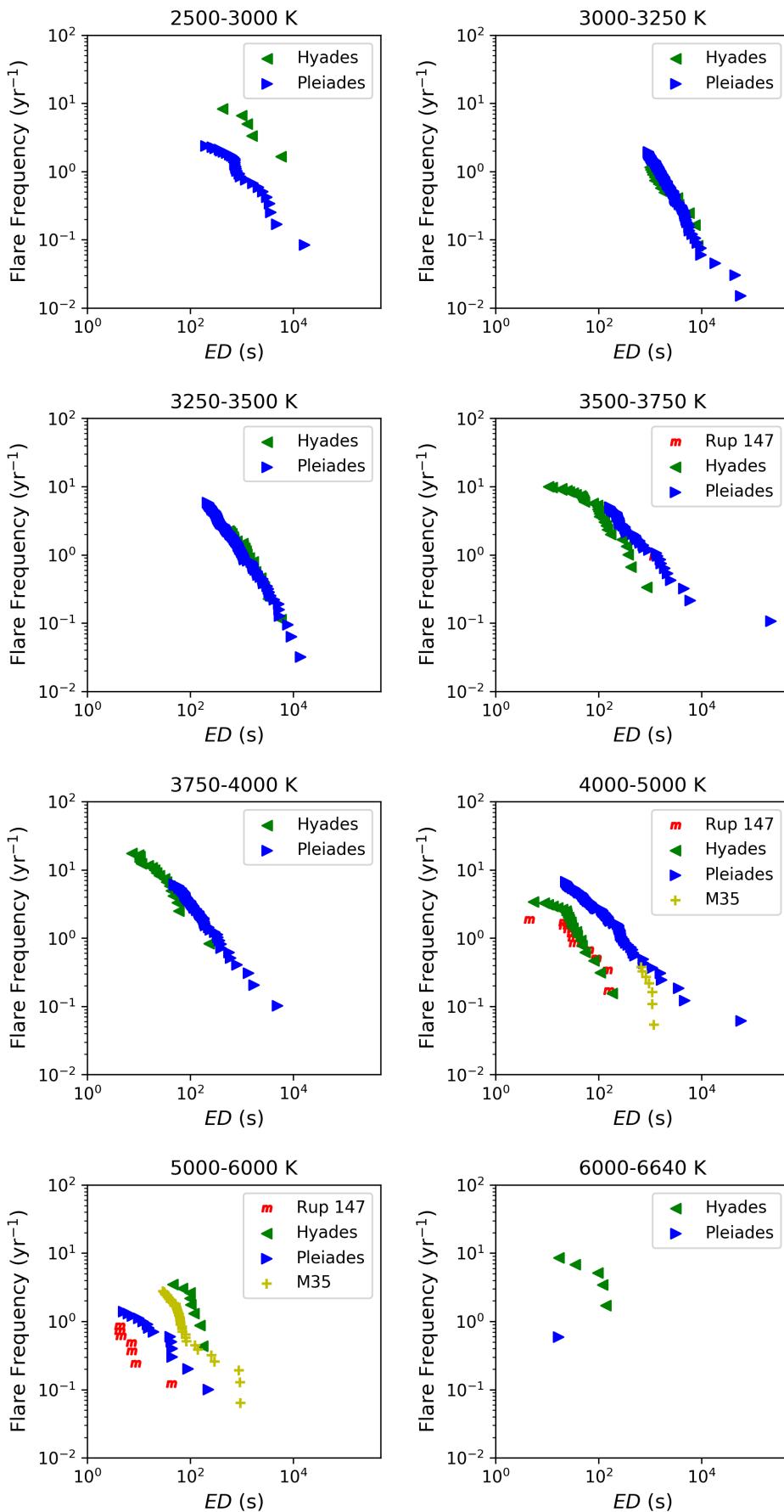


Fig. 5. Cumulative flare frequency distributions (FFDs) of equivalent durations (ED). In each panel, every distribution belongs to one cluster. The panels are binned by T_{eff} .

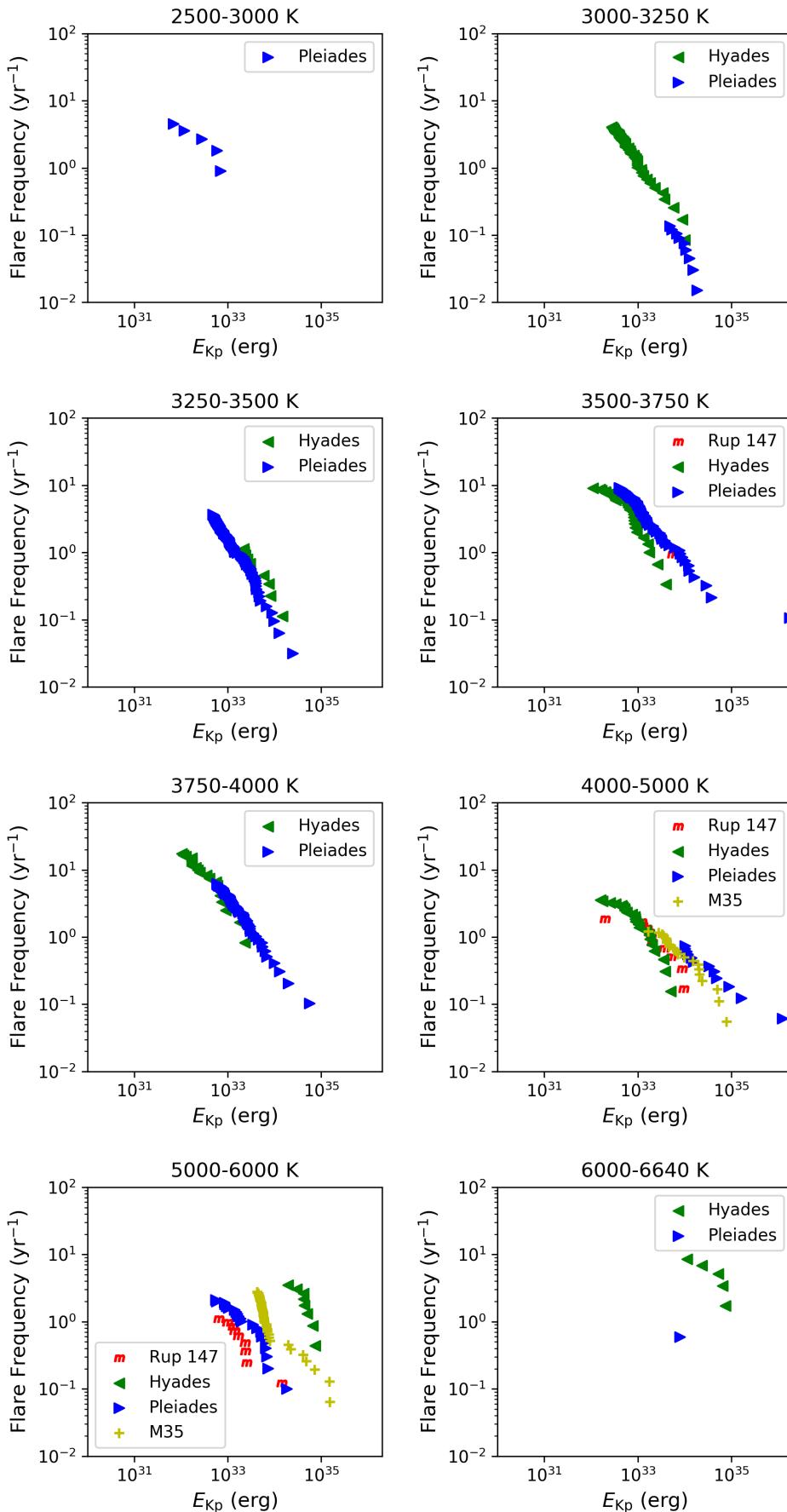


Fig. 6. Same as Fig. 5, but of Kepler flare energies $E_{\text{Kp,flare}}$.

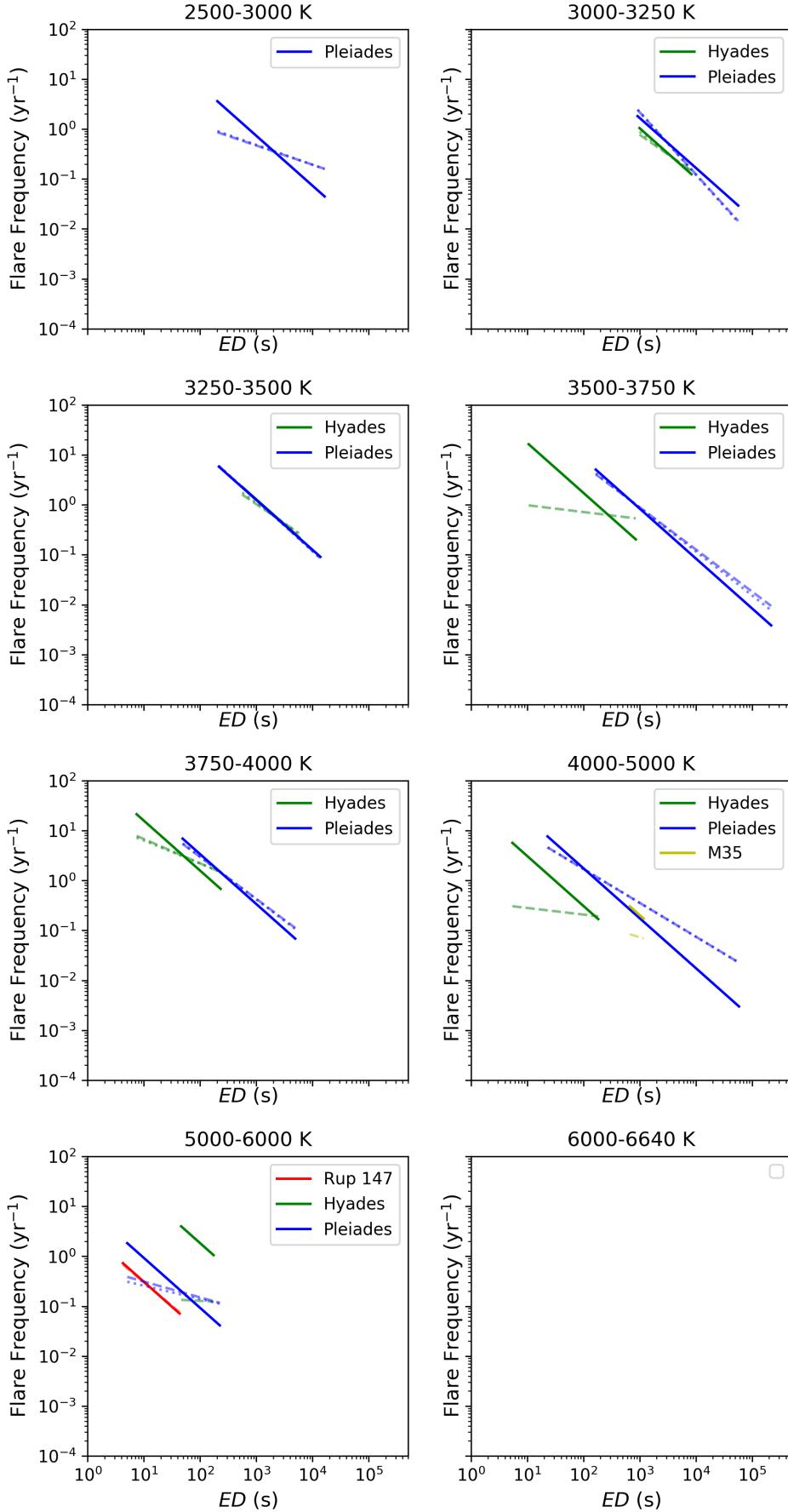


Fig. 7. Power law fits to the FFDs of ED in Fig. 5. Bold line: a power law with $\alpha = 2$. Dashed line: best fit parameters were determined following Maschberger & Kroupa (2009) (see Sec. XX). Dotted line: best fit parameters were determined following Bauke (2007) (see Sec. XX)

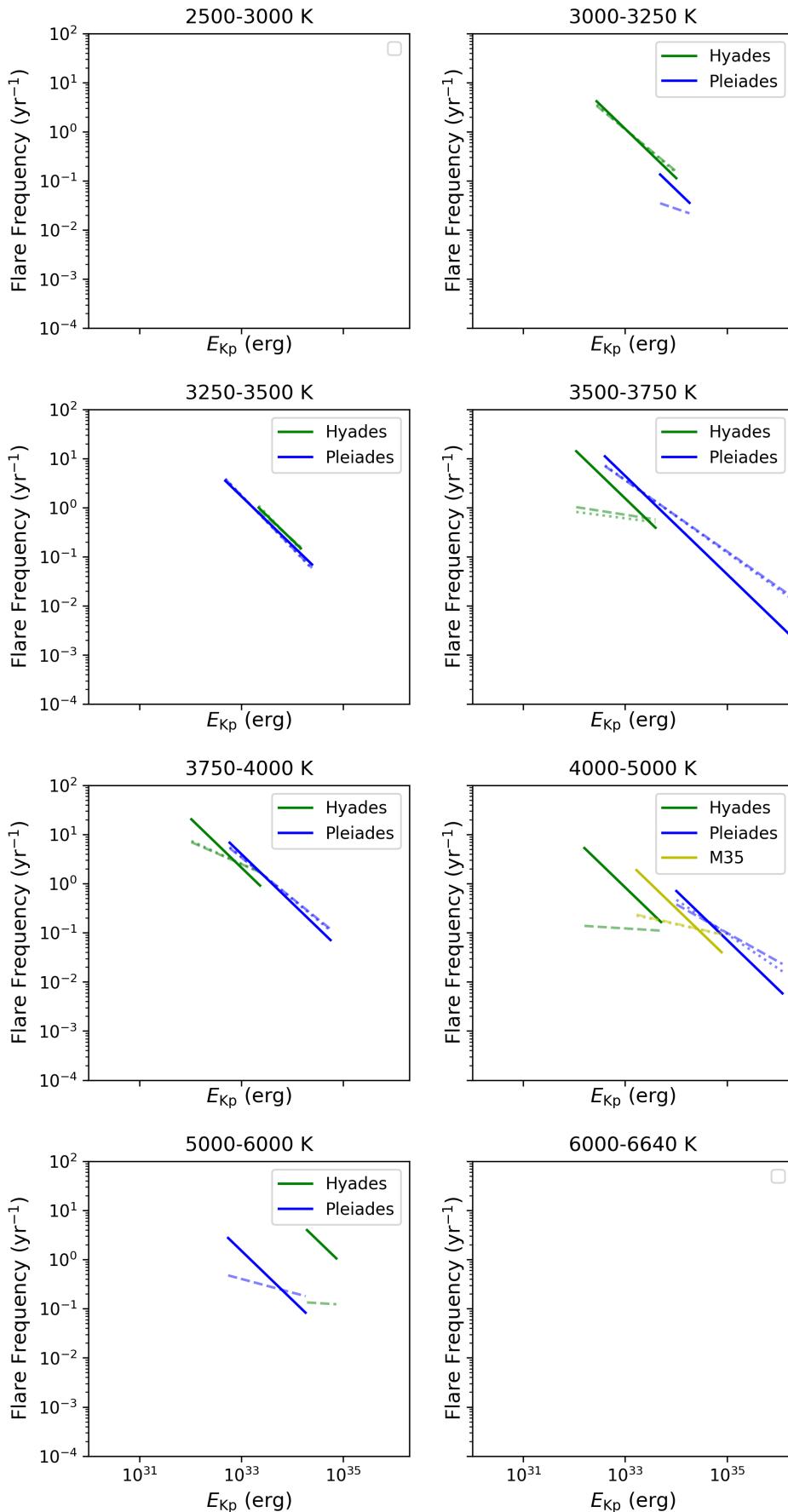


Fig. 8. Power law fits to the FFDs of $E_{Kp,\text{flare}}$ in Fig. 5. See Fig. 7 for details.

772 Appendix A: Membership probabilities

773 To match catalogs on RA and declination we used `astroML.crossmatch` tool for Python (Vanderplas et al. 2018)

774 For the studies with classifiers we assigned membership probabilities as follows. In Gonzalez (2016):

$$\begin{aligned} p(M(\text{member})) &= 0.9, \\ p(BM(\text{binary member})) &= 0.9, \\ p(N(\text{non-member})) &= 0.1, \\ p(SN(\text{single non-member})) &= 0.1, \\ p(BN(\text{binary non-member})) &= 0.1, \\ p(U(\text{unknown member})) &= 0.5. \end{aligned}$$

777 In Curtis et al. (2013):

$$\begin{aligned} p(Y(\text{highest confidence member})) &= 0.9, \\ p(P(\text{possible/probable member})) &= 0.7, \\ p(N(\text{not likely/non-member})) &= 0.7, \\ p(B(\text{photometry consistent with blue stragglers})) &= 0.0. \end{aligned}$$

778 In Rebull et al. (2017):

$$\begin{aligned} p((\text{best})) &= 0.9, \\ p((\text{ok})) &= 0.6, \\ p((\text{else})) &= 0.1. \end{aligned}$$

779 Members from Rebull et al. (2016a); Douglas et al. (2017); and
780 Gaia Collaboration et al. (2018a) were assigned $p = 0.9$ if they
781 appeared in the final catalog.
824
825 Table A.1 gives an overview over different membership catalogs.
826 Figure A.1 shows membership probability histograms of the
827 final sample broken down by membership source. Detailed intr
828 tions on how to reproduce the final sample of members in each
829 cluster, and corresponding tables, Python scripts, and Jupyter
830 notebooks can be found online⁵

788 Appendix B: Cluster parameters

789 Appendix C: Broadband photometry: quality cuts 790 and conversions

791 We required `flux/flux_error` ≥ 10 for Gaia G, BP, and RP
792 bands. We require that the 2MASS measurements for J, H, and
793 K to be "A". "A" means that measurements had $S/N > 10$ and
794 $\sigma < 0.11$. For PanSTARRS photometry, we required that the
795 QF_OBJ_GOOD quality filter flag was set.
796 SDSS and PS1 *ugrizy* bands are similar but not identical, but can
797 be converted using Table 2 in Finkbeiner et al. (2016).

798 Appendix D: Pixel saturation

799 Resolve different levels of pixel saturation (>1 , >10) and how
800 they contribute to the deviations from the single power law at
801 the highest energies.

⁵ <https://github.com/ekaterinailin/flares-in-clusters-with-k2-ii>

802 Appendix E: Solar system objects

803 Solar system objects (SSOs) produce brightness excursions in
804 K2 light curves that can closely resemble flare signatures. Often,
805 they can be distinguished by their symmetric rise and decay
806 shape as contrasted with the typical fast-rise gradual decay flare
807 shape (Davenport et al. 2014). M. H. Christiansen and colleagues
808 developed a routine called SkyBoT that matches positions and
809 times to passages of SSOs listed in YYY. RA, declination, start,
810 stop, and mid epochs of flares in BKJD are the input parameters.
811 We excluded all flare candidates that occurred within X minutes
812 of a SSO passage at the star's position. This procedure removed
813 ZZ% of all flare candidates. In the case of high energy flares, we
814 confirmed the passage by manually inspecting the pixel file with
815 the `lightkurve.interact` function for TargetPixelFiles.

816 Appendix F: Universality of power law exponent α

817 We compiled a exhaustive (?) table of previous work where
818 power laws were fitted to FFDs using different methods. Table
819 F.1 lists the overview. While particular studies consistently find
820 values above or below $\alpha \approx 2$, the comparison of different studies
821 points towards unresolved systematic errors in all these studies.

822 Appendix G: Expanding the likelihood

The rate λ_2 of flares with energies larger than S_2 is given in Wheatland (2004) as

$$\lambda_2 = \lambda_1 \cdot \left(\frac{S_1}{S_2} \right)^{\alpha-1}. \quad (\text{G.1})$$

S_1 denotes the energy above which all flares are detected. λ_1 is the corresponding rate. α remains the power law exponent of the flare frequency distribution.

We are also given the posterior distribution for the rate λ_2 of flares above S_2 in Eq. (20) in Wheatland (2004):

$$\begin{aligned} P_2(\lambda_2) &= \int_1^\infty d\alpha \int_0^\infty d\lambda_1 \delta\left(\lambda_2 - \lambda_1 \cdot \left(\frac{S_1}{S_2} \right)^{\alpha-1}\right) \\ &\quad \cdot P_1(\lambda_1) \cdot P_\alpha(\alpha) \end{aligned} \quad (\text{G.2})$$

As we have additional information in the form of uncertainties in our data $S = \{S_i, \lambda_i, \sigma_{S,i}\}$, we can expand Eq. G.2 with this knowledge. Assuming that the observed flare energies S_i with cumulative rates λ_i are distributed around the real flare energies $S_{0,i}$ with Gaussian uncertainties $\sigma_{S,i}$, we can define:

$$\begin{aligned} p(S_i|\lambda_1, \alpha, \sigma_{S,i}) &= \frac{1}{2\pi\sqrt{\sigma_{S,i}}} e^{-\frac{(S_i - S_{0,i})^2}{2\sigma_{S,i}^2}} \\ &\quad - \frac{\left(S_i - S_1 \left(\frac{\lambda_i}{\lambda_1} \right)^{-1/(\alpha-1)} \right)^2}{2\sigma_{S,i}^2} \end{aligned} \quad (\text{G.3})$$

We assume in Eq. G.3 that uncertainties on λ_1 are negligible. Eq. G.2 then reads:

$$\begin{aligned} P_2(\lambda_2) &= \int_1^\infty d\alpha \int_0^\infty d\lambda_1 \delta\left(\lambda_2 - \lambda_1 \cdot \left(\frac{S_1}{S_2} \right)^{\alpha-1}\right) \\ &\quad \cdot P_1(\lambda_1) \cdot P_\alpha(\alpha) \cdot P_S(S|\lambda_1, \alpha, \sigma_S) \end{aligned} \quad (\text{G.4})$$

Table A.1. Membership catalogs overview. No distance are given for Hyades we adopted individual distances for all members.

source	type	clusters covered	notes
Curtis et al. (2013)	classifier	Rup 147	
Douglas et al. (2014)	probability	Hyades, Praesepe	meta study
Bouy et al. (2015)	probability	M35	DANCe
Gonzalez (2016)	classifier	M67	
Rebull et al. (2016a)	members list	Pleiades	meta study
Rebull et al. (2017)	classifier	Praesepe	meta study
Douglas et al. (2017)	members list	Praesepe	meta study
Gaia Collaboration et al. (2018a)	members list	Hyades, M35, Rup 147, Pleiades, Praesepe	Gaia DR2, (1)
Cantat-Gaudin et al. (2018)	probability	M35, Rup147, Pleiades, Praesepe	Gaia DR2
Gao (2018)	probability	M67	Gaia DR2
Reino et al. (2018)	probability	Hyades	Gaia DR1, (1)
Olivares et al. (2018)	probability	Pleiades	Gaia DR2, DANCe
Olivares et al. (2019)	probability	Rup 147	Gaia DR2, DANCe

Notes. DANCe: DANCe membership study project. (1) Positions for Hyades were propagated to epoch 2000 using Gaia proper motions.

with

$$P_S(S|\lambda_1, \alpha, \sigma_S) = C \prod_{i=1}^M p(S_i|\lambda_1, \alpha, \sigma_{S,i}). \quad (\text{G.5})$$

835 C absorbs the normalization, or evidence term.

836 Following Wheatland (2004), we marginalize over λ_1 using the
837 δ function in G.4 to obtain

$$\begin{aligned} P_2(\lambda_2) &= \int_1^\infty d\alpha \cdot P_1\left(\lambda_2 \cdot \left(\frac{S_2}{S_1}\right)^{\alpha-1}\right) \cdot P_\alpha(\alpha) \\ &\cdot P_S\left(S|\lambda_2 \cdot \left(\frac{S_2}{S_1}\right)^{\alpha-1}, \alpha, \sigma_S\right) \end{aligned} \quad (\text{G.6})$$

838 Transforming P_S into a function of ϵ with $\lambda_1 = -\ln(1-\epsilon)/\Delta T$
839 yields:

$$\begin{aligned} P_S(S|\epsilon, \alpha, \sigma_S) &= C \prod_{i=1}^M p(S_i|\epsilon, \alpha, \sigma_{S,i}) \\ &= \frac{C}{\Delta T(1-\epsilon)} \\ &\cdot \prod_{i=1}^M \left[\frac{1}{2\pi\sqrt{\sigma_{S,i}}} e^{-\frac{\left(S_i - S_2 \left(\frac{-\ln(1-\epsilon)}{\Delta T\lambda_i}\right)^{1/(\alpha-1)}\right)^2}{2\sigma_{S,i}^2}} \right] \end{aligned} \quad (\text{G.7})$$

840 Finally, P_S enters the joint posterior distribution from Eq. 2, that
841 becomes

$$\begin{aligned} p(\epsilon, \alpha) &= C \cdot (-\ln(1-\epsilon)^M) \\ &\cdot (\alpha-1)^M \cdot \Gamma(\alpha) \left[\frac{(S_2/S_1)^{M+1}}{\pi} \right]^\alpha \\ &\cdot (1-\epsilon)^{(T/\Delta T) \cdot (S_2/S_1)^{\alpha-1}-1} \\ &\cdot P_S(S|\epsilon, \alpha, \sigma_S). \end{aligned} \quad (\text{G.8})$$

Table B.1. Non-exhaustive literature overview over OC parameters.

cluster	source	distance [pc]	age [Myr]	[Fe/H]
M35	adopted in this work:	861	$147.5 \pm^{13.5}_{13.5}$	-0.21 ± 0.10
M35	Bossini et al. (2019) ^a		$402.7 \pm^{13.5}_{0.9}$	
M35	Cantat-Gaudin et al. (2018)	861		
M35	Netopil et al. (2016)			-0.21
M35	Scholz et al. (2015)	830	151	
M35	Geller et al. (2010)		133	
M35	Meibom et al. (2009)		$147.5 \pm^{13.5}_{13.5}$	
M35	Bragaglia and Tosi (2006)	912		
M35	Steinhauser and Deliyannis (2004)			-0.143 ± 0.014
M35	Barrado (2001)		180	
M35	Barrado et al. (2001)			-0.21 ± 0.10
M35	Sung and Bessel (1999)	832		
Rup 147	adopted in this work:	305	$2650 \pm^{380}_{380}$	0.08 ± 0.07
Rup 147	Bragaglia et al. (2018)			0.08 ± 0.07
Rup 147	Cantat-Gaudin et al. (2018)	305		
Rup 147	Gaia Collaboration (2018)	309	$1995 \pm^{404}_{257}$	
Rup 147	Torres et al. (2018)	283	$2650 \pm^{380}_{380}$	
Rup 147	Curtis (2016) ^b			0.10 ± 0.02
Rup 147	Scholz et al. (2015)	270	1953	
Rup 147	Curtis et al. (2013)	300	$3125 \pm^{125}_{125}$	0.07 ± 0.03
Pleiades	adopted in this work:	135.6	$135 \pm^{25}_{25}$	-0.037 ± 0.026
Pleiades	Bossini et al. (2019) ^a		$86.5 \pm^{2.4}_{2.4}$	
Pleiades	Cantat-Gaudin et al. (2018)	135.6		
Pleiades	Gossage et al. (2018)		$135 \pm^{25}_{25}$	
Pleiades	Yen et al. (2018)	126.3	$141.3 \pm^{170}_{100}$	
Pleiades	Chelli and Duvert (2016)	139		
Pleiades	Netopil et al. (2016)			-0.01
Pleiades	Dahm (2015)		$112 \pm^{5}_{5}$	
Pleiades	Scholz et al. (2015)	130	120	
Pleiades	Conrad et al. (2014)			-0.037 ± 0.026
Pleiades	Melis et al. (2014)	136		
Pleiades	Bell et al. (2012)	135	125	
Praesepe	adopted in this work:	185.5	$750 \pm^{3}_{3}$	0.16
Praesepe	Bossini et al. (2019)		$750 \pm^{3}_{7}$	
Praesepe	Cantat-Gaudin et al. (2018)	185.5		
Praesepe	Gossage et al. (2018)		590	
Praesepe	Yen et al. (2018)	183	$794 \pm^{253}_{269}$	
Praesepe	Netopil et al. (2016)			0.16
Praesepe	Scholz et al. (2015)	187	832	
Praesepe	Boesgaard et al. (2013)			0.12
Praesepe	Boudreault et al. (2012)	160	630	
Praesepe	Salaris et al. (2004)	175	650	
M67	adopted in this work:	908	$3639 \pm^{17}_{17}$	$-0.102 \pm .081$
M67	Bossini et al. (2019)		$3639 \pm^{17}_{17}$	
M67	Netopil et al. (2016)			0.03
M67	Scholz et al. (2015)		$3428 \pm^{147}_{72}$	
M67	Conrad et al. (2014)			$-0.102 \pm .081$
M67	Dias et al. (2012)	908	4300	
M67	Oñehag et al. (2011)	880	4200	0.02
Hyades	adopted in this work: ^c		$690 \pm^{160}_{100}$	0.13 ± 0.02
Hyades	Gaia Collaboration (2018)		$690 \pm^{160}_{100}$	
Hyades	Gossage et al. (2018)		680	
Hyades	Liu et al. (2016)			± 0.02
Hyades	Netopil et al. (2016)			0.13
Hyades	Taylor and Joner (2005)			0.103 ± 0.008
Hyades	Cummings et al. (2005)			0.146 ± 0.004
Hyades	Salaris et al. (2004)		650	0.15
Hyades	Perryman et al. (1998)		$625 \pm^{50}_{50}$	
Hyades	Martin et al. (1998)		$650 \pm^{70}_{70}$	

Article number, page 20 of 22
Notes. ^(a) Bossini et al. (2019) noted some caveats for their determination of ages of young clusters, for which they used Gaia DR2 photometry for isochrone fitting. ^(b) Curtis (2016) reanalysed HIRES spectra using an improved spectroscopic method as compared to Curtis et al. (2013). ^(c) We did not adopt a mean value for the Hyades distance because the cluster members are on average closer than 50 pc.

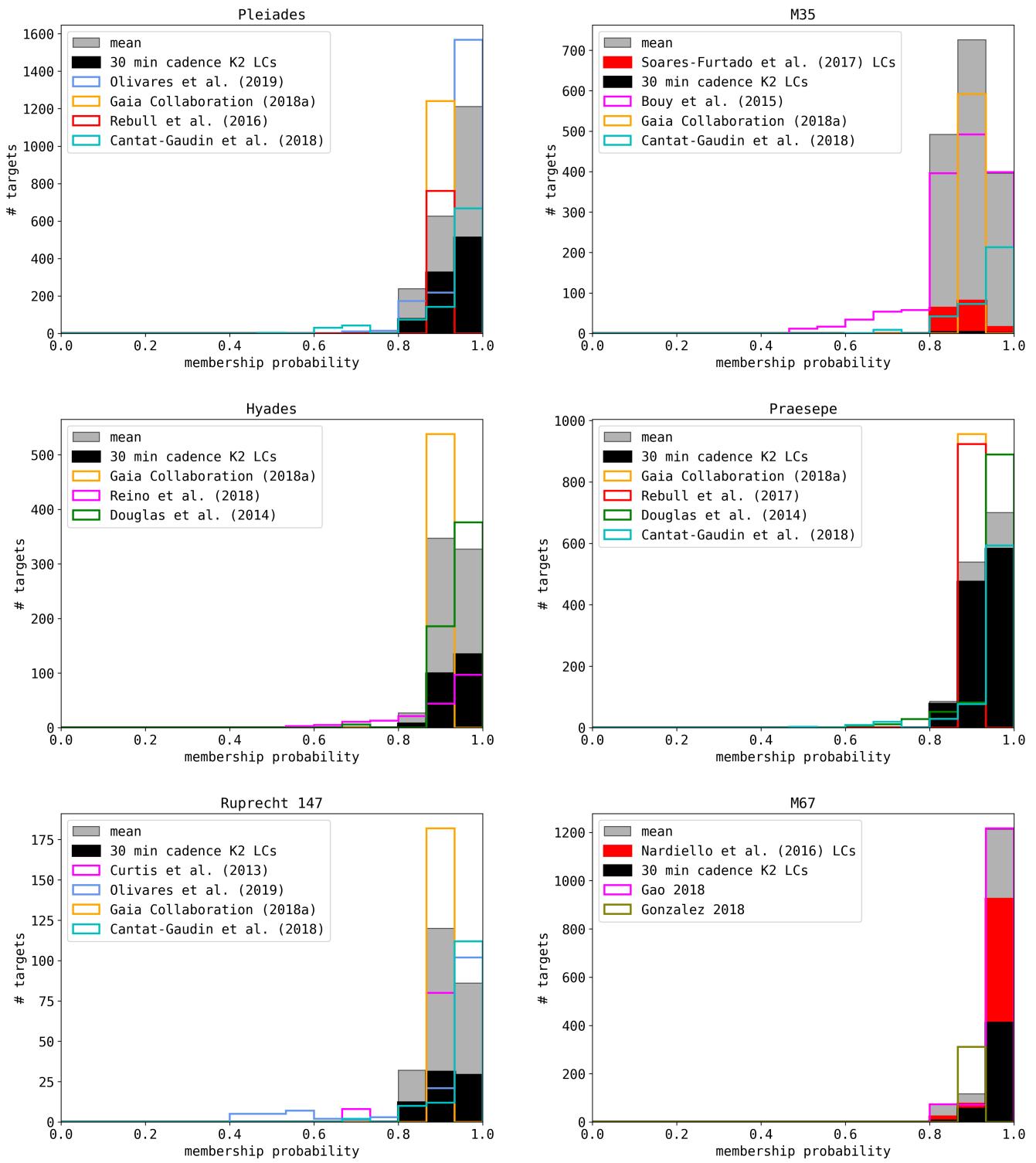


Fig. A.1. Membership histograms.

Table F.1. Literature overview over power law fitting approaches to FFDs.

Who	method	data	$\alpha - 1$
Hawley et al. (2014)	LSq with Poisson uncertainty, increase the low energy limit until the fit is robust		
Davenport (2016)	weighted LSq, asymmetric Poisson confidence intervals following Gehrels1986		
Gizis (2017)	de-biased MLE (Arnold2015), weight each point with $\text{sqrt}(N)$ in each bin (Clauset+2009)		
Paudel et al. (2018)	ML from a paper in 2010, used emcee (Foreman-Mackey2013)		
Lacy (1976)	graphical, linear LSq	386 flares on UV Cetis	.43-1.
Güdel et al.(2003)	-		
Davenport et al. (2012)	Fit $\log_{10} Y = \alpha + (\beta \log_{10} X)(10 - \gamma/(X + \delta))$	~50,000 M dwarfs from SDSS and 1321 M dwarfs from 2MASS	.9-2.1
Lurie et al. (2015)	Bayesian Markov chain Monte Carlo based algorithm (Kelly 2007) for linear regression	2 dMe5 dwarfs	.92-1.03
Audard et al. (2000)	Crawford+1970 MLE (Jauncey-style)	EUVE 12 F-M type stars, 10-20 flares each	.46-1.61
Shakhovskaia (1989)	linear representation, power laws from Gershberg/Shakhovskaya1983	30-40 dK0-dM8, 200 flares	.4-1.4
Yang et al. (2017)	binned FFDs	103187 flares on 540 M-type dwarfs in Kepler	1.07 +/- 0.35
Howard et al. (2018)			