```
%matplotlib inline
[1]
     from os import listdir
      from os.path import isfile, join
      import matplotlib.pyplot as plt
      from collections import Counter
      import math
      from collections import Counter
      import numpy as np
      from scipy.special import comb
      import itertools as it
     %load_ext line_profiler
      from imp import reload
      import itertools as it
      import pandas as pd
      import seaborn as sns
      import sys
      sys.path.insert(0, '../mallows kendall')
      import mallows_kendall as mk
      import cego_lop as cego
      from IPython.core.display import display, HTML
     display(HTML("<style>.container { width:90% !important; }
      </style>"))
```

References

- http://www.spotseven.de/wp-content/papercite-data/pdf/zaef14c.pdf
- https://dl.acm.org/doi/pdf/10.1145/2576768.2598282
- https://pubsonline.informs.org/doi/10.1287/ijoc.1120.0506
- https://link.springer.com/article/10.1007/s11721-015-0106-x

falta encontrar donde habia uno con el LOP

LOP instance generator

The instances M follow this distribution $M_{\phi}[i,j]$

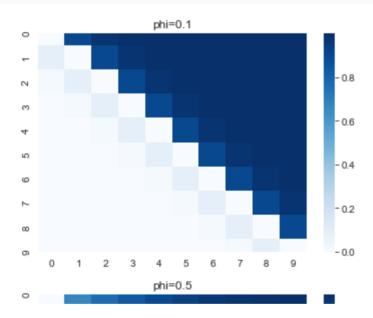
$$M_{\phi}[i,j] = h(j-i+1,\phi) - h(j-i,\phi),$$

where

$$h(k,\phi) = k/(1-\phi^k).$$

Taking different values of ϕ we controll the uniformity of M:

```
[49]
      def h(k,phi):
        if (1-phi**k) == 0 :
          return 0
        return k/(1-phi**k)
        \#h(k, \pi) = k/(1-\pi)
      def mij(i,j,phi):
        return h(j-i+1,phi) - h(j-i,phi)
            \#h(j-i+1,\phi) - h(j-i,\phi)
      n = 10
      for phi in [0.1,0.5,0.7,0.9,0.999]:
        M = np.zeros((n,n))
        for i in range(n):
          for j in range(i+1,n):
            M[i,j] = mij(i,j,phi)
            M[j,i] = 1-M[i,j]
        g = sns.heatmap(M, cmap="Blues")
        g.set_title("phi="+str(phi))
        plt.show()
```



Do similar permutations have similar fitness?

In this experiment we analyse wether similar permutations in terms of Kendall distance have similar fitness funtion evaluation in the LOP instances. The process is as follows:

do 100 times:

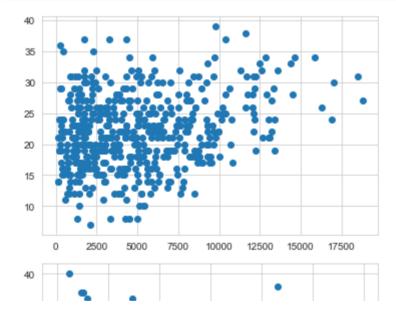
```
1. a,b = generate two u.a.r. permutations  
2. let x=|f(a)-f(b)|  
3. let y=d(a,b)
```

4. draw a point in (x, y)

We see that:

- permutations that are very different in fitness are distant
- permutations that are similar can have similar or differnt fitness values

```
for phi_instance in [0.5,0.7,0.9]:
    instance = cego.synthetic_LOP(n,1000,phi_instance)
    xs, ys = [],[]
    for repes in range(500):
        a,b =
    np.random.permutation(range(n)),np.random.permutation(range(n))
        #cego.get_fitness(a, instance,"LOP"), cego.get_fitness(b, instance,"LOP"), mk.kendallTau(a,b)
        xs.append(abs(cego.get_fitness(a, instance,"LOP")) -
    cego.get_fitness(b, instance,"LOP")))
        ys.append(mk.kendallTau(a,b))
    plt.scatter(xs,ys)
    plt.show()
```



running experimtns

How to run one experiment with a particular parameter configuration

```
reload(cego)
n = 10
m_max = 50
```

```
repe = 0
#m_ini = 10
phi_instance = 0.8
budgetGA = 25

cego.run_and_save(n,repe,phi_instance, budgetGA,m_max=m_max)
```

```
df = pd.read_pickle('pickles/pickLocal.pkl')#pick275670.pkl
[3]
       color_variable = 'Solver'
       y_variables = ['Fitness','Distance']
       palette = sns.color_palette("husl",
        len(df[color_variable].drop_duplicates()))
        for y_variable in y_variables:
             plt.figure(figsize=(15,5))
             sns.lineplot(x='Sample
       size',y=y_variable,hue='Solver',data=df, palette=palette)
             plt.show()
         0.9
       Fitness
                                                                                           CEGO
                                                                                           uMM, rho= 1e-06
                                                                                           uMM, rho= 1e-05
         0.7
                                                                                           uMM, rho= 0.0001
                                                                                           uMM, rho= 0.001
                                                                                           uMM, rho= 0.01
                                                                                           uMM, rho= 0.1
         0.6
                                                                                           uMM, rho= 0.2
                                                                                           uMM, rho= 0.3
                                                20
                                                     Sample size
         40
                                                                                           CEGO
         35
                                                                                           uMM, rho= 1e-06
                                                                                           uMM, rho= 1e-05
                                                                                           uMM, rho= 0.0001
         30
                                                                                           uMM, rho= 0.001
                                                                                           uMM, rho= 0.01
         25
                                                                                           uMM, rho= 0.1
                                                                                           uMM, rho= 0.2
```

Plot the results

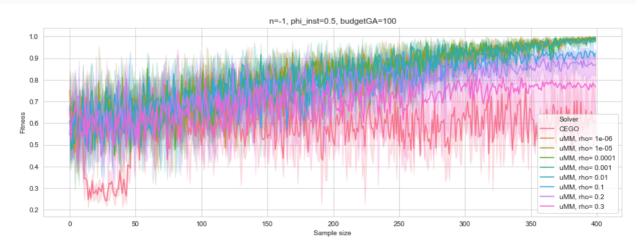
```
df = pd.concat([pd.read_pickle("pickles/"+f) for f in
    listdir("pickles") if (f.endswith(".pkl")and "Local" not in f)]
)
df
```

0	0.673686	LOP	CEGO	0	0	100.0	19

1	0.429744 Fitness	LOP Problem	CEGO Solver	1 Sample	0	100.0 budgetGA	30 Dis
2	0.742816	LOP	CEGO	₂ size	repe 0	100.0	15
3	0.649583	LOP	CEGO	3	0	100.0	20
4	0.636075	LOP	CEGO	4	0	100.0	21
•••			•••				
395	0.920394	LOP	uMM, rho=	395	3	NaN	8

```
[20] df['n']=-1
df['budgetGA'] = 100
```

```
[24]
      sns.set_style("whitegrid")
      color_variable = 'Solver'
      y_variables = ['Fitness','Distance']
      palette = sns.color_palette("husl",
      len(df[color_variable].drop_duplicates()))
      for phi_i in df.phi_instance.drop_duplicates().values:
        for n in df.n.drop_duplicates().values:
          for budgetGA in df.budgetGA.drop_duplicates().values:
            for y_variable in y_variables:
                plt.figure(figsize=(15,5))
                aux = df[(df.phi_instance==phi_i) & (df.n==n) &
      (df.budgetGA==budgetGA) ] #& (df.repe==0)
                g = sns.lineplot(x='Sample
      size',y=y_variable,hue='Solver',data=aux, palette=palette)
                g.set_title('n='+str(n)+', phi_inst='+str(phi_i)+',
      budgetGA='+str(budgetGA))
                plt.show()
```



```
true_sol = list(range(n))
instance = cego.synthetic_LOP(n,m_inst,phi_instance)
print("best* fitness",cego.get_fitness(true_sol,
instance,problem),"worst*
fitness",cego.get_fitness(true_sol[::-1], instance,problem),"
    (*distributed according to)")

dfcego = cego.runCEGO(n,instance, m_ini = m_ini, m =
    ms,repe=repe, best_known_sol=true_sol)
    dfuMM = cego.solve_one_umm("LOP",instance,ms, rho, repe,
        m_ini, phi_ini,true_sol)
    df = pd.concat([dfuMM,dfcego],sort=False)
    df['best'] = cego.get_fitness(true_sol, instance,problem)
    df['worst'] = cego.get_fitness(true_sol[::-1],
    instance,problem)
```

	Problem	Solver	repe	Sample size	rho	Fitness	phi_estin
0	LOP	uMM, \rho= 0.001	0	0	0.001	0.719931	0.718161
1	LOP	uMM, \rho= 0.001	0	1	0.001	0.651240	0.776211
2	LOP	uMM, \rho= 0.001	0	2	0.001	0.626840	0.789803

TODO

- meter más problemas: PFSP, TSP, ...
- comparar con otras alternativas: LS?
- el símil con la optimización bayesiana no está claro, cómo se traslada aquí la función de utilidad?
- demostración de convergencia rápida
- escribir draft para tener el modelo claro

[]