Problem Set 5

Ekkapot Charoenwanit
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Problem 5.1. Binary Insertion Sort

1) In the vanilla version of insertion sort we discussed in the lecture, at any iteration i, we have to traverse the entire subarray $A[1...i-1]$ in the worst case to look for the correct position to place the key $A[i]$ into. How do you apply binary search to improve this? Also analyze the running time in the worst case of your binary insertion sort algorithm.

2) In your binary insertion sort algorithm that you proposed in 1), how many comparisons do you need in the worst case and how many swaps do you need in the worst case?

Problem 5.2. Quick Sort

1) What is the running time of quick sort when all the array elements have the same value?

2) Modify the algorithm of quick sort presented in the lecture so that it sorts an array in non-increasing order.

3) Under which extreme situations does the running time of quick sort end up in the worst case?

Hint: Look at the recurrence of the running time of quick sort and see what causes such a worst-case situation.

Problem 5.3. Divide and Conquer

1) Write a recurrence for the number of scalar additions for Strassen's Algorithm using asymptotic notation (not in the exact form).

2) Solve the recurrence using the recursion tree method and confirm your answer with Master theorem.