

$$A_1 \cdot A_2 \cdot A_3 \cdot A_4$$

$$5 \times 4 \quad 4 \times 6 \quad 6 \times 2 \quad 2 \times 7$$

$$m[1,1] = 0$$

$$m[2,2] = 0$$

$$m[3,3] = 0$$

$$m[4,4] = 0$$

m

	1	2	3	4
1	0	120	84	158
2		0	48	104
3			0	84
4				0

$A_1 \cdot A_2$

$$m[1,2] = 5 \times 4 \times 6 = 120$$

→ split at 1:  $s[1,2] = 1$

$A_2 \cdot A_3$

$$m[2,3] = 4 \times 6 \times 2 = 48$$

→ split at 2:  $s[2,3] = 2$

$A_3 \cdot A_4$

$$m[3,4] = 6 \times 2 \times 7 = 84$$

→ split at 3:  $s[3,4] = 3$

s

	1	2	3	4
1		1	1	3
2			2	3
3				3
4				

$A_1 \cdot A_2 \cdot A_3$

$m[1,3]$

$(A_1 \cdot A_2) \cdot A_3$

$A_1 \cdot (A_2 \cdot A_3)$

$$m[1,1] + m[2,3] + 5 \times 4 \times 2$$

$$0 + 48 + 40 = 84$$

$$m[1,2] + m[3,3] + 5 \times 6 \times 2$$

$$120 + 0 + 60 = 180$$

$\min(84, 180) = 84$

Split at 1:  $s[1,3] = 1$

$(A_1 \cdot A_2 \cdot A_3) \cdot A_4$

$(A_1) \cdot (A_2 \cdot A_3)$

$A_2 \cdot A_3$

$[A_2, A_3, A_4]$

$m[2,4]$

$A_2 \cdot (A_3 \cdot A_4)$

$$m[2,2] + m[3,4] + 4 \times 6 \times 7$$

$$0 + 84 + 168 = 252$$

$(A_2 \cdot A_3) \cdot A_4$

$$m[2,3] + m[4,4] + 4 \times 2 \times 7$$

$$98 + 0 + 56 = 154$$

$$\min(252, 154)$$

split at 3:  $S[2,4] = 3$ .

$m[4,4]$

$A_1 \cdot A_2 \cdot A_3 \cdot A_4$

$$= \min \left\{ \begin{array}{l} 0 + 104 + 140 = 244 \\ m[1,1] + m[2,4] + 5 \times 4 \times 7 \\ 120 + 84 + 210 = 414 \\ m[1,2] + m[3,4] + 5 \times 6 \times 7 \\ 88 + 0 + 210 = 398 \\ m[1,3] + m[4,4] + 5 \times 7 \times 7 \\ 158 \end{array} \right\} = 158$$

$A_1(A_2 \cdot A_3 \cdot A_4)$

$(A_1 \cdot A_2) \cdot A_3 \cdot A_4$

split at 3:  
 $S[4,4] = 3$

$(A_1 \cdot A_2) \cdot (A_3 \cdot A_4)$