## Programming Lab 2: The Pthreads Library

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## Problem 2.1. The Trapezoidal Rule

The definite integral from a to b of a non-negative function f(x) can be though of as the area bounded by the x-axis, the vertical lines x = a and x = b, and the graph of the function f(x). See Figure 1.

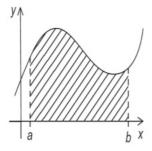


Figure 1: Definite Integral of a non-negative function

One approach to estimating this area of integral is to partition the region into **regular geometric** shapes and then add the areas of these shapes. In the trapezoidal rule, the regular geometric shapes are **trapezoids**; each trapezoid has its base on the x-axis, vertical sides and its top edge joining two points on the graph of f(x). See Figure 2.

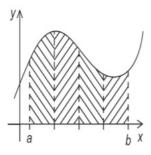


Figure 2: Trapezoids approximating definite integral

For our purposes, we will choose all the bases to have the same width. So if there are n trapezoids, the base of each will be  $h = \frac{(b-1)}{n}$ . The base of the leftmost trapezoid will be the interval [a, a+h]; the base of the next trapezoid will be [a+h, a+2h]; the next, [a+2h, a+3h]; etc. In general, the base of the  $i^{th}$ 

trapezoid will be [a+ih, a+(i+1)h], i=0,...,n-1. In order to simplify notation, let  $x_i$  denote a+ih, i=0,...,n-1. Then, the length of the left side of the  $i^{th}$  trapezoid will be  $f(x_i)$ , and its right side will be  $f(x_{i+1})$ . See Figure 3.

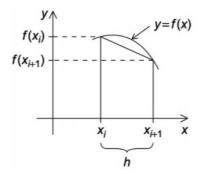


Figure 3: The  $i^{th}$  trapezoid

Thus, the area of the  $i^{th}$  trapezoid will be:

$$\frac{1}{2}h[f(x_i + f(x_{i+1}))]$$

and the area of our entire approximation will be the sum of the areas of the trapezoids:

$$\begin{split} &\frac{1}{2}h[f(x_0+f(x_1)]+\frac{1}{2}h[f(x_1+f(x_2))]+\ldots+\frac{1}{2}h[f(x_{n-1}+f(x_n))]\\ &=\frac{h}{2}[f(x_0)+2f(x_1)+2f(x_2)+\ldots+2f(x_{n-1})+f(x_n)]\\ &=[\frac{f(x_0)}{2}+\frac{f(x_n)}{2}+f(x_1)+f(x_2)+\ldots f(x_{n-1})]h \end{split}$$

Implement a serial and a parallel program that estimate the definite integral  $\int_{a=0}^{b=100} x^2 dx$  using the Pthreads library.

## Problem 2.2. Complexity Analysis

- 1) Derive the running time (in terms of the number of trapezoids n) of the serial algorithm that you implemented in Problem 2.1.
- 2) Derive the running time of the parallel algorithm that you implemented in Problem 2.1. State your assumption(s) as necessary

## Problem 2.3. Experimental Analysis

Measure the running times of the serial and the parallel program in Problem 2.1 for different values of n and different numbers of processors p. Plot the speedup curves. Also state the following parameters of the machine on which you carry out your experiment:

- the number of cores
- the number of threads per core (in case hyperthreading is enabled)

Avoid oversubscribing threads to cores.