

# Programming Lab 2: The Pthreads Library

Ekkapot Charoenwanit  
Course: Parallel Computing

February 18, 2021

## Problem 2.1. The Trapezoidal Rule

The definite integral from  $a$  to  $b$  of a non-negative function  $f(x)$  can be thought of as the area bounded by the x-axis, the vertical lines  $x = a$  and  $x = b$ , and the graph of the function  $f(x)$ . See Figure 1.

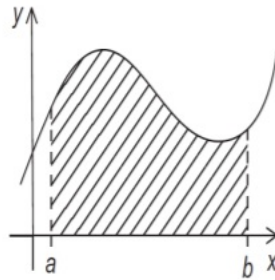


Figure 1: Definite Integral of a non-negative function

One approach to estimating this area of integral is to partition the region into **regular geometric shapes** and then add the areas of these shapes. In the trapezoidal rule, the regular geometric shapes are **trapezoids**; each trapezoid has its base on the x-axis, vertical sides and its top edge joining two points on the graph of  $f(x)$ . See Figure 2.

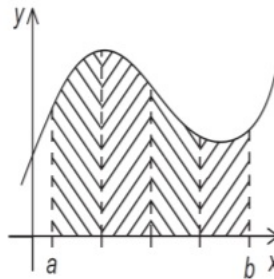


Figure 2: Trapezoids approximating definite integral

For our purposes, we will choose all the bases to have the same width. So if there are  $n$  trapezoids, the base of each will be  $h = \frac{(b-a)}{n}$ . The base of the leftmost trapezoid will be the interval  $[a, a + h]$ ; the base of the next trapezoid will be  $[a + h, a + 2h]$ ; the next,  $[a + 2h, a + 3h]$ ; etc. In general, the base of the  $i^{th}$

trapezoid will be  $[a + ih, a + (i + 1)h]$ ,  $i = 0, \dots, n - 1$ . In order to simplify notation, let  $x_i$  denote  $a + ih$ ,  $i = 0, \dots, n - 1$ . Then, the length of the left side of the  $i^{th}$  trapezoid will be  $f(x_i)$ , and its right side will be  $f(x_{i+1})$ . See Figure 3.

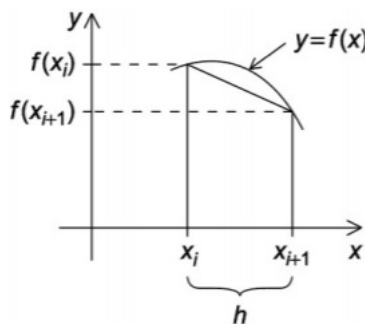


Figure 3: The  $i^{th}$  trapezoid

Thus, the area of the  $i^{th}$  trapezoid will be:

$$\frac{1}{2}h[f(x_i) + f(x_{i+1})]$$

and the area of our entire approximation will be the sum of the areas of the trapezoids:

$$\begin{aligned} & \frac{1}{2}h[f(x_0) + f(x_1)] + \frac{1}{2}h[f(x_1) + f(x_2)] + \dots + \frac{1}{2}h[f(x_{n-1}) + f(x_n)] \\ &= \frac{h}{2}[f(x_0) + 2f(x_1) + 2f(x_2) + \dots + 2f(x_{n-1}) + f(x_n)] \\ &= \left[\frac{f(x_0)}{2} + \frac{f(x_n)}{2} + f(x_1) + f(x_2) + \dots + f(x_{n-1})\right]h \end{aligned}$$

Implement a serial and a parallel program that estimate the definite integral  $\int_{a=0}^{b=10} x^2$  using the Pthreads library.

### Problem 2.2. Complexity Analysis

- 1) Derive the running time (in terms of the number of trapezoids  $n$ ) of the serial algorithm that you implemented in Problem 2.1.
- 2) Derive the running time of the parallel algorithm that you implemented in Problem 2.1. State your assumption(s) as necessary

### Problem 2.3. Experimental Analysis

Measure the running times of the serial and the parallel program in Problem 2.1 for different values of  $n$  and different numbers of processors  $p$ . Plot the speedup curves. Also state the following parameters of the machine on which you carry out your experiment:

- the number of cores
- the number of threads per core (in case hyperthreading is enabled)

Avoid oversubscribing your machine.