

3d) Rewrite a program that generates random square matrices of order  $2^n$ . Implement using the three methods discussed in class:

## C Code:

```
#include <stdio.h>
#include <stdlib.h>
#include <me.h>
int **alloc_matrix(int n) {
    int **mat = (int **)malloc(n * sizeof(int *));
    for (int i = 0; i < n; i++)
        mat[i] = (int *)malloc(n * sizeof(int));
    return mat;
}
void free_matrix(int **mat, int n) {
    for (int i = 0; i < n; i++) free(mat[i]);
    free(mat);
}
void fill_matrix(int **mat, int n) {
    for (int i = 0; i < n; i++)
        for (int j = 0; j < n; j++)
            mat[i][j] = rand() % 10;
}
void copy_matrix(int **src, int **dst, int n) {
    for (int i = 0; i < n; i++)
        for (int j = 0; j < n; j++) dst[i][j] = src[i][j];
}
void add_matrix(int **A, int **B, int **C, int n) {
    for (int i = 0; i < n; i++)
        for (int j = 0; j < n; j++)
            C[i][j] = A[i][j] + B[i][j];
}
void sub_matrix(int **A, int **B, int **C, int n) {
    for (int i = 0; i < n; i++)
        for (int j = 0; j < n; j++)
            C[i][j] = A[i][j] - B[i][j];
}
// --- Iterative ---
void mul_iterative(int **A, int **B, int **C, int n) {
    for (int i = 0; i < n; i++)
        for (int j = 0; j < n; j++) {
            C[i][j] = 0;
            for (int k = 0; k < n; k++)
                C[i][j] += A[i][k] * B[k][j];
        }
}
// --- Recursive ---
void mul_recursive_util(int **A, int **B, int **C, int n,
    int a_row, int a_col, int b_row, int b_col,
    int c_row, int c_col) {
```

```

if (n == 1) {
C[c_row][c_col] += A[a_row][a_col] * B[b_row][b_col];
return;
}
int half = n / 2;
mul_ply_recursive_u l(A, B, C, half, a_row, a_col, b_row, b_col, c_row, c_col);
mul_ply_recursive_u l(A, B, C, half, a_row, a_col + half, b_row + half, b_col, c_row, c_col);
mul_ply_recursive_u l(A, B, C, half, a_row, a_col, b_row, b_col + half, c_row, c_col + half);
mul_ply_recursive_u l(A, B, C, half, a_row, a_col + half, b_row + half, b_col + half, c_row,
c_col + half);
mul_ply_recursive_u l(A, B, C, half, a_row + half, a_col, b_row, b_col, c_row + half, c_col);
mul_ply_recursive_u l(A, B, C, half, a_row + half, a_col + half, b_row + half, b_col, c_row +
half, c_col);
mul_ply_recursive_u l(A, B, C, half, a_row + half, a_col, b_row, b_col + half, c_row + half,
c_col + half);
mul_ply_recursive_u l(A, B, C, half, a_row + half, a_col + half, b_row + half, b_col + half,
c_row + half, c_col + half);
}
void mul_ply_recursive(int **A, int **B, int **C, int n) {
for (int i = 0; i < n; i++)
for (int j = 0; j < n; j++)
C[i][j] = 0;
mul_ply_recursive_u l(A, B, C, n, 0, 0, 0, 0, 0, 0);
// --- Strassen ---
void strassen(int **A, int **B, int **C, int n) {
if (n <= 2) {
mul_ply_iterative(A, B, C, n);
return;
}
int k = n / 2;
int **A11 = alloc_matrix(k), **A12 = alloc_matrix(k),
**A21 = alloc_matrix(k), **A22 = alloc_matrix(k);
int **B11 = alloc_matrix(k), **B12 = alloc_matrix(k),
**B21 = alloc_matrix(k), **B22 = alloc_matrix(k);
int **C11 = alloc_matrix(k), **C12 = alloc_matrix(k),
**C21 = alloc_matrix(k), **C22 = alloc_matrix(k);
int **M1 = alloc_matrix(k), **M2 = alloc_matrix(k), **M3 = alloc_matrix(k),
**M4 = alloc_matrix(k), **M5 = alloc_matrix(k), **M6 = alloc_matrix(k),
**M7 = alloc_matrix(k);
int **T1 = alloc_matrix(k), **T2 = alloc_matrix(k);
for (int i = 0; i < k; i++) {
for (int j = 0; j < k; j++) {
A11[i][j] = A[i][j];
A12[i][j] = A[i][j + k];
A21[i][j] = A[i + k][j];
A22[i][j] = A[i + k][j + k];
B11[i][j] = B[i][j]; B12[i][j] = B[i][j + k];
B21[i][j] = B[i + k][j];
B22[i][j] = B[i + k][j + k];
}
}
add_matrix(A11, A22, T1, k); add_matrix(B11, B22, T2, k); strassen(T1, T2, M1, k);

```

```

add_matrix(A21, A22, T1, k); strassen(T1, B11, M2, k);
sub_matrix(B12, B22, T2, k); strassen(A11, T2, M3, k);
sub_matrix(B21, B11, T2, k); strassen(A22, T2, M4, k);
add_matrix(A11, A12, T1, k); strassen(T1, B22, M5, k);
sub_matrix(A21, A11, T1, k); add_matrix(B11, B12, T2, k); strassen(T1, T2, M6, k);
sub_matrix(A12, A22, T1, k); add_matrix(B21, B22, T2, k); strassen(T1, T2, M7, k);
for (int i = 0; i < k; i++) {
for (int j = 0; j < k; j++) {
C11[i][j] = M1[i][j] + M4[i][j] - M5[i][j] + M7[i][j];
C12[i][j] = M3[i][j] + M5[i][j];
C21[i][j] = M2[i][j] + M4[i][j];
C22[i][j] = M1[i][j] - M2[i][j] + M3[i][j] + M6[i][j];
}
}
for (int i = 0; i < k; i++) {
for (int j = 0; j < k; j++) {
C[i][j] = C11[i][j];
C[i][j + k] = C12[i][j];
C[i + k][j] = C21[i][j]; C[i + k][j + k] = C22[i][j];
}
}
free_matrix(A11, k); free_matrix(A12, k); free_matrix(A21, k); free_matrix(A22, k);
free_matrix(B11, k); free_matrix(B12, k); free_matrix(B21, k); free_matrix(B22, k);
free_matrix(C11, k); free_matrix(C12, k); free_matrix(C21, k); free_matrix(C22, k);
free_matrix(M1, k); free_matrix(M2, k); free_matrix(M3, k); free_matrix(M4, k);
free_matrix(M5, k); free_matrix(M6, k); free_matrix(M7, k);
free_matrix(T1, k); free_matrix(T2, k);
}
// --- Main ---
int main() {
srand( me(NULL));
int n;
prin ("Enter matrix size (power of 2): ");
scanf("%d", &n);
int **A = alloc_matrix(n);
int **B = alloc_matrix(n);
int **C = alloc_matrix(n);
fill_matrix(A, n);
fill_matrix(B, n);
// Itera ve
clock_t start = clock(); mul_ply_itera ve(A, B, C, n);
clock_t end = clock();
prin ("Itera ve Time: %f sec\n", (double)(end - start) / CLOCKS_PER_SEC);
// Recursive
start = clock();
mul_ply_recursive(A, B, C, n);
end = clock();
prin ("Recursive Time: %f sec\n", (double)(end - start) / CLOCKS_PER_SEC);
// Strassen
start = clock();
strassen(A, B, C, n);
end = clock();

```

```

prin ("Strassen Time: %f sec\n", (double)(end - start) / CLOCKS_PER_SEC);
free_matrix(A, n); free_matrix(B, n); free_matrix(C, n);
return 0;
}

```

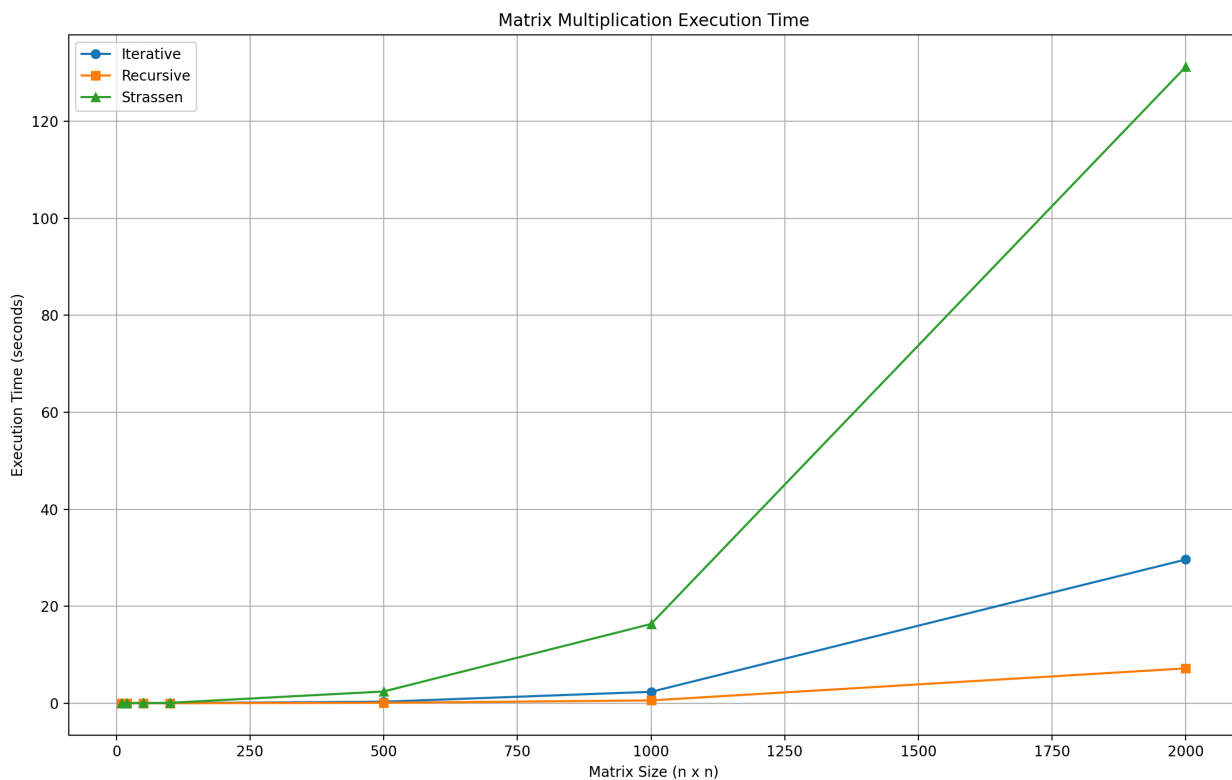
Run time execution:

Matrix Size (n)	Iterative Time (sec)	Recursive Time (sec)	Strassen Time (sec)
10	0.000011	0.000009	0.000003
20	0.000038	0.000030	0.000440
50	0.001007	0.000587	0.019488
100	0.005817	0.003557	0.069076
500	0.300065	0.073808	2.407265
1000	2.337884	0.564442	16.339782
2000	29.630607	7.173957	131.277357

```

cd "/Users/ekl_43/ADA /sorting_algo/" && gcc MatrixCombined.c -o MatrixCombined && "/Users/ekl_43/ADA /sorting_algo/"M
atrixCombined
ekl_43@Eklavyas-MacBook-Air sorting_algo % cd "/Users/ekl_43/ADA /sorting_algo/"
&& gcc MatrixCombined.c -o MatrixCombined && "/Users/ekl_43/ADA /sorting_algo/"
MatrixCombined
Enter matrix size (power of 2): 10
Iterative Time: 0.000011 sec
Recursive Time: 0.000009 sec
Strassen Time: 0.000083 sec
ekl_43@Eklavyas-MacBook-Air sorting_algo % cd "/Users/ekl_43/ADA /sorting_algo/" && gcc MatrixCombined.c -o MatrixComb
ined && "/Users/ekl_43/ADA /sorting_algo/"MatrixCombined
Enter matrix size (power of 2): 20
Iterative Time: 0.000038 sec
Recursive Time: 0.000038 sec
Strassen Time: 0.000440 sec
ekl_43@Eklavyas-MacBook-Air sorting_algo % cd "/Users/ekl_43/ADA /sorting_algo/" && gcc MatrixCombined.c -o MatrixComb
ined && "/Users/ekl_43/ADA /sorting_algo/"MatrixCombined
Enter matrix size (power of 2): 50
Iterative Time: 0.001007 sec
Recursive Time: 0.000587 sec
Strassen Time: 0.019488 sec
ekl_43@Eklavyas-MacBook-Air sorting_algo % cd "/Users/ekl_43/ADA /sorting_algo/" && gcc MatrixCombined.c -o MatrixComb
ined && "/Users/ekl_43/ADA /sorting_algo/"MatrixCombined
Enter matrix size (power of 2): 100
Iterative Time: 0.005817 sec
Recursive Time: 0.003557 sec
Strassen Time: 0.067986 sec
ekl_43@Eklavyas-MacBook-Air sorting_algo % cd "/Users/ekl_43/ADA /sorting_algo/" && gcc MatrixCombined.c -o MatrixComb
ined && "/Users/ekl_43/ADA /sorting_algo/"MatrixCombined
Enter matrix size (power of 2): 500
Iterative Time: 0.300056 sec
Recursive Time: 0.073808 sec
Strassen Time: 2.420705 sec
ekl_43@Eklavyas-MacBook-Air sorting_algo % cd "/Users/ekl_43/ADA /sorting_algo/" && gcc MatrixCombined.c -o MatrixComb
ined && "/Users/ekl_43/ADA /sorting_algo/"MatrixCombined
Enter matrix size (power of 2): 1000
Iterative Time: 2.337884 sec
Recursive Time: 0.564442 sec
Strassen Time: 16.339782 sec
ekl_43@Eklavyas-MacBook-Air sorting_algo % cd "/Users/ekl_43/ADA /sorting_algo/" && gcc MatrixCombined.c -o MatrixComb
ined && "/Users/ekl_43/ADA /sorting_algo/"MatrixCombined
Enter matrix size (power of 2): 2000
Iterative Time: 29.636007 sec
Recursive Time: 4.793577 sec

```



(x, y) = (1185.9, 136.8)



## Conclusion:

- **Recursive multiplication is the most efficient** in your experiments for larger matrices.
- **Iterative multiplication** is simple but becomes inefficient as size grows.
- **Strassen's algorithm** only shows advantage for *very large* matrices (typically beyond 4096×4096 or in optimized libraries like BLAS). In my case, due to small input sizes and lack of advanced optimizations, Strassen is slower.

