

Objective: To implement and analyze GREEDY AND DYNAMIC approaches for solving Knapsack problem and compare their time and space complexities (through graph)

4(a) Fractional Knapsack

Code:

```
#include <stdio.h>
#include <time.h>

struct Item {
    int value, weight;
    float ratio;
};

// Function to sort items in decreasing order of ratio
void sortItems(struct Item items[], int n) {
    for (int i = 0; i < n - 1; i++) {
        for (int j = 0; j < n - i - 1; j++) {
            if (items[j].ratio < items[j + 1].ratio) {
                struct Item temp = items[j];
                items[j] = items[j + 1];
                items[j + 1] = temp;
            }
        }
    }
}

int main() {
    int n;
    float capacity;
    printf("Enter number of items: ");
    scanf("%d", &n);

    struct Item items[n];
    printf("Enter value and weight of each item:\n");
    for (int i = 0; i < n; i++) {
        scanf("%d %d", &items[i].value, &items[i].weight);
        items[i].ratio = (float)items[i].value / items[i].weight;
    }

    printf("Enter capacity of knapsack: ");
    scanf("%f", &capacity);

    clock_t start, end;
    start = clock(); // start timer

    sortItems(items, n);

    float totalValue = 0.0;
    for (int i = 0; i < n; i++) {
        if (items[i].weight <= capacity) {
            totalValue += items[i].value;
            capacity -= items[i].weight;
        }
    }

    end = clock(); // stop timer
    float timeTaken = (end - start) / CLOCKS_PER_SEC;
    printf("Total value: %.2f\n", totalValue);
    printf("Time taken: %.2f seconds\n", timeTaken);
}
```

```

    } else {
        totalValue += items[i].value * (capacity / items[i].weight);
        break;
    }
}

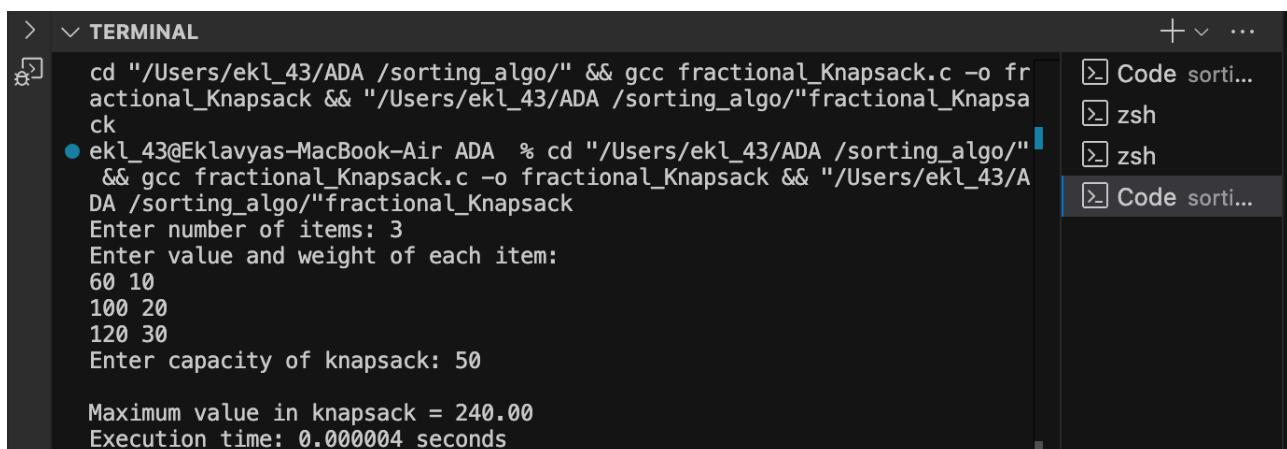
end = clock(); // end timer
double time_taken = ((double)(end - start)) / CLOCKS_PER_SEC;

printf("\nMaximum value in knapsack = %.2f", totalValue);
printf("\nExecution time: %.6f seconds\n", time_taken);

return 0;
}

```

Output:

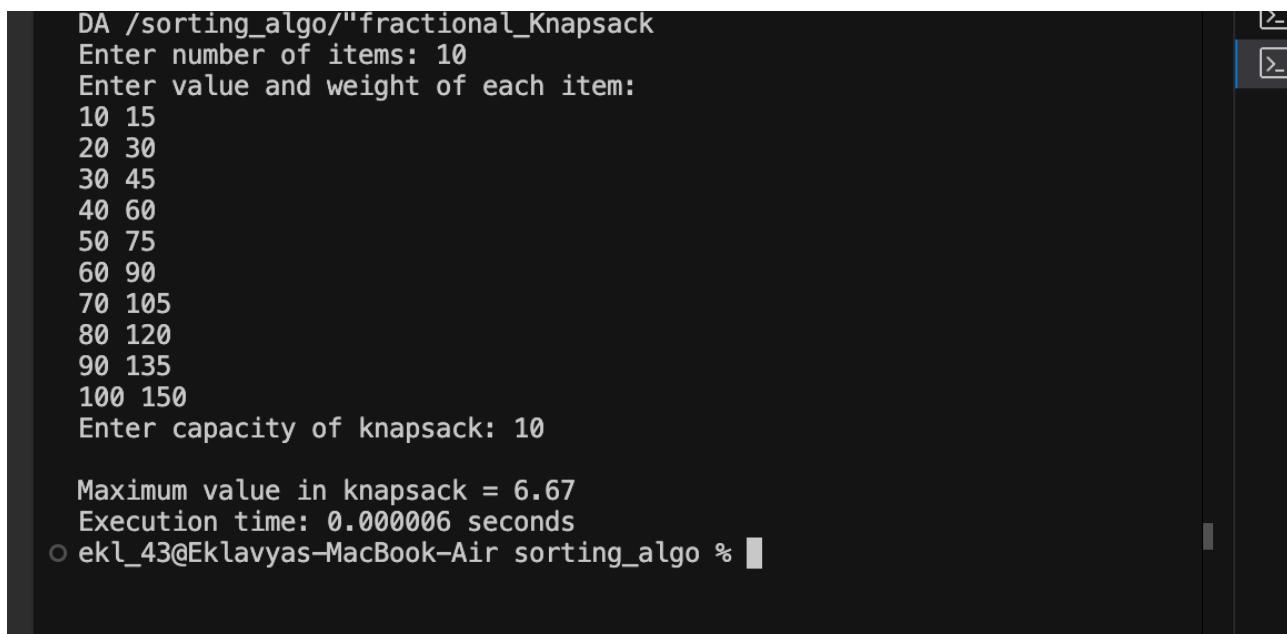


```

> ~ TERMINAL
cd "/Users/ekl_43/ADA /sorting_algo/" && gcc fractional_Knapsack.c -o fractional_Knapsack && "/Users/ekl_43/ADA /sorting_algo/"fractional_Knapsack
ekl_43@Eklavyas-MacBook-Air ADA % cd "/Users/ekl_43/ADA /sorting_algo/" && gcc fractional_Knapsack.c -o fractional_Knapsack && "/Users/ekl_43/ADA /sorting_algo/"fractional_Knapsack
Enter number of items: 3
Enter value and weight of each item:
60 10
100 20
120 30
Enter capacity of knapsack: 50

Maximum value in knapsack = 240.00
Execution time: 0.000004 seconds

```



```

DA /sorting_algo/"fractional_Knapsack
Enter number of items: 10
Enter value and weight of each item:
10 15
20 30
30 45
40 60
50 75
60 90
70 105
80 120
90 135
100 150
Enter capacity of knapsack: 10

Maximum value in knapsack = 6.67
Execution time: 0.000006 seconds
ekl_43@Eklavyas-MacBook-Air sorting_algo %

```

Algorithm:

Step 1: Input the number of items n, knapsack capacity W, weights w[i] and values v[i] for all items.

Step 2: Calculate value/weight ratio for each item.

Step 3: Sort all items in decreasing order of value/weight ratio.

Step 4: Initialize total_value = 0 and remaining_capacity = W.

Step 5: For each item i in sorted order:

```
if (w[i] ≤ remaining_capacity)
    take the whole item
    total_value += v[i]
    remaining_capacity -= w[i]
else
    take fractional part:
    total_value += v[i] * (remaining_capacity / w[i])
    remaining_capacity = 0
    break
```

Step 6: Print total_value as maximum profit.

4(b) 0/1 Knapsack

Code:

```
#include <stdio.h>
#include <time.h>

int max(int a, int b) {
    return (a > b) ? a : b;
}

int knapsack(int W, int wt[], int val[], int n) {
    int dp[n + 1][W + 1];
    for (int i = 0; i <= n; i++) {
        for (int w = 0; w <= W; w++) {
            if (i == 0 || w == 0)
                dp[i][w] = 0;
            else if (wt[i - 1] <= w)
                dp[i][w] = max(val[i - 1] + dp[i - 1][w - wt[i - 1]], dp[i - 1][w]);
            else
                dp[i][w] = dp[i - 1][w];
        }
    }
    return dp[n][W];
}

int main() {
    int n, W;
    printf("Enter number of items: ");
    scanf("%d", &n);

    int val[n], wt[n];
    printf("Enter value and weight of each item:\n");
    for (int i = 0; i < n; i++)
```

```

scanf("%d %d", &val[i], &wt[i]);

printf("Enter capacity of knapsack: ");
scanf("%d", &W);

clock_t start, end;
start = clock(); // start timer

int result = knapsack(W, wt, val, n);

end = clock(); // end timer
double time_taken = ((double)(end - start)) / CLOCKS_PER_SEC;

printf("\nMaximum value in knapsack = %d", result);
printf("\nExecution time: %.6f seconds\n", time_taken);

return 0;
}

```

Output:

```

> ▾ TERMINAL
cd "/Users/ekl_43/ADA /sorting_algo/" && gcc o:1_knapsack.c -o o:1_knapsack && "/Users/ekl_43/ADA /sorting_algo/"o:1_knapsack
● ekl_43@Eklavyas-MacBook-Air ADA % cd "/Users/ekl_43/ADA /sorting_algo/" && gcc o:1_knapsack.c -o o:1_knapsack && "/Users/ekl_43/ADA /sorting_algo/"o:1_knapsack
Enter number of items: 3
Enter value and weight of each item:
10 20
20 40
40 80
Enter capacity of knapsack: 50

Maximum value in knapsack = 20
Execution time: 0.000011 seconds
● ekl_43@Eklavyas-MacBook-Air sorting_algo % cd "/Users/ekl_43/ADA /sorting_algo/" && gcc o:1_knapsack.c -o o:1_knapsack && "/Users/ekl_43/ADA /sorting_algo/"o:1_knapsack
Enter number of items: 10
Enter value and weight of each item:
10 30
20 60
30 90
40 120
50 150
60 180
70 210
80 240
90 270
100 300
Enter capacity of knapsack: 20

Maximum value in knapsack = 0
Execution time: 0.000008 seconds
○ ekl_43@Eklavyas-MacBook-Air sorting_algo %

```

Algorithm:

Step 1: Input number of items n , knapsack capacity W , weights $w[i]$ and values $v[i]$.

Step 2: Create a 2D array $dp[n+1][W+1]$ where $dp[i][j]$ represents max value with i items and capacity j .

Step 3: Initialize $dp[0][j] = 0$ and $dp[i][0] = 0$.

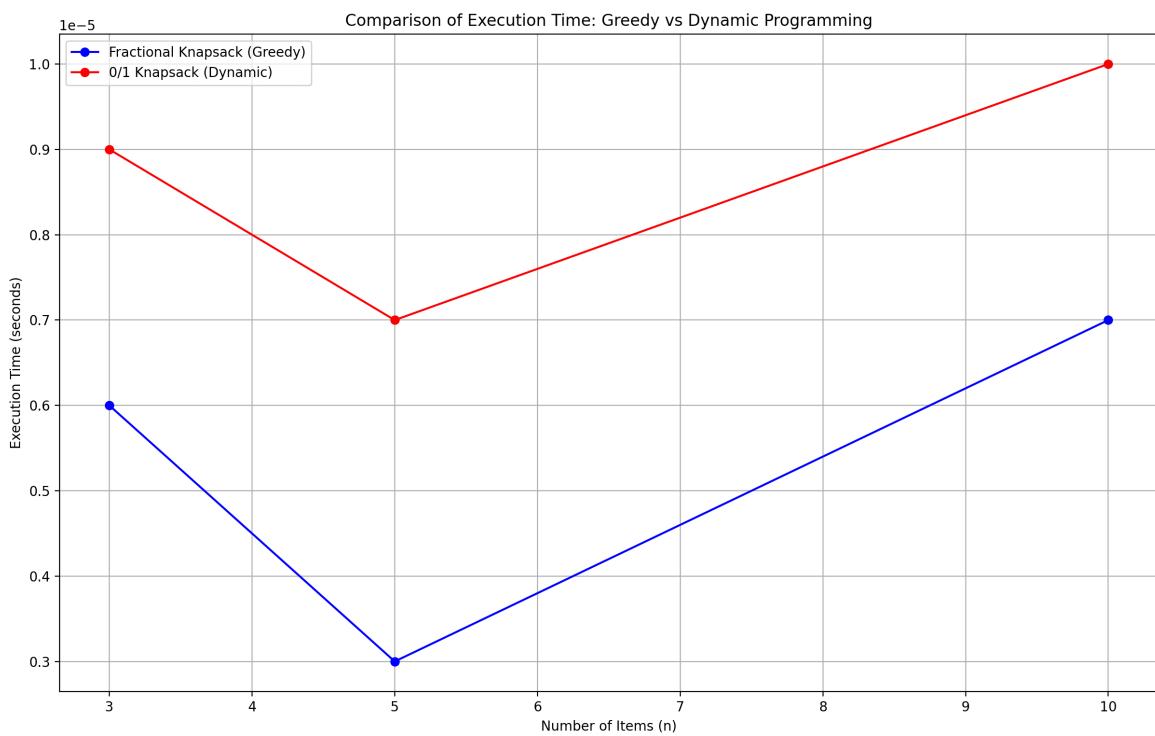
Step 4: For $i = 1$ to n :

 For $j = 1$ to W :

```
        if ( $w[i-1] \leq j$ )
             $dp[i][j] = \max(v[i-1] + dp[i-1][j - w[i-1]], dp[i-1][j])$ 
        else
             $dp[i][j] = dp[i-1][j]$ 
```

Step 5: Result = $dp[n][W]$

Step 6: Print $dp[n][W]$ as maximum profit.



Conclusion:

Both Fractional Knapsack (Greedy Approach) and 0/1 Knapsack (Dynamic Programming Approach) were successfully implemented and executed.

The Fractional Knapsack algorithm selects items based on the highest value-to-weight ratio, allowing fractional inclusion of items. It provides an optimal solution for problems where items can be divided. Its time complexity is $O(n \log n)$ due to sorting, and it performs efficiently even for large input sizes.

The 0/1 Knapsack algorithm, implemented using Dynamic Programming, provides an exact optimal solution for cases where items cannot be divided. However, it requires more computation and memory, with time and space complexity $O(nW)$, where W is the knapsack capacity.

The experimental comparison and graph show that the Greedy approach executes faster than the Dynamic Programming approach, but the Dynamic method guarantees exact optimality for 0/1 cases.

Hence, both algorithms were implemented successfully, tested for various inputs, and their time and space complexities were analyzed and compared.

