

Model

ln(price) = 10.2082 + 0.3618 · waterfront − 0.0160 · bedrooms − 0.0153 · bathrooms + 0.1400 · sqft.living^{0.3} + 0.0088 · floors + 0.1494 · view^{0.5} + 0.0105 · grade² + 0.1187 · ln (sqft.living15)

Explanation of the Model

Before I begin explain the coefficients, I notice that $P > |t|$ for the *floors* variable is 0.155, which makes *floors* insignificant for the analysis.

- 1. The model has the sample intercept of 10.2082. If we assume that all explanatory variables are zeros, this would mean that the price would be $e^{10.2082} \approx 27,124$
- 2. 0.3618 is the coefficient for *waterfront*. *Waterfront* is a categorical variable coded as 0 or 1, a one unit difference represents switching from one category to the other. 10.2082 is then the average difference in *price* between the category for which *waterfront* = 0 (no waterfront) and the category for which *waterfront* = 1 (the house has a waterfront). So compared to ln(*price*) of the house with no waterfront, we would expect the ln(*price*) for the house with waterfront to be 0.3618 higher, on average, if we fix all other explanatory variables.
Let y_2 = price of the house with waterfront and y_1 = price of the house with no waterfront, then

ln y_2 − ln y_1 = 0.3618 \implies ln $\frac{y_2}{y_1}$ = 0.3618 \implies $\frac{y_2}{y_1}$ = $e^{0.3618}$

To understand the change in *price* in percents, if we switch from the house with no waterfront to the house with waterfront while keeping all other variables the same, will use the following formula:

$100 \times \left[\frac{y_2 - y_1}{y_1} \right] = 100 \times \left[\frac{y_2}{y_1} - 1 \right] = 100 \times [e^{0.3618} - 1] \approx 43.59\%$

Thus, switching from the house with no waterfront to the house with waterfront while keeping all other explanatory variables fixed, will increase the price by 43.59%.

- 3. −0.0160 is the coefficient for number of *bedrooms*.

Let y_2 = price for the house with x_2 number of bedrooms and y_1 = price for the house with x_1 number of bedrooms, then

ln y_2 − ln y_1 = −0.016 x_2 − (−0.016 x_1) = −0.016(x_2 − x_1) \implies ln $\frac{y_2}{y_1}$ = −0.016(x_2 − x_1) \implies $\frac{y_2}{y_1}$ = $e^{-0.016(x_2 - x_1)}$

If we increase the number of bedrooms by 1 while keeping the other variables fixed and use percents, we will get the following

$100 \times \left[\frac{y_2}{y_1} - 1 \right] = 100 \times [e^{-0.016} - 1] \approx -1.58\%$

Thus, increasing the number of bedrooms by 1 while keeping the other variables fixed, will decrease the price of the house by 1.58%. Which is a strange result.

- 4. The same explanation we have for −0.0153 which a coefficient for number of bathrooms.
If we increase the number of bathrooms by 1 while keeping the other variables fixed, will decrease the price of the house by 1.51%. Which is a strange result.
- 5. 0.1400 is the coefficient for *sqft.living*. Let y_2 = price for the house with x_2 *sqft.living* and y_1 = price for the house with x_1 *sqft.living*, then

ln y_2 − ln y_1 = 0.1400 $x_2^{0.3}$ − 0.1400 $x_1^{0.3}$ \implies ln $\frac{y_2}{y_1}$ = 0.1400 ($x_2^{0.3}$ − $x_1^{0.3}$) \implies $\frac{y_2}{y_1}$ = $e^{0.1400(x_2^{0.3} - x_1^{0.3})}$

If we increase the *sqft.living* from 1000*ft* to 1100*ft* while keeping the other variables fixed, we will get the following change in price in percents:

$100 \times \left[\frac{y_2}{y_1} - 1 \right] = 100 \times [e^{0.1400(1100^{0.3} - 1000^{0.3})} - 1] \approx 3.28\%$

If the *sqft.living* is 1000*ft* and we increase it to 1100*ft* while keeping the other variables fixed, we will get the change in price of 3.28%. In this particular example 10% change in *sqft.living* starting from x_1 = 1000*ft* forces 3.28% change in price.

- 6. 0.1494 is the coefficient for the *view*. The coefficient for the *view* has the same explanation as the *sqft.living*.

If we increase the *view* by 1 unit from 2 to 3 while keeping the other variables fixed, we will get the following:

$100 \times \left[\frac{y_2}{y_1} - 1 \right] = 100 \times [e^{0.1494(3^{0.5} - 2^{0.5})} - 1] \approx 4.86\%$

In this particular example if the *view* will increase from 2 to 3, the price will increase by 4.86%.

- 7. 0.0105 is the coefficient for the *grade*. The coefficient for the *grade* has the same explanation as the *sqft.living*.

If we increase the *grade* by 1 unit from 2 to 3 while keeping the other variables fixed, we will get the following:

$100 \times \left[\frac{y_2}{y_1} - 1 \right] = 100 \times [e^{0.0105(3^2 - 2^2)} - 1] \approx 5.39\%$

In this particular example if the *grade* will increase from 2 to 3 while other variables stay the same, the price will increase by 5.39%.

- 8. 0.1187 is the coefficient for the *sqft.living15* Let y_2 = price for the house with x_2 *sqft.living15* and y_1 = price for the house with x_1 *sqft.living15*, then

ln y_2 − ln y_1 = 0.1187 ln x_2 − 0.1187 ln x_1 \implies ln $\frac{y_2}{y_1}$ = 0.1187 ln $\frac{x_2}{x_1}$ \implies $\frac{y_2}{y_1}$ = $e^{0.1187 \frac{x_2}{x_1}}$

The change in price in present will be:

$100 \times \left[\frac{y_2}{y_1} - 1 \right] = 100 \times \left[e^{0.1187 \frac{x_2}{x_1}} - 1 \right]$

If we increase the *sqft.living15* by 100 units from 1000 to 1100 while keeping the other variables fixed, we will get the following:

$100 \times \left[e^{0.1187 \times \frac{1100}{1000}} - 1 \right] \approx 23.87\%$

Thus, 10% increase in *sqft.living15* will lead to 23.87% increase in *price*.

R²

The model has $R^2 \approx 0.5$. This means that our model explains about 50% of the variation by using *sqft.living* as independent variable.

ANOVA

Is our model with many explanatory variable better than the model with zero explanatory variables?

Our model has $F - statistic = 1.737 \times 10^4$ and $Prob > F$ is 0.000.

The Null Hypothesis: The slope= 0

The Alternative Hypothesis: The slope≠ 0

Our p-value for this model is $p = 0.000 < 0.05 = \alpha$. Thus, we have enough evidence to reject the Null Hypothesis at 5% level of significance and we conclude that the Test tells us, that at least one of the coefficients is not 0. Since our p-value is 0, there is a 0% probability that the improvements that we are seeing with our independent variables model are due to random chance alone.