

Tugas pertemuan 4 kalkulus

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SOAL

1. $\sqrt{x^2 - 4} = \sqrt{x + 2}$
2. $\sqrt{(x-5)} = 2x - 11$
3. $1 + x\sqrt{5} = \sqrt{5-x}$

JAWABAN

1.

$$\sqrt{x^2 - 4} = \sqrt{x + 2}$$

$$x^2 - 4 = x + 2$$

$$x^2 - x - 4 - 2 = 0$$

$$x^2 - x - 6 = 0$$

$$(x+2)(x-3) = 0$$

$$x+2=0 \quad x-3=0$$

$$x=-2 \quad x=3$$

$$\begin{aligned}\sqrt{x^2 - 4} &= \sqrt{x + 2} \\ \sqrt{-2^2 - 4} &= \sqrt{-2 + 2} \\ \sqrt{+4 - 4} &= \sqrt{0} \\ \sqrt{0} &= \sqrt{0}\end{aligned}$$

$$\begin{aligned}\sqrt{3^2 - 4} &= \sqrt{3 + 2} \\ \sqrt{9 - 4} &= \sqrt{5} \\ \sqrt{5} &= \sqrt{5}\end{aligned}$$

Jadi persamaan $x = -2$ dan $x = 3$



2.

$$\begin{aligned}\sqrt{x-5} &= 2x-11 \\ x-5 &= (2x-11)^2 \\ x-5 &= 4x^2-22x-22x+121 \\ x-5 &= 4x^2-44x+121\end{aligned}$$

$$\begin{aligned}0 &= 4x^2-44x-x+121+5 \\ 0 &= 4x^2-45x+126 \\ 0 &= (4x-21)(x-6)\end{aligned}$$

$$\begin{aligned}4x-21 &= 0 & x-6 &= 0 \\ x &= \frac{21}{4} & x &= 6\end{aligned}$$

$$\begin{aligned}\sqrt{\frac{21}{4}-5} &= 2\frac{21}{4}-11 \\ \sqrt{\frac{21}{4}-\frac{20}{4}} &= \frac{42}{4}-\frac{44}{4}\end{aligned}$$

$$\begin{aligned}\sqrt{\frac{1}{4}} &= -\frac{2}{4} \\ \frac{1}{2} &= -\frac{1}{2}\end{aligned}$$

$$\begin{aligned}\sqrt{6}-5 &= 2(6)-11 \\ \sqrt{1} &= 12-11 \\ 1 &= 1\end{aligned}$$

Jadi persamaan yang memenuhi adalah $x=6$

3.

$$\begin{aligned}1+x\sqrt{5} &= \sqrt{5-x} \\ 1+\sqrt{5}x &= \sqrt{5-x}\end{aligned}$$

$$\begin{aligned}1+\sqrt{5}x &= 5-x \\ (1+\sqrt{5}x)(1+\sqrt{5}x) &= 5-x \\ 1+\sqrt{5}x+\sqrt{5}x^2 &= 5-x \\ 5x^2+2\sqrt{5}x+x+1-5 &= 0 \\ 5x^2(2\sqrt{5}+1)x-4 &= 0\end{aligned}$$

$$x = \frac{-(2\sqrt{5}+1) \pm \sqrt{(2\sqrt{5}+1)^2 - 4(5)(-4)}}{2(5)}$$

$$\frac{-2\sqrt{5}-1 \pm \sqrt{21+4\sqrt{5}+80}}{10}$$

$$\frac{-2\sqrt{5}-1 \pm \sqrt{101+4\sqrt{5}}}{10}$$



$$\text{untuk } x = -1,6$$

$$1 + \sqrt{5}(-1,6) = \sqrt{5 - (-1,6)}$$

$$1 + 5_2^1(-1,6) = \sqrt{6,6}$$

$$1 + 2,2(-1,6) = 2,5$$

$$-2,5 = 2,5$$

$$\text{Untuk } x = 0,5$$

$$1 + \sqrt{5}(0,5) = \sqrt{5 - 0,5}$$

$$1 + 5_2^1(0,5) = \sqrt{4,5}$$

$$1 + 2,2(0,5) = 2,1$$

$$2,1 = 2,1$$

jadi, persamaan tersebut yang memenuhi adalah $x = 0,5$

