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MKs Analisis Numerik

UAS

1. Selesaikan sistem persamaan linier berikut dengan metode eliminasi

Gauss :

$$x_1 + 2x_2 + x_3 = 2$$

$$3x_1 + 6x_2 = 9$$

$$2x_1 + 8x_2 + 4x_3 = 6$$

2. Jika $\log(10) = 1$ dan $\log(100) = 2$, maka carilah

a. $\log(75) =$

c. persamaan interpolasinya.

b. $\log(25) =$

3. Carilah akar pendekatan fungsi : $f(x) = x^3 - x - 1$, $a = 0,1$ dan $x_0 = 2$

4. Gunakan aturan trapesium dan Simpson untuk mencari suatu nilai

hampiran untuk : $y = x^4$ dengan mengambil batas $x=1$ dan $x=4$,serta subinterval ($n=8$)

5. Tentukan deret Taylor dan deret Maclaurin dari fungsi :

a. $f(x) = \cos(x)$

$$f(x) = \ln(x+1)$$

Jawab :

$$1. \left[\begin{array}{ccc|c} 1 & 2 & 3 & 2 \\ 3 & 6 & 0 & 9 \\ 2 & 8 & 4 & 6 \end{array} \right]$$

$$\left[\begin{array}{ccc|c} 1 & 2 & 3 & 2 \\ 0 & 0 & -9 & 3 \\ 0 & 4 & -2 & 2 \end{array} \right]$$

$$\left[\begin{array}{ccc|c} 1 & 2 & 3 & 2 \\ 0 & 4 & -2 & 2 \\ 0 & 0 & -9 & 3 \end{array} \right]$$

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$$\left[\begin{array}{ccc|c} 1 & 2 & 3 & 2 \\ 0 & 1 & -0,5 & 0,5 \\ 0 & 0 & -9 & 3 \end{array} \right]$$

$$x_1 = \frac{7}{3}$$

$$x_2 = \frac{1}{3}$$

$$x_3 = -\frac{1}{3}$$

$$\left[\begin{array}{ccc|c} 1 & 0 & 4 & 1 \\ 0 & 1 & -0,5 & 0,5 \\ 0 & 0 & -9 & -3 \end{array} \right]$$

$$\left[\begin{array}{ccc|c} 1 & 0 & 4 & 1 \\ 0 & 1 & -0,5 & 0,5 \\ 0 & 0 & 1 & -\frac{1}{5} \end{array} \right]$$

a)

$$2. \log(75) =$$

$$y = 1 + \frac{(75-10)(2-1)}{(100-10)}$$

$$= 1 + 0,72 = 1,72$$

b) $\log(25)$

$$y = 1 + \frac{(25-10)(2-1)}{(100-10)}$$

$$= 1 + 0,16 = 1,16$$

c) Persamaan interpolasi

$$\log(75) = 1,87 \quad \text{galat} = \frac{1,87 - 1,72}{1,87} \times 100\% = 8,6$$

$$\log(25) = 1,39 \quad \text{galat} = \frac{1,39 - 1,16}{1,39} \times 100\% = 16$$

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3.

Iterasi	x_0	x_1	x_2	$f(x_2)$	$f(x_0) - f(x_2)$	$(x_0 - x_1)$
1	1	2	1.5	0.875	-0.875	1
2	1	1.5	1.25	-0.291	0.299	0.5

4. $f(x) = x^4$

$x_4 = 4$

$x_0 = 1$

$n = 8$

$h = 0.375$

x	$f(x)$
1	1
1.375	3.574
2	16
2	16
3	81
3	81
4	256

Jadi luas = 122,2779

5. a) $f(x) = \cos(x)$

$$= \cos(x) + \frac{d}{dx}(\cos(x))(x)(x-2) + \frac{d^2}{dx^2}(\cos(x))(x)(x-2)^2 + \frac{d^3}{dx^3}(\cos(x))(x)(x-2)^3 + \dots$$

$$= \cos(x) + \frac{-\sin(x)(x-2)}{2!} + \frac{-\cos(x)(x-2)^2}{3!} + \frac{\sin(x)(x-2)^3}{4!} + \frac{\cos(x)(x-2)^4}{5!} + \dots$$

$$= \cos(x) - \frac{\sin(x)(x-2)}{2} - \frac{\cos(x)(x-2)^2}{6} + \frac{\sin(x)(x-2)^3}{24} + \frac{\cos(x)(x-2)^4}{120} + \dots$$

Maclaurins :

$a = 0$

$$= 1 + \frac{\frac{d}{dx}(\cos(x))(0)}{1!}x + \frac{\frac{d^2}{dx^2}(\cos(x))(0)}{2!}x^2 + \frac{\frac{d^3}{dx^3}(\cos(x))(0)}{3!}x^3 + \dots$$

$$= 1 + \frac{0}{1!}x + \frac{-1}{2!}x^2 + \frac{0}{3!}x^3 + \frac{1}{4!}x^4 + \frac{0}{5!}x^5 + \frac{-1}{6!}x^6 + \frac{0}{7!}x^7 + \frac{1}{8!}x^8 + \dots$$

$$= 1 - \frac{1}{2!}x^2 + \frac{1}{4!}x^4 - \frac{1}{6!}x^6 + \frac{1}{8!}x^8 + \dots$$

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$$= \sum_{n=0}^{\infty} = 0 \cdot (-1)^n \frac{x^{2n}}{(2n)!}$$

b) Taylor $a=2$

$$f(x) = \ln(x)$$

$$= \ln(2) = \frac{\frac{d}{dx} (\ln(1+x))(2)}{1!} + \frac{\frac{d^2}{dx^2} (\ln(1+x))(2)}{2!} (x-2)^2 + \frac{\frac{d^3}{dx^3} (\ln(1+x))(2)}{3!} (x-2)^3 + \dots$$

$$= \frac{d}{dx} (\ln(1+x))(2) = \frac{1}{3}$$

$$\frac{d^2}{dx^2} (\ln(1+x))(2) = -\frac{1}{9}$$

$$\frac{d^3}{dx^3} (\ln(1+x))(2) = \frac{2}{27}$$

$$\frac{d^4}{dx^4}$$

$$(\ln(1+x))(2) = -\frac{2}{27}$$

$$= \ln(2) + \frac{1}{3} \frac{(x-2)}{1!} + \frac{-1}{9} \frac{(x-2)^2}{2!} + \frac{2}{27} \frac{(x-2)^3}{3!} + \frac{-2}{27} \frac{(x-2)^4}{4!} + \dots$$

Maclaurins:

$$f(0) = 0$$

$$= 0 + \frac{\frac{d}{dx} (\ln(1+x))(0)}{1!} x + \frac{\frac{d^2}{dx^2} (\ln(1+x))(0)}{2!} x^2 + \frac{\frac{d^3}{dx^3} (\ln(1+x))(0)}{3!} x^3 + \dots$$

$$\frac{d}{dx} (\ln(1+x))(0) = 1$$

$$\frac{d^4}{dx^4} (\ln(1+x))(0) = -6$$

$$\frac{d^2}{dx^2} (\ln(1+x))(0) = -1$$

$$\frac{d^5}{dx^5} (\ln(1+x))(0) = 24$$

$$\frac{d^3}{dx^3} (\ln(1+x))(0) = 2$$

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$$= 0 + \frac{1}{1!} x + \frac{-1}{2!} x^2 + \frac{2}{3!} x^3 + \frac{-6}{4!} x^4 + \frac{24}{5!} x^5 + \dots$$

$$= x - \frac{1}{2} x^2 + \frac{1}{3} x^3 - \frac{1}{4} x^4 + \frac{1}{5} x^5 + \dots$$

$$= \sum_{n=1}^{\infty} \frac{(-1)^{n+1} x^n}{n}$$