LAPORAN PEMROSESAN PARALEL

(Bubble Sort Python Menggunakan MPI Secara Paralel)



Disusun Oleh:

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FAKULTAS ILMU KOMPUTER
PROGRAM STUDI SISTEM KOMPUTER
UNIVERSITAS SRIWIJAYA
2023

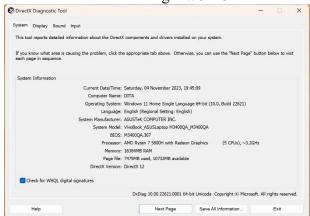
1. Master dan Worker

Menentukan master dan worker dengan melihat spesifikasi masing masing device

• Khairunnisa Junaidi sebagai master



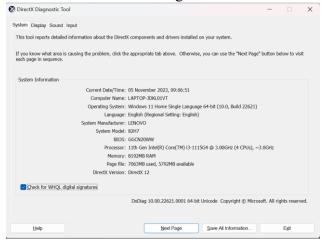
• Eka Ratna Anindita sebagai worker1



• Almirah Callysta Aurelie sebagai worker2



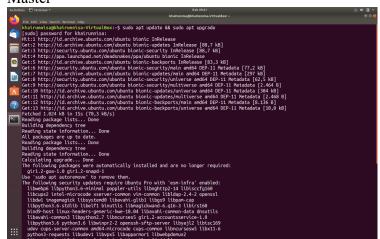
• Nabilla Suci Febriani sebagai worker3



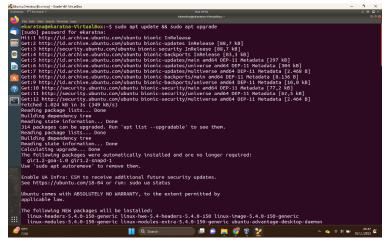
2. Upgrade OS

Menggunakan command 'sudo apt update && sudo apt upgrade' untuk memperbarui OS pada setiap device

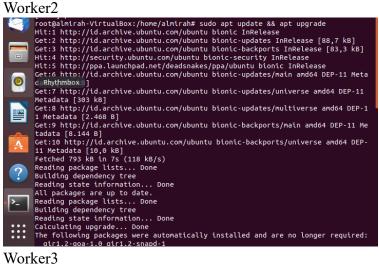
Master



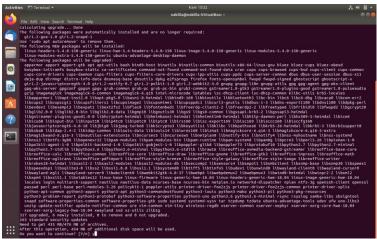
• Worker1



Worker2



Worker3



3. Install net-tools

Melakukan penginstalan net-tools dengan menggunakan command 'sudo apt install net-tools vim' untuk cek IP, vim sebagai teks editor

```
THITTE CONTROL OF THE SUBJECT OF THE
    The following additional packages will be installed:

vim-runtime

Suggested packages:

ctags vim-doc vim-scripts

The following NEW packages will be installed:

net-tools vim vim-runtime

0 upgraded, 3 newly installed, 0 to remove and 0 not upgraded.

Need to get 6.790 kB of archives.

After this operation, 32,8 MB of additional disk space will be used.

Do you want to continue: [Y/n] v

Get:1 http://id.archive.ubuntu.com/ubuntu bionic/main amd64 net-tools amd64 1.6

0+git20161116.90da8a0-1ubuntu1 [194 kB]

Get:2 http://id.archive.ubuntu.com/ubuntu bionic-updates/main amd64 vim-runtime

all 2:8.0.1453-1ubuntu1.13 [5.439 kB]

Get:3 http://id.archive.ubuntu.com/ubuntu bionic-updates/main amd64 vim amd64 2

:8.0.1453-1ubuntu1.13 [1.156 kB]

Fetched 6.790 kB in 12s (544 kB/s)

Selecting previously unselected package net-tools.

(Reading database ... 164777 files and directories currently installed.)

Preparing to unpack .../net-tools_1.60+git20161116.90da8a0-1ubuntu1_amd64.deb ...
```

4. Cek ip

Menggunakan command 'ifconfig' atau 'hostname –I' untuk mengecek IP masing masing device

Master

```
khairunnisa@khairunnisa-VirtualBox:-
khairunnisa-VirtualBox:-
khairun
```

Worker1

```
ekaratna@ekaratna-VirtualBox:~$ hostname -I
192.168.100.144 2001:448a:10ef:2ce7:d88e:f316:e173:79f3 2001:448a:10ef:2ce7:8ad0:530f:b80c:4586
```

Worker2

```
root@almirah-VirtualBox:/home/almirah# hostname -I
192.168.100.145 2001:448a:10ef:2ce7:1025:711e:2e8f:6c24 2001:448a:10ef:2ce7:222
```

• Worker3

```
nabilla@nabilla-VirtualBox:~$ hostname -I
192.168.100.146 2001:448a:10ef_2ce7:441d:73ff:ea6a:b168 2001:448a:10ef:2ce7:2c39:6beb:c7b0:af97
```

5. Konfigurasi file

Membuka file /etc/hosts menggunakan command 'sudo nano /etc/hosts' khairunnisa@khairunnisa-VirtualBox:~\$ sudo nano /etc/hosts

Lalu mengedit file dengan menambahkan IP dan peran.

• Master

```
khairunnisa@khairunnisaVitrualBox:-

GNU nano 2.9.3 /etc/hosts Modified

192.168.100.142 master1 localhost
127.0.1.1 khairunnisa-VirtualBox
# The following lines are desirable for IPv6 capable hosts
::1 ip6-localhost ip6-loopback
fe00::0 ip6-localnet
ff00::0 ip6-mcastprefix
ff00::1 ip6-allnodes
ff00::2 ip6-allnouters

192.168.100.144 worker1
192.168.100.145 worker2
192.168.100.145 worker3
```

Worker1

```
GNU nano 2.9.3 /etc/hosts

192.168.100.144 worker1 localhost
127.0.1.1 ekaratna-VirtualBox

# The following lines are desirable for IPv6 capable hosts
::1 ip6-localhost ip6-loopback
fe00::0 ip6-localnet
ff00::0 ip6-mcastprefix
ff02::1 ip6-allnodes
ff02::2 ip6-allrouters

192.168.100.142 master
192.168.100.145 worker2
192.168.100.146 worker3
```

• Worker2

```
root@almirah-VirtualBox: /home/almirah

File Edit View Search Terminal Help

GNU nano 2.9.3 /etc/hosts Modified

198.168.100.145 worker2 localhost 127.0.1.1 almirah-VirtualBox

# The following lines are desirable for IPv6 capable hosts
::1 ip6-localhost ip6-loopback fe00::0 ip6-mcastprefix ff02::1 ip6-allnodes ff02::2 ip6-allnodes ff02::2 ip6-allrouters

192.168.100.142 master 192.168.100.144 worker1 192.168.100.146 worker3
```

• Worker3

```
File Edit View Search Terminal Help nabilitagnabilita-Virtualitosc - CC COURT AND 21573 Protection of the Court Annual Help Protection of
```

6. User bersama

Membuat user baru bersama dengan command 'sudo adduser <nama user>'

```
root@ekaratna-VirtualBox:/home/ekaratna# adduser dina
Adding user `dina' ...
Adding new group `dina' (1001) ...
Adding new user `dina' (1001) with group `dina' ...
Creating home directory `/home/dina' ...
Copying files from `/etc/skel' ...
Enter new UNIX password:
Retype new UNIX password:
passwd: password updated successfully
Changing the user information for dina
Enter the new value, or press ENTER for the default
    Full Name []: Dina
    Room Number []: 123
    Work Phone []: 011
    Home Phone []: 1234
    Other []:
Is the information correct? [Y/n] y
```

➤ User root

Memberi akses root ke user yang baru ditambahkan dengan command 'sudo usermod -aG sudo <nama user>'

root@almirah-VirtualBox:/home/almirah# sudo usermod -aG sudo dina

➤ Login user

Masuk ke user dengan command 'su - <nama user>'

```
nabilla@nabilla-VirtualBox:~$ su - dina
Password:
To run a command as administrator (user "root"), use "sudo <command>".
See "man sudo_root" for details.
```

7. Konfigurasi SSH

Melakukan konfigurasi SSH, SSH(Secure Shell) digunakan untuk otentikasi dan pertukaran data aman antara node dalam cluster MPI.

> Install SSH

Melakukan penginstallan SSH dengan command 'sudo apt install openssh-server'

```
dina@almirah-VirtualBox:/home/almirah$ sudo apt install openssh-server
[sudo] password for dina:
Readting package lists... Done
Building dependency tree
Readting state information... Done
The following packages were automatically installed and are no longer required:
    gir1.2-goa-1.0 gir1.2-snapd-1
Use 'sudo apt autoremove' to remove them.
The following additional packages will be installed:
    ncurses-term openssh-sftp-server ssh-import-id
Suggested packages:
    molly-guard monkeysphere rssh ssh-askpass
The following NEW packages will be installed:
    ncurses-term openssh-server openssh-sftp-server ssh-import-id
0 upgraded, 4 newly installed, 0 to remove and 0 not upgraded.
Need to get 637 kB of archives.
After this operation, 5.320 kB of additional disk space will be used.
Do you want to continue? [Y/n] y
Get:1 http://id.archive.ubuntu.com/ubuntu bionic-updates/main amd64 ncurses-ter
m all 6.1-1ubuntu1.18.04.1 [248 kB]
Get:2 http://id.archive.ubuntu0.7 [45.5 kB]
```

Dapat dilakukan pengecekan SSH untuk menghubungkan master ke klien, dengan

command 'ssh <nama user>@<host>'

```
dina@ekaratna-VirtualBox:~$ ssh dina@master
The authenticity of host 'master (192.168.100.142)' can't be established.
ECDSA key fingerprint is SHA256:Lmm8CRORCOUPvq0NnBUvxTJ4eQxhxy6BrkQurtwAx1I.
Are you sure you want to continue connecting (yes/no)? y
Please type 'yes' or 'no': yes
Warning: Permanently added 'master,192.168.100.142' (ECDSA) to the list of known hosts.
dina@master's password:
Welcome to Ubuntu 18.04.6 LTS (GNU/Linux 5.4.0-150-generic x86_64)

* Documentation: https://help.ubuntu.com
* Management: https://landscape.canonical.com
* Support: https://ubuntu.com/advantage

Expanded Security Maintenance for Infrastructure is not enabled.
0 updates can be applied immediately.

130 additional security updates can be applied with ESM Infra.
Learn more about enabling ESM Infra service for Ubuntu 18.04 at
https://ubuntu.com/18-04

New release '20.04.6 LTS' available.
Run 'do-release-upgrade' to upgrade to it.

Your Hardware Enablement Stack (HWE) is supported until April 2023.
Last login: Thu Nov 2 16:02:39 2023 from 192.168.100.145

To run a command as administrator (user "root"), use "sudo <command>".
See "man sudo_root" for details.

dina@khairunnisa-VirtualBox:~$
```

Generate keygen

Dilakukan di master, menggunakan command 'ssh-keygen -t rsa'

> Input key publik ke klient

Dilakukan di master, membuat isi dari file *id_rsa.pub* disalin ke file *authorized_keys* menggunakan command 'cd.ssh'

```
dina@khairunnisa-VirtualBox:~$ cd .ssh
```

Master – worker1

```
dina@khairunnisa-VirtualBox:~/.ssh$ cat id_rsa.pub | ssh dina@worker1 " cat>> .ssh/authorized_keys"

dina@ekaratna-VirtualBox:~$ ls .ssh
authorized_keys known_hosts
```

• Master – worker2

```
dina@khairunnisa-VirtualBox:~/.ssh$ cat id_rsa.pub | ssh dina@worker2 " cat>> .ssh/authorized_keys"
dina@almirah-VirtualBox:~$ ls .ssh
authorized_keys known_hosts
```

• Master – worker3

```
dina@khairunnisa-VirtualBox:~/.ssh$ cat id_rsa.pub | ssh dina@worker3 " cat>> .ssh/authorized_keys"

dina@nabilla-VirtualBox:~$ ls .ssh
authorized_keys known_hosts
```

8. Konfigurasi NFS

Konfigurasi NFS (Network File System) merupakan proses mengatur dan mengkonfigurasi sistem berkas yang memungkinkan berbagi sistem berkas antara komputer dalam jaringan.

> Shared folder

Membuat folder bersama menggunakan command 'mkdir <nama folder>'

```
dina@nabilla-VirtualBox:~$ mkdir pempar
dina@nabilla-VirtualBox:~$
```

> Install NFS Server

Menginstall NFS pada master dengan command 'sudo apt install nfs-kernel-server'

```
dina@khairunnisa-VirtualBox:~$ sudo apt install nfs-kernel-server
[sudo] password for dina:
Reading package lists... Done
Building dependency tree
Reading state information... Done
The following packages were automatically installed and are no longer required:
    gir1.2-goa-1.0 gir1.2-snapd-1
Use 'sudo apt autoremove' to remove them.
The following additional packages will be installed:
    keyutils libnfsidmap2 libtirpc1 nfs-common rpcbind
Suggested packages:
    open-iscsi watchdog
The following NEW packages will be installed:
    keyutils libnfsidmap2 libtirpc1 nfs-common nfs-kernel-server rpcbind
0 upgraded, 6 newly installed, 0 to remove and 0 not upgraded.
Need to get 492 kB of archives.
After this operation, 1.709 kB of additional disk space will be used.
Do you want to continue? [Y/n] ■
```

> Konfigurasi file

Dilakukan di master, buka file /etc/exports dengan command 'sudo nano /etc/exports' dina@khairunnisa-VirtualBox:~\$ sudo nano /etc/exports

Dan dilakukan pengeditan pada file, dengan menambahkan < lokasi shared folder> *(rw,sync,no root squash,no subtree check)

```
GNU nano 2.9.3
                                             /etc/exports
                                                                                        Modified
/home/pempar *(rw, sync, no_root_squash, no_subtree_check)
```

Lalu, untuk menyimpan ulang daftar direktori setelah mengedit file dapat menggunakan command 'sudo exports -a' dan untuk memulai ulang layanan pada server dapat menggunakan command 'sudo systemctl restart nfs-kernel-server'

```
dina@khairunnisa-VirtualBox:~$ sudo exportfs -a
dina@khairunnisa-VirtualBox:~$ sudo systemctl restart nfs-kernel-server
```

> Install NFS Klient

Melakukan instalasi NFS pada worker dengan command 'sudo apt install nfscommon'

Worker1

```
dina@ekaratna-VirtualBox:-$ sudo apt install nfs-co
Reading package lists... Done
Building dependency tree
Reading state information... Done
Reading state information... Done nfs-common is already the newest version (1:1.3.4-2.1ubuntu5.5). nfs-common set to manually installed.

The following packages were automatically installed and are no longer required: gir1.2-goa-1.0 gir1.2-snapd-1

Use 'sudo apt autoremove' to remove them.

0 upgraded, 0 newly installed, 0 to remove and 0 not upgraded.
```

Worker2

```
WORKETZ

dina@almirah-VirtualBox:-$ sudo apt install nfs-common
[sudo] password for dina:
Reading package lists... Done
Building dependency tree
Reading state information... Done
The following packages were automatically installed and are no longer required:
    girl.2-goa-1.0 girl.2-snapd-1
Use 'sudo apt autoremove' to remove them.
The following additional packages will be installed:
    keyutils libnfsidmap2 libtirpc1 rpcbind
Suggested packages:
    open-iscsi watchdog
  Suggested packages:
open-iscsi watchdog
The following NEW packages will be installed:
keyutils libnfsidmap2 libtirpci nfs-common rpcbind
0 upgraded, 5 newly installed, 0 to remove and 0 not upgraded.
Need to get 399 kB of archives.
After this operation, 1.364 kB of additional disk space will be used.
Do you want to continue? [Y/n] y
Get:1 http://id.archive.ubuntu.com/ubuntu bionic-updates/main amd64 keyutils am
d64 1.5.9-9.2ubuntu2.1 [48,1 kB]
Get:2 http://id.archive.ubuntu.com/ubuntu bionic/main amd64 libnfsidmap2 amd64
0.25-5.1 [27.2 kB]
  O-25-5.1 [27,2 kB]

Get:3 http://id.archive.ubuntu.com/ubuntu bionic-updates/main amd64 libtirpc1 a md64 0.2.5-1.2ubuntu0.1 [75,7 kB]

Get:4 http://id.archive.ubuntu.com/ubuntu bionic-updates/main amd64 rpcbind amd 64 0.2.3-0.6ubuntu0.18.04.4 [42,1 kB]

Get:5 http://id.archive.ubuntu.com/ubuntu bionic-updates/main amd64 nfs-common
```

Worker3

```
dina@nabilla-VirtualBox:~$ sudo apt install nfs-common
Reading package lists... Done
Building dependency tree
Reading state information... Done
nfs-common is already the newest version (1:1.3.4-2.1ubuntu5.5).
nfs-common set to manually installed.
The following packages were automatically installed and are no longer required:
gir1.2-90a-1.0 gir1.2-snapd-1
Use 'sudo apt autoremove' to remove them.
0 upgraded, 0 newly installed, 0 to remove and 0 not upgraded.
```

> Mounting

Dilakukan pada worker dengan menggunakan command 'sudo mount <server host>:<lokasi shared folder di server> <lokasi shared folder di client>'

• Worker1

```
dina@ekaratna-VirtualBox:~$ sudo mkdir /home/pempar
dina@ekaratna-VirtualBox:~$ sudo mount master:/home/pempar /home/pempar
```

Worker2

```
dina@almirah-VirtualBox:~$ sudo mkdir /home/pempar
dina@almirah-VirtualBox:~$ sudo mount master:/home/pempar /home/pempar
```

• Worker3

```
dina@nabilla-VirtualBox:~$ sudo mkdir /home/pempar
dina@nabilla-VirtualBox:~$ sudo mount master:/home/pempar /home/pempar
```

9. MPI

MPI adalah singkatan dari "Message Passing Interface." Ini adalah standar komunikasi yang digunakan dalam pemrograman paralel, terutama dalam pemrograman terdistribusi untuk sistem berbasis kluster atau superkomputer.

> Install MPI

Melakukan instalasi MPI dengan command 'sudo apt install openmpi-bin libopenmpi-dev'

```
dinagnabile-virtualbox:-$ sudo apt install openmpi-bin libopenmpi-dev
Reading package lists... Done
Building dependency tree
Reading state information... Done
The floating package seminated
Building dependency tree
Reading state information... Done
The floating package seminated
Unbinous package seminated
Authority additional package seminated
unbinous packages
unbinous
unbinous
unbinous packages
unbinous
```

> Testing

Dilakukan di master, membuat file python di folder sebelumnya, dengan command 'touch <nama file>.py'

```
dina@khairunnisa-VirtualBox:/home/pempar$ sudo chmod -R 777 /home/pempar
dina@khairunnisa-VirtualBox:/home/pempar$ touch test.py
dina@khairunnisa-VirtualBox:/home/pempar$
```

Lalu, dapat melakukan pengeditan dalam file dengan menggunakan command 'nano <nama file>.py'

```
dina@khairunnisa-VirtualBox:/home/pempar$ nano test.py
```

10. Konfigurasi python

> Install python

Melakukan instalasi python versi 3 dengan menggunakan command 'sudo apt install python3-pip' dan python versi 2 dengan menggunakan command 'sudo apt install python-pip'

```
dinagkhairunnisa-VirtualBox:/home/pempar$ sudo apt install python3-pip
[sudo] password for dina:
Reading package lists... Done
Building dependency tree
Reading state information... Done
The following packages were automatically installed and are no longer required:
girl.2-goa-1.0 girl.2-snapd-1
Use 'sudo ant autoremove' to remove them
    gtrl.2-god-1.10 gtrl.2-snapo-1
Use 'sudo apt autoremove' to remove them.
The following additional packages will be installed:
build-essential dh-python dpkg-dev fakeroot g++ g++-7 libalgorithm-diff-perl
libalgorithm-diff-xs-perl libalgorithm-merge-perl libexpat1-dev libfakeroot libpython3-dev
libpython3.6-dev libstdc++-7-dev make python-pip-whl python3-dev python3-distutils
python3-lib2to3 python3-setuptools python3-wheel python3.6-dev
Suggested apskages:
        uggested packages:
debian-keyring g++-multilib g++-7-multilib gcc-7-doc libstdc++6-7-dbg libstdc++-7-doc make-doc
python-setuptools-doc
 python-setuptools-doc
The following NEW packages will be installed:
build-essential dh-python dpkg-dev fakeroot g++ g++-7 libalgorithm-diff-perl
libalgorithm-diff-xs-perl libalgorithm-merge-perl libexpat1-dev libfakeroot libpython3-dev
libpython3.6-dev libstdc++-7-dev make python-pip-whl python3-dev python3-distutils
python3-lib2to3 python3-pip python3-setuptools python3-wheel python3.6-dev
0 upgraded, 23 newly installed, 0 to remove and 0 not upgraded.
Need to get 60,0 MB of archives.
After this operation, 131 MB of additional disk space will be used.
Do you want to continue? [Y/n]
```

> Install pustaka MPI4

Melakukan instalasi pustaka MPI4 yang menyediakan dukungan untuk komunikasi dan pemrograman paralel menggunakan MPI (Message Passing Interface) dapat dilakukan dengan command 'pip install mpi4py'

```
khairunnisa-VirtualBox:~$ pip install mpi4py
Collecting mpi4py
Downloading https://files.pythonhosted.org/packages/2e/1a/1393e69df9cf7b04143a51776727dd048586781
bca82543594ab439e2eb4/mpi4py-3.1.5.tar.gz (2.5MB)
100% | | 2.5MB 280kB/s
Building wheels for collected packages: mpi4py
 Running setup.py bdist_wheel for mpi4py ... |
  Stored in directory: /home/dina/.cache/pip/wheels/6a/a2/4d/68998a0c10a3a307e55777b41b3da359a4742f
Successfully built mpi4py
Installing collected packages: mpi4py Successfully installed mpi4py-3.1.5
```

> Input kunci

Dilakukan oleh master untuk menyalin kunci publik SSH ke mesin worker sehingga master dapat masuk ke mesin worker tanpa diminta kata sandi setiap kali menggunakan command 'ssh-copy-id'

• Master - worker1

Master – worker2

```
dina@master:~$ ssh-copy-id dina@worker2
/usr/bin/ssh-copy-id: INFO: Source of key(s) to be installed: "/home/dina/.ssh/
inles sa.pub"
/usr/bin/ssh-copy-id: INFO: attempting to log in with the new key(s), to filter
out any that are already installed
/usr/bin/ssh-copy-id: INFO: 1 key(s) remain to be installed -- if you are promp
ted now it is to install the new keys
dina@worker2's password:

Number of key(s) added: 1

Now try logging into the machine, with: "ssh 'dina@worker2'"
and check to make sure that only the key(s) you wanted were added.
```

• Master – worker3

```
lina@master:~$ ssh-copy-id dina@worker3
/usr/bin/ssh-copy-id: INFO: Source of key(s) to be installed: "/home/dina/.ssh/
.d_rsa.pub"
/usr/bin/ssh-copy-id: INFO: attempting to log in with the new key(s), to filter
out any that are already installed
/usr/bin/ssh-copy-id: INFO: 1 key(s) remain to be installed -- if you are promp.
```

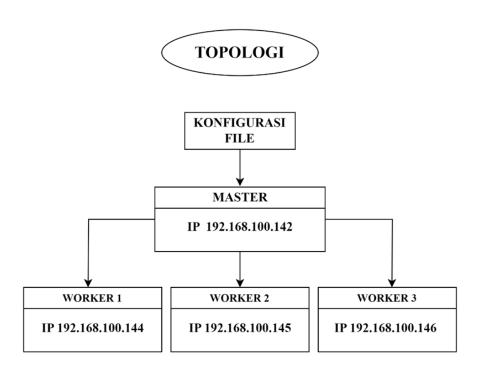
> Testing

Melakukan uji coba untuk menghasilkan perintah dasar python pada setiap device dengan hasil output "Hello, World!" dengan menggunakan command 'mpirun -np <jumlah prosesor> -host <daftar host> python3 test.py'

```
dina@master:~$ mpirun -n 4 -host master,worker1,worker2,worker3 python3 -m mpi4 py.bench helloworld
Hello, World! I am process 0 of 4 on master.
Hello, World! I am process 1 of 4 on worker1.
Hello, World! I am process 2 of 4 on worker2.
Hello, World! I am process 3 of 4 on worker3.
```

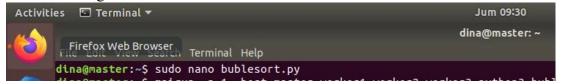
11. Bubble Sort

Bubble Sort adalah salah satu algoritma pengurutan sederhana yang digunakan dalam pemrograman. Algoritma ini bekerja dengan membandingkan dan menukar elemenelemen dalam daftar satu per satu hingga seluruh daftar terurut.



Input coding

Melakukan pengeditan pada file python dengan memasukkan codingan mengenai buble sort dengan command 'sudo nano'



```
Import multiprocessing
import time

def bubble_sort(arr, node_id):
    start_time = time.time()
    n = len(arr)
    for i in range(n):
    Rhythmbox j in range(0, n-i-1):
        if arr[j] > arr[j+1] = arr[j+1], arr[j]
        print(f"Node {node_id}: Step {i + 1} - {arr}")
    end_time = time.time()
    elapsed_time = end_time - start_time
    print(f"Node {node_id}: Sorted array: {arr}")
    print(f"Node {node_id}: Time taken: {elapsed_time} seconds")

if __name__ == '__main__':
    arr = [45 , 90 , 72 , 18 , 11 , 28]
    processes = []

for i in range(4): # specify the number of processes as required
    p = multiprocessing.Process(target=bubble_sort, args=(arr, i))
        processes.append(p)
    p.start()

for process in processes:
    process.join()
```

Menjalankan file yang telah diedit dengan command 'mpirun -np <jumlah prosesor> -host <daftar host> python3 <nama file>.py'

Dari proses yang telah berjalan, maka akan menghasilkan output berupa pengurutan dari data yang telah diinput pada codingan.

```
dina@master:~$ mpirun -n 1 -host master,worker1,worker2,worker3 python3 bublesort.py
Node 1: Step 1 - [45, 72, 18, 11, 28, 90]
Node 0: Step 1 - [45, 72, 18, 11, 28, 90]
Node 0: Step 1 - [45, 72, 18, 11, 28, 90]
Node 0: Step 2 - [45, 18, 11, 28, 72, 90]
Node 0: Step 3 - [11, 18, 28, 45, 72, 90]
Node 0: Step 4 - [11, 18, 28, 45, 72, 90]
Node 0: Step 5 - [11, 18, 28, 45, 72, 90]
Node 0: Step 5 - [11, 18, 28, 45, 72, 90]
Node 0: Step 6 - [11, 18, 28, 45, 72, 90]
Node 1: Step 2 - [45, 18, 11, 28, 72, 90]
Node 0: Sorted array: [11, 18, 28, 45, 72, 90]
Node 0: Sorted array: [11, 18, 28, 45, 72, 90]
Node 0: Time taken: 0.002367734909057617 seconds
Node 2: Step 2 - [45, 18, 11, 28, 45, 72, 90]
Node 1: Step 4 - [11, 18, 28, 45, 72, 90]
Node 1: Step 5 - [11, 18, 28, 45, 72, 90]
Node 2: Step 3 - [18, 11, 28, 45, 72, 90]
Node 2: Step 5 - [11, 18, 28, 45, 72, 90]
Node 2: Step 5 - [11, 18, 28, 45, 72, 90]
Node 2: Step 6 - [11, 18, 28, 45, 72, 90]
Node 2: Step 6 - [11, 18, 28, 45, 72, 90]
Node 2: Step 6 - [11, 18, 28, 45, 72, 90]
Node 2: Step 6 - [11, 18, 28, 45, 72, 90]
Node 2: Step 6 - [11, 18, 28, 45, 72, 90]
Node 2: Sorted array: [11, 18, 28, 45, 72, 90]
Node 3: Step 1 - [45, 72, 18, 11, 28, 90]
Node 3: Step 3 - [18, 11, 28, 45, 72, 90]
Node 3: Step 4 - [11, 18, 28, 45, 72, 90]
Node 3: Step 5 - [11, 18, 28, 45, 72, 90]
Node 3: Step 4 - [11, 18, 28, 45, 72, 90]
Node 3: Step 5 - [11, 18, 28, 45, 72, 90]
Node 3: Step 5 - [11, 18, 28, 45, 72, 90]
Node 3: Step 5 - [11, 18, 28, 45, 72, 90]
Node 3: Step 5 - [11, 18, 28, 45, 72, 90]
Node 3: Step 6 - [11, 18, 28, 45, 72, 90]
Node 3: Step 6 - [11, 18, 28, 45, 72, 90]
Node 3: Step 6 - [11, 18, 28, 45, 72, 90]
Node 3: Step 6 - [11, 18, 28, 45, 72, 90]
Node 3: Step 6 - [11, 18, 28, 45, 72, 90]
Node 3: Step 6 - [11, 18, 28, 45, 72, 90]
Node 3: Step 6 - [11, 18, 28, 45, 72, 90]
Node 3: Step 6 - [11, 18, 28, 45, 72, 90]
Node 3: Step 6 - [11, 18, 28, 45, 72, 90]
Node 3: Step 6 - [11, 18, 28, 45, 72, 90]
Node 3: Step 6 - [11, 18, 28, 45, 72, 90]
Node 3: Step 6 - [11, 18, 28, 45, 72, 90]
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