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LAB REPORT

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# Differential Evolution Algorithms

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# Chapter 1

## Implementation of a Differential Evolution Algorithm

### 1.1 Code

```

%% Parameters %%
num_pop = 45; % Population Number
factor = 0.1; % Scaling Factor
cross_rate = 0.2; % Crossover Rate
max_iter = 1000; % Maximum Number of Iterations

Pop = zeros(num_pop, 4);

%% Initialization phase %%

for i = 1 : num_pop
    Pop(i, 1) = 10 + 70 * rand();
    Pop(i, 2) = 10 + 40 * rand();
    Pop(i, 3) = 0.9 + 4.1 * rand();
    Pop(i, 4) = 0.9 + 4.1 * rand();
end

%% Differential Evolution Algorithm %%
iterations = 0;
while iterations < max_iter
    NewPop = Pop;

    % For every member of the population
    for j = 1 : num_pop
        Parent = Pop(j,:);

        % We choose three random members
        X1 = randi([1, num_pop]);
        while (X1 == j)
            X1 = randi([1, num_pop]);
        end
        X2 = randi([1, num_pop]);
        while (X2 == X1 || X2 == j)
            X2 = randi([1, num_pop]);
        end
        X3 = randi([1, num_pop]);
        while (X3 == X1 || X3 == X2 || X3 == j)
            X3 = randi([1, num_pop]);
        end

        Xr1 = Pop(X1,:);
        Xr2 = Pop(X2,:);
        Xr3 = Pop(X3,:);

        % Compute the mutant member
        Vi = Xr1 + factor * (Xr2 - Xr3);
        Ui = zeros(1,4);
    end
    iterations = iterations + 1;
end

```

```

% Replicate from parent
for k = 1 : 4
    if rand() <= cross_rate
        if k == 1 || k == 2 && Vi(k) < 10
            Vi(k) = 10;
        end
        if k == 1 && Vi(k) > 80
            Vi(k) = 80;
        end
        if k == 2 && Vi(k) > 50
            Vi(k) = 50;
        end
        if k == 3 || k == 4 && Vi(k) < 0.9
            Vi(k) = 0.9;
        end
        if k == 3 || k == 4 && Vi(k) > 5
            Vi(k) = 5;
        end
        Ui(k) = Vi(k);
    else
        Ui(k) = Parent(k);
    end
end

% Select parent or child for the new population
if I_BEAM(Ui) < I_BEAM(Parent)
    Yi = Ui;
else
    Yi = Parent;
end

NewPop(j,:) = Yi;
end

iterations = iterations + 1;
Pop = NewPop;
end

%% Find Best Candidate %%
best = 1;
for i = 2 : num_pop
    if I_BEAM(Pop(best,:)) > I_BEAM(Pop(i,:))
        best = i;
    end
end

Best.Solution = Pop(best,:)
Best.Value = I_BEAM(Pop(best,:))

```

## 1.2 Results

We run the differential algorithm 3 times for 3 different parameter values and compare its results with the genetic algorithm.

1. Parameters:
  - Population number = 25
  - Scaling Factor = 0.5
  - Crossover Rate = 0.5
  - Maximum Iterations = 1000
- (a) 1st run
  - Best solution:  $x = [70.48 \ 36.94 \ 1.00 \ 0.90]$
  - Best value:  $z = 135.78$
- (b) 2nd run
  - Best solution:  $x = [75.80 \ 35.50 \ 1.11 \ 0.90]$
  - Best value:  $z = 146.51$
- (c) 3rd run
  - Best solution:  $x = [68.65 \ 34.35 \ 1.77 \ 0.90]$
  - Best value:  $z = 180.30$

## 2. Parameters:

Population number = 35  
Scaling Factor = 1.5  
Crossover Rate = 0.8  
Maximum Iterations = 1000

## (a) 1st run

Best solution:  $x = [46.14 \ 46.54 \ 2.17 \ 0.90]$   
Best value:  $z = 180.27$

## (b) 2nd run

Best solution:  $x = [65.64 \ 40.08 \ 1.09 \ 0.90]$   
Best value:  $z = 142.27$

## (c) 3rd run

Best solution:  $x = [69.34 \ 38.78 \ 0.98 \ 0.90]$   
Best value:  $z = 136.63$

## 3. Parameters:

Population number = 45  
Scaling Factor = 0.1  
Crossover Rate = 0.2  
Maximum Iterations = 1000

## (a) 1st run

Best solution:  $x = [70.08 \ 35.46 \ 1.13 \ 0.93]$   
Best value:  $z = 143.78$

## (b) 2nd run

Best solution:  $x = [40.97 \ 28.54 \ 0.98 \ 2.27]$   
Best value:  $z = 166.05$

## (c) 3rd run

Best solution:  $x = [71.61 \ 29.88 \ 0.91 \ 1.24]$   
Best value:  $z = 137.32$

## 4. Genetic Algorithm

## (a) 1st run

Best solution:  $x = [63.06 \ 34.86 \ 0.90 \ 1.10]$   
Best value:  $z = 131.83$

## (b) 2nd run

Best solution:  $x = [62.13 \ 23.46 \ 0.90 \ 2.02]$   
Best value:  $z = 147.29$

## (c) 3rd run

Best solution:  $x = [51.95 \ 21.75 \ 0.90 \ 2.65]$   
Best value:  $z = 157.35$

And the `fmincon` Matlab function gave the following results:

1. Starting point:  $x = [10 \ 10 \ 0.9 \ 0.9]$ 

Best solution:  $x = [78.39 \ 34.93 \ 0.90 \ 0.90]$   
Best value:  $z = 131.86$

2. Starting point:  $x = [80 \ 50 \ 5 \ 5]$ 

Best solution:  $x = [44.95 \ 17.99 \ 3.13 \ 3.58]$   
Best value:  $z = 247.45$