Contenidos

• Operaciones.

1. Calcular:

(a)
$$\frac{15}{16} - \frac{1}{48} - \frac{1}{96} - \frac{1}{80}$$

(b)
$$4 + \frac{3}{4} - \left(\frac{1}{2} \cdot 5\right) + \left(\frac{5}{8} \cdot \frac{2}{15}\right) - \frac{3}{2} \left(\frac{1}{2} + \left(\frac{1}{2} \cdot 4\right)\right)$$

(c)
$$3 + \frac{1}{3 + \frac{1}{1 - \frac{1}{3}}}$$

(d)
$$\frac{\frac{3/4}{1/6} + \frac{17/3}{1/12}}{6 + \left(8 - \frac{1}{4}\right)} + 3$$

(e)
$$\frac{\left(\frac{1}{10} + \frac{2}{25} + \frac{3}{40}\right) \cdot \frac{1}{6}}{\frac{1}{8} - \frac{1}{12}}$$

(f)
$$\frac{\left(0.2\overline{4} + \frac{1}{3} + 0.\overline{2}\right) \cdot \frac{5}{4}}{3 + 0.\overline{153}}$$

2. Evaluar las siguientes expresiones algebraicas:

(a)
$$a^2 - ab + b^3$$
, si $a = 2, b = -2$

(b)
$$4x^2 - 3x - 1$$
, si $x = 1$

(c)
$$(x+y)^2 - 4xy$$
, si $x = 3, y = 3$

(d)
$$(x^2 + y^2)^2 - 4xy$$
, si $x = 2, y = x$

(e)
$$2ab - 3(a+b) + 2c^2$$
, si $a = -1, b = \frac{1}{3}, c = -\sqrt{5}$

(f)
$$a^2bc + ab^2c + abc^2$$
, si $a = -2, b = 4$

(g)
$$\frac{p}{q^2} + \frac{q}{p}$$
, si $p = 2, q = 3$

(h)
$$\frac{4}{p} - \frac{5}{p^2} + \frac{1}{p^3}$$
, si $p = -2$

(i)
$$\frac{|a-b|+(a+b)}{2}$$
, si $a > b$

(j)
$$\frac{|a-b| + (a+b)}{2}$$
, si $a < b$

(k)
$$\left(\frac{p^2-1}{p} - \frac{pq^2}{r} + \frac{r^2}{pq}\right)^2 - \frac{pqr}{p+q+r}$$
, si $p = 2, q = 3, r = -4$

(1)
$$\frac{p - \frac{2}{p+1}}{1 - \frac{q+7}{p^2 + q + 3}}, \text{ si } q = 4p, p = 2.$$

3. Reduzca los términos semejantes en las siguientes expresiones algebraicas:

(a)
$$(8x - 4y + 2) + (3x + 2y - 5)$$

(b)
$$\frac{a^2b}{5} - 2\frac{ab^2}{3} + 3\frac{ab^2}{2} - 6\frac{a^2b}{5}$$

(c)
$$-[-(a-2b)-(a+2b)-(a-3b)]$$

(d)
$$3(3x+3y-7)-3(8x-2y+2)$$

(e)
$$-3\{4x(x+2)-2[x^2-(3-x)]\}$$

(f)
$$16x + [-7 - (4x^2 - 1)] - [-(5x + 1) + (-2x^2 + 9 - 6x)]$$

(g)
$$(\frac{2}{3}x-2)(x-\frac{1}{3})$$

(h)
$$(5x^2+2)(x^2-4)$$

(i)
$$(2\sqrt{x}+1)(4\sqrt{x}-3)$$

(j)
$$(4x+8)(x^2-6x)$$

(k)
$$(z^3 + 4z - 3)(2z^3 - 7z + 1)$$

(1)
$$2u(3u+1)(3u-1)$$

4. Factorice las siguientes expresiones

(a)
$$6x^5y^5 + \sqrt{2}x^2y^3 + 14xy^3$$

(b)
$$xyz^3 - xy^3z + x^3yz$$

(c)
$$2p^3 - p^2 + 2p - 1$$

(d)
$$3a^2b^3 - 3\sqrt{2}a^4b^2 + 9a^2b$$

(e)
$$x^4 - y^4$$

(f)
$$8x^3y^3 + 27$$

(g)
$$t^2 - \frac{1}{4}$$

(h)
$$2p^2 + 7p + 5$$

(i)
$$4x^2 + 12x + 9$$

(j)
$$\frac{m^2}{4} + 3\frac{m}{n^2} + \frac{9}{n^4}$$

(k)
$$s^8 - 6561$$

(1)
$$x^2 + 2xy + y^2 + 3x + 3y + 2$$

(m)
$$(x+3)^2(x+2)^3 - 20(x+3)(x+2)^2$$