

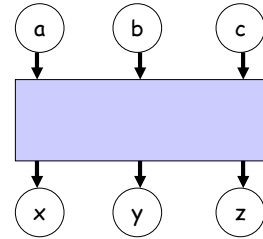
## 5. Boundary Value testing

### Boundary Value Analysis

Robustness  
Worst-Case  
Robust Worst-Case  
Special Value  
Random  
Equivalence classes

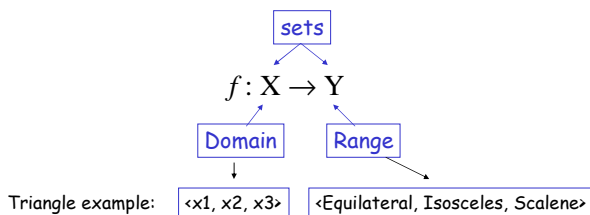
## Boundary Value analysis

- Any software to be tested can be thought of as a function that associates its inputs with its outputs

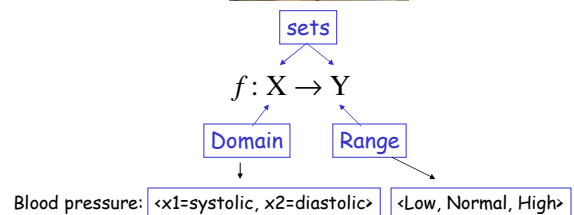


## Boundary Value analysis

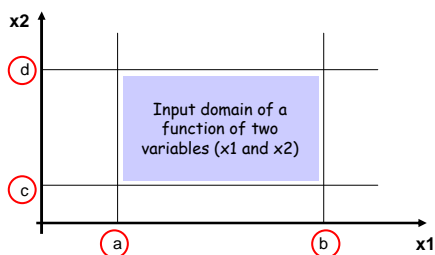
- Any software to be tested can be thought of as a function that associates its inputs with its outputs



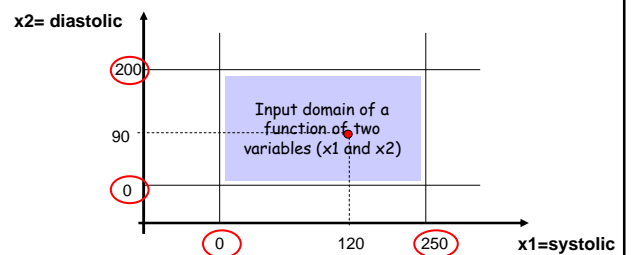
Blood pressure



## Boundary Value analysis



## Boundary Value analysis



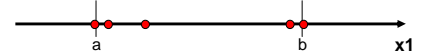
## Boundary Value analysis

- Boundary value analysis focuses on the boundaries of the domain
- Rationale: errors occur most frequently on or near the boundary
- It makes a **Single Fault Assumption**:

"Failures are only rarely the result of the simultaneous occurrence of two or more faults."

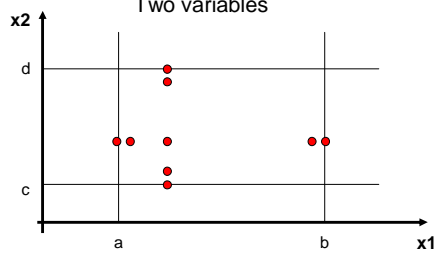
## Boundary Value analysis

Single variable



## Boundary Value analysis

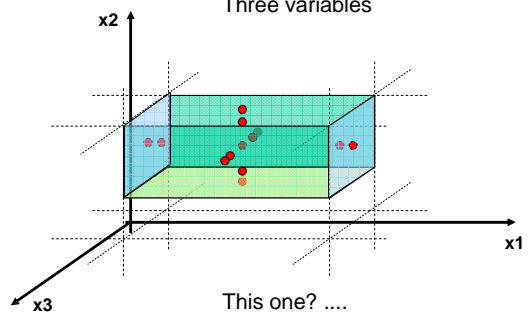
Two variables



- How many boundary tests for 2, 3, ..., n variables?  
 $4n + 1$

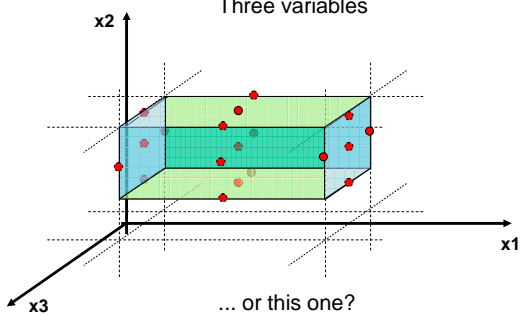
## Boundary Value analysis

Three variables



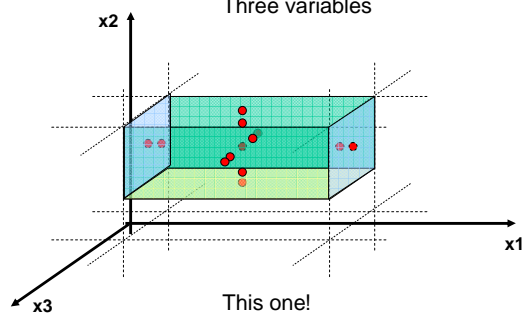
## Boundary Value analysis

Three variables



## Boundary Value analysis

Three variables



## The triangle problem – full specification



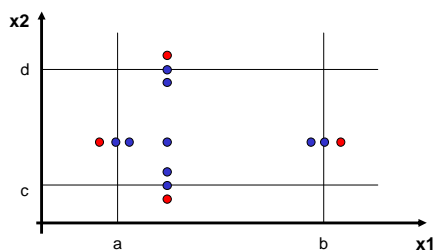
Specify boundary tests for the triangle problem

## Boundary Value analysis Problems and limitations

- Bounds may not be always obvious (e.g. an upper bound for the triangle problem)
- Bounds may not be appropriate (e.g. for boolean values; [Decision Table Testing](#) is better)
- No bounds in cases of enumerated variables (e.g. in bank transactions "deposit", "withdrawal", "query")
- No testing for negative cases ✓

## Robustness testing

- Extension of the Boundary Value Analysis
- Examines the cases when the boundaries are slightly exceeded (negative testing)



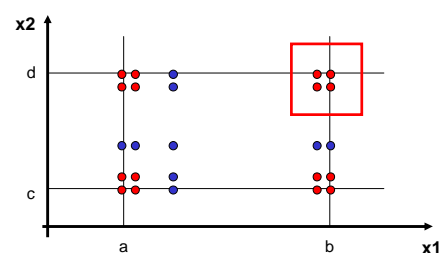
## Robustness testing

- Main value of robustness testing: focuses attention on exception handling
- This can also influence implementation:
  - Do we carry out explicitly exception handling for every case OR
  - Do we let the behaviour associated with "strong typing" to take its course and abort execution? Do we treat such a case as a "FAILED" test?

## Worst case testing

- Boundary Value Analysis makes the "single fault" assumption  
*Failures are only rarely the result of the simultaneous occurrence of two or more faults*
- Worst case testing is interested in what happens when more than one variable has an extreme value simultaneously
- Best used when variables may have complex interactions and where the [impact](#) of failure is large

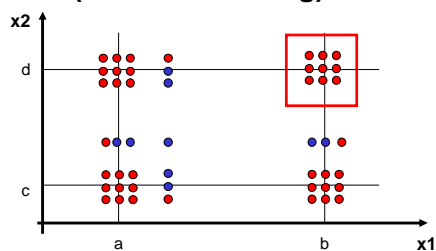
## Worst case testing



- How many boundary tests for 2, 3, ..., n variables?

$$5^n$$

## Robust Worst-Case testing (Paranoid Testing)



- How many boundary tests for 2, 3, ..., n variables?

$$7^n$$

## NextDate function

NextDate is a function of three variables:

- month
- day
- year

It returns the date of the day after the input date in the form of three variables <month, day, year>.

The month, date and year variables have integer values subject to the following conditions:

- $1 \leq \text{month} \leq 12$
- $1 \leq \text{day} \leq 31$
- $1820 \leq \text{year} \leq 2020$

## NextDate function

- What is the Domain for the NextDate problem?
- What is the dimension of the Domain?
- What is the Range for the NextDate problem?
- How many boundary values are there in total?
- Variable types (SNM / ROV / GV):
  - month?
  - day?
  - year?
- Is the Boundary Value testing likely to uncover most of the errors?

## Special value testing

- Tester uses the domain knowledge and experience to select test values
- Ad hoc and not based on any principles
- The least systematic and least uniform of the methods
- Can be of value when used in addition to one of the systematic methods
- Example: computing next date

## Random testing

- Random values are picked from the specified ranges
- The main question: how many values are sufficient?

(Test Coverage Metrics can provide the answer)

- Example – random test cases for the NextDate program

## NextDate function

- What is the key reason why the Boundary Value analysis alone is not adequate for the NextDate function?

## Boundary Value analysis Problems and limitations

- Bounds may not be always obvious (e.g. an upper bound for the triangle problem)
- Bounds may not be appropriate (e.g. for boolean values; "Decision Table" Testing is better)
- No bounds in cases of enumerated variables (e.g. in bank transactions "deposit", "withdrawal", "query")
- No testing for negative cases
- Inadequate when there are dependencies between the variables.

## Dependency between variables

- Testing for the cases where there are dependencies between the variables is better done using the [Equivalence Class Testing](#) methods (next unit)

## Equivalence classes

- In mathematics, given a [set](#)  $X$  and an [equivalence relation](#)  $\sim$  on  $X$ , the [equivalence class](#) of an element  $a$  in  $X$  is the subset of all elements in  $X$  which are equivalent to  $a$ .
- $[a] = \{ x \in X \mid x \sim a \}$
- If  $X$  is the set of all cars, and  $\sim$  is the equivalence relation "has the same colour as", then one particular equivalence class consists of all green cars.
- The set of equivalence classes could be naturally identified with the set of all car colours.

## Equivalence classes



## Equivalence classes

- Because of the properties of an equivalence relation, it holds that
  - the element  $a$  is in the equivalence class  $[a]$
  - any two equivalence classes, according to the same equivalence relation, are either equal or disjoint.
- The set of all equivalence classes of  $X$  forms a [partition of  \$X\$](#) :
  - every element of  $X$  belongs to one and only one equivalence class
  - every partition of  $X$  also defines an equivalence relation over  $X$
  - $a \sim b$  if and only if  $[a] = [b]$ .

Partition of the set  $X$  of cars according to the equivalence relation "has the same colour as"

