

Graphics 2
Matrix and vector operations
Non-assessed exercise

This exercise is to develop practical skills in matrix and vector operations (see handout *Mathematical Tools for Computer Graphics*).

The solutions will be available on 17th January at:
<http://www.cs.bham.ac.uk/~exc/Teaching/Graphics/>

Matrix operations

Let:

$$A = \begin{bmatrix} 3 & 2 \\ 4 & 1 \end{bmatrix} \quad B = \begin{bmatrix} 0 & -2 \\ 4 & 5 \end{bmatrix} \quad C = \begin{bmatrix} 4 & 1 & 0 \\ 1 & 3 & 2 \\ 0 & 2 & 5 \end{bmatrix} \quad D = \begin{bmatrix} 2 \\ 1 \\ 4 \end{bmatrix} \quad E = \begin{bmatrix} 9 & 0 & 5 \end{bmatrix}$$

Calculate the following expressions or give reasons why they are undefined:

- | | |
|-------------|-------------|
| 1. $A + B$ | 8. $B * A$ |
| 2. $B + A$ | 9. $A * D$ |
| 3. $C + D$ | 10. $C * D$ |
| 4. $C + E$ | 11. $D * C$ |
| 5. $3E$ | 12. $E * C$ |
| 6. $2A + B$ | 13. $D * E$ |
| 7. $A * B$ | 14. $E * D$ |

Vector operations

Let:

$$\vec{a} = \begin{bmatrix} 1 & 1 & 0 \end{bmatrix} \quad \vec{b} = \begin{bmatrix} -1 & 2 & 0 \end{bmatrix} \quad \vec{c} = \begin{bmatrix} 2 & 3 & 1 \end{bmatrix} \quad \vec{d} = \begin{bmatrix} 5 & -7 & 2 \end{bmatrix} \quad \vec{e} = \begin{bmatrix} 7 & -7 & 1 \end{bmatrix}$$

Calculate the following expressions:

- | | |
|-----------------------------|---|
| 15. $3 \cdot \vec{a}$ | 21. $\vec{c} \cdot \vec{d}$ |
| 16. $-2 \cdot \vec{c}$ | 22. $\vec{a} \times \vec{b}$ |
| 17. $\vec{a} + \vec{b}$ | 23. $\vec{b} \times \vec{a}$ |
| 18. $\vec{c} - \vec{d}$ | 24. $\vec{a} \times \vec{c} + \vec{c} \times \vec{a}$ |
| 19. $\vec{a} \cdot \vec{b}$ | 25. $\vec{a} \times \vec{e}$ |
| 20. $\vec{b} \cdot \vec{a}$ | |

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SOLUTIONS

Matrix operations

$$A = \begin{bmatrix} 3 & 2 \\ 4 & 1 \end{bmatrix} \quad B = \begin{bmatrix} 0 & -2 \\ 4 & 5 \end{bmatrix} \quad C = \begin{bmatrix} 4 & 1 & 0 \\ 1 & 3 & 2 \\ 0 & 2 & 5 \end{bmatrix} \quad D = \begin{bmatrix} 2 \\ 1 \\ 4 \end{bmatrix} \quad E = [9 \ 0 \ 5]$$

1. $A + B = \begin{bmatrix} 3 & 0 \\ 8 & 6 \end{bmatrix}$

2. $B + A = \begin{bmatrix} 3 & 0 \\ 8 & 6 \end{bmatrix}$

3. $C + D$ Undefined, matrices have to be of the same size

4. $C + E$ Undefined, matrices have to be of the same size

5. $3E = [27 \ 0 \ 15]$

6. $2A + B = \begin{bmatrix} 6 & 2 \\ 12 & 7 \end{bmatrix}$

7. $A * B = \begin{bmatrix} 8 & 4 \\ 4 & -3 \end{bmatrix}$

8. $B * A = \begin{bmatrix} -8 & -2 \\ 32 & 13 \end{bmatrix}$

10. $C * D = \begin{bmatrix} 9 \\ 13 \\ 22 \end{bmatrix}$

11. $D * C$ Undefined. The number of columns in the first matrix must be equal to the number of rows in the second matrix

12. $E * C = [36 \ 19 \ 25]$

$$13. \quad D * E = \begin{bmatrix} 18 & 0 & 10 \\ 9 & 0 & 5 \\ 36 & 0 & 20 \end{bmatrix}$$

$$14. \quad E * D = [38]$$

Vector operations

$$\bar{a} = [1 \quad 1 \quad 0] \quad \bar{b} = [-1 \quad 2 \quad 0] \quad \bar{c} = [2 \quad 3 \quad 1] \quad \bar{d} = [5 \quad -7 \quad 2]$$

$$15. \quad 3 \bar{a} = [3 \quad 3 \quad 0]$$

$$16. \quad -2 \bar{c} = [-4 \quad -6 \quad -2]$$

$$17. \quad \bar{a} + \bar{b} = [0 \quad 3 \quad 0]$$

$$18. \quad \bar{c} - \bar{d} = [-3 \quad 10 \quad -1]$$

$$19. \quad \bar{a} \cdot \bar{b} = 1$$

$$20. \quad \bar{b} \cdot \bar{a} = 1$$

$$21. \quad \bar{c} \cdot \bar{d} = -9$$

$$22. \quad \bar{a} \times \bar{b} = [0 \quad 0 \quad 3]$$

$$23. \quad \bar{b} \times \bar{a} = [0 \quad 0 \quad -3]$$

$$24. \quad \bar{a} \times \bar{c} + \bar{c} \times \bar{a} = [0 \quad 0 \quad 0]$$

$$25. \quad \bar{a} \times \bar{e} = [1 \quad -1 \quad -14]$$