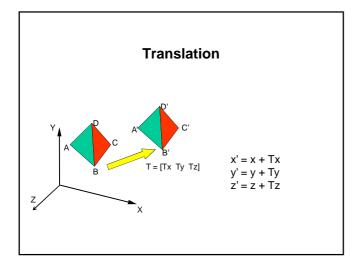


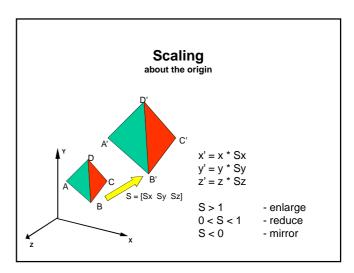
Sweep functions: implementation

3D Transformations – quick revision

Basic transformations

- Translation (shift)
- Scaling
- Rotation

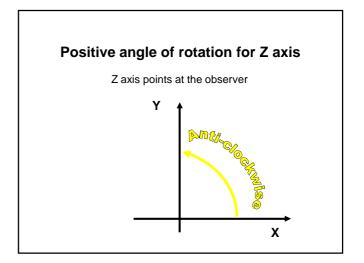


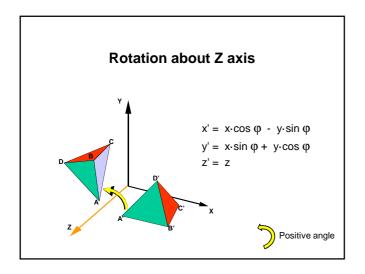


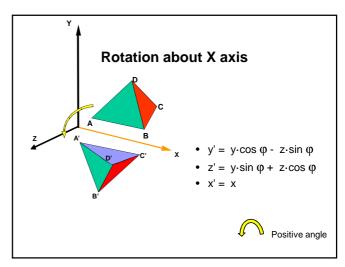
Rotation

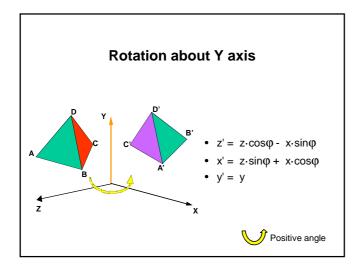
in the right-handed coordinate system

Positive angle of rotation is <u>counter-clockwise</u> when the axis about which it occurs points toward the observer









Rotation	
Axis of rotation is	Direction of positive rotation is
X	from Y to Z
Y	from Z to X
Z	from X to Y

Matrix representation Homogeneous coordinates

- Common notation for ALL transformations
- Common computational mechanism for ALL transformations
- Simple mechanism for combining a number of transformations => computational efficiency

Homogeneous coordinates

• Point P = (x, y, z) represented by a vector

$$P = \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = [x \ y \ z \ 1]^T$$

• Transformations
All represented by a 4 x 4 matrix M

Point transformation in homogeneous coordinates

• Implemented by matrix multiplication P' = M · P

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} a & d & g & j \\ b & e & h & k \\ c & f & i & l \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

Transformation matrices for elementary transformations

- 4 x 4 matrix
- · Homogeneous coordinates
- Translation, scaling, rotation and perspective projection, all defined through matrices

See this website for a nice explanation of homogeneous coordinates:

http://www.devmaster.net/forums/showthread.php?t=2092

Translation

$$x' = x + Tx$$

$$y' = y + Ty$$

$$z' = z + Tz$$

$$T = \begin{bmatrix} 1 & 0 & 0 & T_X \\ 0 & 1 & 0 & T_Y \\ 0 & 0 & 1 & T_Z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Scaling

$$x' = Sx * x$$

$$y' = Sy * y$$

$$z' = Sz * z$$

$$S = \begin{bmatrix} S_X & 0 & 0 & 0 \\ 0 & S_Y & 0 & 0 \\ 0 & 0 & S_Z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Rotation about Z axis

$$x' = x \cdot \cos \phi - y \cdot \sin \phi$$

$$y' = x \cdot \sin \phi + y \cdot \cos \phi$$

z' = z

$$\mathsf{Rz} = \left[\begin{array}{cccc} \cos \phi & -\sin \phi & 0 & 0 \\ \sin \phi & \cos \phi & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right]$$

Rotation about X axis

$$y' = y \cdot \cos \phi - z \cdot \sin \phi$$

$$z' = y \cdot \sin \phi + z \cdot \cos \phi$$

x' = x

$$Rx = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos\varphi & -\sin\varphi & 0 \\ 0 & \sin\varphi & \cos\varphi & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Rotation about Y axis

$$z' = z \cdot \cos \phi - x \cdot \sin \phi$$

 $x' = z \cdot \sin \phi + x \cdot \cos \phi$
 $y' = y$

$$Ry = \begin{bmatrix} \cos \phi & 0 & \sin \phi & 0 \\ 0 & 1 & 0 & 0 \\ -\sin \phi & 0 & \cos \phi & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Key concepts for 3D transformations in Java

Class:

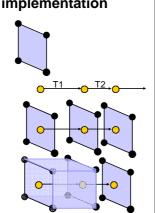
• Transform3D

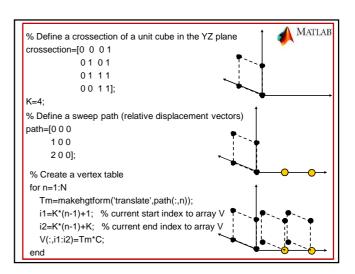
Example methods

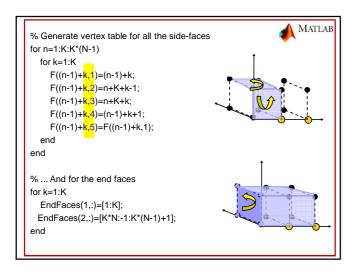
- setTranslation, setRotation, set Scale
- SetTransform
- rotX, rotY, rotZ
- transform
- mul

Sweep functions: implementation

- Translational sweep
 - Define a shape as a polygon vertex table
 - Define a sweep path as a sequence of translation vectors
 - Translate the shape, continue building a vertex
 table
 - Define a surface table

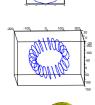




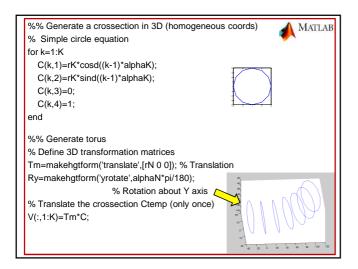


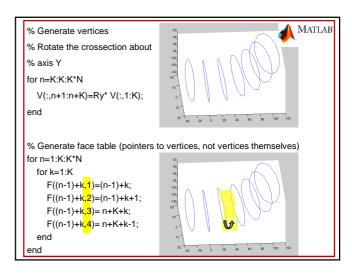
Sweep functions: implementation

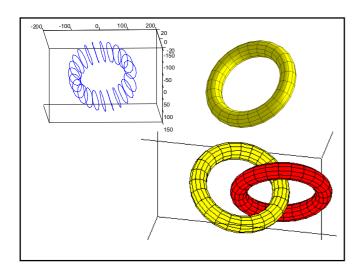
- · Rotational sweep
 - Define a shape as a polygon vertex table
 - Define a sweep path as a sequence of rotations
 - Rotate the shape, continue building a vertex table
 - Define a surface table

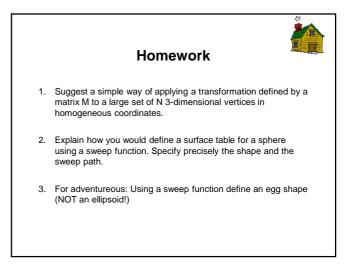












Matlab exercise

- Extend the code in 'ex2_torus.m' to define and display five linked toruses in different colours. You will also need file 'torus.m' which is a function generating the face and the vertex table for a torus. Matlab code for both functions is in file www.cs.bham.ac.uk/~exc/Teaching/Graphics/ex2_torus.zip
- Write Matlab code to generate a surface table for a sphere using a sweep function.

Reminder about Matlab tutorials

- http://www.cyclismo.org/tutorial/matlab/

 Work through the tutorial should take you 2-3 hours.
- http://www.cs.bham.ac.uk/~exc/Teaching/Graphics/Matlab_tutorial.pdf
- Ignore first five slides which have information relevant to the MIT course Matlab Help
- Have a look at the "Programming" and "Graphics" sections

Next lecture

Height maps Parametric surfaces