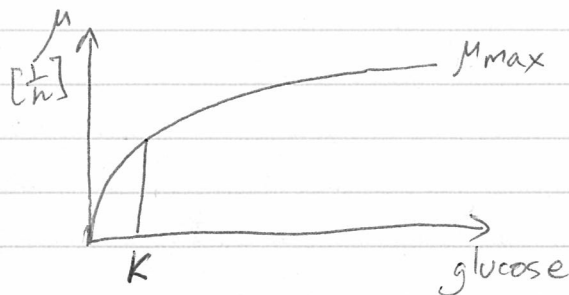


①

cell physiology: 1949 the growth of bacterial cultures

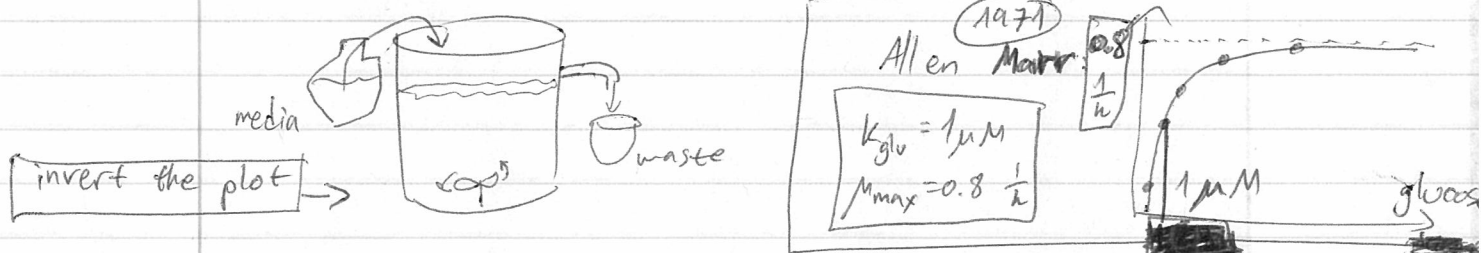


~~Two ways to measure that: batch and chemostat.~~

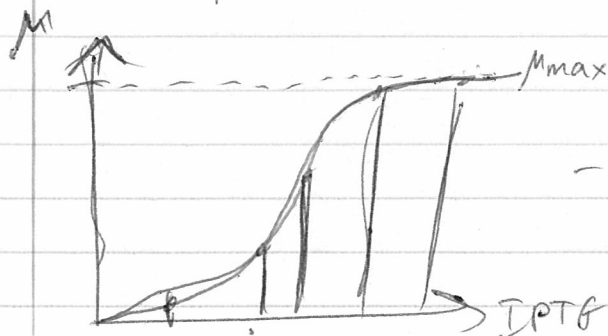
- It's very difficult to control (μ) using carbon limitation in batch.

- Also, chemostats work beautifully, but require high volumes and maintenance.

electronic counting
 $< 10^6$ cell cultures

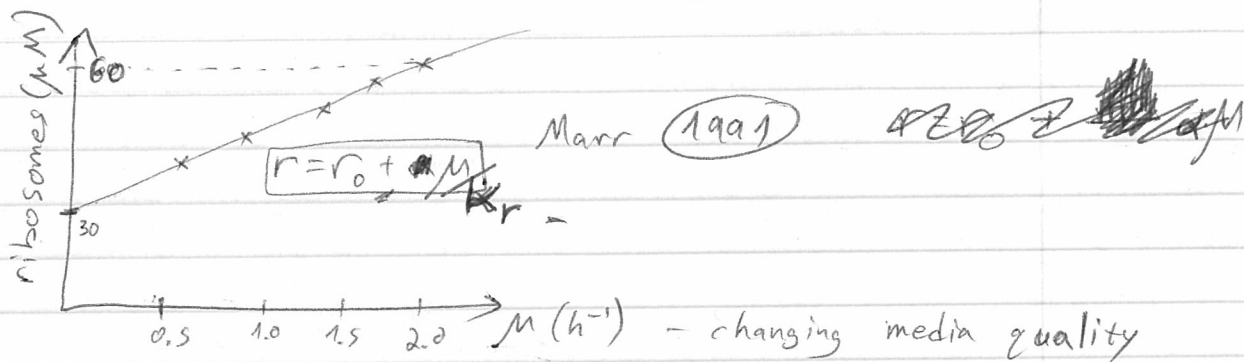


- Clever solution, artificially decrease the maximal uptake rate of glucose by controlling the expression of the transporter with IPTG



- same [glucose]

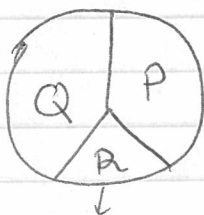
Ribosomes as a function of growth rate:



Terry Hua, Matthew Scott, Carl Gunderson Science 2010



fixed increases with μ

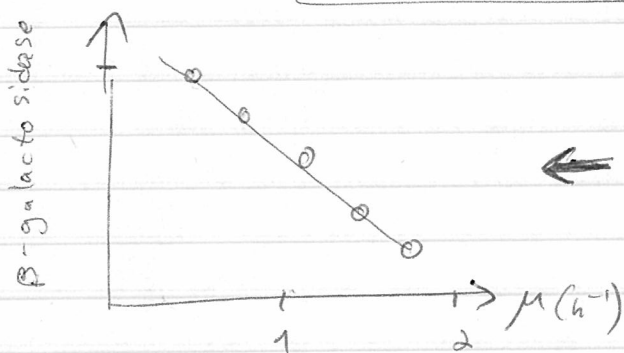


$1 = \phi_Q + \phi_R + \phi_P$ - therefore, must decrease

$\phi_P = 1 - \phi_Q - (\phi_{R_0} + K_r^{-1} \cdot \mu)$

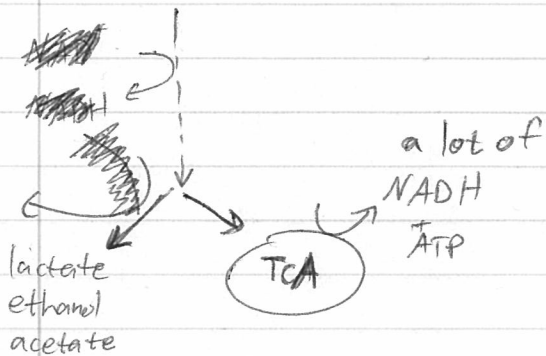
$\phi_P = \phi_{P_0} - K_r^{-1} \cdot \mu$

$\phi_{P_0} = 1 - \phi_Q - \phi_{R_0}$



★ Physiology facts: maximizing yield is not always the chosen strategy:

- Cancer cells - Warburg effect (lactate)
- Yeast cells - Crabtree effect (ethanol)
- Bacteria like E. coli - overflow metabolism (acetate)



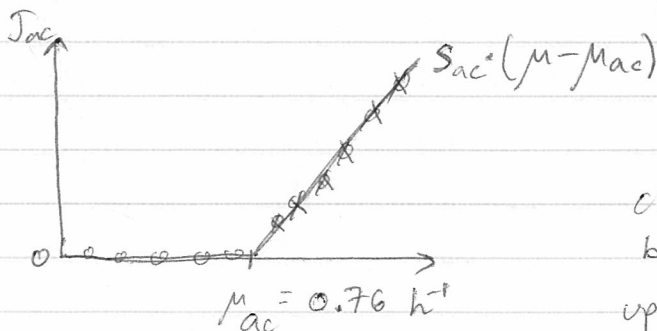
1 not enough oxygen?

2 membrane surface area?

Is this really sub-optimal?

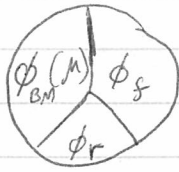
★ rate vs. yield hypothesis

★ Markos' work Basan et al. 2015 Nature



changing " μ " by limiting the uptake of carbon

↓
why?



resource

$$1 = \phi_f + \phi_r + \phi_{BM}$$

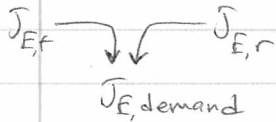
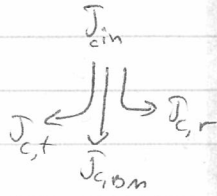
carbon balance

controlled

$$J_{c,in} \geq J_{c,f} + J_{c,r} + J_{c,BM}$$

energy balance

$$J_{E,demand} \leq J_{E,f} + J_{E,r}$$



assumptions: $\phi_{BM} = \phi_0 + \gamma \cdot \mu$

$$J_{c,BM} = \beta \cdot \mu$$

$$J_{E,demand} = \sigma \cdot \mu$$

$$J_{c,t} = k_f \phi_f$$

$$J_{c,r} = k_r \phi_r$$

$$J_{E,f} = \varepsilon_f \phi_f$$

$$J_{E,r} = \varepsilon_r \phi_r$$

$$\phi_f = 1 - \phi_0 - \gamma \cdot \mu - \phi_r$$

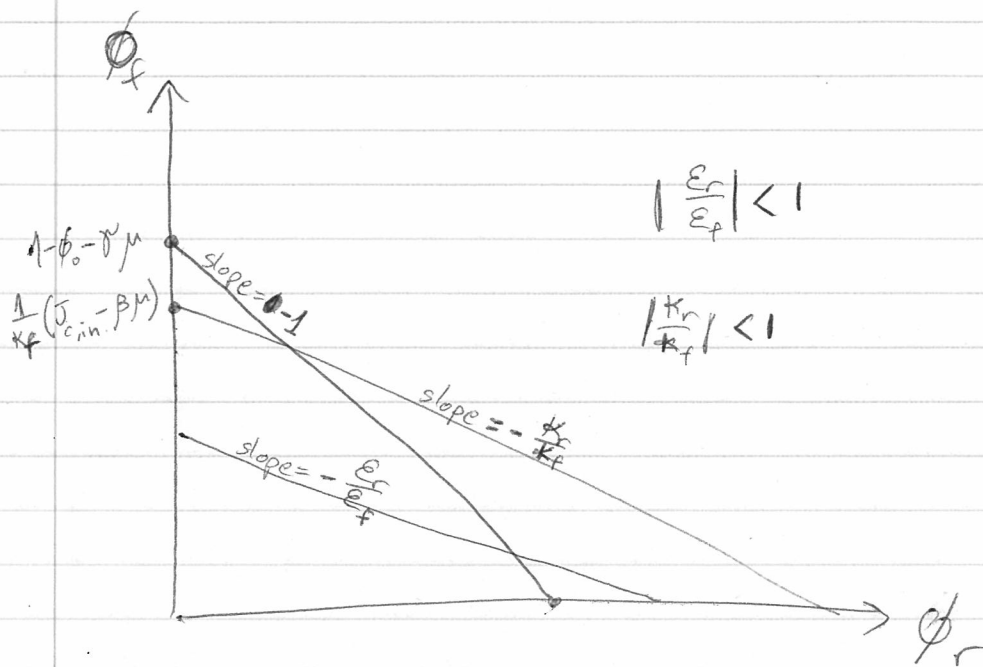
$$\phi_f \leq \frac{1}{k_f} [J_{c,in} - \beta \cdot \mu - k_r \cdot \phi_r]$$

$$\phi_f \geq \frac{1}{\varepsilon_f} [\sigma \cdot \mu - \varepsilon_r \cdot \phi_r]$$

$k_r < k_f$: respiration is carbon efficient

$\varepsilon_r < \varepsilon_f$: respiration requires more enzymes/protein for the same ATP flux

⑤

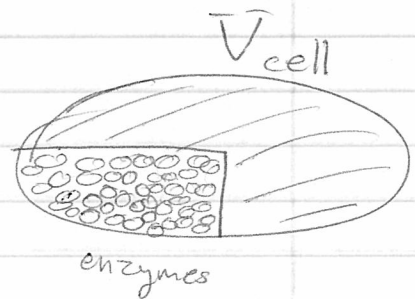


Is there a way to see ~~what~~ what E_f , K_r and K_f are from enzyme properties?

- ① have a full kinetic model and simulate the flux.
- ② use simplified kinetics, e.g. assume saturation.

Beg et al. 2007 PNAS

$$\sum_i \underbrace{V_i}_{\text{molar volume}} \underbrace{n_i}_{\text{copy number}} \leq \underbrace{V_{\text{cell}}}_{\text{cell volume dedicated to enzymes}} \left(\frac{1}{4} \right)$$



$$\underbrace{|v_i|}_{\text{flux}} \leq \underbrace{\quad}_{\text{[redacted]}} k_{\text{cat},i} \cdot n_i$$

$$S \cdot v = 0$$

maximize

v_{biomass}

ddy
ie