

The basic idea of the algorithm is to divide the contribution of a simulation cell (which is assumed to be spherical) over a number of grid-cells in the uniform grid.

For each sim-cell we find a patch in the uniform grid which fully encloses the sim-cell. The contribution of the sim-cell is divided over the grid-cells in the patch. For grid-cells which are only partially covered by the sim-cells (at the edge of sim-cell), we give a lower contribution from the sim-cell, based on the number grid-cell vertices which are within the sim-cell region.

This is how it is implemented:

This part gives, for each sim-cell, the indices of the grid cell in which it is centered.

```
indX=ceil((coords(1,:)./boxSide+0.5).*Ngrid);
indY=ceil((coords(2,:)./boxSide+0.5).*Ngrid);
indZ=ceil((coords(3,:)./boxSide+0.5).*Ngrid);
```

we ignore sim-cells whose center is found beyond the grid:

```
skipFlag= indX > Ngrid | indX < 1 | indY>Ngrid | indY<1 |
indZ>Ngrid | indZ<1;
```

Next, for each sim-cell we want to find the region of the grid which covers the sim-cell completely.

We translate the cell diameter to grid-units :

```
gcl=ceil(cellSize./(boxSide/Ngrid));
gcl=gcl+(1-mod(gcl,2));
gind=(gcl+1)/2
```

And using this we can now find the minimal and maximal grid-cell index, in each direction, which corresponds to a patch of the grid which fully encloses each sim-cell.

```
indXlo=indX-gind;indXhi=indX+gind;
indYlo=indY-gind;indYhi=indY+gind;
indZlo=indZ-gind;indZhi=indZ+gind;
```

We make sure the patch does not extend beyond the actual size of the grid:

```
indXlo(indXlo<1)=1;
indYlo(indYlo<1)=1;
indZlo(indZlo<1)=1;

indXhi(indXhi>Ngrid)=Ngrid;
indYhi(indYhi>Ngrid)=Ngrid;
indZhi(indZhi>Ngrid)=Ngrid;
```

Now we generate physical positions for the vertices of the grid:

```
gl=boxSide/Ngrid;  
xg=-0.5*boxSide:gl:0.5*boxSide;  
yg=xg;zg=xg;  
[vertY,vertX,vertZ]=meshgrid(xg,yg,zg);
```

Next, we loop over the sim-cells, and for every cell we do the following:

These are the indices of the grid-cells in the patch - we use them to assign the values of the contributions to the relevant grid cells:

```
xi=indXlo(i):indXhi(i);  
yi=indYlo(i):indYhi(i);  
zi=indZlo(i):indZhi(i);
```

These are the indices of the vertices of the grid-cells in the patch:

```
xvi=indXlo(i):indXhi(i)+1;  
yvi=indYlo(i):indYhi(i)+1;  
zvi=indZlo(i):indZhi(i)+1;
```

The actual positions of the vertices for the grid-cells in the patch are:

```
vertX(xvi,yvi,zvi), vertY(xvi,yvi,zvi), vertZ(xvi,yvi,zvi)
```

These should be in the same units as the physical positions of the centers of the sim-cells!

We now find the distance of all these vertices from the center of the sim-cell (coords = sim-cell center):

```
vertRad=sqrt((vertX(xvi,yvi,zvi)-coords(1,i)).^2 +...  
             (vertY(xvi,yvi,zvi)-coords(2,i)).^2 + ...  
             (vertZ(xvi,yvi,zvi)-coords(3,i)).^2);
```

Only vertices which are within the sim-cell radius should be counted so each vertex is given a value of 1 or zero accordingly:

```
vertMask=vertRad<=cellSize(i)/2;
```

We create an array for the grid-cells in the patch that counts, for each grid-call, how many of its vertices are found within the sim-cell radius:

```
vw=zeros(length(xi),length(yi),length(zi));

for ii=0:1
    for jj=0:1
        for kk=0:1
            vw=vw+vertMask(1+ii:end-1+ii,...
                           1+jj:end-1+jj,...
                           1+kk:end-1+kk);
        end
    end
end
vw=vw./8; % we divide by the maximal number of vertices per grid-cell.
```

If a sim-cell is totally enclosed by a single grid-cell it may be ignored by this method so we always set the 'weight' of the grid-cell which contains the center of the sim-cell to be 1:

```
mid=floor(size(vw)./2)+1;
vw(mid(1),mid(2),mid(3))=1;
```

We define a total 'vertex-volume'

```
volTot=sum(sum(sum(vw)));
```

- For the extensive case, e.g. adding up mass, the contribution to the relevant grid-cells is:

```
cube(xi,yi,zi)=cube(xi,yi,zi)+vals(i).*vw./volTot;
```

Once the cell-loop is done then that's it!

- For the intensive case, e.g. Temperature, where we may have some sort of weighted-mean:

```
wtRho=wt(i).*vw/volTot;

cube(xi,yi,zi)=cube(xi,yi,zi)+vals(i).*wtRho;

wts(xi,yi,zi)=wts(xi,yi,zi)+wtRho;
```

And after the cell-looping is completed, normalize by the weights:

```
cube=cube./wts;
cube(wts==0)=0;
```