Identifying and characterising coral reef "oases"

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Supporting information

6 Appendix 1.

- 7 We used numerical simulations to evaluate a wide range of empirical possibilities of coral reef
- 8 trajectories. The simulations were intended to capture the behaviour of long-term coral cover
- 9 dynamics based on four predetermined model scenarios considered as representative of trajectories
- observed from long-term monitoring of reefs: (1) linear trends (i.e., where coral cover declines
- or increases linearly; (2) nonlinear oscillations, (3) phase shifts (i.e., where coral cover declines
- suddenly and remains low); and (4) long-term stability (i.e., where coral cover can vary from year
- to year, but does not increase or decrease significantly over time). For each scenario, we generated
- ¹⁴ 30 random values for coral cover for a thirty-year time-series. The model parameters were chosen
- to return values of coral cover between 0 and 65%, a range that is representative of contemporary
- average values from the Caribbean and Indo-West Pacific.

17 Stable

For sites exhibiting stable coral cover (y_i) in year i, we generated 30 random values about an intercept (b) with variation (w_i) , for a thirty-year time-series as follows:

$$y_i = b + w_i$$
 $b = \mathcal{N}(40,5) \mid \mathcal{U}(5,40)$
 $\sigma_b = \mathcal{N}(0.1b,0.5)$
 $w_i = \mathcal{N}(0,\sigma_b)$

- where σ_b is the standard deviation about b. The intercept b is chosen from either a normal (\mathcal{N}) or uniform distribution (\mathcal{U}) , determined by a fair coin flip.
- The R function to return a stable time series is:

```
##' cc = upper value of coral cover, used in normal or uniform distribution (40)
##' yrs = number of years in the time series (30)
##' rnorm_theta = probability of observing a zero or one (0.5)
##' (for the coin flip)

stable_simF <- function(cc = coral_cover, yrs = number_yrs, rnorm_theta = 0.5){
    coin_flip <- sample(c(0, 1), size = 1, prob = c(rnorm_theta, 1 - rnorm_theta))</pre>
```

```
# If coin_flip is 0, sample from normal distribution:
  if(coin_flip == 0){
    cc = rnorm(1, mean = cc, sd = 5)
  # Otherwise, sample from a uniform distribution:
  if(coin_flip == 1){
    cc = runif(1, max = cc, min = 5)
  # Choose the starting coral cover sd from a normal distribution
  cc_sd = 0.1 * cc # make standard deviation 10% of starting coral cover
  cc_sd = rnorm(1, mean = cc_sd, sd = 0.5)
  # Change cc_sd if below some arbitrary threshold
  cc_sd = ifelse(cc_sd < 0.1, 0.1, cc_sd)
  # Get time series
 y = rnorm(number_yrs, mean = cc, sd = cc_sd)
  # Assemble data frame
  sim_df <- data.frame(year = 1:number_yrs,</pre>
                       w = cc - y, slope = 0, intercept = cc,
                       y = y
  return(sim_df)
}
```

26 Phase shift

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For sites exhibiting a phase shift, a new intercept (b_{new}) and variation ($w_{i_{new}}$) was selected at a year chosen randomly between year 10 and year 30 (x_{shift}) of a thirty-year time-series as follows:

$$egin{aligned} y_i &= egin{cases} b + w_i & ext{if } x < x_{shift} \ b_{new} + w_{i_{new}} & ext{if } x \geq x_{shift} \end{cases} \ x_{shift} &= \mathcal{U}(10,30) \ b_{new} &= \mathcal{U}(1,0.5b) \ \sigma_{b_{new}} &= \mathcal{N}(\sigma_b,0.1) \ w_{i_{new}} &= \mathcal{N}(0,\sigma_{b_{new}}) \end{aligned}$$

where $\sigma_{b_{new}}$ is the new standard deviation about b_{new} . The effect of the phase shift is to reduce the coral cover to a value chosen uniformly between 1 and half of the original b.

The R function to return a phase shift is:

```
##' cc = upper value of coral cover, used in normal or uniform distribution (40)
##' yrs = number of years in the time series (30)
##' rnorm_theta = probability of observing a zero or one (0.5)
##' (for the coin flip)
##' shift_min = the earliest year in which a phase shift can begin (10)
##' shift_max = the latest year in which a phase shift can begin (30)
phase_shift_simF <- function(cc = coral_cover, yrs = number_yrs, rnorm_theta = 0.5,</pre>
                             shift_min = 10, shift_max = 30){
 coin_flip <- sample(c(0, 1), size = 1, prob = c(rnorm_theta, 1 - rnorm_theta))</pre>
  # If coin_flip is 0, sample from normal distribution:
 if(coin_flip == 0){
    cc = rnorm(1, mean = cc, sd = 5)
  # Otherwise, sample from a uniform distribution:
  if(coin_flip == 1){
   cc = runif(1, max = cc, min = 5)
  # Choose the starting coral cover sd from a normal distribution
  cc_sd = 0.1 * cc # make standard deviation 10% of starting coral cover
  cc_sd = rnorm(1, mean = cc_sd, sd = 0.5)
  # Change cc_sd if below some arbitrary threshold
  cc_sd = ifelse(cc_sd < 0.1, 0.1, cc_sd)
  # Get time series
 y = rnorm(number_yrs, mean = cc, sd = cc_sd)
  # Now choose when the phase shift happens
 begin_shift = floor(runif(1, min = shift_min, max = shift_max))
  # Get the new coral cover mean
  cc_new = runif(1, max = 0.5*cc, min = 1)
  # Get the coral cover sd, similar to old sd
  cc_sd_new = rnorm(1, mean = cc_sd, sd = 0.1)
  # Change cc_sd_new if below some arbitrary threshold
  cc_sd_new = ifelse(cc_sd_new < 0.1, 0.1, cc_sd_new)</pre>
  # Get phase shift time series
 y_new = rnorm(number_yrs, mean = cc_new, sd = cc_sd_new)
  # Assemble data frame
  sim_df <- data.frame(year = 1:number_yrs,</pre>
```

```
w = cc - y, slope = 0, intercept = cc,
y = y) %>%
mutate(y = ifelse(year < begin_shift, y, y_new))
return(sim_df)
}</pre>
```

35 Linear trend

For sites exhibiting a linear trend in coral cover, a slope (m) was also selected randomly with a thirty-year time series determined by the equation for a line, as follows:

```
y_i = mx + b + w_i
b = \mathcal{N}(40,5) \mid \mathcal{U}(5,40)
\sigma_b = \mathcal{N}(0.1b,0.5)
w_i = \mathcal{N}(0,\sigma_b)
m = \mathcal{N}(-0.5,0.25)
```

- where σ_b is the standard deviation about b.
- The R function to return a linear trend is:

```
##' cc = upper value of coral cover, used in normal or uniform distribution (40)
##' yrs = number of years in the time series (30)
##' rnorm_theta = probability of observing a zero or one (0.5)
##' (for the coin flip)
##' trend = slope of the linear trend (-0.5)
##' trend_sd = standard deviation for the trend (0.25)
linear_simF <- function(cc = coral_cover, yrs = number_yrs,</pre>
                        trend = linear_trend, trend_sd = linear_trend_sd,
                        rnorm\_theta = 0.5){
 coin_flip \leftarrow sample(c(0, 1), size = 1, prob = c(rnorm_theta, 1 - rnorm_theta))
  # If coin_flip is 0, sample from normal distribution:
  if(coin_flip == 0){
    cc = rnorm(1, mean = cc, sd = 5)
  # Otherwise, sample from a uniform distribution:
  if(coin_flip == 1){
    cc = runif(1, max = cc, min = 5)
  # Choose the starting coral cover sd from a normal distribution
  cc_sd = 0.1 * cc # make standard deviation 10% of starting coral cover
```

```
cc_sd = rnorm(1, mean = cc_sd, sd = 0.5)
  # Change cc_sd if below some arbitrary threshold
  cc_sd = ifelse(cc_sd < 0.1, 0.1, cc_sd)
  # Random variation for each time point
  w <- rnorm(number_yrs, mean = 0, sd = cc_sd)</pre>
  # Random value for slope
  slope <- rnorm(1, mean = trend, sd = trend_sd)</pre>
  # Random value for intercept (i.e., the starting coral cover)
  intercept <- rnorm(1, cc, sd = cc_sd)</pre>
 ## Get time series
 y <- slope * x + intercept + w
  # Assemble data frame
  sim_df <- data.frame(year = 1:number_yrs,</pre>
                        w = w, slope = slope, intercept = intercept,
                        y = y
  return(sim_df)
}
```

44 Oscillations

Finally, we used a cosine curve to simulate oscillations over time:

```
y_i = acos(rac{2\pi x}{p} + \pi c) + b + w_i
a = \mathcal{N}(15, 7.5)
p = \mathcal{N}(40, 5)
c = \mathcal{N}(0, 0.25)
b = \mathcal{N}(30, 5) \mid \mathcal{U}(5, 30)
```

with an amplitude (a), period (p) and horizontal shift (πc). In this equation, b represents the vertical shift of the cosine curve. Note that the b_{mu} is 30 instead of 40 as previously, to prevent unusually high coral covers due to the oscillations.

The R function to return oscillations is:

```
##' cc = upper value of coral cover, used in normal or uniform distribution (30)
##' yrs = number of years in the time series (30)
##' rnorm_theta = probability of observing a zero or one (0.5)
##' (for the coin flip)
```

```
##' trend = slope of the linear trend (0)
##' trend_sd = standard deviation for the trend (0)
##' amp = amplitude
##' period (years) [for a 30 yr time series, a period of 30 results in a U] (40)
non_linear_simF <- function(cc = coral_cover, yrs = number_yrs,</pre>
                        trend = linear_trend, trend_sd = linear_trend_sd,
                        rnorm_theta = 0.5, amplitude = amp){
 coin_flip <- sample(c(0, 1), size = 1, prob = c(rnorm_theta, 1 - rnorm_theta))</pre>
  # If coin_flip is 0, sample from normal distribution:
  if(coin_flip == 0){
   cc = rnorm(1, mean = cc, sd = 5)
  # Otherwise, sample from a uniform distribution:
  if(coin_flip == 1){
   cc = runif(1, max = cc, min = 5)
  # Choose the starting coral cover sd from a normal distribution
  cc_sd = 0.1 * cc # make standard deviation 10% of starting coral cover
  cc_sd = rnorm(1, mean = cc_sd, sd = 0.5)
  # Change cc_sd if below some arbitrary threshold
  cc_sd = ifelse(cc_sd < 0.1, 0.1, cc_sd)
  # Random variation for each time point
  w <- rnorm(number_yrs, mean = 0, sd = cc_sd)</pre>
  # Random value for slope
  slope <- rnorm(1, mean = trend, sd = trend_sd)</pre>
  # Random value for intercept (i.e., the starting coral cover)
  intercept <- rnorm(1, cc, sd = cc_sd)</pre>
  # Phase shift
 phase_shift = runif(1, 0, 0.25) * pi
  # Amplitude
  amp = rnorm(1, mean = amp, sd = amp*0.5)
  # Period
 period = rnorm(1, mean = period_yrs, sd = period_yrs_sd)
  # Vector representing the nonlinear trend
  cs = amp * cos(2*pi*1:number_yrs/period + phase_shift)
```

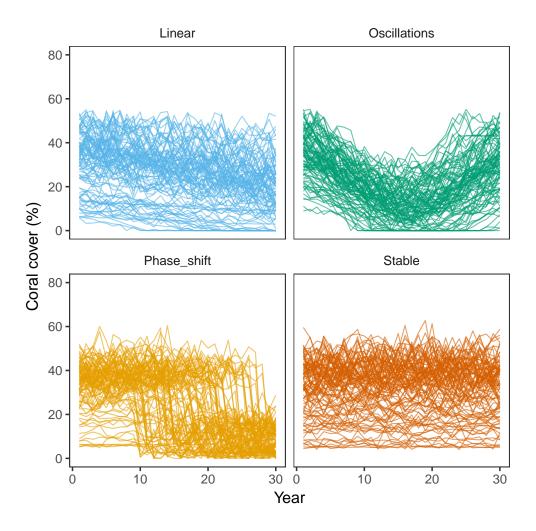


Figure 1: Time series of coral cover from numerical simulations representing four different reef trajectories (n = 100 per trajectory).