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**1: Hybrid Gibbs Sampler to estimate Poisson Distribution  $\lambda$  (30%)**

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For these Poisson distributed random variables (r.v.s) ( $n = 500$ ) with mean parameter  $\lambda$ , unobserved variables are  $\lambda, y_1, y_2, \dots, y_{78}$ , in which  $y_i$ 's denote the r.v.s which are more than or equal to five.

$$\begin{aligned} \text{Prior} : \pi(\lambda) &\propto \frac{1}{\lambda}; \\ P(X, Y|\lambda) &= \prod_{i=1}^{422} \frac{e^{-\lambda} \lambda^{x_i}}{x_i!} \prod_{j=1}^{78} \frac{e^{-\lambda} \lambda^{y_j}}{y_j!} I(y_j \geq 4); \end{aligned}$$

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**2: Bayesian Inference (30%)**

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**3: Hybrid Gibbs Sampler (40%)**

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