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# TERM PROJECT

## MECH-530

### Progress Report 2

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**OVERVIEW:** This progress report features the output of a Python script in IPython Notebook. The input interface has been modified to output the off-axis Q and S matrices as well as stress/strain quantities. The output is organized in two parts corresponding to the layups given in the Assignment 2 instructions.

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In [1]: run MECH530_main.py
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-----QUESTION 1-----
The laminate is given by the following plybook where the highest ply number '8'
indicates the top layer, while the first ply number '1' indicates the bottom l
ayer.
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Unique Ply #,	Fiber/Matrix,	Orientation, (degrees)	Thickness (mm)
8	Kev49/Epoxy	45	0.125
7	Kev49/Epoxy	0	0.125
6	Kev49/Epoxy	-45	0.125
5	Kev49/Epoxy	90	0.125
4	Kev49/Epoxy	90	0.125
3	Kev49/Epoxy	-45	0.125
2	Kev49/Epoxy	0	0.125
1	Kev49/Epoxy	45	0.125

#### PLIES AND THICKNESSES

- Total number of plies in the laminate: 8
- Total thickness of laminate is: 1.000 mm
- There is no core in the laminate ( $Z_c = 0$  mm)
- Laminate contains 1 Fiber/Matrix combination. The material properties for this combination shall be listed below.

RESIN/MATRIX 1 of 1: For Kev49/Epoxy, the given material properties are:

-Stiffness and Strength:

$E_x = 76.0000$  GPa,  $E_y = 5.5000$  GPa,  $E_s = 2.3000$  GPa and  $\nu_{x,y} = 0.3400$

$X_t = 1400.0000$  MPa,  $X_c = 235.0000$  MPa,  $Y_t = 12.0000$  MPa,  $Y_c = 53.0000$  MPa and  $S_c = 34.0000$  MPa.

-The 'on-axis' matrices are given by the following:

$S_{on} =$   
 $\begin{bmatrix} 0.0132 & -0.0045 & 0.0000 \\ -0.0045 & 0.1818 & 0.0000 \\ 0.0000 & 0.0000 & 0.4348 \end{bmatrix} [1/GPa]$

$Q_{on} =$   
 $\begin{bmatrix} 76.6412 & 1.8858 & 0.0000 \\ 1.8858 & 5.5464 & 0.0000 \\ 0.0000 & 0.0000 & 2.3000 \end{bmatrix} [GPa]$

Now the off-axis [S] and [Q] matrices will be printed for each of the first 4 layers in the layup (from the top) along with their respective [U] values.

PLY: 8

ORIENTATION: 45 degrees

$U_{s,1} = 0.1263 [1/GPa]$

$U_{s,2} = -0.0843 [1/GPa]$

Us\_3 = -0.0289 [1/GPa]  
Us\_4 = -0.0333 [1/GPa]  
Us\_5 = 0.3194 [1/GPa]

S\_off =  
[[ 0.1552 -0.0622 -0.0843]  
[ -0.0622 0.1552 -0.0843]  
[ -0.0843 -0.0843 0.2039]] [1/GPa]

Uq\_1 = 32.4418 GPa  
Uq\_2 = 35.5474 GPa  
Uq\_3 = 8.6520 GPa  
Uq\_4 = 10.5378 GPa  
Uq\_5 = 10.9520 GPa

Q\_off =  
[[ 23.7898 19.1898 17.7737]  
[ 19.1898 23.7898 17.7737]  
[ 17.7737 17.7737 19.6040]] [GPa]

PLY: 7

ORIENTATION: 0 degrees

Us\_1 = 0.1263 [1/GPa]  
Us\_2 = -0.0843 [1/GPa]  
Us\_3 = -0.0289 [1/GPa]  
Us\_4 = -0.0333 [1/GPa]  
Us\_5 = 0.3194 [1/GPa]

S\_off =  
[[ 0.0132 -0.0045 -0.0000]  
[ -0.0045 0.1818 0.0000]  
[ -0.0000 0.0000 0.4348]] [1/GPa]

Uq\_1 = 32.4418 GPa  
Uq\_2 = 35.5474 GPa  
Uq\_3 = 8.6520 GPa  
Uq\_4 = 10.5378 GPa  
Uq\_5 = 10.9520 GPa

Q\_off =  
[[ 76.6412 1.8858 0.0000]  
[ 1.8858 5.5464 0.0000]  
[ 0.0000 0.0000 2.3000]] [GPa]

PLY: 6

ORIENTATION: -45 degrees

Us\_1 = 0.1263 [1/GPa]  
Us\_2 = -0.0843 [1/GPa]  
Us\_3 = -0.0289 [1/GPa]  
Us\_4 = -0.0333 [1/GPa]  
Us\_5 = 0.3194 [1/GPa]

S\_off =  
[[ 0.1552 -0.0622 0.0843]  
[ -0.0622 0.1552 0.0843]  
[ 0.0843 0.0843 0.2039]] [1/GPa]

```

Uq_1 = 32.4418 GPa
Uq_2 = 35.5474 GPa
Uq_3 = 8.6520 GPa
Uq_4 = 10.5378 GPa
Uq_5 = 10.9520 GPa

Q_off =
[[ 23.7898 19.1898 -17.7737]
 [ 19.1898 23.7898 -17.7737]
 [-17.7737 -17.7737 19.6040]] [GPa]

```

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PLY: 5
ORIENTATION: 90 degrees
Us_1 = 0.1263 [1/GPa]
Us_2 = -0.0843 [1/GPa]
Us_3 = -0.0289 [1/GPa]
Us_4 = -0.0333 [1/GPa]
Us_5 = 0.3194 [1/GPa]

```

```

S_off =
[[ 0.1818 -0.0045 0.0000]
 [-0.0045 0.0132 -0.0000]
 [ 0.0000 -0.0000 0.4348]] [1/GPa]

```

```

Uq_1 = 32.4418 GPa
Uq_2 = 35.5474 GPa
Uq_3 = 8.6520 GPa
Uq_4 = 10.5378 GPa
Uq_5 = 10.9520 GPa

```

```

Q_off =
[[ 5.5464 1.8858 0.0000]
 [ 1.8858 76.6412 0.0000]
 [ 0.0000 0.0000 2.3000]] [GPa]

```

In [1]: run MECH530\_main.py

-----QUESTION 2-----  
The laminate is given by the following plybook where the highest ply number '1' indicates the top layer, while the first ply number '1' indicates the bottom layer.

Unique Ply #,	Fiber/Matrix,	Orientation,	Thickness
		(degrees)	(mm)
1	Kev49/Epoxy	30	0.125

#### PLIES AND THICKNESSES

- Total number of plies in the laminate: 1
- Total thickness of laminate is: 0.125 mm
- There is no core in the laminate ( $Z_c = 0$  mm)
- Laminate contains 1 Fiber/Matrix combination. The material properties for this combination shall be listed below.

RESIN/MATRIX 1 of 1: For Kev49/Epoxy, the given material properties are:

-Stiffness and Strength:

Ex = 76.0000 GPa, Ey = 5.5000 GPa, Es = 2.3000 GPa and nu\_x = 0.3400

Xt = 1400.0000 MPa, Xc = 235.0000 MPa, Yt = 12.0000f MPa, Yc = 53.0000 MPa and Sc = 34.0000 MPa.

-The 'on-axis' matrices are given by the following:

S\_on =  
[[ 0.0132 -0.0045 0.0000]  
[ -0.0045 0.1818 0.0000]  
[ 0.0000 0.0000 0.4348]] [1/GPa]

Q\_on =  
[[ 76.6412 1.8858 0.0000]  
[ 1.8858 5.5464 0.0000]  
[ 0.0000 0.0000 2.3000]] [GPa]

PLY: 1

ORIENTATION: 30 degrees

Us\_1 = 0.1263 [1/GPa]

Us\_2 = -0.0843 [1/GPa]

Us\_3 = -0.0289 [1/GPa]

Us\_4 = -0.0333 [1/GPa]

Us\_5 = 0.3194 [1/GPa]

S\_off =  
[[ 0.0986 -0.0478 -0.1230]  
[ -0.0478 0.1829 -0.0230]  
[ -0.1230 -0.0230 0.2616]] [1/GPa]

Uq\_1 = 32.4418 GPa

Uq\_2 = 35.5474 GPa

Uq\_3 = 8.6520 GPa

Uq\_4 = 10.5378 GPa

Uq\_5 = 10.9520 GPa

Q\_off =  
[[ 45.8895 14.8638 22.8853]  
[ 14.8638 10.3421 7.8996]  
[ 22.8853 7.8996 15.2780]] [GPa]

COMPUTE OFF-AXIS STRAIN, ON-AXIS STRESS AND STRAIN FROM OFF-AXIS STRESS GIVEN:

Transpose of Off-axis stress =  
[[ 0.4200 -0.1650 -0.1350]] [GPa]

Transpose of Off-axis strain =  
[[ 0.0659 -0.0471 -0.0832]] [unitless]

Transpose of On-axis stress =  
[[ 0.1568 0.0982 -0.3208]] [GPa]

Transpose of On-axis strain =

[[ 0.0016 0.0171 -0.1395]] [unitless]