
Input: Graph $G = \langle V, E \rangle$

Output: Edge set T forming a min. span tree

▷ Here, the *MakeSet*, *FindSet*, *Union* make use of a disjoint-set structure.

procedure KRUSKAL(G)

$T \leftarrow \emptyset$

▷ set of edges

$S \leftarrow \emptyset$

▷ set of disjoint sets

for $v \in V$ **do**

$S \leftarrow S \cup \text{MakeSet}(v)$

for $(u, v) \in G.E$ (ordered by weight) **do**

$set_u \leftarrow \text{FindSet}(u)$

$set_v \leftarrow \text{FindSet}(v)$

if $set_u \neq set_v$ **then**

$T \leftarrow T \cup \{(u, v)\}$

$\text{Union}(set_u, set_v)$

return T

Input: Graph $G = \langle V, E \rangle$
Output: E of G containing only the edges belonging to a min. span tree
▷ Connectivity can be checked via graph traversal algorithms, namely BFS or DFS.

```
procedure REVERSE_DELETE( $G$ )  
  Sort  $G.E$  in descending order  
   $i \leftarrow 0$   
  while  $i < |E|$  do  
     $e \leftarrow E[i]$   
    Delete  $e$                                 ▷  $i$  is now at the next edge  
    if  $G$  not connected then  
       $E[i] \leftarrow e$                                 ▷ Re-add edge  
       $i \leftarrow i + 1$                                 ▷ Move on to next edge  
  return  $G.E$ 
```

Input: Graph $G = \langle V, E \rangle$
Output: Total cost c of minimum spanning tree of G

procedure PRIM_JARNIK(G)
 $dist \leftarrow$ initialize to array of size $|G.V|$
 $Q \leftarrow$ empty priority queue with vertex as value and weight as key
 $T \leftarrow \emptyset$

$s \leftarrow$ some node $\in G.V$ \triangleright Here, the choice of the node does not matter
 $dist[s] \leftarrow 0$
 $c \leftarrow 0$

for $v \in G.V$ **do**
 $dist[v] \leftarrow \infty$
 if $v \neq s$ **then**
 $Q.add(v, \infty)$

$Q.push(s, 0)$

while $Q \neq \emptyset$ **do**
 $u \leftarrow Q.remove_min()$
 $c \leftarrow c + dist[u]$

if $dist[u] = \infty$ **then**
 return ∞ \triangleright Spanning tree does not exist

for $e = (u, v) \in u.edges$ **do**
 if $e.weight < dist[v]$ **then**
 $dist[v] \leftarrow w$
 $Q.update_priority(v, w)$

return c
