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For our disjoint set structure, every element has an associated *parent*, *rank* and *size*. The functions below are part of the disjoint set structure itself.

```
procedure MAKE_SET( $x$ )  
  if  $x$  not present in structure then  
    add  $x$  to structure  
     $x.parent \leftarrow x$   
     $x.size \leftarrow 1$   
     $x.rank \leftarrow 0$ 
```

**Path compression find**

```
procedure FIND( $x$ )  
  if  $x \neq x.parent$  then  
     $x.parent \leftarrow Find(x.parent)$   
  return  $x.parent$ 
```

**Union by Rank**

```
procedure UNION( $x, y$ )  
   $xRoot \leftarrow Find(x)$   
   $yRoot \leftarrow Find(y)$   
  
  if  $xRoot \neq yRoot$  then ▷ Only union if sets are different  
    if  $xRoot.rank < yRoot.rank$  then  
       $xRoot, yRoot \leftarrow yRoot, xRoot$  ▷ Swap roots so that  $x$  is largest  
  
     $yRoot.parent = xRoot$   
    if  $xRoot.rank = yRoot.rank$  then  
       $xRoot.rank \leftarrow xRoot.rank + 1$ 
```

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