

# Supplementary Materials for Smoothed Local Histogram Filters

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## 1 Parameters

For all the examples in the paper, the spatial weighting function  $W$  is a two-dimensional isotropic Gaussian with standard deviation  $\sigma_W$ , and the histogram smoothing kernel  $K$  is a one-dimensional Gaussian with standard deviation  $\sigma_K$ . The following parameters were used in creating the figures.

Figure	Parameters
1(b)	$m = 15$
1(c)	$m = 15$
1(d)	$\sigma_K = .021, \sigma_W = 7.1$
4(b)	$\sigma_K = .042, \sigma_W = 7.1$
4(c)	$\sigma_K = .042, \sigma_W = 7.1$
6(b)	$\sigma_K = .014, \sigma_W = 2.8, 5\%/95\% \text{ close/open}$
8(a)	$\sigma_K = .042, \sigma_W = 10.6$
9(b)	$\sigma_K = .042, \sigma_W = 10.6$
10(b)	$\sigma_K = .18, \sigma_W = 21.2$
11(b), 12	$\sigma_K = (.07, .007, .0035), \sigma_W = 7.1$

## 2 Algorithms

What follows is pseudocode for all the algorithms in the paper. The pseudocode is presented in a simple form for exposition. For maximum memory efficiency, the loops of all the algorithms can be rearranged so that the outermost loop is over the index  $i$  and the inner loop is over the pixel indices  $p$ . This will make the memory footprint independent of  $m$ .

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**Algorithm 1** Percentile filter:  $t = .5$  gives a median filter, smaller  $t$  values perform a dilation, and larger  $t$  values perform erosion.

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Compute  $R_i(\mathbf{p})$  for all  $\mathbf{p}, i$ .
for  $i = 1$  to  $m - 1$  do
   $target \leftarrow R_1(\mathbf{p}) + t(R_m(\mathbf{p}) - R_1(\mathbf{p}))$ 
  for  $i = 1$  to  $b - 1$  do
    if  $R_i(\mathbf{p}) \leq target$  and  $R_{i+1}(\mathbf{p}) \geq target$  then
       $out(\mathbf{p}) \leftarrow s_i + (s_{i+1} - s_i)(target - R_i(\mathbf{p})) / (R_{i+1}(\mathbf{p}) - R_i(\mathbf{p}))$ 
    end if
  end for
end for

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**Algorithm 2** Dominant mode filter.

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Compute  $R_i(\mathbf{p}), D_i(\mathbf{p})$  for all  $\mathbf{p}, i$ .
for all  $\mathbf{p} \in I$  do
   $curPeak \leftarrow 0$ 
   $bestPeak \leftarrow 0$ 
   $bestIntegral \leftarrow 0$ 
   $leftIntegral \leftarrow R_1(\mathbf{p})$ 
  for  $i = 1$  to  $m - 1$  do
    if  $D_i(\mathbf{p}) \leq 0$  and  $D_{i+1}(\mathbf{p}) > 0$  then
      // Valley
       $bucketDistance \leftarrow D_i(\mathbf{p}) / (D_i(\mathbf{p}) - D_{i+1}(\mathbf{p}))$ 
       $rightIntegral \leftarrow R_i(\mathbf{p}) + (R_{i+1}(\mathbf{p}) - R_i(\mathbf{p})) \cdot bucketDistance$ 
       $integral \leftarrow rightIntegral - leftIntegral$ 
      if  $integral \geq bestIntegral$  then
         $bestIntegral \leftarrow integral$ 
         $bestPeak \leftarrow curPeak$ 
      end if
       $leftIntegral \leftarrow rightIntegral$ 
    else if  $D_i(\mathbf{p}) \geq 0$  and  $D_{i+1}(\mathbf{p}) < 0$  then
      // Peak
       $bucketDistance \leftarrow D_i(\mathbf{p}) / (D_i(\mathbf{p}) - D_{i+1}(\mathbf{p}))$ 
       $curPeak \leftarrow s_i + (s_{i+1} - s_i) \cdot bucketDistance$ 
    end if
  end for
   $lastIntegral \leftarrow R_m(\mathbf{p}) - leftIntegral$ 
  if  $lastIntegral \geq bestIntegral$  then
    if  $curPeak = 0$  then
      // Histogram monotonically increases
       $bestPeak \leftarrow s_m$ 
    else
      // Only one peak
       $bestPeak \leftarrow curPeak$ 
    end if
  end if
   $out(\mathbf{p}) \leftarrow bestPeak$ 
end for

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**Algorithm 3** Local mode filter

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Compute  $D_i(\mathbf{p})$  for all  $\mathbf{p}, i$ .
for all  $\mathbf{p} \in I$  do
   $out(\mathbf{p}) \leftarrow 0$ 
   $dist \leftarrow \infty$ 
  for  $i = 1$  to  $m - 1$  do
    if  $D_i(\mathbf{p}) \geq 0$  and  $D_{i+1}(\mathbf{p}) < 0$  then
      // Peak
       $bucketDistance \leftarrow D_i(\mathbf{p}) / (D_i(\mathbf{p}) - D_{i+1}(\mathbf{p}))$ 
       $curPeak \leftarrow s_i + (s_{i+1} - s_i) \cdot bucketDistance$ 
       $curDist \leftarrow |I(\mathbf{p}) - curPeak|$ 
      if  $curDist < dist$  then
         $dist \leftarrow curDist$ 
         $out(\mathbf{p}) \leftarrow curPeak$ 
      end if
    end if
  end for
  if  $D_1(\mathbf{p}) < 0$  and  $I(\mathbf{p}) < dist$  then
    // Closer peak at leftmost bucket
     $dist \leftarrow I(\mathbf{p})$ 
     $out(\mathbf{p}) \leftarrow s_1$ 
  end if
  if  $D_1(\mathbf{p}) > 0$  and  $|I(\mathbf{p}) - s_m| < dist$  then
    // Closer peak at rightmost bucket
     $out(\mathbf{p}) \leftarrow s_m$ 
  end if
end for
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**Algorithm 4** Diffusion.

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// We use  $\alpha = \sqrt{2}$  and  $\eta = .2$ 
 $\sigma \leftarrow \sigma_{min}$ 
 $D_0 \leftarrow S$  //  $S$  is the original base layer
 $i \leftarrow 1$ 
while  $\sigma \leq \sigma_{max}$  do
   $B_i \leftarrow D_{i-1} * G(\sigma)$ 
   $E_u \leftarrow (D_{i-1} - I)^2 * G(\eta\sigma)$ 
   $E_b \leftarrow (B_i - I)^2 * G(\eta\sigma)$ 
   $R \leftarrow E_u / E_b$ 
  for all  $\mathbf{p} \in I$  do
    if  $R(\mathbf{p}) < .5$  then
       $D_i(\mathbf{p}) \leftarrow B_i(\mathbf{p})$ 
    else if  $R(\mathbf{p}) \in [.1, 1)$  then
       $D_i(\mathbf{p}) \leftarrow 2(R(\mathbf{p}) - \frac{1}{2})(D_{i-1}(\mathbf{p}) - B_i(\mathbf{p})) + B_i(\mathbf{p})$ 
    else
       $D_i(\mathbf{p}) \leftarrow D_{i-1}(\mathbf{p})$ 
    end if
  end for
   $i \leftarrow i + 1$ 
   $\sigma \leftarrow \alpha\sigma$ 
end while
 $D \leftarrow D_{i-1}$ 
Output  $D$  // Selectively diffused base layer
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