

QUESTION 6

**Theorem** the only prime triple is 3, 5, 7.

*Proof:* by reductio ad absurdum.

Any prime triple is of the form  $n, n + 2, n + 4$ .

We know that 2, 4, 6 is not a prime triple.

So assume there is a prime triple  $n, n + 2, n + 4$  where  $n > 3$ .

But we know from the result in question 5 that one of  $n, n + 2, n + 4$  must be divisible by 3 and hence not prime. Therefore there can be no such prime triple.  $\square$