CSE221

Lecture 15:
Splay Trees

Acknowledgment: The content of this file is based on the slides of the textbook as well as the slides provided in former lectures at UNIST.

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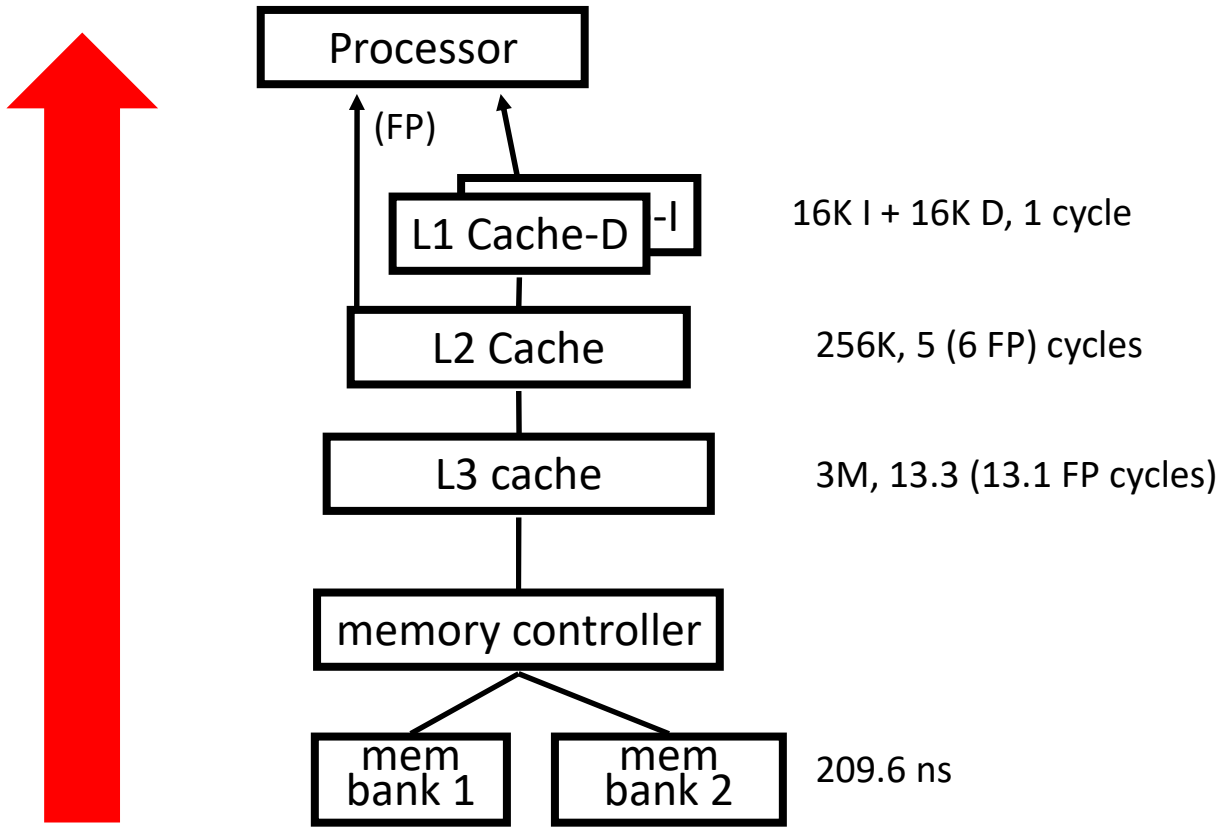
Memory Hierarchy

Smaller unit & capacity
Faster access



Temporal locality: The same data is accessed soon
Spatial locality: Neighboring data is accessed soon

Splay Trees

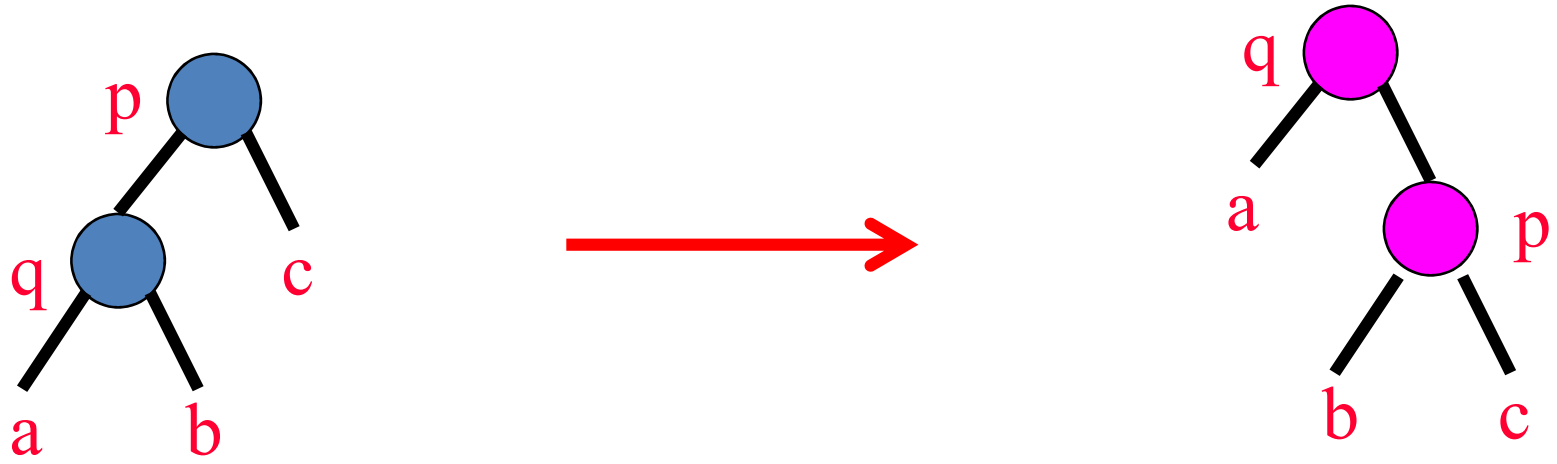
- Two heuristics to make search tree efficient
  - Make search depth shorter
  - Make frequently accessed data closer to root
- Splay trees use the latter idea
  - Rearrange tree whenever an element is accessed so that the recently used data is in the root node
- Worst-case O(n) for operation, but O(log n) amortized

Splaying

- Designate splay node *q*
  - E.g., accessed node, inserted node …
- Move *q* to the root using a series of splay steps
- In a splay step, *q* moves up the tree by 0, 1, or 2 levels
- Apply to all normal operations on a binary search tree

Splay Step

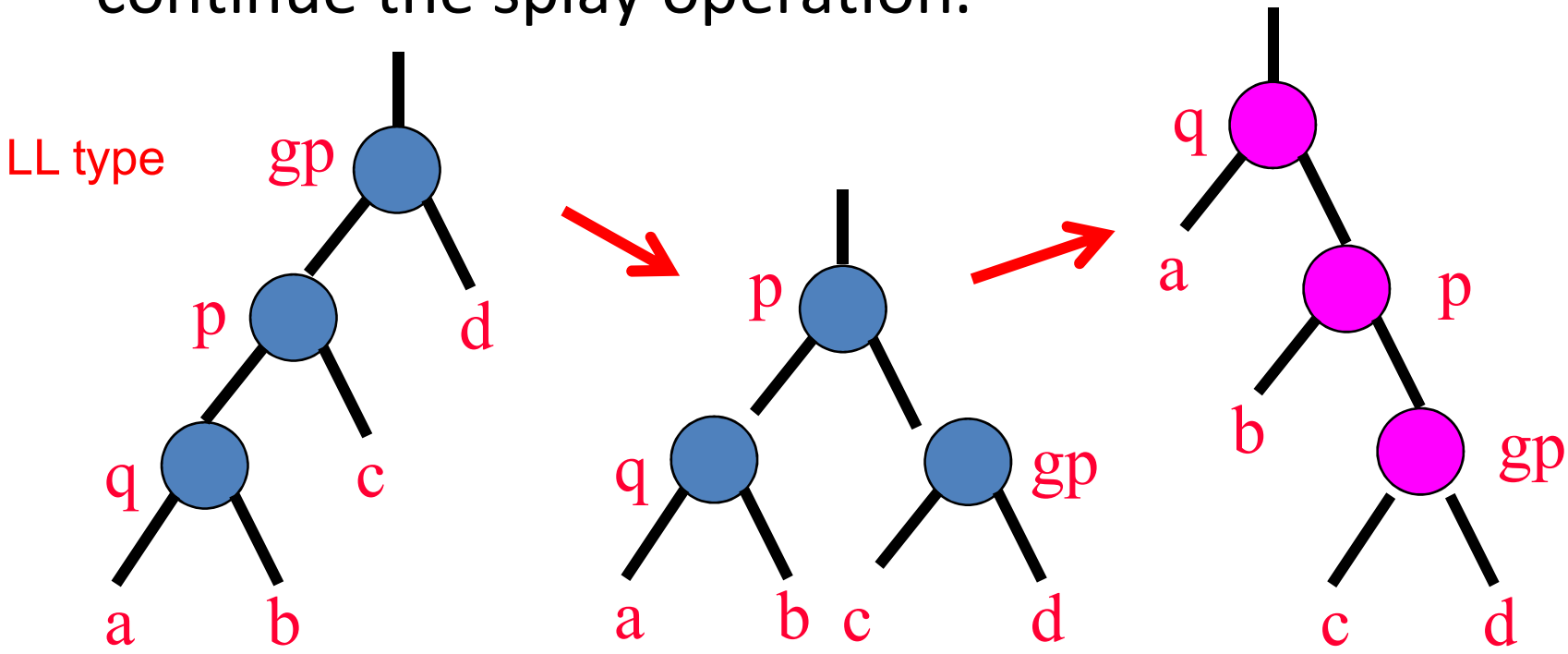
- If *q* = *null* or *q* is the root, stop (splay is over)
- If *q* is at level 1, do a one-level move and terminate the splay operation



- Symmetric: right child of *p*

Splay Step

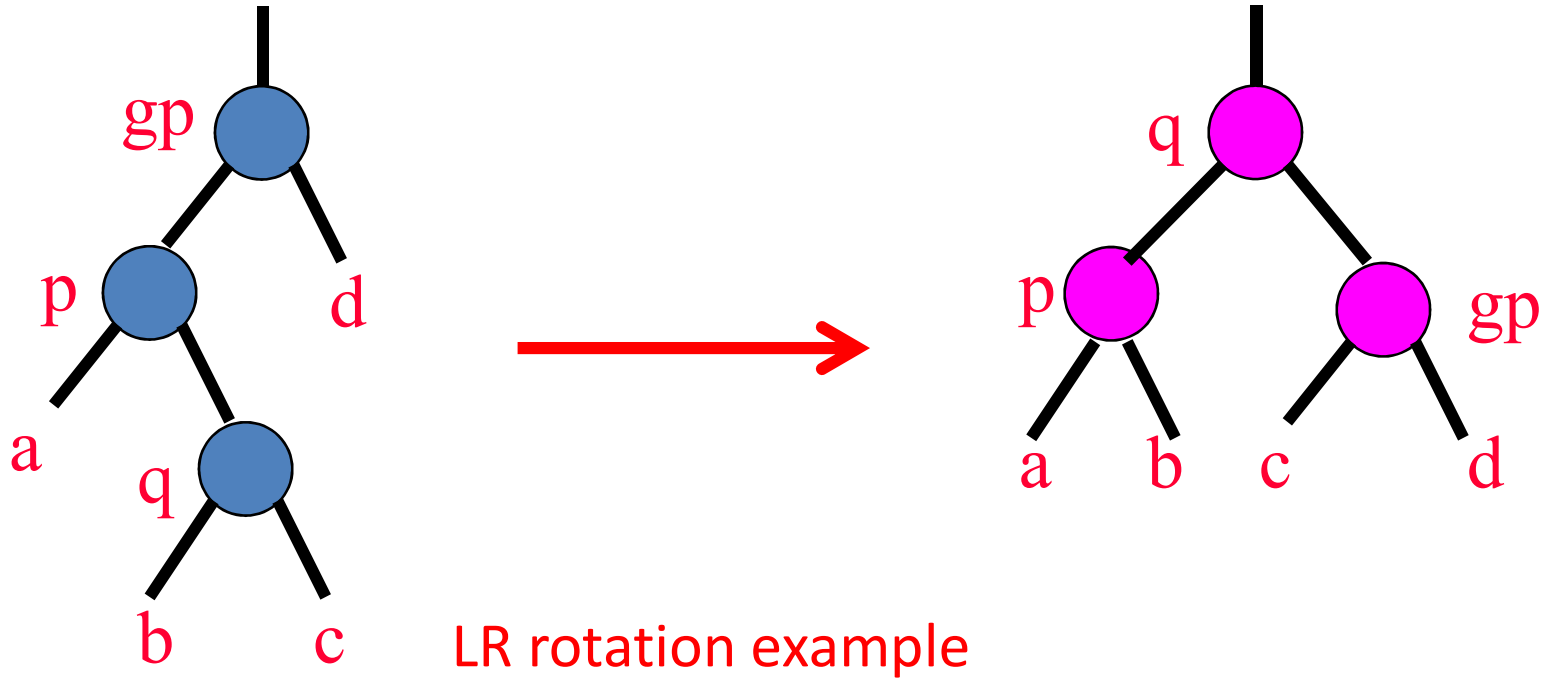
- If *q* is at a level >= 2, do a two-level move and continue the splay operation.



- Symmetric: right child of right child of *gp (RR type)*

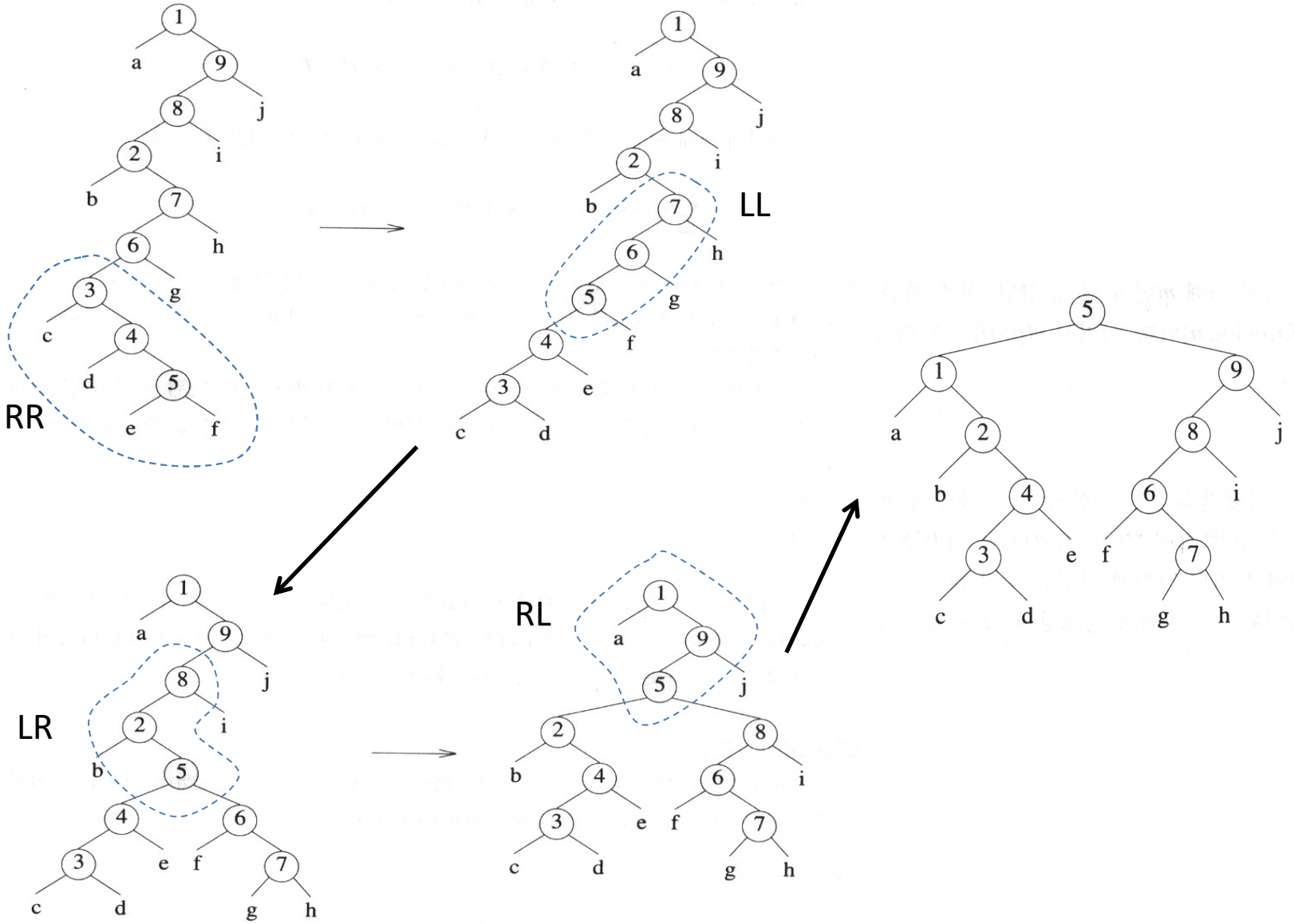
2-Level Move

- LR, RL rotations
  - –Similar to AVL/Red-Black



LR rotation example

Splay node : 5

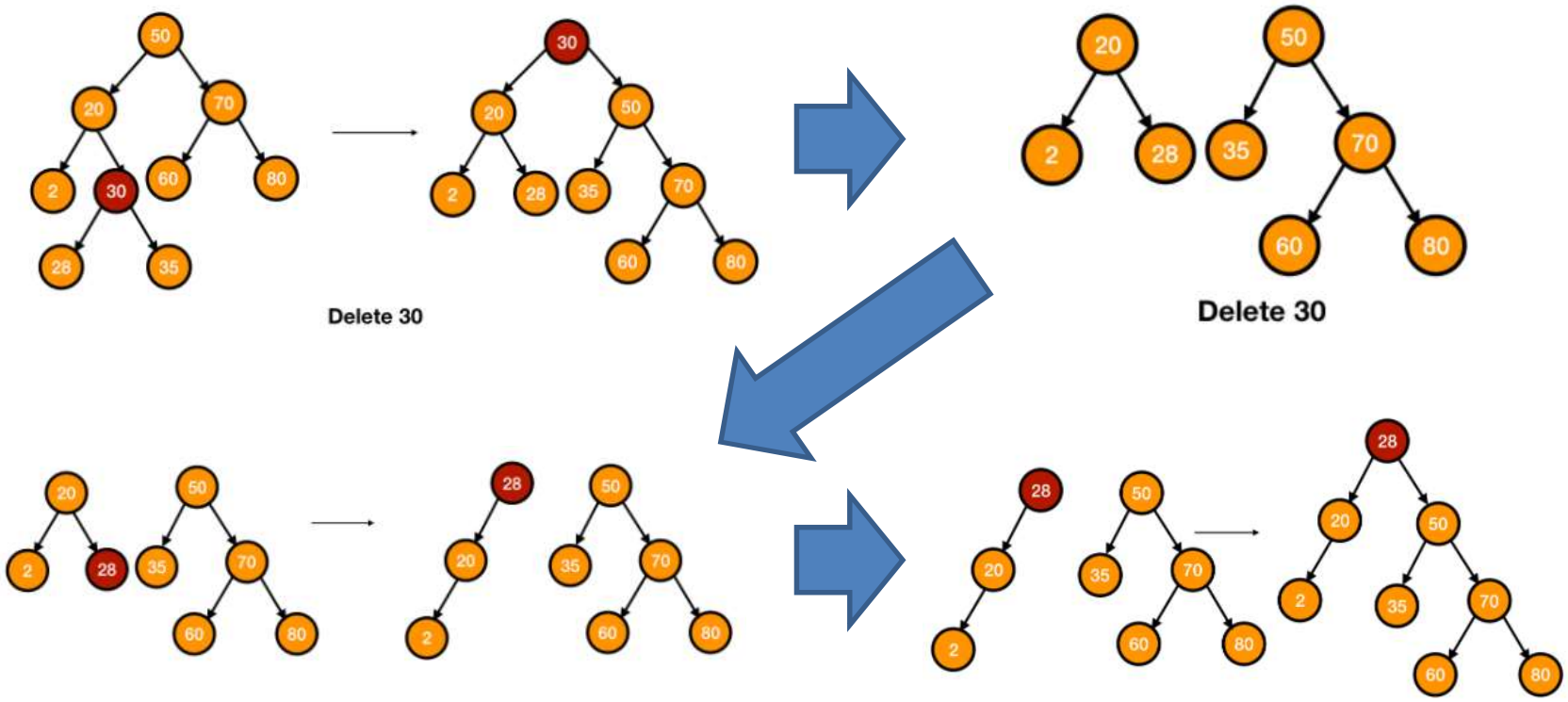


Designating Splay Node

- Search (k)
  - If there is key *k*, the node containing *k* is the splay node
- Insert (k)
  - The newly inserted node is the splay node
- Delete (k)
  - If k is present, splay it. Or, splay the last accessed node
  - Delete k if it is present: Two subtrees are generated
    - Splay the largest key r of the left subtree
    - Then, attach the right subtree as the right child of r

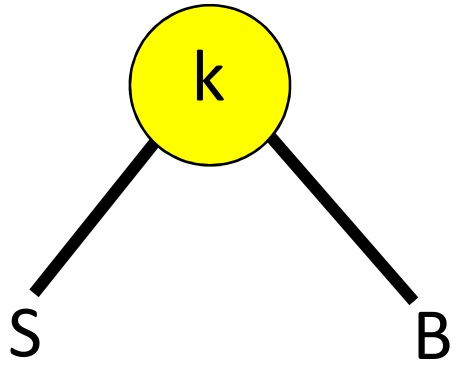
Designating Splay Node

- Delete (k)



Designating Splay Node

- Split (k)
  - Suppose that the key *k* is actually present in the tree
  - Perform a splay at the node that contains k
  - Then split the tree



Discussion

- Pros
  - Simple to implement when compared with AVL/Red-Black
  - Low memory footprint: no bookkeeping data
  - Optimized for temporal locality
  - O(log n) amortized, faster average performance
- Cons
  - Search gets more expensive since tree rotation can occur
  - No height constraint, the worst time can be O(n)
  - Parallel access is difficult: read-only operation will change the tree

Questions?