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## DSC 40B - Discussion 03

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### Problem 1.

Solve the following recurrence relations.

a)  $T(n) = T(n-1) + n$   
 $T(0)=0$

b)  $T(n)=4T(n/4) + n$   
 $T(1)=1$

### Problem 2.

Determine the recurrence relation describing the time complexity of each of the recursive algorithms below.

```
a) def fact(n):
    if(n <= 1)
        return 1
    else
        return n*fact(n-1)

b) def max_arr(arr):
    if(len(arr) == 1):
        return arr[0]
    mid = len(arr)//2
    left_max = max_arr(arr[:mid])
    right_max= max_arr(arr[mid:])
    if(left_max>right_max):
        return left_max
    else:
        return right_max
```

### Problem 3.

Determine whether each piece of code is correct or incorrect.

```
a) def max_arr(arr):
    max1 = arr[0]
    max2 = max_arr(arr[1:])
    if(max1 > max2):
        return max1
    else:
        return max2

b) def fib(n):
    if (n==1):
        return 1
    return fib(n-1)+fib(n-2)
```

### Problem 4.

Given a sorted array of distinct integers  $A[1 \dots n]$ , give an algorithm to find out whether there is an index  $i$  for which  $A[i] = i$ . Analyze the time complexity of the algorithm.  
(Hint : There is a solution that runs in better than linear  $\Theta(n)$  time!)