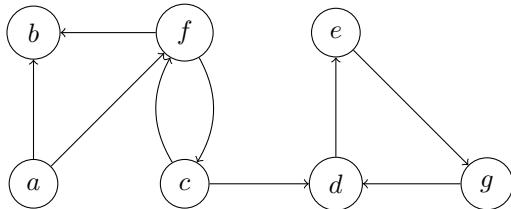

DSC 40B - Discussion 07

Problem 1.

Consider a *breadth-first search* on the graph shown in the figure, starting with node c .



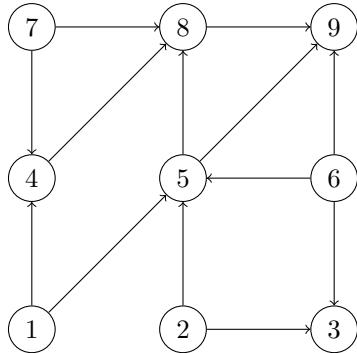
- a) Suppose you call `bfs_shortest_paths(graph, 'c')` on the graph above. This function returns dictionaries `distance` and `predecessor`. Write down the contents of these dictionaries as they are when the function exits.

```
def bfs_shortest_paths(graph, source):
    status = {node:'undiscovered' for node in graph.nodes}
    distance= {node:float('inf') for node in graph.nodes}
    predecessor = {node: None for node in graph.nodes}
    status[source] = 'pending'
    distance[source]=0
    pending = deque([source])
    # while there are still pending nodes
    while pending:
        u = pending.popleft()
        for v in graph.neighbors(u):
            # explore edge (u,v)
            if status[v] == 'undiscovered':
                status[v]='pending'
                distance[v]=distance[u]+1
                predecessor[v]=u
                # append to right
                pending.append(v)
        status[u]='visited'
    return predecessor, distance
```

- b) Mark the BFS trees produced on executing BFS on this graph.

Problem 2.

Consider the following directed graph.



- a) Make a bold arrow from node u to node v if u is the predecessor of node v in DFS. Use the convention that a node's neighbors are processed in ascending order by label.

- b) Fill in the table below so that it contains the start and finish times of each node after a DFS is performed on the above graph using node 1 as the source. Begin your start times with 1.

Node	Start	Finish
1		
2		
3		
4		
5		
6		
7		
8		
9		

c) Topologically sort the vertices of the graph.

Problem 3.

State whether the following statements are true or false.

- a) Breadth first search on a directed graph always produces same number of BFS trees irrespective of order in which vertices are given and the neighbouring nodes are visited.

- b) Breadth first search on an undirected graph always produces same number of BFS trees irrespective of order in which vertices are given and the neighbouring nodes are visited.

- c) Both BFS and DFS require atleast $\Omega(V)$ memory.

- d) Consider a graph G on which BFS is run with node s as the source. Assume that BFS visits a node u in the graph before node v. Then $d(s, u) < d(s, v)$

- e) Every directed acyclic graph has exactly one topological ordering.

Problem 4.

Given an undirected graph $G=(V,E)$, give an algorithm to find if the graph is disconnected.

Figure 1: "Full" DFS

```
from dataclasses import dataclass
@dataclass
class Times:
    clock: int
    start: dict
    finish: dict

def full_dfs_times(graph):
    status = {node: 'undiscovered' for node in graph.nodes}
    predecessor = {node: None for node in graph.nodes}
    times=Times(clock=0, start={}, finish={})
    for u in graph.nodes:
        if status[u]=='undiscovered':
            dfs_times(graph, u, status, times)
    return times, predecessor

def dfs_times(graph, u, status, predecessor, times):
    times.clock+=1
    times.start[u]=times.clock
    status[u]='pending'
    for v in graph.neighbors(u):
        # explore edge (u, v)
        if status[v]=='undiscovered':
            predecessor[v]=u
            dfs_times(graph, v, status, times)
    status[u]='visited'
    times.clock+=1
    times.finish[u]=times.clock
```